

# O<sub>2</sub>scl - An Object-Oriented Scientific Computing Library

Version 0.910

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## 1 O2scl User's Guide

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### 1.1 Feature Overview

O2scl is a C++ class library for object-oriented numerical programming. It includes

- Classes based on numerical routines from GSL and CERNLIB
- Vector and matrix classes which are fully compatible with `gsl_vector` and `gsl_matrix`, yet offer indexing with `operator[]` and other object-oriented features
- CERNLIB-based classes which are completely rewritten in C++
- Classes which require function inputs are designed to accept (public or private) member functions, even if they are virtual.
- Classes use templated vector types, which allow the use of user-specified object-oriented vectors or C-style arrays.
- Highly compatible - Recent versions have been tested on Linux (32- and 64-bit systems, with Intel and AMD chips), Windows XP with Cygwin, and MacOSX.
- Free! O2scl is provided under Version 3 of the GNU Public License (see [License Information](#) for more).
- Two sub-libraries
  - Thermodynamics of ideal and nearly-ideal particles with quantum statistics
  - Equations of state for finite density relevant for neutron stars

This is a beta version. The library should install and test successfully, and most of the classes are ready for production use. Some of the interfaces may change slightly in future versions. There are a few classes which are more experimental, and this is clearly stated at the top of the documentation for these classes.

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### 1.2 Quick Reference to User's Guide

- [Installation](#)
  - [General Usage](#)
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## 2 Installation

The rules for installation are generally the same as that for other GNU libraries. The file `INSTALL` has some details on this procedure. Generally, you should be able to run `./configure` and then type `make` and `make install`. More information on the `configure` command can also be obtained from `./configure --help`. `O2scl` requires the GSL library. If the `configure` script cannot find them, you may have to specify their location in the `CPPFLAGS` and `LDFLAGS` environment variables (`./configure --help` shows some information on this). The documentation is included in the distribution and automatically installed by `make install`.

After `make install`, you may test the library with `make o2scl-test`. At the end, the phrase `All O2scl tests passed` indicates that the testing was successful. You may also run `make o2scl-test` in the individual subdirectories of the `src` directory to individually test the classes and functions in that part of `O2scl`. Note that `make check` will not work.

This library requires GSL and is designed to work with GSL versions 1.15 or greater, which can be obtained from <http://www.gnu.org/software/gsl>. Some classes may work with older versions of GSL, but this cannot be guaranteed. A CBLAS library is also required, and `./configure` will look for `libcblas` first, and if not found then it will look for `libgslcblas`. If neither is present, then you may have to manually specify a CBLAS library using the `LIBS` and `LDFLAGS` environment variables.

This library also performs file I/O using the HDF5 (not HDF4) library, which can be obtained from <http://www.hdfgroup.org>. To compile `O2scl` without HDF support, use the argument `--disable-hdf` to `configure` during installation. If HDF5 is not located in a typical location for your system, in order to compile `O2scl` with HDF support you may have to specify the location of the HDF header files and libraries with the `-I` and `-L` flags. Some `O2scl` functions use the high-level HDF routines found in the `hdf5_hl` library, but this library is usually in the same location as the base `hdf5` library.

Range-checking for vectors and matrices is turned on by default. You can disable range-checking by defining `-DO2SCL_NO_RANGE_CHECK`, e.g.

```
CPPFLAGS="-DO2SCL_NO_RANGE_CHECK" ./configure
```

The separate libraries `O2scl_eos` and `O2scl_part` are installed by default. To disable the installation of these libraries and their associated documentation, run `./configure` with the flags `--disable-eoslib` or `--disable-partlib`. Note that `O2scl_eos` depends on `O2scl_part` so using `--disable-partlib` without `--disable-eoslib` will not work. Note also that both `O2scl_part` and `O2scl_eos` require HDF support.

There are several warning flags that are useful when configuring and compiling with `O2scl`. See the GSL documentation for an excellent discussion, and also see the generic installation documentation in the file `INSTALL` in the `O2scl` top-level directory. For running `configure`, for example, if you do not have privileges to write to `/usr/local`,

```
CPPFLAGS="-O3 -I/home/asteiner/install/include" \
LDFLAGS="-L/home/asteiner/install/lib" ./configure -C \
--prefix=/home/asteiner/install
```

In this example, specifying `-I/home/asteiner/install/include` and `-L/home/asteiner/install/lib` above ensures that the GSL libraries can be found (this is where they are installed on my machine). The `--prefix=/home/asteiner/install` argument to `./configure` ensures that `O2scl` is installed there as well.

For those users wanting to compile `O2scl` under Xcode on a Mac, some advice for doing this has been posted to the `o2scl-help` mailing list.

The `O2scl` documentation is generated with Doxygen. In principle, the documentation can be regenerated by the end-user, but this is not supported and requires several external applications not included in the distribution.

**Un-installation:** While there is no explicit "uninstall" makefile target, there are only a couple places to check. - Installation creates directories named `o2scl` in the include, doc and shared files directory (which default to `/usr/local/include`, `/usr/local/doc`, and `/usr/local/share`) which can be removed. Finally, all of the libraries are named with the prefix `libo2scl` and are created by default in `/usr/local/lib`. As configured with the settings above, the files are in `/home/asteiner/install/include/o2scl`, `/home/asteiner/install/lib`, `/home/asteiner/install/share/o2scl`, and `/home/asteiner/install/doc/o2scl`.

## 3 General Usage

### 3.1 Namespaces

Most of the classes reside in the namespace `o2scl` (this namespace has been removed from the documentation for clarity). - Numerical constants (many of them based on the GSL constants) are placed in separate namespaces (`gsl_cgs`, `gsl_cgsm`, `gsl_mks`, `gsl_mkssa`, `gsl_num`, `o2scl_const`, and `o2scl_fm`). There are also two namespaces which hold integration coefficients, `o2scl_inte_gk-coeffs` and `o2scl_inte_qng-coeffs`. There are also some namespaces for the linear algebra functions, see [Linear Algebra](#) for more information.

### 3.2 Documentation conventions

In the following documentation, function parameters are denoted by `parameter`, except when used in mathematical formulas as in variable .

### 3.3 Nomenclature

Classes directly derived from the GNU Scientific Library are preceded by the prefix `gsl_` and classes derived from CERNLIB are preceded by the prefix `cern_`. Some of those classes derived from GSL and CERNLIB operate slightly differently from the original versions. The differences are detailed in the corresponding class documentation.

### 3.4 Basic error handling

Error handling is a hybrid approach combining GSL with C++ exceptions. An abstract type has been defined which operates as a GSL-like error handler. The default error handler is a implementation of this abstract type which throws a C++ exception when an error is encountered. The various exceptions, and their correspondence with the GSL error codes, are given in the [GSL error codes and C++ exception types](#) section. By default in `O2scl`, the default GSL error handler is replaced with the `O2scl` default error handler, i.e. GSL functions will throw C++ exceptions.

Errors can be set by the user through the macros `O2SCL_ERR`, which sets an error, and `O2SCL_ERR_RET`, which sets an error and returns the error number.

The error handler, `err_hnd` is a global pointer to an object of type `err_hnd_type`. There is a global default error handler, `def_err_hnd`, of type `err_hnd_cpp`, which throws C++ exceptions, and an alternate default error handler, `alt_err_hnd`, of type `err_hnd_gsl`, which outputs an error message and aborts execution.

Generally, functions also follow the GSL-like behavior of calling a GSL-like error handler and (when appropriate) return a non-zero value. When functions succeed they return `gsl_success` (zero). `O2scl` functions never reset the error handler. Also, object destructors do not generally call the error handler. Internally, `O2scl` does not use `try` blocks, but these can easily be effectively employed by an `O2scl` user.

The list of GSL error codes (including a few extra ones for `O2scl`) is given in the documentation for the file `err_hnd.h`. The default error handler can be replaced by simply assigning the address of a descendant of `err_hnd_type` to `err_hnd`.

Functionality similar to `assert()` is provided with the macro `O2SCL_ASSERT`, which exits if its argument is non-zero, and `O2SCL_BOOL_ASSERT` which exits if its argument is false.

One can instruct the library to use the GSL-like `O2scl` error handler `alt_err_hnd` by default, by defining the constant `O2SCL_USE-_GSL_HANDLER`. This is also useful if one wants to compile without C++ exceptions (which does have a small overhead).

### 3.5 What is an error?

`O2scl` assumes that errors are events which should happen infrequently. Error handling strategies are often time-consuming and they are not a replacement for normal code flow. However, even with this in mind, one can still distinguish a large spectrum of possibilities from "fatal" errors, those likely to corrupt the stack and/or cause a dreaded "segmentation fault" and "non-fatal" errors, those errors

which might cause incorrect results, but might be somehow recoverable. One of the purposes of error handling is to decide if and how these different types of errors should be handled differently.

Sometimes, it is undesirable to abort execution upon a failure to reach numerical convergence. While these failures are treated as errors (and by default an exception is thrown), some of the classes which attempt to reach numerical convergence have an option (e.g. `mroot::err_nonconv`) to turn this default behavior off for these convergence errors. To set these "convergence" errors in code provided by the user, the macros `O2SCL_CONV` and `O2SCL_CONV_RET` can be used.

Of course, the standard `try, catch` mechanism of error handling may also be used for finer-grained control.

Another related issue is that `O2scl` often calls functions which are supplied by the user, these user-designed functions may create errors, and the library needs to decide how to deal with them, even though it knows little about what is actually happening inside these user-defined functions. Most of the time, `O2scl` assumes that if a function returns a nonzero value, then an error has occurred and the present calculation should abort.

### 3.6 GSL error codes and C++ exception types

See also the description of the error codes in `err_hnd.h`.

`gsl_success=0`, (no error thrown)

`gsl_failure=-1`, `exc_exception`

`gsl_continue=-2`, (no error thrown)

`gsl_edom=1`, `exc_range_error`

`gsl_erange=2`, `exc_range_error`

`gsl_efault=3`, `exc_runtime_error`

`gsl_einval=4`, `exc_invalid_argument`

`gsl_efailed=5`, `exc_exception`

`gsl_efactor=6`, `exc_runtime_error`

`gsl_esanity=7`, `exc_exception`

`gsl_enomem=8`, `exc_runtime_error`

`gsl_ebadfunc=9`, `exc_runtime_error`

`gsl_erunaway=10`, `exc_runtime_error`

`gsl_emaxiter=11`, `exc_runtime_error`

`gsl_ezerodiv=12`, `exc_overflow_error`

`gsl_ebadtol=13`, `exc_invalid_argument`

`gsl_etol=14`, `exc_runtime_error`

`gsl_eundrflw=15`, `exc_range_error`

`gsl_eovrflw=16`, `exc_overflow_error`

`gsl_ellos=17`, `exc_runtime_error`

`gsl_eround=18`, `exc_runtime_error`

`gsl_ebadlen=19`, `exc_invalid_argument`

`gsl_enotsqr=20`, `exc_invalid_argument`

`gsl_esing=21`, `exc_runtime_error`

`gsl_ediverge=22`, `exc_runtime_error`

`gsl_eunsup=23`, `exc_exception`

---

```

gsl_eunimpl=24, exc\_exception
gsl_ecache=25, exc\_runtime\_error
gsl_etable=26, exc\_runtime\_error
gsl_enoprog=27, exc\_runtime\_error
gsl_enoprogj=28, exc\_runtime\_error
gsl_etolf=29, exc\_runtime\_error
gsl_etolx=30, exc\_runtime\_error
gsl_etolg=31, exc\_runtime\_error
gsl_eof=32, exc\_ios\_failure
gsl_enotfound=33, exc\_runtime\_error
gsl_ememtype=34, exc\_logic\_error
gsl_efilenotfound=35, exc\_ios\_failure
gsl_eindex=36, exc\_invalid\_argument
gsl_outsidecons=37, exc\_runtime\_error

```

### 3.7 Objects and scope

O<sub>2</sub>scl objects frequently take inputs which are of the form of a reference to a smaller object. This is particularly convenient because it allows a lot of flexibility, while providing a certain degree of safety. In many cases, the user retains the responsibility of ensuring that input objects do not go out of scope before they are utilized by objects which require them. This is actually no different than the requirements on the user imposed by GSL, for example.

A simple example of this is provided by the multi-dimensional integrator [composite\\_inte](#). It works by combining several one-dimensional integrators to integrate over a multi-dimensional hypercube. If the specified one-dimensional integrator goes out of scope an integration is attempted, the integration will fail, for example,

```

// How not to provide subobjects to O2scl classes

void set_integrator(multi_inte<int> &mi) {
    gsl_inte_qag<size_t> one_dim_it[2];
    mi.set_oned_inte(one_dim_it[0],0);
    mi.set_oned_inte(one_dim_it[1],1);
}

void function() {
    composite_inte<int> cit;
    set_integrator(cit);
    cit.minteg_err(func,2,a,b,pa,res,err);
}

```

This will fail because the one-dimensional integration objects go out of scope (it's a local variable in the function and its destructor is called before the `set_integrator()` function exits) before the `minteg_err()` function is called.

In C++, this difficulty can be solved by using shared pointers, which ensure that an object is deleted only when it has no more references which are pointing to it. While shared pointer objects are part of the new TR1 standard, not all compilers implement this standard yet. O<sub>2</sub>scl defines a template struct [o2\\_shared\\_ptr](#), which provides the user a consistent interface to a working shared pointer type, [o2\\_shared\\_ptr<T>::type](#) (located in the [o2scl](#) namespace). If TR1 is not available, then one can compile O<sub>2</sub>scl with O2SCL\_NO\_TR1\_MEMORY. In this case, if O2SCL\_HAVE\_BOOST is defined, then the boost shared pointer type is used, and otherwise an internal O<sub>2</sub>scl shared pointer template named [o2\\_int\\_shared\\_ptr](#) is used. See the documentation for [o2\\_shared\\_ptr](#) for more details.

### 3.8 Reference parameters

When a `O2scl` function contains two reference parameters for objects, it is not typically possible to provide the same object to both parameters or to provide two objects which share the same memory. This is particularly an issue when the associated types are template types, since then the `O2scl` library has no way of knowing how memory is organized in these unspecified types.

## 4 Compiling Examples

The example programs are in the `examples` directory. After installation, they can be compiled and executed by running `make o2scl-examples` in that directory. This will also test the output of the examples to make sure it is correct. If all the examples succeed, the message `All O2scl tests passed.` will appear at the end. The output for each example is placed in the corresponding file with a `.scr` extension.

Alternatively, you can make the executable for each example in the `examples` directory individually using, e.g. `make ex_mroot`.

Also, the testing code for each class is occasionally useful for providing examples of their usage. The testing source code for each source file is named with an `_ts.cpp` prefix in the same directory as the class source.

#### Note

All of these examples are provided under the GPLv3 license, although to save space the licenses are not reproduced in the documentation for each example. See [License Information](#) for more information.

## 5 Related Projects

Several noteworthy related projects:

- **GSL - The GNU Scientific Library**

The first truly free, ANSI-compliant, fully tested, and well-documented scientific computing library. The GSL is located at <http://www.gnu.org/software/gsl>, and the manual is available at

[http://www.gnu.org/software/gsl/manual/html\\_node/](http://www.gnu.org/software/gsl/manual/html_node/). Many GSL routines are included and reworked in `O2scl` (the corresponding classes begin with the `gsl_` prefix) and `O2scl` was specifically designed to be used with GSL. GSL is a must-have for most serious numerical work in C or C++ and is required for installation of `O2scl`.

- **HDF - Hierarchical Data Format**, (<http://www.hdfgroup.org>)

A library developed for file I/O of scientific data. Contains C, C++, FORTRAN and Java APIs, several command-line tools, and a longstanding active community of users.

- **CERNLIB** - (<http://cernlib.web.cern.ch/cernlib/mathlib.html>)

The gold standard in FORTRAN computing libraries. Several CERNLIB routines are rewritten completely in C++ and included in `O2scl` (they begin with the `cern_` prefix). CERNLIB is located at

- **LAPACK and ATLAS - The gold standard for linear algebra**

Available at <http://www.netlib.org/lapack> and <http://www.netlib.org/atlas>. See also <http://www.netlib.org/clapack>.

- **QUADPACK - FORTRAN adaptive integration library**, <http://www.netlib.org/quadpack>

This is the library on which the GSL integration routines are based (prefix `gsl_inte_`).

- **Blitz++** - (<http://www.oonumerics.org/blitz>)

Another linear algebra library designed in C++ which includes vector and matrix types and basic arithmetic. As the name implies, Blitz++ has the capability to be particularly fast. Distributed with a Perl-like artistic license "or the GPL".



- Eigen - (<http://eigen.tuxfamily.org>)  
A linear algebra library in C++. Eigen is licensed under GPLv2 or LGPLv3.
- Boost - (<http://www.boost.org>)  
Free (license is compatible with GPL) peer-reviewed portable C++ source libraries that work well with the C++ Standard Library. Boost also contains uBlas, for linear algebra computing.
- FLENS - (<http://flens.sourceforge.net>)  
A C++ library with object-oriented linear algebra types and an interface to BLAS and LAPACK.
- MESA - Modules for Experiments in Stellar Astrophysics, (<http://mesa.sourceforge.net>)  
An excellent FORTRAN library with accurate low-density equations of state, interpolation, opacities and other routines useful in stellar physics. Work is currently under way to rewrite some of the MESA routines in C/C++ for O<sub>2</sub>scl . Licensed with LGPL (not GPL).
- TNT - Template numerical toolkit (<http://math.nist.gov>)  
TNT provides vector and matrix types and basic arithmetic operations. Most of the classes in O<sub>2</sub>scl which use vector and matrix types are templated to allow compatibility with TNT. (Though there are a few small differences.) This software is in the public domain. TNT appears not to be under current development.
- OOL - Open Optimization Library (<http://ool.sourceforge.net>)  
Constrained minimization library designed with GSL in mind. The O<sub>2</sub>scl constrained minimization classes are derived from this library, though OOL appears not to be under current development. [Constrained Minimization](#) .
- Root - CERN's new C++ analysis package (<http://root.cern.ch>)  
A gargantuan library for data analysis, focused mostly on high-energy physics. Their histograms, graphics, file I/O and support for large data sets is particularly good. See [graph.h](#) for some functions which provide some plotting functions for use with Root.
- Aegis - a transaction-based software configuration management system (<http://aegis.sourceforge.net>)  
Related because the [o2\\_int\\_shared\\_ptr](#) class was adapted from Aegis.

## 6 Complex Numbers

Several arithmetic operations for `gsl_complex` are defined in [cx\\_arith.h](#), but no constructor has been written. The object `gsl_complex` is still a struct, not a class. For example,

```
#include <o2scl/cx_arith.h>
gsl_complex a={{1,2}}, b={{3,4}};
gsl_complex c=a+b;
cout << GSL_REAL(c) << " " << GSL_IMAG(C) << endl;
```

In case the user needs to convert between `gsl_complex` and `std::complex<double>`, two conversion functions [gsl\\_to\\_complex\(\)](#) and [complex\\_to\\_gsl\(\)](#) are also provided in [cx\\_arith.h](#).

A short example using complex number arithmetic is given below.

### 6.1 Mandelbrot set

```
/* Example: ex_mandel.cpp
-----
Mandelbrot example demonstrating table3d and complex arithmetic
```

```

*/

#include <iostream>
#include <o2scl/cx_arith.h>
#include <o2scl/test_mgr.h>
#include <o2scl/table3d.h>
#ifdef O2SCL_HDF_IN_EXAMPLES
#include <o2scl/hdf_file.h>
#include <o2scl/hdf_io.h>
#endif

using namespace std;
using namespace o2scl;
#ifdef O2SCL_HDF_IN_EXAMPLES
using namespace o2scl_hdf;
#endif

int main(void) {

    test_mgr tm;
    tm.set_output_level(2);

    // Create a table3d object
    table3d t;

    // Add parameters
    double delta=0.001, minx=-1.5, maxx=0.8, miny=-1.0, maxy=1.0;
    size_t maxtime=0, limit=100;
    t.add_constant("delta",delta);
    t.add_constant("minx",minx);
    t.add_constant("maxx",maxx);
    t.add_constant("miny",miny);
    t.add_constant("maxy",maxy);

    // Set grid
    ovector ox, oy;
    for(double x=minx;x<=maxx;x+=delta) ox.push_back(x);
    for(double y=miny;y<=maxy;y+=delta) oy.push_back(y);
    t.set_xy("x",ox.size(),ox,"y",oy.size(),oy);

    // Create slice
    t.new_slice("time");

    // Compute escape times
    for(size_t i=0;i<ox.size();i++) {
        for(size_t j=0;j<oy.size();j++) {
            gsl_complex c={ox[i],oy[j]};
            gsl_complex z={0,0};
            size_t time=0;
            for(size_t k=0;k<limit;k++) {
                // Arithmetic with gsl_complex objects
                z=z*z+c;
                if (abs(z)>10.0) {
                    time=k;
                    k=limit;
                }
            }
            t.set(i,j,"time",time);
            if (time>maxtime) maxtime=time;
        }
    }

    // Maximum escape time for color normalization
    t.add_constant("maxtime",maxtime);

    // Output to file if O2scl is compiled with HDF support
#ifdef O2SCL_HDF_IN_EXAMPLES
    hdf_file hf;
    hf.open("ex_mandel.o2");
    hdf_output(hf,t,"mandel");
#endif
}

```

```

    hf.close();
#endif

    tm.test_gen(maxtime==99,"maxtime test");
    tm.report();

    return 0;
}
// End of example

```

The information stored in the [table3d](#) object in `ex_mandel.out` can be plotted:

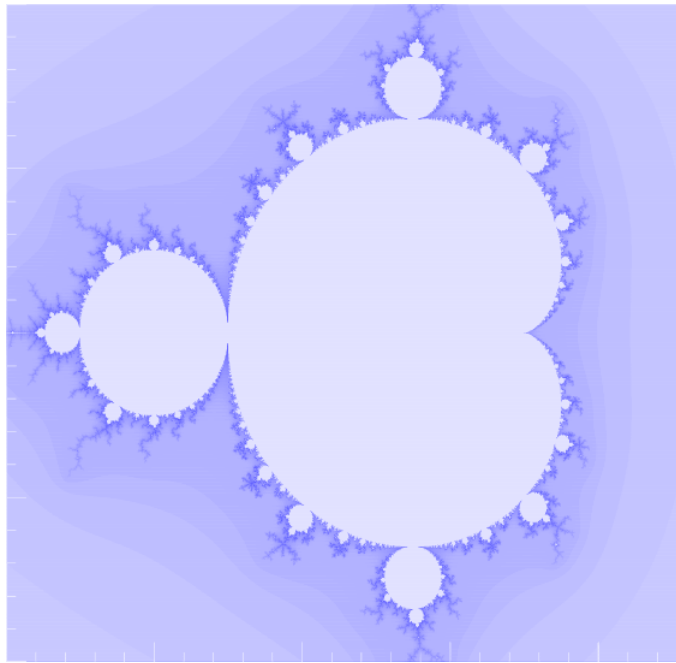


Figure 1: Mandelbrot example plot

## 7 Arrays, Vectors, Matrices and Tensors

### 7.1 Introduction

The `O2scl` library uses a standard nomenclature to distinguish a couple different concepts. The word "array" is always used to refer to C-style arrays, i.e. `double[]`. If there are two dimensions in the array, it is a "two-dimensional array", i.e. `double[][]`. The word "vector" is reserved generic objects with array-like semantics, i.e. any type of object or class which can be treated similar to an array in that it has an function `operator[]` which gives array-like indexing. Thus arrays are vectors, but not all vectors are arrays. There are a couple specific vector types defined in `O2scl` like [ovector](#) and [uvector](#). The STL vector `std::vector<double>` is also a vector type in this language. The word "matrix" is reserved for the a generic object which has matrix-like semantics and can be accessed using either `operator()` or two successive applications of `operator[]` (or sometimes both). The `O2scl` objects [omatrix](#) and [umatrix](#) are matrix objects, as is a C-style two-dimensional array, `double[][]`. The header files are named in this spirit also: functions and classes which operate on generic vector types are in [vector.h](#) and functions and classes which work only with C-style arrays are in [array.h](#). The word "tensor" is used for a generic object which has rank  $n$  and then has  $n$  associated indices. A vector is just a tensor of rank 1 and a matrix is just a tensor of rank 2.

Most of the classes in `O2scl` which use vectors and/or matrices are designed so that they can be used with any appropriately-defined vector or matrix types. This is a major part of the design goals for `O2scl` and most of the classes are compatible with matrix and vector objects from `GSL`, `TNT`, `MV++`, `uBlas`, and `Blitz++`.

The first index of a matrix type is defined always to be the index associated with "rows" and the second is associated with "columns". The `O2scl` matrix output functions respect this notation as well, so that all of the elements of the first row is sent to the screen, then all of the elements in the second row, and so on. With this in mind, one can make the distinction between "row-major" and "column-major" matrix storage. C-style two-dimensional arrays are "row-major" in that the elements of the first row occupy the first locations in memory as opposed "column-major" where the first column occupies the first locations in memory. It is important to note that the majority of the classes in `O2scl` do not care about the details of the underlying memory structure, so long as two successive applications of `operator[]` (or in some cases `operator(,)`) works properly. The storage format used by [omatrix](#) and [umatrix](#) is row-major, and there are no column-major matrix classes in `O2scl` (yet).

## 7.2 Matrix indexing with `[][]` vs. `(,)`

While vector indexing with `operator[]` is very compatible with almost any vector type, matrix indexing is a bit more difficult. There are two options: assume matrix objects provide an `operator[]` method which can be applied twice, i.e. `m[i][j]`, or assume that matrix elements should be referred to with `m(i, j)`. Most of the `O2scl` classes use the former approach so that they are also compatible with two-dimensional arrays. However, there are sometimes good reasons to want to use `operator()` for matrix-intensive operations from linear algebra. For this reason, some of the functions given in the `linalg` directory are specified in two forms: the first default form which assumes `[][]`, and the second form with the same name, but in a namespace which has a suffix `_paren` and assumes matrix types use `(,)`.

## 7.3 Vector types for template classes

Many of the classes and functions are designed to be generic with regard to vector types, permitting the user to use any type which has a suitably defined `operator[]` method (or sometimes `operator()` method). In order to do this, some classes also require the ability to allocate new vectors, and for this reason they have three different templated vector types:

- `vec_t` - the generic vector type
- `alloc_t` - a vector allocation type
- `alloc_vec_t` - a vector type which can be allocated with an object of type `alloc_t` and can be passed as an argument of type `vec_t`.

The typical requirement is that one must be able to write something like

```
alloc_t ao;
alloc_vec_t vec;
ao.allocate(vec, 5);
```

to allocate a new vector `vec` of length 5. In addition, to provide exception safety, either the objects of type `alloc_vec_t` must either free its memory in its destructor, or it must be taken care of in the destructor of the `alloc_t` object. The native `O2scl` vector classes provide this kind of functionality by default, so some typical choices for these template types are

- `vec_t = ovector_base`, `alloc_t = ovector_alloc`, and `alloc_vec_t = ovector`
- `vec_t = uvector_base`, `alloc_t = uvector_alloc`, and `alloc_vec_t = uvector`
- `vec_t = double[n]`, `alloc_t = array_alloc<double[n]>`, and `alloc_vec_t = double[n]`
- `vec_t = double *`, `alloc_t = pointer_alloc<double>`, and `alloc_vec_t = double *`

An example demonstrating how this works is given in the [Multi-dimensional solver](#) example.

## 7.4 Rows and columns vs. x and y

Sometimes its useful to think about the rows and columns in a matrix as referring to a elements of a grid, and the matrix indices refer to points in a grid in  $(x,y)$ . It might seem intuitive to think of a matrix as  $A[ix][iy]$  where  $ix$  and  $iy$  are the  $x$  and  $y$  indices because the ordering of the indices is alphabetical. However, it is useful to note that because functions like `matrix_out` print the first "row" first rather than the first column, a matrix constructed as  $A[ix][iy]$  will be printed out with  $x$  on the "vertical axis" and  $y$  on the "horizontal axis", so it is sometimes useful to store data in the form  $A[iy][ix]$  (for example, in the two dimensional interpolation class, `twod_intp`). In any case, all classes which take matrix data as input will document how the matrix ought to be arranged.

## 7.5 Generic vector functions

There are a couple functions which operate on generic vectors of any type in `vector.h`. They perform sorting, summing, rotating, copying, and computations of minima and maxima. For more statistically-oriented operations, see also `vec_stats.h`.

## 7.6 Native matrix and vector types

The rest of this section in the User's guide is dedicated to describing the O<sub>2</sub>scl implementations of vector, matrix, and tensor types.

Vectors and matrices are designed using the templates `ovector_tlate` and `omatrix_tlate`, which are compatible with `gsl_vector` and `gsl_matrix`. Vectors and matrices with unit stride are provided in `uvector_tlate` and `umatrix_tlate`. The most commonly used double-precision versions of these template classes are `ovector`, `omatrix`, `uvector` and `umatrix`, and their associated "views" (analogous to GSL vector and matrix views) which are named with a `_view` suffix. The classes `ovector_tlate` and `omatrix_tlate` offer the syntactic simplicity of array-like indexing, which is easy to apply to vectors and matrices created with GSL.

The following sections primarily discuss the operation objects of type `ovector`. The generalizations to objects of type `uvector`, `omatrix`, and the complex vector and matrix objects `ovector_cx`, `omatrix_cx`, `uvector_cx`, and `umatrix_cx` are straightforward.

## 7.7 Vector and matrix views

Vector and matrix views are provided as parents of the vector and matrix classes which do not have methods for memory allocation. As in GSL, it is simple to "view" normal C-style arrays or pointer arrays (see `ovector_array`), parts of vectors (`ovector_subvector`), and rows and columns of matrices (`omatrix_row` and `omatrix_col`). Several operations are defined, including addition, subtraction, and dot products.

## 7.8 Vector and matrix typedefs

Several typedefs are used to give smaller names to often used templates. Vectors and matrices of double-precision numbers all begin with the prefixes `ovector` and `omatrix`. Integer versions begin with the prefixes `ovector_int` and `omatrix_int`. Complex versions have an additional `"_cx"`, e.g. `ovector_cx`. See `ovector_tlate.h`, `ovector_cx_tlate.h`, `omatrix_tlate.h`, and `omatrix_cx_tlate.h`.

## 7.9 Unit-stride vectors

The `uvector_tlate` objects are naturally somewhat faster albeit less flexible than their finite-stride counterparts. Conversion to GSL vectors and matrices is not trivial for `uvector_tlate` objects, but demands copying the entire vector. Vector views, operators, and the nomenclature is similar to that of `ovector`.

## 7.10 Memory allocation

Memory for vectors can be allocated using `ovector::allocate()` and `ovector::free()`. Allocation can also be performed by the constructor, and the destructor automatically calls `free()` if necessary. In contrast to `gsl_vector_alloc()`, `ovector::allocate()` will

call `ovector::free()`, if necessary, to free previously allocated space. Allocating memory does not clear the recently allocated memory to zero. You can use `ovector::set_all()` with a zero argument to clear a vector (and similarly for a matrix).

If the memory allocation fails, either in the constructor or in `allocate()`, then the error handler will be called, partially allocated memory will be freed, and the size will be reset to zero.

Although memory allocation in `O2scl` vectors is very similar to that in `GSL`, the user must not mix allocation and deallocation between `GSL` and `O2scl`.

## 7.11 Get and set

Vectors and matrices can be modified using `ovector::get()` and `ovector::set()` methods analogous to `gsl_vector_get()` and `gsl_vector_set()`, or they can be modified through `ovector::operator[]` (or `ovector::operator()`), e.g.

```
ovector a(4);
a.set(0, 2.0);
a.set(1, 3.0);
a[2]=4.0;
a[3]=2.0*a[1];
```

If you want to set all of the values in an `ovector` or an `omatrix` at the same time, then use `ovector::set_all()` or `omatrix::set_all()`.

## 7.12 Range checking

Range checking is performed depending on whether or not `O2SCL_NO_RANGE_CHECK` is defined. It can be defined in the arguments to `./configure` upon installation to turn off range checking. Note that this is completely separate from the `GSL` range checking mechanism, so range checking may be on in `O2scl` even if it has been turned off in `GSL`. Range checking is used primarily in the vector, matrix, and tensor `get()` and `set()` methods.

To see if range checking was turned on during installation (without calling the error handler), use `lib_settings_class::range_check()`.

Note that range checking in `O2scl` code is most often present in header files, rather than in source code. This means that range checking can be turned on or off in user-defined functions separately from whether or not it was used in the library classes and functions.

## 7.13 Shallow and deep copy

Copying `O2scl` vectors using constructors or the `=` operator is performed according to what kind of object is on the left-hand side (LHS) of the equals sign. If the LHS is a view, then a shallow copy is performed, and if the LHS is a `ovector`, then a deep copy is performed. If an attempt is made to perform a deep copy onto a vector that has already been allocated, then that previously allocated memory is automatically freed. The user must be careful to ensure that information is not lost this way, even though no memory leak will occur.

For generic deep vector and matrix copying, you can use the template functions `vector_copy()`, `matrix_copy()`. These would allow you, for example, to copy an `ovector` to a `std::vector<double>` object. These functions do not do any memory allocation so that must be handled beforehand by the user.

## 7.14 Vector and matrix arithmetic

Several operators are available as member functions of the corresponding template:

Vector\_view unary operators:

- `vector_view += vector_view`
- `vector_view -= vector_view`

- `vector_view += scalar`
- `vector_view -= scalar`
- `vector_view *= scalar`
- `scalar = norm(vector_view)`

Matrix\_view unary operators:

- `matrix_view += matrix_view`
- `matrix_view -= matrix_view`
- `matrix_view += scalar`
- `matrix_view -= scalar`
- `matrix_view *= scalar`

Binary operators like addition, subtraction, and matrix multiplication are also defined for [ovector](#), [uvector](#), and related objects. The generic template for a binary operator, e.g.

```
template<class vec_t> vec_t &operator+(vec_t &v1, vec_t &v2);
```

is difficult because the compiler has no way of distinguishing vector and non-vector classes. At the moment, this is solved by creating a define macro for the binary operators. In addition to the predefined operators for native classes, the user may also define binary operators for other classes using the same macros. For example,

```
O2SCL_OP_VEC_VEC_ADD(o2scl::ovector, std::vector<double>,
std::vector<double>)
```

would provide an addition operator for [ovector](#) and vectors from the Standard Template Library. A full list of the operators which are defined by default and the associated macros are detailed in the documentation for [vec\\_arith.h](#).

The GSL BLAS routines can also be used directly with [ovector](#) and [omatrix](#) objects.

Note that some of these arithmetic operations succeed even with non-matching vector and matrix sizes. For example, adding a 3x3 matrix to a 4x4 matrix will result in a 3x3 matrix and the 7 outer elements of the 4x4 matrix are ignored.

## 7.15 Converting to and from GSL forms

Because of the way [ovector](#) is constructed, you may use type conversion to convert to and from objects of type `gsl_vector`.

```
ovector a(2);
a[0]=1.0;
a[1]=2.0;
gsl_vector *g=(gsl_vector *)(&a);
cout << gsl_vector_get(g,0) << " " << gsl_vector_get(g,1) << endl;
```

Or,

```
gsl_vector *g=gsl_vector_alloc(2);
gsl_vector_set(0,1.0);
gsl_vector_set(1,2.0);
ovector &a=(ovector &)(*g);
cout << a[0] << " " << a[1] << endl;
```

This sort of type-casting is discouraged among unrelated classes, but is permissible here because [ovector\\_tlate](#) is a descendant of `gsl_vector`. In particular, this will not generate "type-punning" warnings in later gcc versions. If this bothers your sensibilities, however, then you can use the following approach:

```
ovector a(2);
gsl_vector *g=a.get_gsl_vector();
```

The ease of converting between these two kind of objects makes it easy to use gsl functions on objects of type `ovector`, i.e.

```
ovector a(2);
a[0]=2.0;
a[1]=1.0;
gsl_vector_sort((gsl_vector *)(&a));
cout << a[0] << " " << a[1] << endl;
```

## 7.16 Converting from STL form

To "view" a `std::vector<double>`, you can use `ovector_array`

```
std::vector<double> d;
d.push_back(1.0);
d.push_back(3.0);
ovector_array aa(d.size,&(d[0]));
cout << aa[0] << " " << aa[1] << endl;
```

However, you should note that if the memory for the `std::vector` is reallocated (for example because of a call to `push_back()`), then a previously created `ovector_view` will be incorrect.

## 7.17 push\_back() and pop() methods

These two functions give a behavior similar to the corresponding methods for `std::vector<>`. This will work in `O2scl` classes, but may not be compatible with all of the GSL functions. This will break if the address of a `ovector_tlate` is given to a GSL function which accesses the `block->size` parameter instead of the `size` parameter of a `gsl_vector`. Please contact the author of `O2scl` if you find a GSL function with this behavior.

## 7.18 Vector and matrix views

Views are slightly different than in GSL in that they are now implemented as parent classes. Effectively, this means that vector views are just the same as normal vectors, except that they have no memory allocation functions (because the memory is presumably owned by a different object or scope). The code

```
double x[2]={1.0,2.0};
gsl_vector_view_array v(2,x);
gsl_vector *g=&(v.vector);
gsl_vector_set(g,0,3.0);
cout << gsl_vector_get(g,0) << " " << gsl_vector_get(g,1) << endl;
```

can be replaced by

```
double x[2]={1.0,2.0};
ovector_array a(2,x);
a[0]=3.0;
cout << a << endl;
```

## 7.19 Passing ovector parameters

It is often best to pass an `ovector` as a const reference to an `ovector_base`, i.e.

```
void function(const ovector_base &a);
```

If the function may change the values in the `ovector`, then just leave out `const`



```
void function(ovector_base &a);
```

This way, you ensure that the function is not allowed to modify the memory for the vector argument.

If you intend for a function (rather than the user) to handle the memory allocation, then some care is necessary. The following code

```
class my_class {
    int afunction(ovector &a) {
        a.allocate(1);
        // do something with a
        return 0;
    }
};
```

is confusing because the user may have already allocated memory for `a`. To avoid this, you may want to ensure that the user sends an empty vector. For example,

```
class my_class {
    int afunction(ovector &a) {
        if (a.get_size()>0 && a.is_owner()==true) {
            O2SCL_ERR("Unallocated vector not sent to afunction().",1);
            return 1;
        } else {
            a.allocate(1);
            // do something with a
            return 0;
        }
    }
};
```

In lieu of this, it is often preferable to use a local variable for the storage and offer a `get()` function,

```
class my_class {
protected:
    ovector a;
public:
    int afunction() {
        a.allocate(1);
        // do something with a
        return 0;
    }
    int get_result(const ovector_view &av) { av=a; return 0; }
};
```

The `O2scl` classes run into this situation quite frequently, but the vector type is specified through a template

```
template<class vec_t> class my_class {
protected:
    vec_t a;
public:
    int afunction(vec_t &a) {
        // do something with a
        return 0;
    }
};
```

where the drawback is that the user must perform the allocation.

## 7.20 Vectors and operator=()

An `"operator=(value)"` method for setting all vector elements to the same value is not included because it leads to confusion between, `ovector_tlate::operator=(const data_t &val)` and `ovector_tlate::ovector_tlate(size_t val)` For example, after implementing `operator=()` and executing the following

```
ovector_int o1=2;
ovector_int o2;
o2=2;
```

`o1` will be a vector of size two, and `o2` will be an empty vector!

To set all of the vector elements to the same value, use `ovector_tlate::set_all()`. Because of the existence of constructors like `ovector_tlate::ovector_tlate(size_t val)`, the following code

```
ovector_int o1=2;
```

still compiles, and is equivalent to

```
ovector_int o1(2);
```

while the code

```
ovector_int o1;
o1=2;
```

will not compile. As a matter of style, `ovector_int o1(2);` is preferable to `ovector_int o1=2;` to avoid confusion.

## 7.21 Matrix structure

The matrices from `omatrix_tlate` are structured in exactly the same way as in GSL. For a matrix with 2 rows, 4 columns, and a "tda" or "trailing dimension" of 7, the memory for the matrix is structured in the following way:

```
00 01 02 03 XX XX XX
10 11 12 13 XX XX XX
```

where XX indicates portions of memory that are unreferenced. The tda can be accessed through, for example, the method `omatrix_view_tlate::tda()`. The `get(size_t, size_t)` methods always take the row index as the first argument and the column index as the second argument. The matrices from `umatrix_tlate` have a trailing dimension which is always equal to the number of columns.

## 7.22 Reversing the order of vectors

You can get a reversed vector view from `ovector_reverse_tlate`, or `uvector_reverse_tlate`. For these classes, `operator[]` and related methods are redefined to perform the reversal. If you want to make many calls to these indexing methods for a reversed vector, then simply copying the vector to a reversed version may be faster.

## 7.23 Const-correctness with vectors

Vector objects, like `ovector`, can be const in the usual way. However because vector views, like `ovector_view` are like pointers to vectors, there are two ways in which they can be const. The view can point to a const vector, or the view can be a 'const view' which is fixed to point only to one vector (whether or not the vector pointed to happens to be const). This is exactly analogous to the distinction between `const double *p`, `double * const p`, and `const double * const p`. The first is a non-const pointer to const data, the second is a const pointer to non-const data, and the third is a const pointer to const data. The equivalent expressions in `O2scl` are

```
ovector_const_view v1;
const ovector_view v2;
const ovector_const_view v3;
```

Explicitly,

- `ovector_const_view` is a view of a const vector, the view may change, but the vector may not.

- `const ovector_const_view` is a const view of a const vector, the view may not point to a different vector and the vector may not change.
- `const ovector_view` is a const view of a normal vector, the view may not change, but the vector can.

This same distinction is also present, for example, in `ublas` vectors views within Boost.

A reference of type `ovector_base` is often used as a function argument, and can hold either a `ovector` or a `ovector_view`. The important rule to remember with `ovector_base` is that, a const reference, i.e.

```
const ovector_base &v;
```

is always a const reference to data which cannot be changed. A normal `ovector_base` reference does not refer to const data.

## 7.24 Vector and matrix output

Both the `ovector_view_tlate` and `omatrix_view_tlate` classes have an `<<` operator defined for each class. For writing generic vectors to a stream, you can use `vector_out()` which is defined in `vector.h`. Pretty matrix output is performed by global template functions `matrix_out()`, `matrix_cx_out_paren()`, and `matrix_out_paren()` which are defined in `columnify.h` since they internally use a `columnify` object to format the output.

## 7.25 Tensors

Some preliminary support is provided for tensors of arbitrary rank and size in the class `tensor`. Classes `tensor1`, `tensor2`, `tensor3`, and `tensor4` are rank-specific versions for 1-, 2-, 3- and 4-rank tensors. For n-dimensional data defined on a grid, `tensor_grid` provides a space to define a hyper-cubic grid in addition to the the tensor data. This class `tensor_grid` also provides simple n-dimensional interpolation of the data defined on the specified grid.

## 8 Permutations

Permutations are implemented through the `permutation` class. This class is fully compatible with `gsl_permutation` objects since it is inherited from `gsl_permutation_struct`. The class also contains no new data members, so upcasting and downcasting can always be performed. It is perfectly permissible to call GSL permutation functions from `permutation` objects by simply passing the address of the permutation, i.e.

```
permutation p(4);
p.init();
gsl_permutation_swap(&p, 2, 3);
```

The functions which apply a permutation to a user-specified vector are member template functions in the `permutation` class (see `permutation::apply()`).

Memory allocation/deallocation between the class and the `gsl_struct` is compatible in many cases, but mixing these forms is strongly discouraged, i.e. avoid using `gsl_permutation_alloc()` on a `permutation` object, but rather use `permutation::allocate()` instead. The use of `permutation::free()` is encouraged, but any remaining memory will be deallocated in the object destructor.

## 9 Linear Algebra

There is a small set of linear algebra routines. These are not intended to be a replacement for higher performance linear algebra libraries, but offer a very generic and flexible interface while providing performance sufficient for all but the most intensive applications. They work for almost all vector and matrix types. For vector and matrix types using `operator[]`, the BLAS and linear algebra routines are inside the `o2scl_cblas` and `o2scl_linalg` namespaces. For vector and matrix types using `operator()`, the BLAS and linear algebra routines are inside the `o2scl_cblas_paren` and `o2scl_linalg_paren` namespaces.

The linear algebra classes and functions include:

- Householder transformations ([householder.h](#))
- Householder solver ([hh.h](#))
- LU decomposition and solver ([lu.h](#))
- Cholesky decomposition ([cholesky.h](#))
- QR decomposition and solver ([qr.h](#))
- Solve tridiagonal systems ([tridiag.h](#))
- Lanczos diagonalization is inside class [lanczos](#), which also can compute the eigenvalues of a tridiagonal matrix.
- Givens rotations ([givens.h](#))

There is also a set of linear solvers for generic matrix and vector types which descend from [o2scl\\_linalg::linear\\_solver](#). These classes provide GSL-like solvers, but are generalized so that they are compatible with vector and matrix types which allow access through `operator[]`.

For users who require high-performance linear algebra, the [ovector](#) and [omatrix](#) objects can be used to call LAPACK routines directly, just as can be done with GSL. For an example of how to do this, see

<http://sourceware.org/ml/gsl-discuss/2001/msg00326.html> . Finally, there are also a couple of examples, `gesvd.cpp` and `zheev.cpp` in the `src/internal` directory which show how to call LAPACK with `O2scl` objects which may be adaptable for your platform and configuration.

## 10 Interpolation

The lower-level interpolation types based on GSL all inherit from [base\\_interp](#). These lower-level interpolation classes automatically use the GSL accelerated lookup system and have also been modified to handle monotonically decreasing vectors. They are template classes compatible with any vector type whose elements can be accessed with `operator[]`.

Integrals are always computed assuming that if the limits are ordered so that if the upper limit appears earlier in the array `x` in comparison to the lower limit, that the value of the integral has the opposite sign than if the upper limit appears later in the array `x` .

The classes [o2scl\\_interp](#) and [o2scl\\_interp\\_vec](#) provide simpler interfaces to the lower-level interpolation types taking care of memory allocation and initialization automatically. The difference between the two classes, [o2scl\\_interp](#) and [o2scl\\_interp\\_vec](#), analogous to the difference between using `gsl_interp_eval()` and `gsl_spline_eval()` in GSL. You can create a [o2scl\\_interp](#) object and use it to interpolate among any pair of chosen vectors, i.e.

```
ovector x(20), y(20);
// fill x and y with data
o2scl_interp oi;
double y_half=oi.interp(0.5,20,x,y);
```

Alternatively, you can create a [o2scl\\_interp\\_vec](#) object which can be optimized for a pair of vectors that you specify in advance

```
ovector x(20), y(20);
// fill x and y with data
o2scl_interp_vec oi(20,x,y);
double y_half=oi.interp(0.5);
```

Two specializations for C-style arrays of double-precision numbers are provided in [array\\_interp](#) and [array\\_interp\\_vec](#).

### 10.1 Lookup and binary search

The classes [search\\_vec](#) and [search\\_vec\\_ext](#) contain searching functions for generic vector types which contain monotonic (either increasing or decreasing) data. It is [search\\_vec](#) which is used internally by the interpolation classes to perform cached binary searching. These classes also allow one to exhaustively search for the index of an element in a vector without regard to any kind of ordering, e.g. [search\\_vec::ordered\\_lookup\(\)](#) (see also [ovector::lookup\(\)](#)).

## 10.2 "Smart" interpolation

The classes [smart\\_interp](#) and [smart\\_interp\\_vec](#) allow interpolation, lookup, differentiation, and integration of data which is non-monotonic or multiply-valued outside the region of interest. As with [o2scl\\_interp](#) above, the corresponding array versions are given in [sma\\_interp](#) and [sma\\_interp\\_vec](#).

## 10.3 Interpolation manager objects

Many O2scl classes require the ability to create and destroy several interpolation objects to interpolate many different vectors at the same time. For this purpose, interpolation managers have been created, which allow the user to provide a class with an interpolation manager associated with a low-level interpolation type (and thus free the user from having to worry about the associated memory management). The abstract base interpolation manager type is [base\\_interp\\_mgr](#), and the default interpolation manager object is [def\\_interp\\_mgr](#). The [def\\_interp\\_mgr](#) class has two template arguments: the first is the vector type to be interpolated, and the second is the lower-level interpolation type. The user is free to use the same interpolation manager instance for many different classes which require interpolation because the interpolation manager allocates separate interpolation instances for each class as necessary.

For an example usage of the default interpolation manager, see the [Contour lines](#), which specifies an interpolation manager for the [contour](#) class. The [table](#) class also works with interpolation manager objects (see [table::set\\_interp\(\)](#)).

## 10.4 Two and higher dimensional interpolation

Support for two-dimensional interpolation (by successive one-dimensional interpolations) is given in [twod\\_intp](#) (see [Two-dimensional Interpolation](#)), and a simple version of n-dimensional interpolation in [tensor\\_grid](#).

## 10.5 Inverse interpolation and other functions

The equivalent to "inverse" linear interpolation, which computes all the abscissae which have a fixed value of the ordinate is implemented in the template function [vector\\_find\\_level\(\)](#) which is documented in [smart\\_interp.h](#). This function together with [vector\\_invert\\_enclosed\\_sum\(\)](#) can be used to determine confidence limits surrounding the peak of a 1-dimensional data set using linear interpolation.

# 11 Physical Constants

The constants from GSL are reworked with the type `const double` and placed in namespaces called [gsl\\_cgs](#), [gsl\\_cgsm](#), [gsl\\_mks](#), [gsl\\_mkssa](#), and [gsl\\_num](#). Some additional constants are given in the namespace [o2scl\\_const](#). Some of the numerical values have been updated from recently released data from NIST.

# 12 Function Objects

Functions are passed to numerical routines using template-based function classes, sometimes called "functors". There are several basic kinds of function objects:

- [funct](#) : One function of one variable
- [multi\\_funct](#) : One function of several variables
- [mm\\_funct](#) : n functions of n variables
- [fit\\_funct](#) : One function of one variable with n fitting parameters
- [ode\\_funct](#) : n derivatives as a function of n function values and the value of the independent variable

- [jac\\_func](#) : Jacobian function for solver
- [ool\\_hfunc](#) : Hessian product for constrained minimization

The class name suffixes denote children of a generic function type which are created using different kinds of inputs:

- `_fptr`: function pointer for a static or global function
- `_gsl`: GSL-like function pointer
- `_mfptr`: function pointer template for a class member function
- `_cmfptr`: function pointer template for a class member function which is const
- `_strings`: functions specified using strings, e.g. "x^2-2", which are in the separate `O2scl_ext` package.
- `_noerr`: (for [func](#) and [multi\\_func](#)) a function which directly returns the function value rather than returning an integer error value
- `_nopar`: (for [func](#)) a function which has no parameters and directly returns the function value.

See the [Function object example](#) and the [Multi-dimensional solver](#) which provide detailed examples of how functions can be specified to classes through these function objects.

## 12.1 Connection to STL and Boost

The `O2scl` function types are very closely related to similar types in the Standard Template Library (STL) and in Boost. In the language of the STL, [func](#) implements the concept of a [Unary Function](#) where the argument and return types are both `double`. In turn, most `O2scl` classes which have a template parameter `func_t` will accept all classes which implement this same concept. Note that in the STL, Unary Functions also implement the Assignable concept, and `O2scl` classes often do not require this for objects of type `func_t`. The Boost library handles things in a very similar way, except that STL concepts are referred to as "traits", and there is a much more complete list of "type traits".

## 12.2 Function object details

There is a small overhead associated with the indirection: a "user class" accesses the function class which then calls function which was specified in the constructor of the function class. In many problems, the overhead associated with the indirection is small. Some of this overhead can always be avoided by inheriting directly from the function class and thus the user class will make a direct virtual function call. To eliminate the overhead entirely, one can specify a new type for the template parameter in the user class.

Virtual functions can be specified through this mechanism as well. For example, if [cern\\_mroot](#) is used to solve a set of equations specified as

```
class my_type_t {
    virtual member_func();
};
my_type_t my_instance;
class my_derived_type_t : public my_type_t {
    virtual member_func();
};
my_derived_type_t my_inst2;
mm_func_t_mfptr<my_type_t> func(&my_inst2, &my_instance::member_func);
```

Then the solver will solve the member function in the derived type, not the parent type.

Note that providing a user access to a function object instantiated with a protected or private member function is (basically) the same as providing them access to that function.

## 12.3 Function object example

This example shows how to provide functions to O<sub>2</sub>scl classes by solving the equation

$$\left\{ 1 + \frac{1}{p_2} \sin[50(x - p_1)] \right\} \tan^{-1}[4(x - p_1)] = 0$$

Where  $p_1 = 0.01$  and  $p_2 = 1.1$ . The parameter  $p_1$  is stored as member data for the class, and the parameter  $p_2$  is an argument to the member function.

The image below shows how the solver progresses to the solution of the example function.

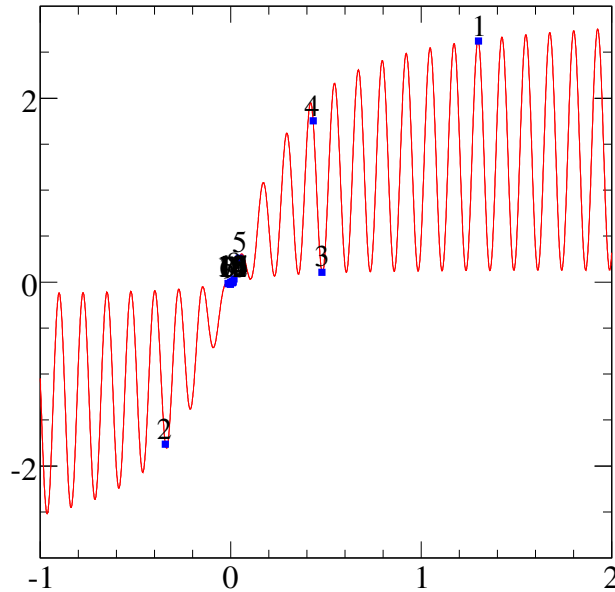


Figure 2: Function object example plot

```

/* Example: ex_fptr.cpp
-----
This gives an example of the how member functions and external
parameters are supplied to numerical routines. In this case, a
member function with two parameters is passed to the gsl_root_brent
class, which solves the equation. One of the parameters is member
data, and the other is specified using the extra parameter argument
to the function.
*/

#include <o2scl/funct.h>
#include <o2scl/gsl_root_brent.h>
#include <o2scl/test_mgr.h>

using namespace std;
using namespace o2scl;

class my_class {
private:
    double parameter;

public:

```

```

void set_parameter() { parameter=0.01; }

// A function demonstrating the different ways of implementing
// function parameters
double function_to_solve(double x, double &p) {
    return atan((x-parameter)*4)*(1.0+sin((x-parameter)*50.0)/p);
}

};

// Simple code to write the function to a file
int write_file(double sol);

int main(void) {

    cout.setf(ios::scientific);

    test_mgr t;
    // Only print something out if one of the tests fails
    t.set_output_level(1);

    // The solver, specifying the type of the parameter (double)
    // and the function type (funct<double>)
    gsl_root_brent<> solver;

    my_class c;
    c.set_parameter();

    double p=1.1;

    // This is the code that allows specification of class member
    // functions as functions to solve. This approach avoids the use of
    // static variables and functions and multiple inheritance at the
    // expense of a little overhead. We need to provide the address of
    // an instantiated object and the address of the member function.
    funct_mfptr_param<my_class,double>
        function(&c,&my_class::function_to_solve,p);

    double x1=-1;
    double x2=2;

    // The value verbose=1 prints out iteration information
    // and verbose=2 requires a keypress between iterations.
    solver.verbose=1;
    solver.solve_bkt(x1,x2,function);

    // This is actually a somewhat difficult function to solve because
    // of the sinusoidal behavior.
    cout << "Solution: " << x1
         << " Function value: " << c.function_to_solve(x1,p) << endl;

    // Write the function being solved to a file (see source code
    // in examples directory for details)
    write_file(x1);

    // Obtain and summarize test results
    t.test_abs(c.function_to_solve(x1,p),0.0,1.0e-10,"ex_fptr");
    t.report();

    return 0;
}
// End of example

```



## 13 Data Tables

The class `table` is a container to hold and perform operations on related columns of data. It supports column operations, interpolation, column reference by either name or index, binary searching (in the case of ordered columns), sorting, and fitting two columns to a user-specified function.

## 14 String Manipulation

There are a couple classes and functions to help manipulate strings of text. Conversion routines for `std::string` objects are given in `string_conv.h` and include

- `ptos()` - pointer to string
- `itos()` - integer to string
- `dtos()` - double to string
- `stoi()` - string to integer
- `stod()` - string to double

See also `size_of_exponent()` and `double_to_ieee_string()`.

The `columnify` class converts a set of strings into nicely formatted columns by padding with the necessary amount of spaces. This class operates on string objects of type `std::string`, and also works well for formatting columns of floating-point numbers. This class is used to provide output for matrices in the functions `matrix_out()`, `matrix_out_paren()`, and `matrix_cx_out_paren()`. For output of vectors, see `vector_out()` in `array.h`.

The `format_float` class will reformat double precision numbers into a form appropriate for HTML or LaTeX documents.

A related function, `screenify()`, reformats a column of strings into many columns stored row-by-row in a new string array. It operates very similar to the way the classic Unix command `ls` organizes files and directories in multiple columns in order to save screen space.

The function `count_words()` counts the number of "words" in a string, which are delimited by whitespace.

## 15 Differentiation

Differentiation is performed by descendants of `deriv` and the classes are provided. These allow one to calculate either first, second, and third derivatives. The GSL approach is used in `gsl_deriv`, and the CERNLIB routine is used in `cern_deriv`. Both of these compute derivatives for a function specified using a descendant of `funct`. For functions which are tabulated over equally-spaced abscissas, the class `eqi_deriv` is provided which applies the formulas from Abramowitz and Stegun at a specified order. The class `cern_deriv` is slower and sometimes more accurate, but also fails more often than `gsl_deriv`, which never calls the error handler.

**Warning:** For `gsl_deriv` and `cern_deriv`, the second and third derivatives are calculated by naive repeated application of the code for the first derivative and can be particularly troublesome if the function is not sufficiently smooth. Error estimation is not provided for second and third derivatives.

### 15.1 Numerical differentiation

This example computes first and second derivatives of

$$y(x) = \sin(2x) + \frac{1}{2}$$

with both `gsl_deriv` and `cern_deriv`.

```

/* Example: ex_deriv.cpp
-----
An example to demonstrate numerical differentiation
*/

#include <cmath>
#include <o2scl/test_mgr.h>
#include <o2scl/funct.h>
#include <o2scl/ovector_tlate.h>
#include <o2scl/gsl_deriv.h>
#include <o2scl/cern_deriv.h>

using namespace std;
using namespace o2scl;

class cl {

public:

    // This is the function we'll take the derivative of
    double function(double x) {
        return sin(2.0*x)+0.5;
    }
};

int main(void) {

    test_mgr t;
    t.set_output_level(2);

    // The class and associated function
    cl acl;
    funct_mfptr<cl> f1(&acl,&cl::function);

    gsl_deriv<> gd;
    // Note that the GSL derivative routine requires an initial stepsize
    gd.h=1.0e-3;
    cern_deriv<> cd;

    // Compute the first derivative using the gsl_deriv class and
    // verify that the answer is correct
    double d1=gd.calc(1.0,f1);
    t.test_rel(d1,2.0*cos(2.0),1.0e-10,"gsl_deriv");

    // Compute the first derivative using the cern_deriv class and
    // verify that the answer is correct
    double d2=cd.calc(1.0,f1);
    t.test_rel(d2,2.0*cos(2.0),1.0e-10,"cern_deriv");

    // Compute the second derivative also
    double d3=gd.calc2(1.0,f1);
    t.test_rel(d3,-4.0*sin(2.0),5.0e-7,"gsl_deriv");

    double d4=cd.calc2(1.0,f1);
    t.test_rel(d4,-4.0*sin(2.0),1.0e-8,"cern_deriv");

    t.report();
    return 0;
}
// End of example

```

## 16 Integration

## 16.1 One-dimensional integration

Several classes integrate arbitrary one-dimensional functions

- Integration over a finite interval: `cern_adapt`, `cern_gauss`, `cern_gauss56`, `gsl_inte_qag`, and `gsl_inte_qng`.
- Integration from 0 to  $\infty$ : `gsl_inte_qagiu`
- Integration from  $-\infty$  to 0: `gsl_inte_qagil`
- Integration from  $-\infty$  to  $\infty$ : `gsl_inte_qagi`
- Integration over a finite interval for a function with singularities: `gsl_inte_qags` (see also `gsl_inte_qaws`).
- Cauchy principal value integration over a finite interval: `cern_cauchy` and `gsl_inte_qawc`
- Integration over a function weighted by  $\cos(x)$  or  $\sin(x)$ : `gsl_inte_qawo_cos` and `gsl_inte_qawo_sin`
- Fourier integrals: `gsl_inte_qawf_cos` and `gsl_inte_qawf_sin`
- Integration over a weight function

$$W(x) = (x-a)^\alpha (b-x)^\beta \log^\mu(x-a) \log^\nu(b-x)$$

is performed by `gsl_inte_qaws`.

All of these classes are children of `inte`, and the relative and absolute tolerances are stored in `inte::tol_rel` and `inte::tol_abs`, respectively.

## 16.2 GSL-based integration routines

For the GSL-based integration routines, the variables `inte::tol_abs` and `inte::tol_rel` have the same role as the quantities usually denoted in the GSL integration routines by `epsabs` and `epsrel`. In particular, the integration classes attempt to ensure that

$$|\text{result} - I| \leq \text{Max}(\text{tolx}, \text{tolf}|I|)$$

and returns an error to attempt to ensure that

$$|\text{result} - I| \leq \text{abserr} \leq \text{Max}(\text{tolx}, \text{tolf}|I|)$$

where  $I$  is the integral to be evaluated. Even when the corresponding descendant of `inte::integ()` returns success, these inequalities may fail for sufficiently difficult functions. All of the GSL integration routines except for `gsl_inte_qng` use a workspace given in `gsl_inte_table` which holds the results of the various subdivisions of the original interval. The size of this workspace (and thus then number of subdivisions) can be controlled with `gsl_inte_table::set_workspace()`.

The GSL routines were originally based on QUADPACK, which is available at <http://www.netlib.org/quadpack>.

For adaptive GSL integration classes, the type of Gauss-Kronrod quadrature rule that is used to approximate the integral and estimate the error of a subinterval is set by `gsl_inte_kronrod::set_rule()`.

There are two competing factors that can slow down an adaptive integration algorithm: (1) each evaluation of the integrand can be numerically expensive, depending on how the function is defined, and (2) the process of subdividing regions and recalculating values is almost always numerically expensive in its own right. For integrands that are very smooth (e.g., analytic functions), a high-order Gauss-Kronrod rule (e.g., 61-point) will achieve the desired error tolerance with relatively few subdivisions. For integrands with discontinuities or singular derivatives, a low-order rule (e.g., 15-point) is often more efficient.

The number of subdivisions of the integration region is limited by the size of the workspace, set in `gsl_inte_kronrod::set_limit()`. The number of subdivisions required for the most recent call to `inte::integ()` or `inte::integ_err()` is given in `inte::last_iter`. This number will always be less than or equal to the workspace size.

### Note

The GSL integration routines can sometimes lose precision if the integrand is everywhere much smaller than unity. Some rescaling is required in these cases.

## 16.3 GSL-based integration error messages

The error messages given by the adaptive GSL integration routines tend to follow a standard form and are documented here. - There are several error messages which indicate improper usage and cause the error handler to be called regardless of the value of `inte::err_nonconv` :

- "Iteration limit exceeds workspace in `class::function()` ." [gsl\_einval]
- "Could not integrate function in `class::function()` (it may have returned a non-finite result) ." [gsl\_efaield] This often occurs when the user-specified function returns `inf` or `nan`.
- "Tolerance cannot be achieved with given value of `tol_abs` and `tol_rel` in `class::function()` ." [gsl\_ebadtol]  
This occurs if the user supplies unreasonable values for `inte::tol_abs` and `inte::tol_rel`. All positive values for `inte::tol_abs` are allowed. If zero-tolerance for `inte::tol_abs` is desired, then `inte::tol_rel` must be at least  $50 \cdot \epsilon_{\text{mach}}$  ( $\approx 1.11 \times 10^{-14}$ ).
- "Cannot integrate with singularity on endpoint in `gsl_inte_qawc::qawc()` ." [gsl\_einval] The class `gsl_inte_qawc` cannot handle the case when a singularity is one of the endpoints of the integration.

There are also convergence errors which will call the error handler unless `inte::err_nonconv` is false:

- "Cannot reach tolerance because of roundoff error on first attempt in `class::function()` ." [gsl\_eround]  
Each integration attempt tests for round-off errors by comparing the computed integral with that of the integrand's absolute value (i.e.,  $L^1$ -norm). A highly oscillatory integrand may cause this error.
- "A maximum of 1 iteration was insufficient in `class::function()` ." [gsl\_emaxiter]  
This occurs if the workspace is allocated for one interval and a single Gauss-Kronrod integration does not yield the accuracy demanded by `inte::tol_abs` and `inte::tol_rel`.
- "Bad integrand behavior in `class::function()` ." [gsl\_esing]  
This occurs if the integrand is (effectively) singular in a region, causing the subdivided intervals to become too small for floating-point precision.
- "Maximum number of subdivisions 'value' reached in `class::function()` ." [gsl\_emaxiter]  
This occurs if the refinement algorithm runs out of allocated workspace. The number of iterations required for the most recent call to `inte::integ()` or `inte::integ_err()` is given in `inte::last_iter`. This number will always be less than or equal to the workspace size.
- "Roundoff error prevents tolerance from being achieved in `class::function()` ." [gsl\_eround]  
The refinement procedure counts round-off errors as they occur and terminates if too many such errors accumulate.
- "Roundoff error detected in extrapolation table in `gsl_inte_singular::qags()` ." [gsl\_eround]  
This occurs when error-terms from the  $\epsilon$ -algorithm are monitored and compared with the error-terms from the refinement procedure. The algorithm terminates if these sequences differ by too many orders of magnitude. See `gsl_inte_singular::qelg()`.
- "Integral is divergent or slowly convergent in `gsl_inte_singular::qags()` ." [gsl\_ediverge]  
This occurs if the approximations produced by the refinement algorithm and the extrapolation algorithm differ by too many orders of magnitude.
- "Exceeded limit of trigonometric table in `gsl_inte_qawo_sin()::qawo()` ." [gsl\_etable]  
This occurs if the maximum **level** of the table of Chebyshev moments is reached.

## 16.4 Multi-dimensional integration routines

Multi-dimensional hypercubic integration is performed by `composite_inte`, the sole descendant of `multi_inte`. `composite_inte` allows you to specify a set of one-dimensional integration routines (objects of type `inte`) and apply them to a multi-dimensional problem.

General multi-dimensional integration is performed by `comp_gen_inte`, the sole descendant of `gen_inte`. The user is allowed to specify a upper and lower limits which are functions of the variables for integrations which have not yet been performed, i.e. the  $n$ -dimensional integral

$$\int_{x_0=a_0}^{x_0=b_0} f(x_0) \int_{x_1=a_1(x_0)}^{x_1=b_1(x_0)} f(x_0, x_1) \dots \int_{x_{n-1}=a_{n-1}(x_0, x_1, \dots, x_{n-2})}^{x_{n-1}=b_{n-1}(x_0, x_1, \dots, x_{n-2})} f(x_0, x_1, \dots, x_{n-1}) dx_{n-1} \dots dx_1 dx_0$$

Again, one specifies a set of `inte` objects to apply to each variable to be integrated over.

Monte Carlo integration is also provided (see [Monte Carlo Integration](#)).

## 16.5 Integration Example

This example computes the integral  $\int_{-\infty}^{\infty} e^{-x^2} dx$  with `gsl_inte_qagi`, the integral  $\int_0^{\infty} e^{-x^2} dx$  with `gsl_inte_qagiu`, the integral  $\int_{-\infty}^0 e^{-x^2} dx$  with `gsl_inte_qagil`, and the integral  $\int_0^1 [\sin(2x) + \frac{1}{2}] dx$  with both `gsl_inte_qag` and `cern_adapt`, and compares the computed results with the exact results.

```
/* Example: ex_inte.cpp
-----
An example to demonstrate numerical integration.
*/

#include <cmath>
#include <o2scl/test_mgr.h>
#include <o2scl/constants.h>
#include <o2scl/funct.h>
#include <o2scl/gsl_inte_qag.h>
#include <o2scl/gsl_inte_qagi.h>
#include <o2scl/gsl_inte_qagiu.h>
#include <o2scl/gsl_inte_qagil.h>
#include <o2scl/cern_adapt.h>

using namespace std;
using namespace o2scl;
using namespace o2scl_const;

class cl {

public:

    // We'll use this to count the number of function
    // evaluations required by the integration routines
    int nf;

    // A function to be integrated
    double integrand(double x) {
        nf++;
        return exp(-x*x);
    }

    // Another function to be integrated
    double integrand2(double x) {
        nf++;
        return sin(2.0*x)+0.5;
    }
};

int main(void) {
    cl acl;
    test_mgr t;
```

```

t.set_output_level(1);

funct_mfptr<cl> f1(&acl,&cl::integrand);
funct_mfptr<cl> f2(&acl,&cl::integrand2);

// We don't need to specify the function type in the integration
// objects, because we're using the default function type (type
// funct).
gsl_inte_qag<> g;
gsl_inte_qagi<> gi;
gsl_inte_qagiu<> gu;
gsl_inte_qagil<> gl;
cern_adapt<> ca;

// The result and the uncertainty
double res, err;

// An integral from -infinity to +infinity (the limits are ignored)
acl.nf=0;
int ret1=gi.integ_err(f1,0.0,0.0,res,err);
cout << "gsl_inte_qagi: " << endl;
cout << "Return value: " << ret1 << endl;
cout << "Result: " << res << " Uncertainty: " << err << endl;
cout << "Number of iterations: " << gi.last_iter << endl;
cout << "Number of function evaluations: " << acl.nf << endl;
cout << endl;
t.test_rel(res,sqrt(pi),1.0e-8,"inte 1");

// An integral from 0 to +infinity (the second limit argument is
// ignored in the line below)
acl.nf=0;
gu.integ_err(f1,0.0,0.0,res,err);
cout << "gsl_inte_qagiu: " << endl;
cout << "Return value: " << ret1 << endl;
cout << "Result: " << res << " Uncertainty: " << err << endl;
cout << "Number of iterations: " << gu.last_iter << endl;
cout << "Number of function evaluations: " << acl.nf << endl;
cout << endl;
t.test_rel(res,sqrt(pi)/2.0,1.0e-8,"inte 2");

// An integral from -infinity to zero (the first limit argument is
// ignored in the line below)
acl.nf=0;
gl.integ_err(f1,0.0,0.0,res,err);
cout << "gsl_inte_qagil: " << endl;
cout << "Return value: " << ret1 << endl;
cout << "Result: " << res << " Uncertainty: " << err << endl;
cout << "Number of iterations: " << gl.last_iter << endl;
cout << "Number of function evaluations: " << acl.nf << endl;
cout << endl;
t.test_rel(res,sqrt(pi)/2.0,1.0e-8,"inte 3");

// An integral from 0 to 1 with the GSL integrator
acl.nf=0;
g.integ_err(f2,0.0,1.0,res,err);
cout << "gsl_inte_qag: " << endl;
cout << "Return value: " << ret1 << endl;
cout << "Result: " << res << " Uncertainty: " << err << endl;
cout << "Number of iterations: " << g.last_iter << endl;
cout << "Number of function evaluations: " << acl.nf << endl;
cout << endl;
t.test_rel(res,0.5+sin(1.0)*sin(1.0),1.0e-8,"inte 4");

// The same integral with the CERNLIB integrator
acl.nf=0;
ca.integ_err(f2,0.0,1.0,res,err);
cout << "cern_adapt: " << endl;
cout << "Return value: " << ret1 << endl;
cout << "Result: " << res << " Uncertainty: " << err << endl;

```

```

cout << "Number of iterations: " << ca.last_iter << endl;
cout << "Number of function evaluations: " << acl.nf << endl;
cout << endl;
t.test_rel(res, 0.5*sin(1.0)*sin(1.0), 1.0e-8, "inte 5");

t.report();
return 0;
}
// End of example

```

## 17 Roots of Polynomials

Classes are provided for solving quadratic, cubic, and quartic equations as well as general polynomials. There is a standard nomenclature: classes which handle polynomials with real coefficients and real roots end with the suffix `_real` ([quadratic\\_real](#), [cubic\\_real](#) and [quartic\\_real](#)), classes which handle real coefficients and complex roots end with the suffix `_real_coeff` ([quadratic\\_real\\_coeff](#), [cubic\\_real\\_coeff](#), [quartic\\_real\\_coeff](#), and [poly\\_real\\_coeff](#)), and classes which handle complex polynomials with complex coefficients end with the suffix `_complex` ([quadratic\\_complex](#), [cubic\\_complex](#), [quartic\\_complex](#), and [poly\\_complex](#)). As a reminder, complex roots may not occur in conjugate pairs if the coefficients are not real. Most of these routines will return an error if the leading coefficient is zero.

In the public interfaces to the polynomial solvers, the complex type `std::complex<double>` is used. These can be converted to and from the GSL complex type using the [complex\\_to\\_gsl\(\)](#) and [gsl\\_to\\_complex\(\)](#) functions.

For quadratics, [gsl\\_quadratic\\_real\\_coeff](#) is the best if the coefficients are real, while if the coefficients are complex, use [quadratic\\_std\\_complex](#). For cubics with real coefficients, [cern\\_cubic\\_real\\_coeff](#) is the best, while if the coefficients are complex, use [cubic\\_std\\_complex](#).

For a quartic polynomial with real coefficients, [cern\\_quartic\\_real\\_coeff](#) is the best, unless the coefficients of odd powers happen to be small, in which case, [gsl\\_quartic\\_real2](#) tends to work better. For quartics, generic polynomial solvers such as [gsl\\_poly\\_real\\_coeff](#) can provide more accurate (but slower) results. If the coefficients are complex, then you can use [simple\\_quartic\\_complex](#).

### 17.1 Polynomial solver example

This example shows how to find the roots of the second-, third-, fourth-, and fifth-order Chebyshev polynomials

$$\begin{aligned}
 &2x^2 - 1 \\
 &4x^3 - 3x \\
 &8x^4 - 8x^2 + 1 \\
 &16x^5 - 20x^3 + 5x
 \end{aligned}$$

For the Chebyshev polynomial of order  $n$ , the roots are given by

$$\cos \left[ \frac{\pi(k-1/2)}{n} \right]$$

for  $k = 1, \dots, n$ . These roots are used in [gsl\\_chebapp](#) to approximate functions using Chebyshev polynomials.

```

/* Example: ex_poly.cpp
-----
Demonstrate the solution of the Chebyshev polynomials
*/

#include <o2scl/poly.h>
#include <o2scl/ovector_tlate.h>
#include <o2scl/vector.h>
// For pi
#include <o2scl/constants.h>
#include <o2scl/test_mgr.h>

```

```

using namespace std;
using namespace o2scl;
using namespace o2scl_const;

int main(void) {

    cout.setf(ios::scientific);
    cout.setf(ios::showpos);

    test_mgr t;
    t.set_output_level(1);

    // Quadratic solver
    gsl_quadratic_real_coeff quad;
    // Cubic solver
    cern_cubic_real_coeff cubic;
    // Quartic solver
    cern_quartic_real_coeff quart;
    // Generic polynomial solver
    gsl_poly_real_coeff gen;

    // Storage for the roots
    ovector v(5);
    double d;
    std::complex<double> ca[5];

    // The second order polynomial
    cout << "Second order roots: " << endl;
    quad.solve_r(2.0,0.0,-1.0,v[0],v[1]);

    // Sort the roots and compare with the exact results
    vector_sort<ovector,double>(2,v);
    for(size_t i=0;i<2;i++) {
        double exact=cos(pi*(((double) (2-i))-0.5)/2.0);
        cout << v[i] << " " << exact << endl;
        t.test_abs(v[i],exact,1.0e-14,"2nd order");
    }
    cout << endl;

    // The third order polynomial
    cout << "Third order roots: " << endl;
    cubic.solve_rc(4.0,0.0,-3.0,0.0,v[0],ca[0],ca[1]);

    // Sort the roots and compare with the exact results
    v[1]=ca[0].real();
    v[2]=ca[1].real();
    vector_sort<ovector,double>(3,v);
    for(size_t i=0;i<3;i++) {
        double exact=cos(pi*(((double) (3-i))-0.5)/3.0);
        cout << v[i] << " " << exact << endl;
        if (i==1) {
            t.test_abs(v[i],exact,1.0e-14,"3rd order");
        } else {
            t.test_abs(v[i],exact,1.0e-14,"3rd order");
        }
    }
    cout << endl;

    // The fourth order polynomial
    cout << "Fourth order roots: " << endl;
    quart.solve_rc(8.0,0.0,-8.0,0.0,1.0,ca[0],ca[1],ca[2],ca[3]);

    // Sort the roots and compare with the exact results
    for(size_t i=0;i<4;i++) v[i]=ca[i].real();
    vector_sort<ovector,double>(4,v);
    for(size_t i=0;i<4;i++) {
        double exact=cos(pi*(((double) (4-i))-0.5)/4.0);
        cout << v[i] << " " << exact << endl;
        t.test_abs(v[i],exact,1.0e-14,"4th order");
    }
}

```



```

}
cout << endl;

// The fifth order polynomial
cout << "Fifth order roots: " << endl;
double co[6]={16.0,0.0,-20.0,0.0,5.0,0.0};
gen.solve_rc(5,co,ca);

// Sort the roots and compare with the exact results
for(size_t i=0;i<5;i++) v[i]=ca[i].real();
vector_sort<ovector,double>(5,v);
for(size_t i=0;i<5;i++) {
    double exact=cos(pi*((double)(5-i))-0.5)/5.0);
    cout << v[i] << " " << exact << endl;
    t.test_abs(v[i],exact,1.0e-14,"5th order");
}
cout << endl;

t.report();
return 0;
}
// End of example

```

## 18 Equation Solving

### 18.1 One-dimensional solvers

Solution of one equation in one variable is accomplished by children of the class `root`.

For one-dimensional solving, use `cern_root` or `gsl_root_brent` if you have the root bracketed, or `gsl_root_stef` if you have the derivative available. If you have neither a bracket or a derivative, you can use `cern_mroot_root`.

The `root` base class provides the structure for three different solving methods:

- `root::solve()` which solves a function given an initial guess  $x$
- `root::solve_bkt()` which solves a function given a solution bracketed between  $x_1$  and  $x_2$ . The values of the function at  $x_1$  and  $x_2$  should have different signs.
- `root::solve_de()` which solves a function given an initial guess  $x$  and the derivative of the function  $df$ .

If not all of these three functions are overloaded, then the source code in the `root` base class is designed to try to automatically provide the solution using the remaining functions. Most of the one-dimensional solving routines, in their original form, are written in the second or third form above. For example, `gsl_root_brent` is originally a bracketing routine of the form `root::solve_bkt()`, but calls to either `root::solve()` or `root::solve_de()` will attempt to automatically bracket the function given the initial guess that is provided. Of course, it is frequently most efficient to use the solver in the way it was intended.

### 18.2 Multi-dimensional solvers

Solution of more than one equation is accomplished by descendants of the class `mroot`. The higher-level interface is provided by the function `mroot::msolve()`.

For multi-dimensional solving, you can use either `cern_mroot` or `gsl_mroot_hybrids`. While `cern_mroot` cannot utilize user-supplied derivatives, `gsl_mroot_hybrids` can use user-supplied derivative information (as in the GSL hybridsj method) using the function `gsl_mroot_hybrids::msolve_de()`.

## 18.3 Multi-dimensional solver

This demonstrates several ways of using the multi-dimensional solvers to solve the equations

$$\sin\left(x_0 - \frac{1}{4}\right) = 0$$

$$\sin\left(x_1 - \frac{1}{5}\right) = 0$$

```

/* Example: ex_mroot.cpp
-----
Several ways to use an O2scl solver to solve a simple function
*/

#include <cmath>
#include <o2scl/test_mgr.h>
#include <o2scl/mm_funct.h>
#include <o2scl/gsl_mroot_hybrids.h>
#include <o2scl/cern_mroot.h>

using namespace std;
using namespace o2scl;

int gfn(size_t nv, const ovector_base &x, ovector_base &y) {
    y[0]=sin(x[1]-0.2);
    y[1]=sin(x[0]-0.25);
    return 0;
}

typedef double arr_t[2];
typedef double mat_t[2][2];

class cl {
public:

    // Store the number of function and derivative evaluations
    int nf, nd;

    int mfn(size_t nv, const ovector_base &x, ovector_base &y) {
        y[0]=sin(x[1]-0.2);
        y[1]=sin(x[0]-0.25);
        nf++;
        return 0;
    }

    int operator()(size_t nv, const ovector_base &x, ovector_base &y) {
        y[0]=sin(x[1]-0.2);
        y[1]=sin(x[0]-0.25);
        nf++;
        return 0;
    }

    int mfnd(size_t nv, ovector_base &x, ovector_base &y, omatrix_base &j) {
        j[0][0]=0.0;
        j[0][1]=cos(x[1]-0.2);
        j[1][0]=cos(x[0]-0.25);
        j[1][1]=0.0;
        nd++;
        return 0;
    }

    int mfna(size_t nv, const arr_t &x, arr_t &y) {
        y[0]=sin(x[1]-0.2);
        y[1]=sin(x[0]-0.25);
        return 0;
    }
}

```

```

int mfnad(size_t nv, arr_t &x, arr_t &y, mat_t &j) {
    j[0][0]=0.0;
    j[0][1]=cos(x[1]-0.2);
    j[1][0]=cos(x[0]-0.25);
    j[1][1]=0.0;
    return 0;
}

};

int main(void) {
    cl acl;
    ovector x(2);
    double xa[2];
    int i;
    size_t tmp;
    int r1, r2, r3;
    bool done;
    test_mgr t;

    t.set_output_level(1);

    /*
     * Using a member function with \ref ovector objects
     */
    mm_funct_mfp_ptr<cl> f1(&acl,&acl::mfn);
    gsl_mroot_hybrids<> cr1;

    x[0]=0.5;
    x[1]=0.5;
    acl.nf=0;
    int ret1=cr1.solve(2,x,f1);
    cout << "GSL solver (numerical Jacobian): " << endl;
    cout << "Return value: " << ret1 << endl;
    cout << "Number of iterations: " << cr1.last_ntrial << endl;
    cout << "Number of function evaluations: " << acl.nf << endl;
    cout << endl;
    t.test_rel(x[0],0.25,1.0e-6,"1a");
    t.test_rel(x[1],0.2,1.0e-6,"1b");

    /*
     * Using the CERNLIB solver
     */
    cern_mroot<> cr2;

    x[0]=0.5;
    x[1]=0.5;
    acl.nf=0;
    int ret2=cr2.solve(2,x,f1);
    cout << "CERNLIB solver (numerical Jacobian): " << endl;
    cout << "Return value: " << ret2 << endl;
    cout << "INFO parameter: " << cr2.get_info() << endl;
    cout << "Number of function evaluations: " << acl.nf << endl;
    cout << endl;
    t.test_rel(x[0],0.25,1.0e-6,"2a");
    t.test_rel(x[1],0.2,1.0e-6,"2b");

    /*
     * Using a member function with \ref ovector objects, but
     * using the GSL-like interface with set() and iterate().
     */
    gsl_mroot_hybrids<> cr3;

    x[0]=0.5;
    x[1]=0.5;
    cr3.allocate(2);
    cr3.set(2,x,f1);
    done=false;
    do {
        r3=cr3.iterate();

```

---

```

    double resid=fabs(cr3.f[0])+fabs(cr3.f[1]);
    if (resid<cr3.tol_rel || r3>0) done=true;
} while (done==false);
t.test_rel(cr3.x[0],0.25,1.0e-6,"3a");
t.test_rel(cr3.x[1],0.2,1.0e-6,"3b");
cr3.free();

/*
   Now instead of using the automatic Jacobian, using
   a user-specified Jacobian.
*/
jac_funct_mfp_ptr<cl,ovector_base,omatrix_base> j4(&acl,&cl::mfnd);

x[0]=0.5;
x[1]=0.5;
acl.nf=0;
acl.nd=0;
int ret4=cr1.msolve_de(2,x,f1,j4);
cout << "GSL solver (analytic Jacobian): " << endl;
cout << "Return value: " << ret4 << endl;
cout << "Number of iterations: " << cr1.last_ntrial << endl;
cout << "Number of function evaluations: " << acl.nf << endl;
cout << "Number of Jacobian evaluations: " << acl.nd << endl;
cout << endl;
t.test_rel(x[0],0.25,1.0e-6,"4a");
t.test_rel(x[1],0.2,1.0e-6,"4b");

/*
   Using a user-specified Jacobian and the GSL-like interface
*/
gsl_mroot_hybrids<> cr5;

x[0]=0.5;
x[1]=0.5;
cr5.allocate(2);
cr5.set_de(2,x,f1,j4);
done=false;
do {
    r3=cr5.iterate();
    double resid=fabs(cr5.f[0])+fabs(cr5.f[1]);
    if (resid<cr5.tol_rel || r3>0) done=true;
} while (done==false);
t.test_rel(cr5.x[0],0.25,1.0e-6,"5a");
t.test_rel(cr5.x[1],0.2,1.0e-6,"5b");
cr5.free();

/*
   Using C-style arrays instead of ovector objects
*/
mm_funct_mfp_ptr<cl,arr_t> f6(&acl,&cl::mfna);
gsl_mroot_hybrids<mm_funct_mfp_ptr<cl,arr_t>,arr_t,
    arr_t,array_alloc<arr_t> > cr6;

xa[0]=0.5;
xa[1]=0.5;
cr6.msolve(2,xa,f6);
t.test_rel(xa[0],0.25,1.0e-6,"6a");
t.test_rel(xa[1],0.2,1.0e-6,"6b");

/*
   Using the CERNLIB solver with C-style arrays instead of ovector objects
*/
cern_mroot<mm_funct_mfp_ptr<cl,arr_t>,arr_t,
    arr_t,array_alloc<arr_t> > cr7;

xa[0]=0.5;
xa[1]=0.5;
cr7.msolve(2,xa,f6);
t.test_rel(xa[0],0.25,1.0e-6,"7a");
t.test_rel(xa[1],0.2,1.0e-6,"7b");

```

```

/*
  Using C-style arrays with a user-specified Jacobian
*/
jac_funct_mfp_ptr<cl, arr_t, mat_t> j8(&acl, &cl::mfnd);
gsl_mroot_hybrids<mm_funct_mfp_ptr<cl, arr_t>, arr_t,
  arr_t, array_alloc<arr_t>, mat_t, mat_t,
  array_2d_alloc<mat_t>, jac_funct<arr_t, mat_t> > cr8;

xa[0]=0.5;
xa[1]=0.5;
cr8.msolve_de(2, xa, f6, j8);
t.test_rel(xa[0], 0.25, 1.0e-6, "8a");
t.test_rel(xa[1], 0.2, 1.0e-6, "8b");

/*
  Using a class with an operator(). Note that there can be only one
  operator() function in each class.
*/
gsl_mroot_hybrids<cl> cr9;

x[0]=0.5;
x[1]=0.5;
cr9.msolve(2, x, acl);
t.test_rel(x[0], 0.25, 1.0e-6, "9a");
t.test_rel(x[1], 0.2, 1.0e-6, "9b");

/*
  Using a function pointer to a global function.
*/
typedef int (*gfnt)(size_t, const ovector_base &, ovector_base &);
gsl_mroot_hybrids<gfnt> cr10;
gfnt f10=&gfn;

x[0]=0.5;
x[1]=0.5;
cr10.msolve(2, x, f10);
t.test_rel(x[0], 0.25, 1.0e-6, "10a");
t.test_rel(x[1], 0.2, 1.0e-6, "10b");

t.report();
return 0;
}
// End of example

```

## 19 Minimization

One-dimensional minimization is performed by descendants of [minimize](#). There are two one-dimensional minimization algorithms, [cern\\_minimize](#) and [gsl\\_min\\_brent](#), and they are both bracketing algorithms type where an interval and an initial guess must be provided. If only an initial guess and no bracket is given, these two classes will attempt to find a suitable bracket from the initial guess. While the [minimize](#) base class is designed to allow future descendants to optionally use derivative information, this is not yet supported for any one-dimensional minimizers.

Multi-dimensional minimization is performed by descendants of [multi\\_min](#): [gsl\\_mmin\\_simp2](#), [gsl\\_mmin\\_conp](#), [gsl\\_mmin\\_conf](#), and [gsl\\_mmin\\_bfgs2](#). (The class [gsl\\_mmin\\_simp2](#) has been updated with the new "simplex2" method from GSL-1.12. The older "simplex" method is also available in [gsl\\_mmin\\_simp](#).) The classes [gsl\\_mmin\\_simp](#) and [gsl\\_mmin\\_simp2](#) do not require any derivative information. The remaining minimization classes are intended for use when the gradient of the function is available, but they can also automatically compute the gradient numerically. The standard way to provide the gradient is to use a child of [mm\\_funct](#). Finally, the user may specify the automatic gradient object of type [gradient](#) which is used by the minimizer to compute the gradient numerically when a function is not specified.

Generally, when a closed expression is available for the gradient, the [gsl\\_mmin\\_conp](#), [gsl\\_mmin\\_conf](#), and [gsl\\_mmin\\_bfgs2](#) are probably better. The simplex methods are somewhat robust for sufficiently difficult functions, though restarts are sometimes required

to find the correct minimum.

See an example for the usage of the multi-dimensional minimizers in the [Multidimensional minimizer](#) example.

Simulated annealing methods are also provided for multi-dimensional minimization (see [Simulated Annealing](#)).

It is important to note that not all of the minimization routines test the second derivative to ensure that it doesn't vanish to ensure that we have indeed found a true minimum.

The class `multi_min_fix` provides a convenient way of fixing some of the parameters and minimizing over others, without requiring a the function interface to be rewritten. An example is given in the [Minimizer fixing variables](#) example.

## 19.1 Multidimensional minimizer

This example uses the O2scl minimizers based on GSL to minimize a rather complicated three-dimensional function which has constant level surfaces which look like springs oriented along the z-axis. This example function, originally created here for O2scl, was added later to the GSL library minimization test functions.

```

/* Example: ex_mmin.cpp
-----
Example usage of the multidimensional minimizers with and without
gradients.
*/
#include <fstream>
#include <string>
#include <cmath>
#include <o2scl/test_mgr.h>
#include <o2scl/multi_funct.h>
#include <o2scl/constants.h>
#include <o2scl/gsl_mmin_simp2.h>
#include <o2scl/gsl_mmin_conf.h>
#include <o2scl/gsl_mmin_conp.h>
#include <o2scl/gsl_mmin_bfgs2.h>

using namespace std;
using namespace o2scl;

class cl {
public:

    cl() {
        param=30.0;
    }

    // To output function evaluations to a file
    ofstream fout;

    // Parameter of the quadratic
    double param;

    // Updated spring function
    double spring_two(size_t nv, const ovector_base &x) {
        double theta=atan2(x[1],x[0]);
        double r=sqrt(x[0]*x[0]+x[1]*x[1]);
        double z=x[2];
        double tmz=theta-z;
        double fact=8.0-pow(sin(tmz+o2scl_const::pi/2.0)+1.0,3.0);
        double rml=r-1.0;
        double ret=fact+exp(rml*rml)+z*z/param;
        fout << x << " " << ret << endl;
        return ret;
    }

    // Gradient of the spring function
    int sgrad(size_t nv, ovector_base &x, ovector_base &g) {

```

```

double theta=atan2(x[1],x[0]);
double r=sqrt(x[0]*x[0]+x[1]*x[1]);
double z=x[2];
double tmz=theta-z;
double rml=r-1.0;
double fact=8.0-pow(sin(tmz+o2scl_const::pi/2.0)+1.0,3.0);

double dtdx=-x[1]/r/r;
double dtdy=x[0]/r/r;
double drdx=x[0]/r;
double drdy=x[1]/r;
double dfdt=-3.0*pow(sin(tmz+o2scl_const::pi/2.0)+1.0,2.0)*
    cos(tmz+o2scl_const::pi/2.0);
double dfdz=2.0*z/param+3.0*pow(sin(tmz+o2scl_const::pi/2.0)+1.0,2.0)*
    cos(tmz+o2scl_const::pi/2.0);
double dfdr=2.0*rml*exp(rml*rml);

g[0]=dfdr*drdx+dfdt*dtdx;
g[1]=dfdr*drdy+dfdt*dtdy;
g[2]=dfdz;

return 0;
}

};

int main(void) {
    cl acl;
    ovector x(3);
    double fmin;
    test_mgr t;

    t.set_output_level(1);
    cout.setf(ios::scientific);

    // Using a member function with \ref ovector objects
    multi_funct_mfptr<cl> f1(&acl,&acl::spring_two);
    grad_funct_mfptr<cl> f1g(&acl,&acl::sgrad);

    gsl_mmin_simp2<> gm1;
    gsl_mmin_conf<> gm2;
    gsl_mmin_conp<> gm3;
    gsl_mmin_bfgs2<> gm4;

    // This function is difficult to minimize, so more trials
    // are required.
    gm1.ntrial*=10;
    gm2.ntrial*=10;
    gm3.ntrial*=10;
    gm4.ntrial*=10;

    // Simplex minimization
    acl.fout.open("ex_mmin1.dat");
    x[0]=1.0;
    x[1]=1.0;
    x[2]=7.0*o2scl_const::pi;
    gm1.mmin(3,x,fmin,f1);
    acl.fout.close();
    cout << gm1.last_ntrial << endl;
    cout << "Found minimum at: " << x << endl;
    t.test_rel(x[0],1.0,1.0e-4,"1a");
    t.test_rel(x[1],0.0,1.0e-4,"1b");
    t.test_rel(x[2],0.0,1.0e-4,"1c");

    // Fletcher-Reeves conjugate
    acl.fout.open("ex_mmin2.dat");
    x[0]=1.0;
    x[1]=0.0;
    x[2]=7.0*o2scl_const::pi;
    gm2.mmin(3,x,fmin,f1);

```

```

acl.fout.close();
cout << gm2.last_ntrial << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],1.0,4.0e-3,"2a");
t.test_rel(x[1],0.0,4.0e-3,"2b");
t.test_rel(x[2],0.0,4.0e-3,"2c");

// Fletcher-Reeves conjugate with gradients
acl.fout.open("ex_mmin2g.dat");
x[0]=1.0;
x[1]=0.0;
x[2]=7.0*o2scl_const::pi;
gm2.mmin_de(3,x,fmin,f1,flg);
acl.fout.close();
cout << gm2.last_ntrial << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],1.0,4.0e-3,"2a");
t.test_rel(x[1],0.0,4.0e-3,"2b");
t.test_rel(x[2],0.0,4.0e-3,"2c");

// Polak-Ribere conjugate
acl.fout.open("ex_mmin3.dat");
x[0]=1.0;
x[1]=0.0;
x[2]=7.0*o2scl_const::pi;
gm3.mmin(3,x,fmin,f1);
acl.fout.close();
cout << gm3.last_ntrial << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],1.0,4.0e-3,"3a");
t.test_rel(x[1],0.0,4.0e-3,"3b");
t.test_rel(x[2],0.0,4.0e-3,"3c");

// Polak-Ribere conjugate with gradients
acl.fout.open("ex_mmin3g.dat");
x[0]=1.0;
x[1]=0.0;
x[2]=7.0*o2scl_const::pi;
gm3.mmin_de(3,x,fmin,f1,flg);
acl.fout.close();
cout << gm3.last_ntrial << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],1.0,4.0e-3,"3a");
t.test_rel(x[1],0.0,4.0e-3,"3b");
t.test_rel(x[2],0.0,4.0e-3,"3c");

// BFGS method

// BFGS has trouble converging (especially to zero, since the
// minimum of x[0] is exactly at zero) if the derivative is not
// very accurate.
gm4.def_grad.epsrel=1.0e-8;

gm4.err_nonconv=false;
acl.fout.open("ex_mmin4.dat");
x[0]=1.0;
x[1]=0.0;
x[2]=7.0*o2scl_const::pi;
gm4.mmin(3,x,fmin,f1);
acl.fout.close();
cout << gm4.last_ntrial << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],1.0,1.0e-4,"4a");
t.test_rel(x[1],0.0,1.0e-4,"4b");
t.test_rel(x[2],0.0,1.0e-4,"4c");

t.report();
return 0;
}
// End of example

```



**Idea for Future** Plot the spring function

## 19.2 Minimizer fixing variables

This example uses the `multi_min_fix` class to minimize the function

$$y = (x_0 - 2)^2 + (x_1 - 1)^2 + x_2^2$$

while fixing some of the parameters.

```

/* Example: ex_mmin_fix.cpp
-----
Example usage of the mmin_fix class, which fixes some of the
parameters for a multidimensional minimization.
*/

#include <cmath>
#include <o2scl/test_mgr.h>
#include <o2scl/multi_funcnt.h>
#include <o2scl/gsl_mmin_simp2.h>
#include <o2scl/multi_min_fix.h>

using namespace std;
using namespace o2scl;

class cl {

public:

    double mfn(size_t nv, const ovector_base &x) {
        return (x[0]-2.0)*(x[0]-2.0) + (x[1]-1.0)*(x[1]-1.0) + x[2]*x[2];
    }

};

int main(void) {
    cl acl;
    ovector x(3);
    double fmin;
    test_mgr t;

    t.set_output_level(1);
    cout.setf(ios::scientific);

    /*
    Perform the minimization the standard way, with the
    simplex2 minimizer
    */
    multi_funcnt_mfptr<cl> f1(&acl, &cl::mfn);
    gsl_mmin_simp2<> gml;

    x[0]=0.5;
    x[1]=0.5;
    x[2]=0.5;
    gml.mmin(3, x, fmin, f1);
    cout << gml.last_ntrial << " iterations." << endl;
    cout << "Found minimum at: " << x << endl;
    t.test_rel(x[0], 2.0, 1.0e-4, "1a");
    t.test_rel(x[1], 1.0, 1.0e-4, "1b");
    t.test_rel(x[2], 0.0, 1.0e-4, "1c");

    // Create a new multi_min_fix object
    multi_min_fix<bool[3]> gmf;

```

```

// Create a base minimizer which can be used by the multi_min_fix
// object. Note that we can't use 'gm1' here, because it has a
// different type than 'gm2', even though its functionality is
// effectively the same.
gsl_mmin_simp2<multi_funct_mfptr<multi_min_fix<bool[3]>>> gm2;

// Set the base minimizer
gmf.set_mmin(gm2);

/*
  First perform the minimization as above.
*/
x[0]=0.5;
x[1]=0.5;
x[2]=0.5;
gmf.mmin(3,x,fmin,f1);
cout << gmf.last_ntrial << " iterations." << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],2.0,1.0e-4,"2a");
t.test_rel(x[1],1.0,1.0e-4,"2b");
t.test_rel(x[2],0.0,1.0e-4,"2c");

/*
  Now fix the 2nd variable, and re-minimize.
*/
bool fix[3]={false,true,false};
x[0]=0.5;
x[1]=0.5;
x[2]=0.5;
gmf.mmin_fix(3,x,fmin,fix,f1);
cout << gmf.last_ntrial << " iterations." << endl;
cout << "Found minimum at: " << x << endl;
t.test_rel(x[0],2.0,1.0e-4,"3a");
t.test_rel(x[1],0.5,1.0e-4,"3b");
t.test_rel(x[2],0.0,1.0e-4,"3c");

t.report();
return 0;
}
// End of example

```

## 20 Constrained Minimization

O<sub>2</sub>scl reimplements the Open Optimization Library (OOL) available at <http://ool.sourceforge.net>. The associated classes allow constrained minimization when the constraint can be expressed as a hyper-cubic constraint on all of the independent variables. The routines have been rewritten and reformatted for C++ in order to facilitate the use of member functions and user-defined vector types as arguments. The base class is `ool_constr_mmin` and there are two different constrained minimization algorithms implemented in `ool_mmin_pgrad`, `ool_mmin_spg`. (The `ool_mmin_gencan` minimizer is not yet finished). The O<sub>2</sub>scl implementation should be essentially identical to the most recently released version of OOL.

The constrained minimization classes operate in a similar way to the other multi-dimensional minimization classes (which are derived from `multi_min`). The constraints are specified with the function

```

ool_constr_mmin::set_constraints(size_t nc, vec_t &lower,
vec_t &upper);

```

and the minimization can be performed by calling either `multi_min::mmin()` or `multi_min::mmin_de()` (if the gradient is provided by the user). The method in `ool_mmin_gencan` requires a Hessian vector product and the user can specify this product for the minimization by using `ool_constr_mmin::mmin_hess()`. The Hessian product function can be specified as an object of type `ool_hfunct` in a similar way to the other function objects in O<sub>2</sub>scl.

There are five error codes defined in `ool_constr_mmin` which are specific to the classes derived from OOL.

The class `gsl_anneal` can handle some kinds of constraints by ignoring proposed steps which cause the user-specified function to

return a non-zero value.

Also, a simple way of implementing constraints is to add a function to the original which increases the value outside of the allowed region. This can be done with the functions `constraint()` and `lower_bound()`. There are two analogous functions, `cont_constraint()` and `cont_lower_bound()`, which continuous and differentiable versions. Where possible, it is better to use the constrained minimization routines described above.

## 20.1 Constrained minimization example

This example minimizes the function

$$f(x,y) = [x^2 \log(x) + 1] [\sqrt{y}(y-1) + 1]$$

which is undefined for  $x < 0$  and  $y < 0$ . The function is also minimized by `gsl_mmin_simp2`, which goes outside the allowed region where the function is undefined.

```
/* Example: ex_conmin.cpp
-----
This gives an example of the use of a constrained minimizer. This
code finds the global minimum of a two-dimensional function which
is not well-defined outside the region of interest.
*/
#include <gsl/gsl_math.h>
#include <gsl/gsl_blas.h>
#include <o2scl/test_mgr.h>
#include <o2scl/ool_mmin_spg.h>
#include <o2scl/gsl_mmin_simp2.h>

using namespace std;
using namespace o2scl;

double func(size_t nv, const ovector_base &x) {
    if (x[0]<0.0 || x[1]<0.0 || x[0]>100.0 || x[1]>100.0) {
        cout << "Outside constraint region." << endl;
    }
    double ret=(log(x[0])*x[0]*x[0]+1.0)*(sqrt(x[1])*(x[1]-1.0)+1.0);
    return ret;
}

int dfunc(size_t nv, ovector_base &x, ovector_base &g) {
    g[0]=(x[0]+2.0*x[0]*log(x[0]))*(sqrt(x[1])*(x[1]-1.0)+1.0);
    g[1]=(log(x[0])*x[0]*x[0]+1.0)*(sqrt(x[1])+(x[1]-1.0)/2.0/sqrt(x[1]));
    return 0;
}

int main(void) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

    static const size_t nv=2;

    // Specify the function to minimize and its gradient
    multi_func_ptr<> mff(func);
    grad_func_ptr<> gff(dfunc);

    // The unconstrained minimizer
    gsl_mmin_simp2<> gml;
    // The constrained minimizer
    ool_mmin_spg<> omp;

    // The constraints and the location of the minimum
    ovector c1(nv), c2(nv), x(nv);
    double fmin;

    cout << "Simple minimizer: " << endl;
```

```

// Initial guess
for(size_t i=0;i<nv;i++) {
    x[i]=10.0;
}

// Minimize
gml.mmin(nv,x,fmin,mff);
cout << endl;

cout << "Constrained minimizer: " << endl;

// Initial guess
for(size_t i=0;i<nv;i++) {
    x[i]=10.0;
}

// Set constraints
c1.set_all(1.0e-9);
c2.set_all(100.0);
omp.set_constraints(nv,c1,c2);

// Minimize
omp.mmin_de(nv,x,fmin,mff,gff);

// Output results
cout << x[0] << " " << x[1] << " " << fmin << endl;

// Test the constrained minimizer results
t.test_rel(x[0],0.60655,1.0e-4,"x0");
t.test_rel(x[1],1.0/3.0,1.0e-4,"x1");

t.report();
return 0;
}
// End of example

```

## 21 Monte Carlo Integration

Monte Carlo integration is performed by descendants of `mcarlo_inte` ([gsl\\_monte](#), [gsl\\_miser](#), and [gsl\\_vegas](#)). These routines are generally superior to the direct methods for integrals over regions with large numbers of spatial dimensions.

### 21.1 Monte Carlo Integration Example

This example computes the integral

$$\int_0^\pi \int_0^\pi \int_0^\pi \frac{1}{\pi^3} (1 - \cos x \cos y \cos z)^{-1}$$

and compares the result with the exact value, 1.3932039296.

```

/* Example: ex_minte.cpp
-----
An example to demonstrate multidimensional integration
*/

#include <o2scl/test_mgr.h>
#include <o2scl/multi_funct.h>
#include <o2scl/composite_inte.h>
#include <o2scl/gsl_inte_qng.h>
#include <o2scl/gsl_vegas.h>

/// For M_PI
#include <gsl/gsl_math.h>

```

```

using namespace std;
using namespace o2scl;

double test_fun(size_t nv, const ovector_base &x) {
    double y=1.0/(1.0-cos(x[0])*cos(x[1])*cos(x[2]))/M_PI/M_PI/M_PI;
    return y;
}

int main(void) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

    double exact=1.3932039296;
    double res;

    double err;

    gsl_vegas<multi_funct<> > gm;
    ovector a(3), b(3);
    a.set_all(0.0);
    b.set_all(M_PI);

    multi_funct_fptr<> tf(test_fun);

    gm.n_points=100000;
    gm.minteg_err(tf,3,a,b,res,err);

    cout << res << " " << exact << " " << (res-exact)/err << endl;
    t.test_rel(res,exact,err*10.0,"O2scl");

    t.report();

    return 0;
}
// End of example

```

## 22 Simulated Annealing

Minimization by simulated annealing is performed by descendants of [sim\\_anneal](#) (see [gsl\\_anneal](#)). Because simulated annealing is particularly well-suited to parallelization, a multi-threaded minimizer analogous to [gsl\\_anneal](#) is given in [anneal\\_mt](#). This header-only class uses the Boost libraries and requires it for use.

### 22.1 Simulated annealing

This example minimizes the function

$$f(x,y) = J_0(x-2)J_0(y+3)$$

over  $(x,y)$  where  $J_0(x)$  is the Bessel function given in `gsl_sf_bessel_J0`. The initial guess at (9,9) is several local minima away from the global minimum.

The plot below plots the function above, the initial guess, and the minimum obtained by the example program.

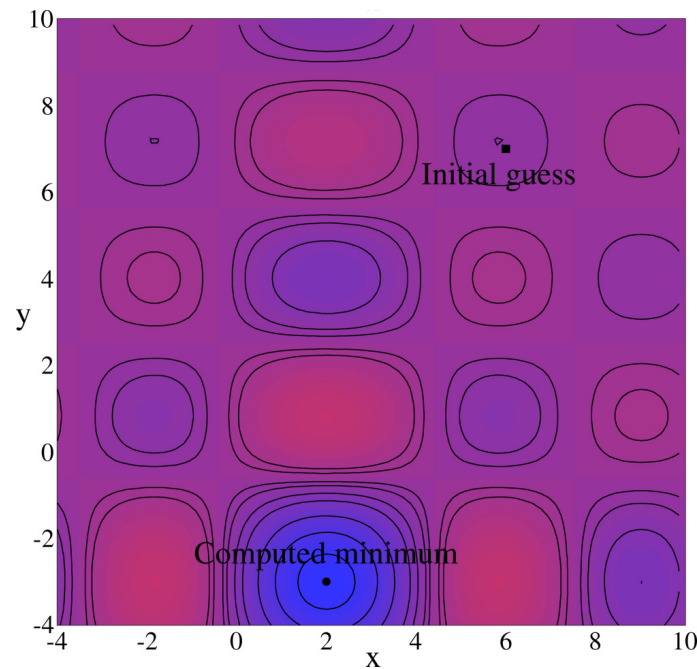


Figure 3: Simulated annealing example plot

```

/* Example: ex_anneal.cpp
-----
An example to demonstrate minimization by simulated annealing
*/

#include <iostream>
#include <cmath>
#include <gsl/gsl_sf_bessel.h>
#include <o2scl/ovector_tlate.h>
#include <o2scl/multi_funct.h>
#include <o2scl/funct.h>
#include <o2scl/gsl_anneal.h>
#include <o2scl/test_mgr.h>

using namespace std;
using namespace o2scl;

// A simple function with many local minima. A "greedy" minimizer
// would likely fail to find the correct minimum.
double function(size_t nvar, const ovector_base &x) {

    double a, b;
    a=(x[0]-2.0);
    b=(x[1]+3.0);

    // This is important to prevent the annealing algorithm to
    // random walk to infinity since the product of Bessel
    // functions is flat far from the origin
    if (fabs(x[0])>10.0 || fabs(x[1])>10.0) return 10.0;

    return -gsl_sf_bessel_J0(a)*gsl_sf_bessel_J0(b);
}

int main(int argc, char *argv[]) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

```

```

gsl_anneal<> ga;
double result;
ovector init(2);

multi_funct_fptr<> fx(function);

ga.ntrial=4000;
ga.verbose=1;
ga.tol_abs=1.0e-7;
ga.T_dec=1.1;

// Set a large initial step size
double step[1]={10.0};
ga.set_step(1,step);

// Choose an initial point at a local minimum away from
// the global minimum
init[0]=6.0;
init[1]=7.0;

// Perform the minimization
ga.mmin(2,init,result,fx);
cout << "x: " << init[0] << " " << init[1]
    << ", minimum function value: " << result << endl;
cout << endl;

// Test that it found the global minimum
t.test_rel(init[0],2.0,1.0e-3,"another test - value");
t.test_rel(init[1],-3.0,1.0e-3,"another test - value 2");
t.test_rel(result,-1.0,1.0e-3,"another test - min");

t.report();

return 0;
}
// End of example

```

## 23 Non-linear Least-Squares Fitting

Fitting is performed by descendants of [fit\\_base](#) and fitting functions can be specified using [fit\\_funct](#). The GSL fitting routines (scaled and unscaled) are implemented in [gsl\\_fit](#). A generic fitting routine using a minimizer object specified as a child of [multi\\_min](#) is implemented in [min\\_fit](#). When the [multi\\_min](#) object is (for example) a [sim\\_anneal](#) object, [min\\_fit](#) can avoid local minima which can occur when fitting noisy data.

## 24 Ordinary Differential Equations

Classes for non-adaptive integration are provided as descendants of [ode\\_step](#) and classes for adaptive integration are descendants of [adapt\\_step](#). To specify a set of functions to these classes, use a child of [ode\\_funct](#) for a generic vector type. The classes [gsl\\_rkf45](#) and [gsl\\_rkck](#) are reasonable general-purpose non-adaptive integrators and [gsl\\_astep](#) is a good general-purpose adaptive method for non-stiff problems. For stiff ODE's, use [gsl\\_bsimp](#) (see the [Stiff differential equations](#) example).

Solution of simple initial value problems is performed by [ode\\_iv\\_solve](#). This class uses an adaptive integrator (default is [gsl\\_astep](#)) and does some bookkeeping to simplify the solution of initial value problems. The [ode\\_iv\\_solve](#) class will give you only the final value of the functions at the endpoint, will provide the functions on a user-specified grid, or will tabulate the ODE solution for you using the grid chosen with the adaptive stepper. A example demonstrating the solution of initial value problems is given in the [Ordinary differential equations](#) example.

The solution of boundary-value problems is based on the abstract base class [ode\\_bv\\_solve](#). At the moment, a simple shooting method is the only implementation of this base class and is given in [ode\\_bv\\_shoot](#). An experimental multishooting class is given in [ode\\_bv\\_multishoot](#).

An application of linear solvers to solve finite-difference equations approximating a boundary value problem is given in [ode\\_iv\\_solve](#). A example demonstrating the iterative solution of a boundary value problem is given in the [Iterative solution of ODEs](#) example.

## 24.1 Ordinary differential equations

This example solves the differential equations defining the the Bessel and Airy functions with both the Cash-Karp and Prince--Dormand steppers. It demonstrates the use of [gsl\\_rkck](#), [gsl\\_rk8pd](#), [gsl\\_astep](#), and [ode\\_iv\\_solve](#).

The Bessel functions are defined by

$$y'' = \frac{1}{x^2} [y(\alpha^2 - x^2) - xy']$$

The Bessel functions of the first kind,  $J_\alpha(x)$  are finite at the origin, and the example solves the  $\alpha = 1$  case, where  $J_1(0) = 0$  and  $J_1'(0) = 1/2$ .

```

/* Example: ex_ode.cpp
-----
An example to demonstrate solving differential equations
*/

#include <gsl/gsl_sf_bessel.h>
#include <gsl/gsl_sf_airy.h>
#include <gsl/gsl_sf_gamma.h>
#include <o2scl/test_mgr.h>
#include <o2scl/ovector_tlate.h>
#include <o2scl/ode_funct.h>
#include <o2scl/gsl_rkck.h>
#include <o2scl/gsl_rk8pd.h>
#include <o2scl/gsl_astep.h>
#include <o2scl/ode_iv_solve.h>
#include <o2scl/table.h>
#ifdef O2SCL_HDF_IN_EXAMPLES
#include <o2scl/hdf_file.h>
#include <o2scl/hdf_io.h>
#endif

using namespace std;
using namespace o2scl;
#ifdef O2SCL_HDF_IN_EXAMPLES
using namespace o2scl_hdf;
#endif

// Differential equation defining the Bessel function. This assumes
// the second derivative at x=0 is 0 and thus only works for odd alpha.
int derivs(double x, size_t nv, const ovector_base &y,
           ovector_base &dydx, double &alpha) {
    dydx[0]=y[1];
    if (x==0.0) dydx[1]=0.0;
    else dydx[1]=(-x*y[1]+(-x*x+alpha*alpha)*y[0])/x/x;
    return 0;
}

// Differential equation defining the Airy function, Ai(x)
int derivs2(double x, size_t nv, const ovector_base &y,
            ovector_base &dydx, double &alpha) {
    dydx[0]=y[1];
    dydx[1]=y[0]*x;
    return 0;
}

int main(void) {

    cout.setf(ios::scientific);
    cout.setf(ios::showpos);

    // The independent variable and stepsize
    double x, dx=1.0e-1;

```



```

// The function and derivative values and the estimated errors
ovector y(2), dydx(2), yout(2), yerr(2), dydx_out(2);

test_mgr t;
t.set_output_level(1);

// The parameter for the Bessel function
double alpha=1.0;

// Specify the differential equations to solve
ode_funct_fptr_param<double,ovector_base> od(derivs,alpha);
ode_funct_fptr_param<double,ovector_base> od2(derivs2,alpha);

// The basic ODE steppers
gsl_rkck<> ode;
gsl_rk8pd<> ode2;

// -----
// Store the results in tables

table tab[8];
tab[0].line_of_names("x calc exact diff err");
tab[1].line_of_names("x calc exact diff err");
tab[2].line_of_names("x calc exact diff err");
tab[3].line_of_names("x calc exact diff err");
tab[4].line_of_names("x calc exact diff err0 err1");
tab[5].line_of_names("x calc exact diff err0 err1");
tab[6].line_of_names("x calc exact diff err0 err1");
tab[7].line_of_names("x calc exact diff err0");

// -----
// Solution 1: Solve using the non-adaptive Cash-Karp stepper.

cout << "Bessel function, Cash-Karp: " << endl;

// Initial values at x=0
x=0.0;
y[0]=0.0;
y[1]=0.5;

// The non-adaptive ODE steppers require the derivatives as
// input
derivs(x,2,y,dydx,alpha);

cout << " x          J1(calc)      J1(exact)      rel. diff.      "
      << "err" << endl;

while (x<1.0) {

    // Perform a step. Since the fourth and sixth arguments are
    // the same, the values in 'y' are updated with the new values
    // at x+dx.
    ode.step(x,dx,2,y,dydx,y,yerr,dydx,od);

    // Update the x value
    x+=dx;

    // Print and test
    cout << x << " " << y[0] << " "
          << gsl_sf_bessel_J1(x) << " ";
    cout << fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)) << " ";
    cout << yerr[0] << endl;
    t.test_rel(y[0],gsl_sf_bessel_J1(x),5.0e-5,"rkck");

    // Also output the results to a table
    double line[5]={x,y[0],gsl_sf_bessel_J1(x),
                   fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)),
                   yerr[0]};
    tab[0].line_of_data(5,line);

```

```

}

// Compare with the exact result at the last point
cout << "Accuracy at end: "
    << fabs(y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x) << endl;
cout << endl;

// End of Solution 1
// -----
// Solution 2: Solve using the non-adaptive Prince-Dormand stepper.
// Note that for the Bessel function, the 8th order stepper performs
// worse than the 4th order. The error returned by the stepper is
// larger near x=0, as expected.

cout << "Bessel function, Prince-Dormand: " << endl;
x=0.0;
y[0]=0.0;
y[1]=0.5;
derivs(x,2,y,dydx,alpha);
cout << " x          J1(calc)          J1(exact)          rel. diff.          "
    << "err" << endl;
while (x<1.0) {
    ode2.step(x,dx,2,y,dydx,y,yerr,dydx,od);
    x+=dx;
    cout << x << " " << y[0] << " "
        << gsl_sf_bessel_J1(x) << " ";
    cout << fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)) << " ";
    cout << yerr[0] << endl;
    t.test_rel(y[0],gsl_sf_bessel_J1(x),5.0e-4,"rk8pd");

    // Also output the results to a table
    double line[5]={x,y[0],gsl_sf_bessel_J1(x),
        fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)),
        yerr[0]};
    tab[1].line_of_data(5,line);
}
cout << "Accuracy at end: "
    << fabs(y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x) << endl;
cout << endl;

// End of Solution 2

```

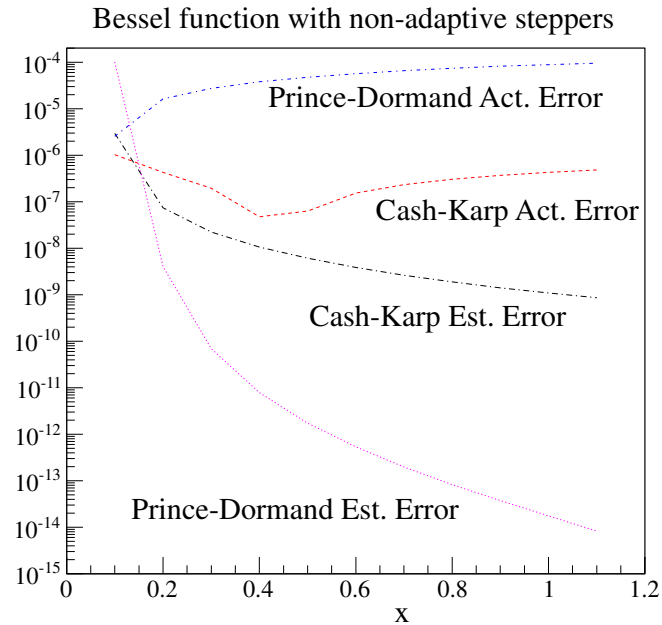


Figure 4: Bessel example plot

Note that with a Bessel function and a fixed step size, the Prince-Dormand stepper (even though of higher order than the Cash-Karp stepper) is actually less accurate, and seriously underestimates the error.

The Airy functions are defined by

$$y'' = yx$$

This example solves for the Airy function of the first kind,  $Ai(x)$ .

```
// Solution 3: Solve using the non-adaptive Cash-Karp stepper.

cout << "Airy function, Cash-Karp: " << endl;
x=0.0;
y[0]=1.0/pow(3.0,2.0/3.0)/gsl_sf_gamma(2.0/3.0);
y[1]=-1.0/pow(3.0,1.0/3.0)/gsl_sf_gamma(1.0/3.0);
derivs2(x,2,y,dydx,alpha);
cout << " x          Ai(calc)      Ai(exact)      rel. diff.      "
    << "err" << endl;
while (x<1.0) {
    ode.step(x,dx,2,y,dydx,y,yerr,dydx,od2);
    x+=dx;
    cout << x << " " << y[0] << " "
        << gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE) << " ";
    cout << fabs((y[0]-gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE))/
        gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE)) << " ";
    cout << yerr[0] << endl;
    t.test_rel(y[0],gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE),1.0e-8,"rkck");

    // Also output the results to a table
    double line[5]={x,y[0],gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE),
        fabs((y[0]-gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE))/
            gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE)),
        yerr[0]};
    tab[2].line_of_data(5,line);
}
cout << "Accuracy at end: "
    << fabs(y[0]-gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE))/
    gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE) << endl;
cout << endl;
```

```

// End of Solution 3
// -----
// Solution 4: Solve using the non-adaptive Prince-Dormand stepper.
// On this function, the higher-order routine performs significantly
// better.

cout << "Airy function, Prince-Dormand: " << endl;
x=0.0;
y[0]=1.0/pow(3.0,2.0/3.0)/gsl_sf_gamma(2.0/3.0);
y[1]=-1.0/pow(3.0,1.0/3.0)/gsl_sf_gamma(1.0/3.0);
derivs2(x,2,y,dydx,alpha);
cout << " x          Ai(calc)          Ai(exact)          rel. diff.      "
    << "err" << endl;
while (x<1.0) {
    ode2.step(x,dx,2,y,dydx,y,yerr,dydx,od2);
    x+=dx;
    cout << x << " " << y[0] << " "
        << gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE) << " ";
    cout << fabs((y[0]-gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE))/
        gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE)) << " ";
    cout << yerr[0] << endl;
    t.test_rel(y[0],gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE),1.0e-14,"rk8pd");

    // Also output the results to a table
    double line[5]={x,y[0],gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE),
        fabs((y[0]-gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE))/
            gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE)),
        yerr[0]};
    tab[3].line_of_data(5,line);
}
cout << "Accuracy at end: "
    << fabs(y[0]-gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE))/
    gsl_sf_airy_Ai(x,GSL_PREC_DOUBLE) << endl;
cout << endl;

// End of Solution 4

```

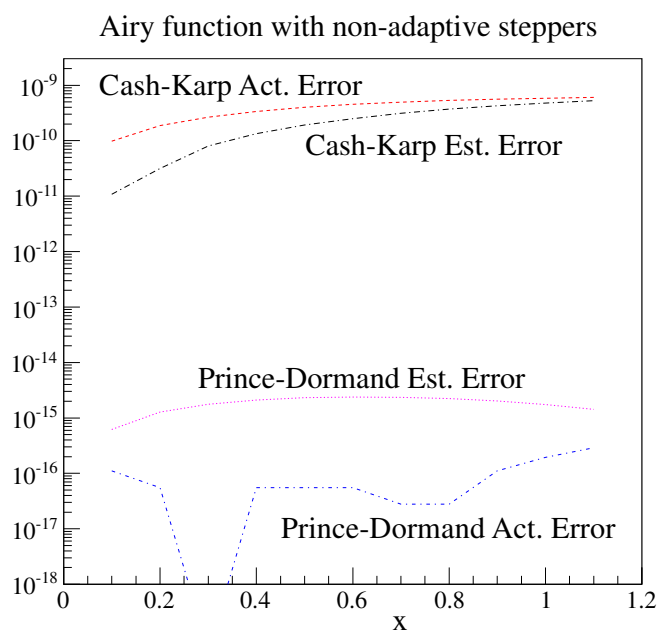


Figure 5: Airy example plot

Here the higher order stepper is more accurate.

```
// Solution 5: Solve using the GSL adaptive stepper

// Lower the output precision to fit in 80 columns
cout.precision(5);

cout << "Adaptive stepper: " << endl;
gsl_astep<> ode3;
x=0.0;
y[0]=0.0;
y[1]=0.5;
cout << "      x          J1(calc)      J1(exact)      rel. diff.";
cout << "      err_0          err_1" << endl;
int k=0;
while (x<10.0) {
    int retx=ode3.astep(x,10.0,dx,2,y,dydx,yerr,od);
    if (k%3==0) {
        cout << retx << " " << x << " " << y[0] << " "
            << gsl_sf_bessel_J1(x) << " ";
        cout << fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)) << " ";
        cout << yerr[0] << " " << yerr[1] << endl;
    }
    t.test_rel(y[0],gsl_sf_bessel_J1(x),5.0e-3,"astep");
    t.test_rel(y[1],0.5*(gsl_sf_bessel_J0(x)-gsl_sf_bessel_Jn(2,x)),
        5.0e-3,"astep 2");
    t.test_rel(yerr[0],0.0,4.0e-6,"astep 3");
    t.test_rel(yerr[1],0.0,4.0e-6,"astep 4");
    t.test_gen(retx==0,"astep 5");

    // Also output the results to a table
    double line[6]={x,y[0],gsl_sf_bessel_J1(x),
        fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)),
        yerr[0],yerr[1]};
    tab[4].line_of_data(6,line);

    k++;
}
cout << "Accuracy at end: "
    << fabs(y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x) << endl;
cout << endl;

// End of Solution 5
// -----
// Solution 6: Solve using the GSL adaptive stepper.
// Decrease the tolerances, and the adaptive stepper takes
// smaller step sizes.

cout << "Adaptive stepper with smaller tolerances: " << endl;
ode3.con.eps_abs=1.0e-8;
ode3.con.a_dydt=1.0;
x=0.0;
y[0]=0.0;
y[1]=0.5;
cout << "      x          J1(calc)      J1(exact)      rel. diff.";
cout << "      err_0          err_1" << endl;
k=0;
while (x<10.0) {
    int retx=ode3.astep(x,10.0,dx,2,y,dydx,yerr,od);
    if (k%3==0) {
        cout << retx << " " << x << " " << y[0] << " "
            << gsl_sf_bessel_J1(x) << " ";
        cout << fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)) << " ";
        cout << yerr[0] << " " << yerr[1] << endl;
    }
    t.test_rel(y[0],gsl_sf_bessel_J1(x),5.0e-3,"astep");
    t.test_rel(y[1],0.5*(gsl_sf_bessel_J0(x)-gsl_sf_bessel_Jn(2,x)),
        5.0e-3,"astep 2");
    t.test_rel(yerr[0],0.0,4.0e-8,"astep 3");
    t.test_rel(yerr[1],0.0,4.0e-8,"astep 4");
```

```

t.test_gen(retx==0,"astep 5");

// Also output the results to a table
double line[6]={x,y[0],gsl_sf_bessel_J1(x),
               fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)),
               yerr[0],yerr[1]};
tab[5].line_of_data(6,line);

k++;
}
cout << "Accuracy at end: "
      << fabs(y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x) << endl;
cout << endl;

// End of Solution 6
// -----
// Solution 7: Solve using the GSL adaptive stepper.
// Use the higher-order stepper, and less steps are required. The
// stepper automatically takes more steps near x=0 in order since
// the higher-order routine has more trouble there.

cout << "Adaptive stepper, Prince-Dormand: " << endl;
ode3.set_step(ode2);
x=0.0;
y[0]=0.0;
y[1]=0.5;
cout << "    x          J1(calc)      J1(exact)      rel. diff.";
cout << "    err_0          err_1" << endl;
k=0;
while (x<10.0) {
    int retx=ode3.astep(x,10.0,dx,2,y,dydx,yerr,od);
    if (k%3==0) {
        cout << retx << " " << x << " " << y[0] << " "
              << gsl_sf_bessel_J1(x) << " ";
        cout << fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)) << " ";
        cout << yerr[0] << " " << yerr[1] << endl;
    }
    t.test_rel(y[0],gsl_sf_bessel_J1(x),5.0e-3,"astep");
    t.test_rel(y[1],0.5*(gsl_sf_bessel_J0(x)-gsl_sf_bessel_Jn(2,x)),
              5.0e-3,"astep");
    t.test_rel(yerr[0],0.0,4.0e-8,"astep 3");
    t.test_rel(yerr[1],0.0,4.0e-8,"astep 4");
    t.test_gen(retx==0,"astep 5");

    // Also output the results to a table
    double line[6]={x,y[0],gsl_sf_bessel_J1(x),
                   fabs((y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x)),
                   yerr[0],yerr[1]};
    tab[6].line_of_data(6,line);

    k++;
}
cout << "Accuracy at end: "
      << fabs(y[0]-gsl_sf_bessel_J1(x))/gsl_sf_bessel_J1(x) << endl;
cout << endl;

// End of Solution 7

```

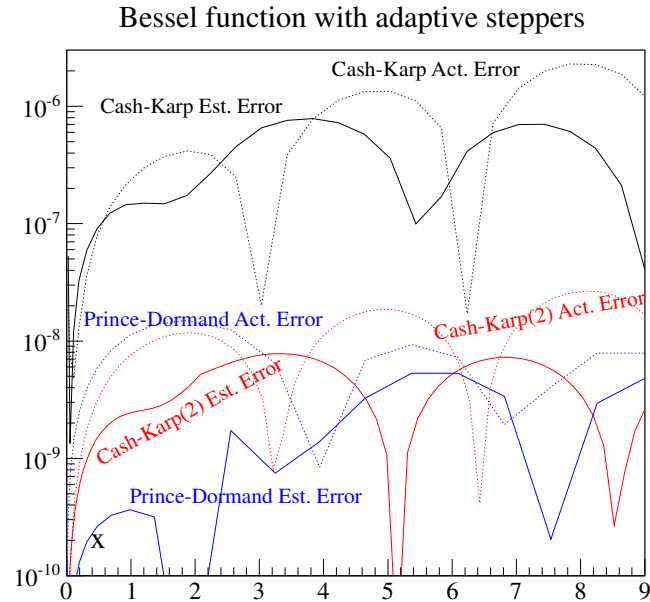


Figure 6: Bessel example plot

```
// Solution 8: Solve using the O2scl initial value solver

// Return the output precision to the default
cout.precision(6);

cout << "Initial value solver: " << endl;
ode_iv_solve<> ode4;

// Define the grid and the storage for the solution
const size_t ngrid=101;
ovector xg(ngrid), yinit(2);
omatrix yg(ngrid,2), ypg(ngrid,2), yerrg(ngrid,2);
for(size_t i=0;i<ngrid;i++) xg[i]=((double)i)/10.0;

// Set the initial value
xg[0]=0.0;
xg[ngrid-1]=10.0;
yg[0][0]=0.0;
yg[0][1]=0.5;

// Perform the full solution
ode4.solve_grid(omatrix,omatrix_row>(0.1,2,ngrid,xg,yg,ypg,yerrg,od);

// Output and test the results
cout << " x          J1(calc)      J1(exact)      rel. diff." << endl;
for(size_t i=1;i<ngrid;i++) {

    if (i%10==0) {
        cout << xg[i] << " " << yg[i][0] << " "
            << gsl_sf_bessel_J1(xg[i]) << " ";
        cout << fabs(yg[i][0]-gsl_sf_bessel_J1(xg[i])) << " "
            << fabs(yerrg[i][0]) << endl;
    }
    t.test_rel(yg[i][0],gsl_sf_bessel_J1(xg[i]),5.0e-7,"astep");
    t.test_rel(yg[i][1],0.5*(gsl_sf_bessel_J0(xg[i])-
        gsl_sf_bessel_Jn(2,xg[i])),5.0e-7,"astep 2");

    // Also output the results to a table
    double line[5]={xg[i],yg[i][0],gsl_sf_bessel_J1(xg[i]),
```

```

        fabs(yg[i][0]-gsl_sf_bessel_J1(xg[i])),
        fabs(yerrg[i][0]));
    tab[7].line_of_data(5,line);
}

cout << "Accuracy at end: "
    << fabs(yg[ngrid-1][0]-gsl_sf_bessel_J1(xg[ngrid-1]))/
    gsl_sf_bessel_J1(xg[ngrid-1]) << endl;
cout << endl;

// End of Solution 8
// -----
// Output results to a file

#ifdef O2SCL_HDF_IN_EXAMPLES
    hdf_file hf;
    hf.open("ex_ode.o2");
    for(size_t i=0;i<8;i++) {
        hdf_output(hf,tab[i],((string)"table_")+itos(i));
    }
    hf.close();
#endif

// -----

cout.unsetf(ios::showpos);
t.report();

return 0;
}
// End of example

```

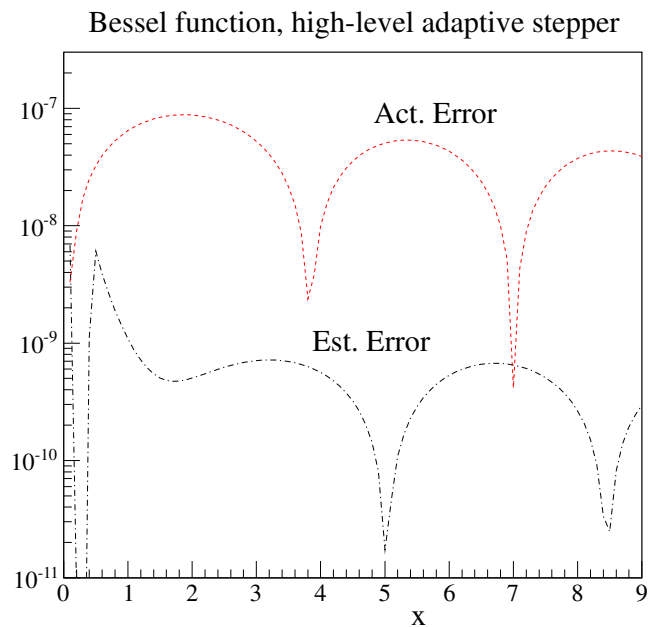


Figure 7: Bessel example plot



## 24.2 Stiff differential equations

This example solves the differential equations

$$\begin{aligned} y_0' &= 480y_0 + 980y_1 \\ y_1' &= -490y_0 - 990y_1 \end{aligned}$$

which have the exact solution

$$\begin{aligned} y_0 &= -e^{-500x} + 2e^{-10x} \\ y_1 &= e^{-500x} - e^{-10x} \end{aligned}$$

using both the stiff stepper `gsl_bsimp` and the standard adaptive stepper `gsl_astep`. The relative error on the adaptive stepper is orders of magnitude larger.

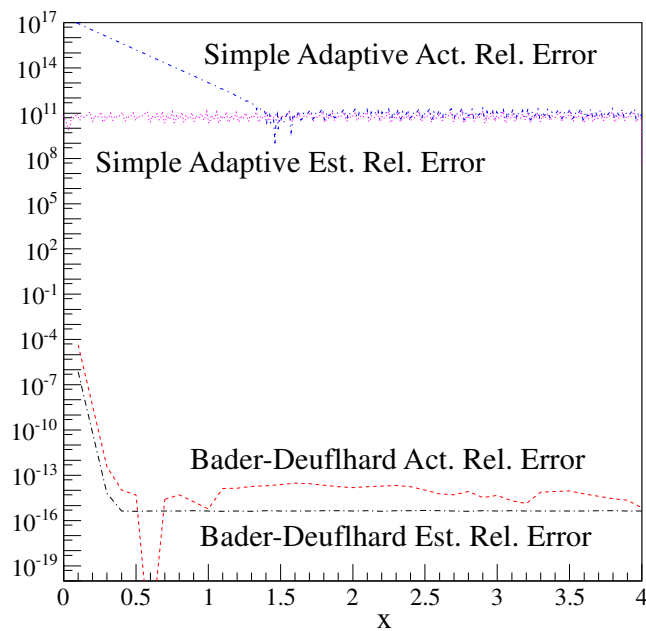


Figure 8: Bader-Deuflhard example plot

```
/* Example: ex_stiff.cpp
-----
An example to demonstrate solving stiff differential equations
*/

#include <o2scl/test_mgr.h>
#include <o2scl/ovector_tlate.h>
#include <o2scl/funct.h>
#include <o2scl/ode_funct.h>
#include <o2scl/gsl_astep.h>
#include <o2scl/gsl_bsimp.h>
#include <o2scl/table.h>

#ifdef O2SCL_HDF_IN_EXAMPLES
#include <o2scl/hdf_file.h>
#include <o2scl/hdf_io.h>
#endif

using namespace std;
using namespace o2scl;
```

```

#ifdef O2SCL_HDF_IN_EXAMPLES
using namespace o2scl_hdf;
#endif

int derivs(double x, size_t nv, const ovector_base &y,
           ovector_base &dydx) {
    dydx[0]=480.0*y[0]+980.0*y[1];
    dydx[1]=-490.0*y[0]-990.0*y[1];
    return 0;
}

int jac(double x, size_t nv, const ovector_base &y,
        omatrix_base &dfdy, ovector_base &dfdx) {
    dfdy[0][0]=480.0;
    dfdy[0][1]=980.0;
    dfdy[1][0]=-490.0;
    dfdy[1][1]=-990.0;
    dfdx[0]=0.0;
    dfdx[1]=0.0;
    return 0;
}

int main(void) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);
    cout.precision(3);

    // Specification of the differential equations and the Jacobian
    ode_funct_fptr<ovector_base> od(derivs);
    ode_jac_funct_fptr<ovector_base> oj(jac);

    table tab[2];
    tab[0].line_of_names("x calc exact rel_err rel_diff");
    tab[1].line_of_names("x calc exact rel_err rel_diff");

    // -----
    // First solve with gsl_bsim, designed to handle stiff ODEs

    gsl_bsim<ode_funct_fptr<>,ode_jac_funct_fptr<> > gb;

    double x1, dx=1.0e-1;
    ovector y1(2), dydx1(2), yout1(2), yerr1(2), dydx_out1(2);

    x1=0.0;
    y1[0]=1.0;
    y1[1]=0.0;

    derivs(x1,2,y1,dydx1);

    for(size_t i=1;i<=40;i++) {

        gb.step(x1,dx,2,y1,dydx1,y1,yerr1,dydx1,od,oj);
        x1+=dx;

        double exact[2]={-exp(-500.0*x1)+2.0*exp(-10.0*x1),
                        exp(-500.0*x1)-exp(-10.0*x1)};

        cout.setf(ios::showpos);
        cout << x1 << " " << y1 << " " << yerr1 << " " << exact[0] << " "
             << exact[1] << endl;
        cout.unsetf(ios::showpos);

        double line[5]={x1,y1[0],exact[0],yerr1[0]/exact[0],
                       fabs((y1[0]-exact[0])/exact[0])};
        tab[0].line_of_data(5,line);

        t.test_rel(y1[0],exact[0],3.0e-4,"y0");
        t.test_rel(y1[1],exact[1],3.0e-4,"y1");
    }
}

```

```

}

cout << endl;

// -----
// Now compare to the traditional adaptive stepper

gsl_astep<ode_funct_fptr> > ga;

double x2;
ovector y2(2), dydx2(2), yout2(2), yerr2(2), dydx_out2(2);

x2=0.0;
y2[0]=1.0;
y2[1]=0.0;

derivs(x2,2,y2,dydx2);

size_t j=0;
while (x2<4.0) {

    ga.astep(x2,4.0,dx,2,y2,dydx2,yerr2,od);

    double exact[2]={-exp(-500.0*x1)+2.0*exp(-10.0*x1),
                    exp(-500.0*x1)-exp(-10.0*x1)};

    if (j%25==0) {
        cout.setf(ios::showpos);
        cout << x2 << " " << y2 << " " << yerr2 << " "
            << exact[0] << " " << exact[1] << endl;
        cout.unsetf(ios::showpos);
    }
    j++;

    double line[5]={x2,y2[0],exact[0],yerr2[0]/exact[0],
                  fabs((y2[0]-exact[0])/exact[0])};
    tab[1].line_of_data(5,line);

}

cout << endl;

// -----
// Output results to a file

#ifdef O2SCL_HDF_IN_EXAMPLES
    hdf_file hf;
    hf.open("ex_stiff.o2");
    for(size_t i=0;i<2;i++) {
        hdf_output(hf,tab[i],((string)"table_"+itos(i)));
    }
    hf.close();
#endif

// -----

t.report();

return 0;

}
// End of example

```

## 24.3 Iterative solution of ODEs

This example solves the ODEs

$$\begin{aligned}y_0'' &= y_1 \\ y_1'' &= y_0 + y_1 \\ y_2'' &= y_0 + y_2\end{aligned}$$

given the boundary conditions

$$\begin{aligned}y_0(x=0) &= 1 \\ y_1(x=0)^2 + y_2(x=0)^2 &= 2 \\ y_1(x=1) &= 3\end{aligned}$$

by linearizing the ODEs on a mesh and using an iterative method (sometimes called relaxation). The `ode_it_solve` class demonstrates how this works, but is slow for large grid sizes because the matrix is very sparse. See `O2scl_uml` which shows how a similar problem can be done more efficiently using the native iterative method and sparse matrix format.

```
/* Example: ex_ode_it.cpp
-----
Demonstrate the iterative method for solving ODEs
*/

#include <o2scl/ode_it_solve.h>
#include <o2scl/ode_iv_solve.h>
#include <o2scl/linear_solver.h>

using namespace std;
using namespace o2scl;
using namespace o2scl_linalg;

// The three-dimensional ODE system
class ode_system {

public:

    // The LHS boundary conditions
    double left(size_t ieq, double x, ovector_base &yleft) {
        if (ieq==0) return yleft[0]-1.0;
        return yleft[1]*yleft[1]+yleft[2]*yleft[2]-2.0;
    }

    // The RHS boundary conditions
    double right(size_t ieq, double x, ovector_base &yright) {
        return yright[1]-3.0;
    }

    // The differential equations
    double derivs(size_t ieq, double x, ovector_base &y) {
        if (ieq==1) return y[0]+y[1];
        else if (ieq==2) return y[0]+y[2];
        return y[1];
    }

    // This is the alternative specification for ode_iv_solve for
    // comparison
    int shoot_derivs(double x, size_t nv, const ovector_base &y,
                     ovector_base &dydx) {
        dydx[0]=y[1];
        dydx[1]=y[0]+y[1];
        dydx[2]=y[0]+y[2];
        return 0;
    }

};
```

```

int main(void) {

    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

    // The ODE solver
    ode_it_solve<ode_it_func<ovector_base>,ovector_base,
        omatrix_base,omatrix_row,ovector_base,omatrix_base> oit;

    // The class which contains the functions to solve
    ode_system os;

    // Make function objects for the derivatives and boundary conditions
    ode_it_func_ptr<ode_system> f_d(&os,&ode_system::derivs);
    ode_it_func_ptr<ode_system> f_l(&os,&ode_system::left);
    ode_it_func_ptr<ode_system> f_r(&os,&ode_system::right);

    // Grid size
    size_t ngrid=40;

    // Number of ODEs
    size_t neq=3;

    // Number of LHS boundary conditions
    size_t nbleft=2;

    // Create space for the solution and make an initial guess
    ovector x(ngrid);
    omatrix y(ngrid,neq);
    for(size_t i=0;i<ngrid;i++) {
        x[i]=((double)i)/((double)(ngrid-1));
        y[i][0]=1.0+x[i]+1.0;
        y[i][1]=3.0*x[i];
        y[i][2]=-0.1*x[i]-1.4;
    }

    int pa=0;

    // Workspace objects
    omatrix A(ngrid*neq,ngrid*neq);
    ovector rhs(ngrid*neq), dy(ngrid*neq);

    // Perform the solution
    oit.verbose=1;
    oit.solve(ngrid,neq,nbleft,x,y,f_d,f_l,f_r,A,rhs,dy);

    // Compare with the initial value solver ode_iv_solve
    ode_iv_solve<> ois;
    ode_func_ptr<ode_system> f_sd(&os,&ode_system::shoot_derivs);
    ovector ystart(neq), yend(neq);
    for(size_t i=0;i<neq;i++) ystart[i]=y[0][i];
    ois.solve_final_value(0.0,1.0,0.01,neq,ystart,yend,f_sd);

    // Test the result
    t.test_rel(y[0][0],1.0,1.0e-3,"ya");
    t.test_rel(y[ngrid-1][0],yend[0],1.0e-3,"yb");
    t.test_rel(y[0][1],0.25951,1.0e-3,"yc");
    t.test_rel(y[ngrid-1][1],yend[1],1.0e-3,"yd");
    t.test_rel(y[0][2],-1.3902,1.0e-3,"ye");
    t.test_rel(y[ngrid-1][2],yend[2],1.0e-3,"yf");

    t.report();

    return 0;
}
// End of example

```

## 25 Random Number Generation

Random number generators are descendants of [rnga](#). While the base object [rnga](#) is created to allow user-defined random number generators, the only random number generator presently included are from GSL. Because speed is frequently an issue, some design choices were made to ensure fast execution

- The GSL random number generator code is reimplemented, rather than simply wrapped around the GSL code.
- The interface does not use virtual functions.
- Random number generators are implemented as template parameters in [sim\\_anneal](#) and [mcarlo\\_inte](#), rather than as pointers.

### 25.1 Generate an arbitrary distribution

This examples creates a Markov chain for an arbitrary distribution using the Metropolis-Hastings algorithm. It generates the one-dimensional distribution

$$f(x) = e^{-x^2} [\sin(x - 1.4) + 1]$$

for  $x \in [-5, 5]$ .

```
/* Example: ex_markov.cpp
-----

An example to demonstrate generation of an arbitrary distribution
through the creation of a Markov chain using the Metropolis
algorithm.
*/

#include <iostream>
#include <cmath>
#include <o2scl/test_mgr.h>
#include <o2scl/hist.h>
#include <o2scl/gsl_rnga.h>
#include <o2scl/expect_val.h>
#include <o2scl/gsl_inte_qag.h>

using namespace std;
using namespace o2scl;

/*
An unusual two-peaked probability distribution. This distribution is
is strongly bimodal, and thus the algorithm has to step over a
region where the probability distribution is small.
*/
double function(double x) {
    return exp(-x*x)*(sin(x-1.4)+1.0);
}

// Same function but now weighted with x
double function2(double x) {
    return x*exp(-x*x)*(sin(x-1.4)+1.0);
}

int main(int argc, char *argv[]) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

    // The square root of the number of iterations
    static const size_t N=1000;

    // The stepsize for the Metropolis algorithm. If this stepsize was
    // too small, the algorithm would fail to step between the two
    // peaks and give incorrect results.
```

```

double step=1.0;

// The random number generator
gsl_rnga gr;
if (argc>=2) {
    gr.set_seed(stoi(argv[1]));
}

// Construct a histogram of the distribution. Initialize the grid
// spacing with a uniform grid between -5 and 5.
hist h;
h.set_bins(uniform_grid_end_width<>(-5.0,5.0,0.1));

// Compute the average value of the distribution, and use
// a scalar_ev object to estimate the uncertainty
static const size_t M=20;
scalar_ev sev(M,N*N/M);

// An initial point and the initial weight
double x_old=0.01;
double w_old=function(x_old);

for(size_t k=0;k<N;k++) {
    for(size_t i=0;i<N;i++) {

        // Perform a step and compute the new weight
        double r=gr.random();
        double x_new=x_old+r*step*2.0-step;
        double w_new=function(x_new);

        // The Metropolis algorithm
        double r2=gr.random();
        if (r2<w_new/w_old && x_new>-5.0 && x_new<5.0) {
            x_old=x_new;
            w_old=w_new;
        }

        // Update the histogram
        h.update(x_old);

        // Update the average value
        sev.add(x_old);

    }
}

// Normalize by the value of the distribution at x=1.05
double norm=h.get_wgt(1.05)/function(1.05);

// Output the generated distribution and compare to the real
// distribution.

for(size_t i=0;i<h.size();i++) {

    double xx=h.get_rep_i(i);

    // Limit output to every third point
    if (i%3==0) {
        cout.width(2);
        cout << i << " ";
        cout.setf(ios::showpos);
        cout << xx << " ";
        cout.unsetf(ios::showpos);
        cout << h.get_wgt_i(i)/norm << " "
            << function(xx) << endl;
    }

    // Only test regions where we'll have enough statistics
    if (function(xx)>5.0e-3) {
        t.test_rel(h.get_wgt_i(i)/norm,function(xx),1.0e-1,"dist");
    }
}

```

```

    }

}
cout << endl;

// Output the average value and its uncertainty
double avg, std_dev, avg_err;
sev.current_avg(avg,std_dev,avg_err);
cout << avg << " " << avg_err << endl;

// Compare to result from direct integration
funct_fptr ff(function);
funct_fptr ff2(function2);
gsl_inte_qag<> qag;
double exact=qag.integ(ff2,-5.0,5.0)/qag.integ(ff,-5.0,5.0);
cout << exact << endl;

t.test_abs(avg,exact,3.0*avg_err,"Average value");

t.report();

return 0;
}
// End of example

```

Typical output is

```

0 -4.950000e+00 0.000000e+00 2.131525e-11
3 -4.650000e+00 0.000000e+00 5.009023e-10
6 -4.350000e+00 0.000000e+00 9.131547e-09
9 -4.050000e+00 0.000000e+00 1.309343e-07
12 -3.750000e+00 4.095279e-06 1.488688e-06
15 -3.450000e+00 1.228584e-05 1.348287e-05
18 -3.150000e+00 5.323863e-05 9.747130e-05
21 -2.850000e+00 5.487674e-04 5.624059e-04
24 -2.550000e+00 2.706979e-03 2.584240e-03
27 -2.250000e+00 9.587048e-03 9.410936e-03
30 -1.950000e+00 2.736465e-02 2.693191e-02
33 -1.650000e+00 5.785401e-02 5.970011e-02
36 -1.350000e+00 1.004859e-01 9.993669e-02
39 -1.050000e+00 1.204053e-01 1.202766e-01
42 -7.500000e-01 9.158682e-02 9.293227e-02
45 -4.500000e-01 3.099307e-02 3.162602e-02
48 -1.500000e-01 6.757210e-04 2.114248e-04
51 +1.500000e-01 4.999517e-02 4.988035e-02
54 +4.500000e-01 1.519635e-01 1.523810e-01
57 +7.500000e-01 2.238029e-01 2.249580e-01
60 +1.050000e+00 2.181842e-01 2.181842e-01
63 +1.350000e+00 1.529259e-01 1.535435e-01
66 +1.650000e+00 8.190148e-02 8.196725e-02
69 +1.950000e+00 3.340519e-02 3.397864e-02
72 +2.250000e+00 1.076239e-02 1.108511e-02
75 +2.550000e+00 3.153365e-03 2.868544e-03
78 +2.850000e+00 7.576266e-04 5.914089e-04
81 +3.150000e+00 5.733391e-05 9.733109e-05
84 +3.450000e+00 4.095279e-06 1.278395e-05
87 +3.750000e+00 0.000000e+00 1.336916e-06
90 +4.050000e+00 0.000000e+00 1.107648e-07
93 +4.350000e+00 0.000000e+00 7.207155e-09
96 +4.650000e+00 0.000000e+00 3.628586e-10
99 +4.950000e+00 0.000000e+00 1.376924e-11
46 tests performed.
All tests passed.

```



## 26 Two-dimensional Interpolation

Successive use of [smart\\_interp](#) is implemented in [twod\\_intp](#), which is useful for interpolating data presented on a two-dimensional grid (though the spacings between grid points need not be equal). An example demonstrating the use of [twod\\_intp](#) is given in [ex\\_twod\\_intp\\_sect](#). Also, one can compute contour lines from data represented on a grid using the [contour](#) class.

If data is arranged without a grid, then [planar\\_intp](#) can be used. At present, the only way to compute contour lines on data which is not defined on a grid is to use [planar\\_intp](#) to recast the data on a grid and then use [contour](#) afterwards.

Higher-dimensional interpolation is possible with [tensor\\_grid](#).

### 26.1 Two-dimensional interpolation

```
/* Example: ex_twod_intp.cpp
-----
A simple example for two-dimensional interpolation using
the twod_intp class.
*/

#include <o2scl/twod_intp.h>
#include <o2scl/test_mgr.h>

using namespace std;
using namespace o2scl;

// A function for filling the data and comparing results
double f(double x, double y) {
    return pow(sin(0.1*x+0.3*y),2.0);
}

int main(void) {
    int i,j;

    test_mgr t;
    t.set_output_level(1);

    // Create the sample data

    ovector x(3), y(3);
    omatrix data(3,3);

    cout.setf(ios::scientific);

    // Set the grid
    x[0]=0.0;
    x[1]=1.0;
    x[2]=2.0;
    y[0]=3.0;
    y[1]=2.0;
    y[2]=1.0;

    // Set and print out the data
    cout << endl;
    cout << "Data: " << endl;
    cout << "      x | ";
    for(i=0;i<3;i++) cout << x[i] << " ";
    cout << endl;
    cout << " y      |" << endl;
    cout << "-----|-----";
    for(i=0;i<3;i++) cout << "-----";
    cout << endl;
    for(i=0;i<3;i++) {
        cout << y[i] << " | ";
        for(j=0;j<3;j++) {
            data[i][j]=f(x[j],y[i]);
            cout << data[i][j] << " ";
        }
    }
}
```

```

    cout << endl;
}
cout << endl;

// Perform the interpolation

cout << "x          y          Calc.          Exact" << endl;

twod_intp ti;

// Interpolation, x-first
double tol=0.05;
double tol2=0.4;

ti.set_data(3,3,x,y,data,true);

double x0, y0, x1, y1;

x0=0.5; y0=1.5;
cout << x0 << " " << y0 << " "
    << ti.interp(x0,y0) << " " << f(x0,y0) << endl;

x0=0.99; y0=1.99;
cout << x0 << " " << y0 << " "
    << ti.interp(x0,y0) << " " << f(x0,y0) << endl;

x0=1.0; y0=2.0;
cout << x0 << " " << y0 << " "
    << ti.interp(x0,y0) << " " << f(x0,y0) << endl;

cout << endl;

// Interpolation, y-first

ti.set_data(3,3,x,y,data,false);

x0=0.5; y0=1.5;
cout << x0 << " " << y0 << " "
    << ti.interp(x0,y0) << " " << f(x0,y0) << endl;

x0=0.99; y0=1.99;
cout << x0 << " " << y0 << " "
    << ti.interp(x0,y0) << " " << f(x0,y0) << endl;

x0=1.0; y0=2.0;
cout << x0 << " " << y0 << " "
    << ti.interp(x0,y0) << " " << f(x0,y0) << endl;

cout << endl;

t.report();
return 0;
}
// End of example

```

This example creates a sample 3 by 3 grid of data with the function  $[\sin(x/10 + 3y/10)]^2$  and performs some interpolations and compares them with the exact result.

```

Data:
      x | 0.000000e+00 1.000000e+00 2.000000e+00
      y |
-----|-----
3.000000e+00 | 6.136010e-01 7.080734e-01 7.942506e-01
2.000000e+00 | 3.188211e-01 4.150164e-01 5.145998e-01
1.000000e+00 | 8.733219e-02 1.516466e-01 2.298488e-01

x          y          Calc.          Exact
5.000000e-01 1.500000e+00 2.380255e-01 2.298488e-01

```

```

9.900000e-01 1.990000e+00 4.112589e-01 4.110774e-01
1.000000e+00 2.000000e+00 4.150164e-01 4.150164e-01

5.000000e-01 1.500000e+00 2.380255e-01 2.298488e-01
9.900000e-01 1.990000e+00 4.112589e-01 4.110774e-01
1.000000e+00 2.000000e+00 4.150164e-01 4.150164e-01

```

## 26.2 Contour lines

This example generates contour lines of the function

$$z = f(x,y) = 15 \exp \left[ -\frac{1}{20^2} (x-20)^2 - \frac{1}{5^2} (y-5)^2 \right] + 40 \exp \left[ -\frac{1}{500} (x-70)^2 - \frac{1}{2^2} (y-2)^2 \right]$$

```

/* Example: ex_contour.cpp
-----
Example for generating contour lines
*/

#include <iostream>
#include <o2scl/test_mgr.h>
#include <o2scl/contour.h>
#include <o2scl/ovector_tlate.h>

using namespace std;
using namespace o2scl;

// A function defining the three-dimensional surface
// for which we want to compute contour levels
double fun(double x, double y) {
    return 15.0*exp(-pow(x-20.0,2.0)/400.0-pow(y-5.0,2.0)/25.0)
        +40.0*exp(-pow(x-70.0,2.0)/500.0-pow(y-2.0,2.0)/4.0);
}

// A function for outputting the data to cout
int print_data(int nx, int ny, ovector_base &x, ovector_base &y,
              omatrix_base &data);

// A function for printing the contour information to a file
int file_out(vector<contour_line> &conts, vector<contour_line> &conts2);

int main(void) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

    contour co;

    // Initialize the data

    ovector x(12), y(10);
    omatrix data(10,12);
    for(size_t i=0;i<10;i++) {
        y[i]=((double)i);
    }
    for(size_t i=0;i<12;i++) {
        x[i]=((double)i)*((double)i);
    }

    for(size_t j=0;j<12;j++) {
        for(size_t k=0;k<10;k++) {
            data[k][j]=fun(x[j],y[k]);
        }
    }
    co.set_data(12,10,x,y,data);

```

```

// Print out the data
print_data(12,10,x,y,data);

// Set the contour levels
ovector levels(7);
levels[0]=5.0;
levels[1]=10.0;
levels[2]=0.002;
levels[3]=20.0;
levels[4]=0.2;
levels[5]=30.0;
levels[6]=2.0;

co.set_levels(7,levels);

// Compute the contours
vector<contour_line> conts;
co.calc_contours(conts);

// Print the contours to the screen and test to make sure
// that they match the requested level

size_t nc=conts.size();
for(size_t i=0;i<nc;i++) {
    cout << "Contour " << i << " at level " << conts[i].level << ":" << endl;
    size_t cs=conts[i].x.size();
    for(size_t j=0;j<cs;j++) {
        cout << "(" << conts[i].x[j] << ", " << conts[i].y[j] << ") "
            << fun(conts[i].x[j],conts[i].y[j]) << endl;
        t.test_rel(fun(conts[i].x[j],conts[i].y[j]),conts[i].level,
            1.0,"curve");
    }
    cout << endl;
}

// Refine the data using cubic spline interpolation
def_interp_mgr<ovector_const_view,cspline_interp> dim1;
def_interp_mgr<ovector_const_subvector,cspline_interp> dim2;
co.regrid_data(5,5,dim1,dim2);

// Recompute the contours

vector<contour_line> conts2;
co.calc_contours(conts2);

// Output the contour information to a file for the documentation
file_out(conts,conts2);

t.report();

return 0;
}
// End of example

```

The figure below shows contour lines in the region  $x \in (0, 120), y \in (0, 9)$ . The data grid is represented by plus signs, and the associated generated contours. The figure clearly shows the obvious peaks at (20,5) and (70,2) .

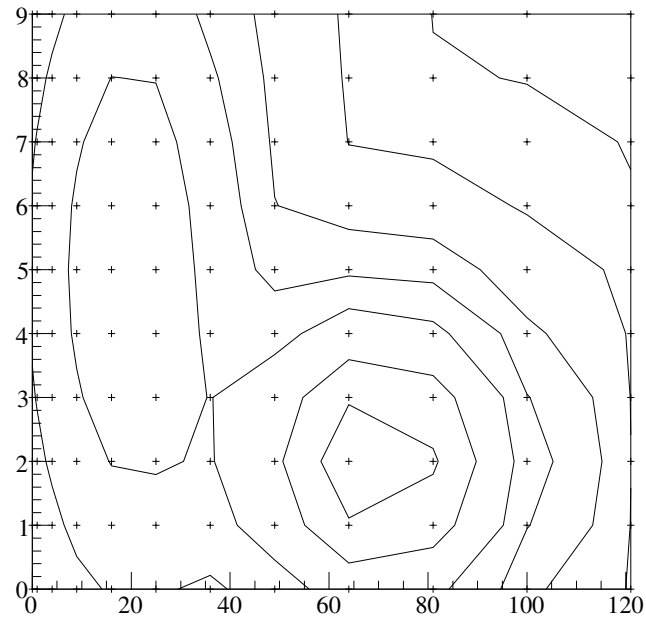


Figure 9: Contour example plot

The `contour` class can also use interpolation to attempt to refine the data grid. The new contours after a refinement of a factor of 5 is given in the figure below.

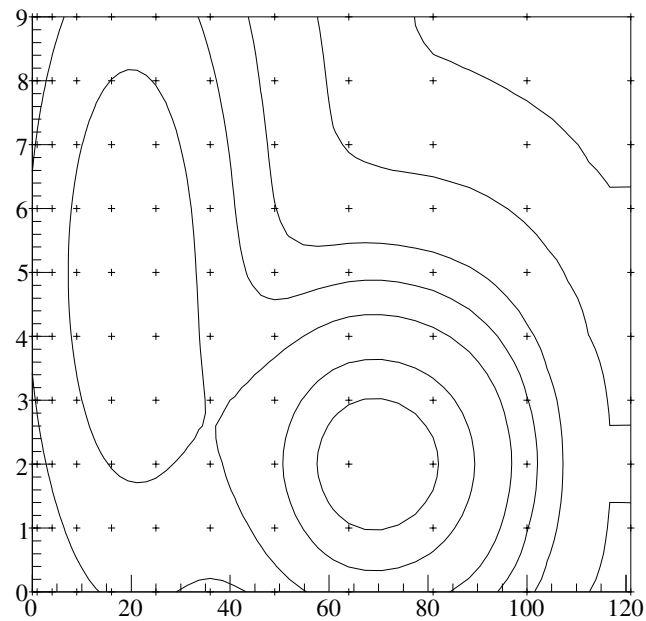


Figure 10: Contour example plot

## 27 Chebyshev Approximation

A class implementing the Chebyshev approximations based on GSL is given in [gsl\\_chebapp](#). This class has its own copy constructor, so that Chebyshev approximations can be copied and passed as arguments to functions. Derivatives and integrals of [gsl\\_chebapp](#) objects are created as new [gsl\\_chebapp](#) objects which can be easily manipulated.

### 27.1 Chebyshev approximation example

This example performs an approximation of the function  $y = \sin[1/(x + 0.08)]$  over  $[0, 2\pi]$ . This function oscillates strongly over this interval and requires a high order approximation to be accurate.

The image below shows the approximation for  $n = 50$  and  $n = 25$ . The  $n = 100$  would be nearly indistinguishable from the exact result on this scale.

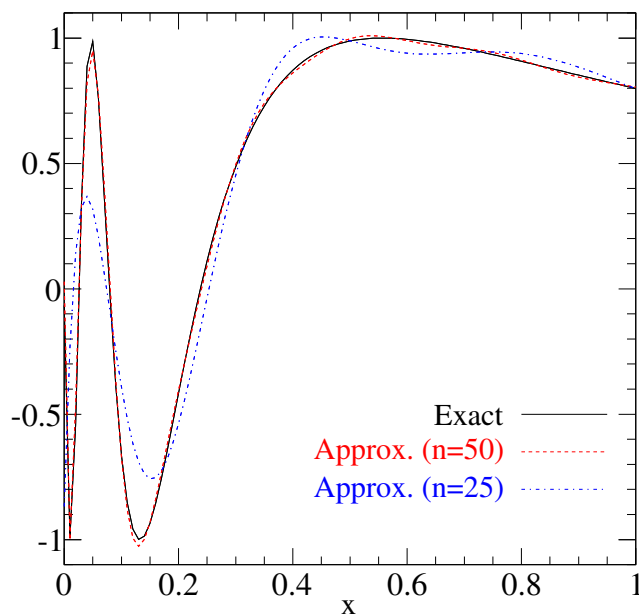


Figure 11: Chebyshev approximation plot

```
/* Example: ex_chebapp.cpp
-----
*/

#include <iostream>
#include <o2scl/constants.h>
#include <o2scl/test_mgr.h>
#include <o2scl/gsl_chebapp.h>
#include <o2scl/bern_deriv.h>
#include <o2scl/gsl_inte_qag.h>

using namespace std;
using namespace o2scl;

double func(double x) {
    return sin(1.0/(x+0.08));
}

double dfunc(double x) {
    return -cos(1.0/(x+0.08))/pow(x+0.08,2.0);
}
```

```
// Simple function to output information to file for plotting
void write_file(gsl_chebapp &gc);

int main(void) {
    test_mgr t;
    t.set_output_level(1);

    cout.setf(ios::scientific);

    funct_fptr tf(func);

    gsl_chebapp gc;
    cern_deriv<> cd;
    gsl_inte_qag<> gi;

    double res, err;
    double x0=0.55;

    // Initialize the Chebyshev approximation
    gc.init(func,100,0.0,2.0*o2scl_const::pi);

    // Evaluate the approximation and compare with the exact result
    cout << "f(0.55)" << endl;
    cout << "Exact      : " << func(x0) << endl;
    gc.eval_err(x0,res,err);
    cout << "Approx (n=100): " << res << endl;
    cout << " Est. Error   : " << err << endl;
    cout << " Act. Error   : " << fabs(res-func(x0)) << endl;

    // Evaluate the approximation at lower order
    gc.eval_n_err(50,x0,res,err);
    cout << "Approx (n=50) : " << res << endl;
    cout << " Est. Error   : " << err << endl;
    cout << " Act. Error   : " << fabs(res-func(x0)) << endl;
    gc.eval_n_err(25,x0,res,err);
    cout << "Approx (n=25) : " << res << endl;
    cout << " Est. Error   : " << err << endl;
    cout << " Act. Error   : " << fabs(res-func(x0)) << endl;
    cout << endl;

    t.test_rel(gc.eval(x0),func(x0),1.0e-4,"eval");

    // Show how to use operator=() to create a new approximation
    gsl_chebapp gc2=gc;
    cout << "Using operator=(): " << gc2.eval(x0) << " " << func(x0) << endl;
    cout << endl;

    t.test_rel(gc2.eval(x0),gc.eval(x0),1.0e-10,"op=");

    // Show how to compute the derivative
    gsl_chebapp gc_deriv;
    gc.deriv(gc_deriv);

    cout << "f' (0.55)" << endl;
    cout << "Exact      : " << dfunc(x0) << endl;
    gc_deriv.eval_err(x0,res,err);
    cout << "Approx (n=100): " << res << endl;
    cout << " Est. Error   : " << err << endl;
    cout << " Act. Error   : " << fabs(res-dfunc(x0)) << endl;
    cd.calc_err(x0,tf,res,err);
    cout << "Direct deriv : " << res << endl;
    cout << " Est. Error   : " << err << endl;
    cout << " Act. Error   : " << fabs(res-dfunc(x0)) << endl;
    cout << endl;

    t.test_abs(res,dfunc(x0),1.0e-12,"deriv with cern_deriv");
    t.test_abs(gc_deriv.eval(x0),dfunc(x0),5.0e-3,"deriv with cheb");

    // Show how to compute the integral
```

```

gsl_chebapp gc_integ;
gc.integ(gc_integ);

cout << "int(f,0,0.55)" << endl;
gc_integ.eval_err(x0,res,err);
cout << "Approx (n=100): " << res << endl;
cout << " Est. Error   : " << err << endl;
gi.integ_err(tf,0.0,x0,res,err);
cout << "Direct integ  : " << res << endl;
cout << " Est. Error   : " << err << endl;
cout << "Rel. Error    : " << fabs(res-gc_integ.eval(x0)) << endl;
cout << endl;

t.test_abs(gc_integ.eval(x0),gi.integ(tf,0.0,x0),1.0e-6,"integral");

write_file(gc);

t.report();
return 0;
}
// End of example

```

## 28 Unit Conversions

There is a class which performs conversion between units specified with strings in [convert\\_units](#). The [convert\\_units\\_gnu](#) class also uses a `system()` call to the GNU units command to obtain the proper conversion factors. Unit conversions are cached so that future requests of the same conversion factor don't require additional `system()` calls.

## 29 File I/O with HDF5

The class [hdf\\_file](#) facilitates I/O of data to hdf files. This class implements a simple way to I/O basic data types and O<sub>2</sub>scl data types. All files created by the [hdf\\_file](#) class are normal HDF5 files, and can be manipulated in the usual way, for example with `h5dump` command-line tool. Users can easily mix code which performs I/O with [hdf\\_file](#) and other O<sub>2</sub>scl functions with their own HDF code. The sole caveat is that O<sub>2</sub>scl cannot parse generic HDF5 files, so that HDF files which contain data not output through O<sub>2</sub>scl cannot always be read by O<sub>2</sub>scl.

Objects are stored by referring to their dataset name. I/O for basic objects is provided directly in the [hdf\\_file](#) class, I/O for [table](#), [table3d](#), and other related objects is documented in [hdf\\_io.h](#).

O<sub>2</sub>scl formats complicated data types for HDF I/O by combining basic data into groups. For that reason, one cannot use O<sub>2</sub>scl to read or write HDF files where groups have the same name as a dataset in the current HDF id. All O<sub>2</sub>scl groups in HDF files come with a string named `o2scl_type`, which refers to the type of object which has been written to the HDF file as a group.

There are some current limitations regarding the matching of error handling policies between O<sub>2</sub>scl and the HDF library. HDF functions do not always call the O<sub>2</sub>scl error handler and thus do not always throw O<sub>2</sub>scl exceptions.

**Idea for Future** Create an HDF file I/O example.

## 30 Other Classes and Functions

The O<sub>2</sub>scl library contains several classes which are still under development and are to be considered experimental. While it is expected that the testing code associated with these classes will succeed on most any system, the interface, structure, and basic approaches used by these classes may change in future versions of O<sub>2</sub>scl.

**Three-dimensional data tables** - [table3d](#)

**Series acceleration** - [gsl\\_series](#)



**Command-line interface** - [cli](#)

**Automatic bin sizing** - [bin\\_size](#)

**Fourier transforms** - [gsl\\_fft](#)

**Polylogarithms** - [polylog](#)

**Histograms** - [hist](#)

**Two-dimensional histograms** - [hist\\_2d](#)

## 31 Library Settings

There are a couple library settings which are handled by a global object `lib_settings` of type `lib_settings_class`.

There are several data files that are used by various classes in the library. The installation procedure should ensure that these files are automatically found. However, if these data files are moved after installation, then a call to `lib_settings_class::set_data_dir()` can adjust the library to use the new directory. It is assumed that the directory structure within the data directory has not changed.

## 32 Development Team

The current O2scl development team is:

- Andrew W. Steiner (Lead dev.)
- Jerry Gagelman

## 33 Design Considerations

The design goal is to create an object-oriented computing library with classes that perform common numerical tasks. The most important principle is that the library should add functionality to the user while at the same time retaining as much freedom for the user as possible and allowing for ease of use and extensibility. To that end,

- The classes which utilize user-specified functions should be able to operate on member functions without requiring a particular inheritance structure,
- The interfaces ought to be generic so that the user can create new classes which perform related numerical tasks through inheritance.
- The classes should not use static variables or status functions.
- Const-correctness and type-safety should be respected wherever possible.
- The design should be somewhat compatible with GSL.

### Header file dependencies

For reference, it's useful to know how the top-level header files depend on each other, since it can be difficult to trace everything down. In the `base` directory, the following are the most "top-level" header files and their associated dependencies within O2scl (there are other dependencies on GSL and the C standard library not listed here).

```
err_hnd.h : (none)
funct.h : (none)
lib_settings.h : (none)
array.h: err_hnd.h
exception.h: err_hnd.h
vector.h: err_hnd.h
```

```

string_conv.h : lib_settings.h
misc.h : err_hnd.h lib_settings.h
test_mgr.h : string_conv.h
uvector_tlate.h: err_hnd.h string_conv.h array.h vector.h
ovector_tlate.h: err_hnd.h string_conv.h uvector_tlate.h array.h vector.h
search_vec.h: err_hnd.h ovector_tlate.h vector.h

```

### Define constants

An attempt at a complete list:

- O2SCL\_NEVER\_DEFINED
- O2SCL\_NO\_EXCEPTIONS
- O2SCL\_READLINE
- O2SCL\_NO\_SYSTEM\_FUNC
- O2SCL\_NO\_RANGE\_CHECK
- O2SCL\_USE\_GSL\_HANDLER

### The use of templates

Templates are used extensively, and this makes for longer compilation times so any code that can be removed conveniently from the header files should be put into source code files instead.

## 33.1 Error handling

### Thread safety

Two approaches to thread-safe error handling which are worth comparing: the first is GSL which uses return codes and global function for an error handler, and the second is the Math/Special Functions section of Boost, which uses a separate policy type for each function. One issue is thread safety: the GSL approach is thread safe only in the sense that one can in principle use the return codes in different threads to track errors. What one cannot do in GSL is use different user-defined error handlers for different threads. The Special Functions library allows one to choose a different Policy for every special function call, and thus allows quite a bit more flexibility in designing multi-threaded error handling.

## 33.2 Memory allocation

Several classes have `allocate()` and `free()` functions to allocate and deallocate memory. If an error occurs in an `allocate()` function, the function should `free()` the partial memory that was allocated and then call the error handler. Functions which deallocate memory should never fail and should never be required to call the error handler. Similarly, class destructors should never be required to call the error handler.

## 33.3 Vector design

O2scl vector and matrix types are a hybrid approach: creating objects compatible with GSL, while providing syntactic simplicity and object-oriented features common to C++ vector classes. In terms of their object-oriented nature, they are not as elegant as the ublas vector types from ublas, but for many applications they are also faster (and they are always at least as fast).

## 33.4 Type-casting in vector and matrix design

O2scl uses a GSL-like approach where viewing `const double *` arrays is performed by explicitly casting away `const`'ness internally and then preventing the user from changing the data.

In GSL, the preprocessor output for `vector/view_source.c` is:

```

gsl_vector_const_view_array (const double * base, size_t n)
{
    _gsl_vector_const_view view = {{0, 0, 0, 0, 0}};

    if (n == 0)
    {
        do { gsl_error ("vector length n must be positive integer", "
            view_source.c", 28, GSL_EINVAL) ; return view ; } while (0);

    }

    {
        gsl_vector v = {0, 0, 0, 0, 0};

        v.data = (double *)base ;
        v.size = n;
        v.stride = 1;
        v.block = 0;
        v.owner = 0;
        ((_gsl_vector_view *)&view)->vector = v;

        return view;
    }
}

```

Note the explicit cast from `const double *` to `double *`. This is similar to what is done in [src/base/ovector\\_tlate.h](#).

### 33.5 Define constants and macros

There are a couple define constants and macros that O<sub>2</sub>scl understands, they are all in upper case and begin with the prefix `O2SCL_`.

Range-checking for arrays and matrices is turned on by default, but can be turned off by defining `O2SCL_NO_RANGE_CHECK` during the initial configuration of the library. To see how the library was configured at runtime, use the [lib\\_settings](#) class.

There are several macros for error handling defined in [err\\_hnd.h](#), and several for vector/matrix arithmetic in [vec\\_arith.h](#).

There is a define constant `O2SCL_NO_SYSTEM_FUNC` which permanently disables the shell command `' ! '` in [cli](#) (when the constant is defined, the shell command doesn't work even if [cli::shell\\_cmd\\_allowed](#) is `true`).

The constant `O2SCL_DATA_DIR` is defined internally to provide the directory which contains the O<sub>2</sub>scl data files. After installation, this can be accessed in [lib\\_settings](#).

All of the header files have their own define constant of the form `O2SCL_HEADER_FILE_NAME` which ensures that the header file is only included once.

Finally, I sometimes comment out sections of code with

```

#ifdef O2SCL_NEVER_DEFINED
...
#endif

```

This constant should not be defined by the user as it will cause compilation to fail.

### 33.6 Parameter ordering

In functions where this makes sense, generally input parameters will appear first, while output parameters or parameters which handle both input and output will appear later.

### 33.7 Global objects

There are four global objects that are created in `libo2scl`:

---

- `def_err_hnd` is the default error handler
- `alt_err_hnd` is the GSL-like error handler
- `err_hnd` is the pointer to the error handler (points to `def_err_hnd` by default)
- `lib_settings` to control a few library settings

All other global objects are to be avoided.

### 33.8 Thread safety

Most of the classes are thread-safe, meaning that two instances of the same class will not clash if their methods are called concurrently since static variables are only used for compile-time constants. However, two threads cannot, in general, safely manipulate the same instance of a class. In this respect, `O2scl` is no different from GSL.

### 33.9 Documentation design

The commands `\comment` and `\endcomment` delineate comments about the documentation that are present in the header files but don't ever show up in the HTML or LaTeX documentation.

### 33.10 Copyright notices

For files where it is appropriate to do so, I have followed the prescription suggested in <http://lists.gnu.org/archive/html/help-gsl/2005-08/msg00001.html> retaining the GSL copyright notices and putting the `O2scl` notices at the top. CERNLIB has no such standard, but their licensing information is outlined at <http://cernlib.web.cern.ch/cernlib/conditions.html>.

### 33.11 Design plans

#### Boost and linear algebra:

I would like to ensure this class is compatible with boost, and start integrating things accordingly. IMHO object-oriented linear algebra is in a rather sad state at the moment. `uBlas` and `MTL` are both promising, however, and I'd like to start implementing some sort of compatibility with `uBlas` vectors and matrices soon. The `uBlas` documentation is pretty sparse, but that's the pot calling the kettle a cheap piece of metal.

#### Other Improvements:

I'm particularly interested in improving the ODE and fitting classes, as well as updating the BFGS2 minimizer. Of course, more examples and better documentation are also a must.

#### Algorithms to include

- Method of lines for PDEs
- Some of the MESA interpolation routines.
- C++ translation of MINUIT (done already by ROOT, but quite difficult).
- Creating closed regions from contour lines (I have no idea how to do this at the moment, though I'm sure someone has solved this problem already somewhere.)

#### Complex numbers

I'm not sure where to go with complex numbers. My guess is that `std::complex` is not significantly slower (or is faster) than `gsl_complex`, but it would be good to check this. Then there's the C99 standard, which is altogether different. Unfortunately the interfaces may be sufficiently different that it's not easy to make templated classes which operate on generic complex number types.

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## 36 Bibliography

Some of the references which contain links should direct you to the work referred to using its DOI identifier.

- Bader83: G. Bader and P. Deuffhard, *Numer. Math.* **41** (1983) 373.
- Birgin00: E.G. Birgin, J.M. Martinez, and M. Raydan, Nonmonotone Spectral Projected Gradient Methods on Convex Sets, *SIAM Journal on Optimization* 10:1196-1211, 2000.
- Broyden65: C.G. Broyden, "A Class of Methods for Solving Nonlinear Simultaneous Equations", *Mathematics of Computation*, vol 19 (1965), p 577-593
- Bus75: **J. C. P. Bus** and **T. J. Dekker**, *ACM Trans. Math. Soft.* **1** (1975) 330.
- Cash90: **J. R. Cash** and **A. H. Karp**, *ACM Trans. Math. Soft.* **16** (1990) 201.
- EngelnMullges96: G. Engeln-Müllges and F. Uhlig, *Numerical Algorithms in C* (1996) Springer, p. 96.
- Fletcher87: R. Fletcher, *Practical methods of optimization* (John Wiley & Sons, Chichester 1987) p. 39.
- Garbow80: B. S. Garbow, K. E. Hillstom, and J. J. More, MINPACK project, Argonne Nat'l Lab, March 1980.
- Hairer00: Hairer, E., Norsett S.P., Wanner, G. *Solving ordinary differential equations I, Nonstiff Problems*, 2nd revised edition, Springer, 2000.
- Kelley99: C.T. Kelley, *Iterative Methods of Optimization*, SIAM, Philadelphia, 1999.
- Krabs83: W. Krabs, *Einführung in die lineare und nichtlineare Optimierung für Ingenieure* (BSB B.G. Teubner, Leipzig 1983) p. 84.
- Lepage78: **G. P. Lepage**, *J. Comp. Phys.* **27** (1978) 192.
- Lewin83: L. Lewin, *Polylogarithms and Associated Functions* (North-Holland, New York, 1983).
- Longman58: I.M. Longman, *MTAC* (later renamed *Math. Comp.*) **12** (1958) 205.
- More79: J.J. More' and M.Y. Cosnard, *ACM Trans. Math. Software*, **5** (1979) 64-85.
- More80: J.J. More' and M.Y. Cosnard, *Algorithm 554 BRENTM*, *Collected Algorithms from CACM* (1980).
- Muller96: H. Muller and B.D. Serot, *Nucl. Phys. A*, 606 (1996) 508.
- Nelder65: J.A. Nelder and R. Mead, *Computer Journal* 7 (1965) pp. 308-313.
- Piessens83: R. Piessens, E. de Doncker-Kapenga, C. Uberhuber, and D. Kahaner *QUADPACK, A Subroutine Package for Automatic Integration* (1983) Springer-Verlag.
- Press90: W.H. Press and G.R. Farrar, "Recursive Stratified Sampling for Multidimensional Monte Carlo Integration", *Computers in Physics*, v4 (1990), pp. 190-195.
- Prince81: P.J. Prince and J.R. Dormand *J. Comp. Appl. Math.*, 7 (1981) 67.
- Rutishauser63: H. Rutishauser, *Ausdehnung des Rombergschen Prinzips* (Extension of Romberg's Principle), *Numer. Math.* **5** (1963) 48-54.
- Tolstov62: G.P. Tolstov, *"Fourier Series"* (1962) Englewood Cliffs: Prentice Hall.
- Wynn56: P. Wynn On a device for computing the  $e_m(S_n)$  transformation, *Math. Tables Aids Comput.* 10 (1956) 91.

## 37 Developer Guidelines

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### General coding guidelines:

- Comment code liberally.
- Avoid goto statements.

- Avoid hard-coded numerical values which are not either: (i) well-commented, or (ii) parameters modifiable by a class-user.
- Match the existing coding style when possible.
- Make sure all lines fit in 78 columns.
- Because this is a library (and not a end-user executable), it is generally better to call the error handler when an input is incorrectly specified instead of assuming some alternative correct value.
- All new classes deserve new documentation and new testing code.
- Documentation and code should be in standard American English.
- All code must be released in GPLv3.
- Global variables and static member data should be avoided.
- When reasonable, put input parameters first and output parameters last.
- When possible, templated vector parameters with `size_t` arguments should appear similar to `size_t &n`, `vec_t &v`, and in that order.
- All code should be ANSI-compatible, and, inasmuch as is possible, operating system and platform independent.
- Exception messages should be as informative as possible.
- Exception messages should end with the full class and function name from where they are thrown.
- Functions which deallocate memory should never fail and should never be required to call the error handler. Also, class destructors should never be required to call the error handler.
- Avoid passing pointers. Pass either bare objects (which then require copy constructors), shared pointers, or const references.
- For numeric parameters to functions, if not all values are permissible, then the error handler should be called when a non-permissible value is given by the user and the function documentation should clearly explain why.
- Wherever possible, objects should be usable by default. Avoid zombie objects which are instantiated but unusable.
- Objects should thread-safe in the weak sense, that is, different processes should be able to safely access and modify different instances of the same class at any time. Functions which read (but not modify) class data should be thread-safe in the strong sense, that is, different processes should be able to read the same instance of a class at any time.
- Whereever possible, ensure your code compiles without warnings using flags analogous to the gcc string

```
-ansi -pedantic -Wno-long-long -Wall -Wno-unused -Wextra
-Wconversion -Wshadow -Wpointer-arith -Wcast-align -Wwrite-strings
```

- Avoid 'try' blocks, as a goal is that O<sub>2</sub>scl should compile with `-fno-exceptions`.
- Functions which return `void` should end with `return;`.

#### Documentation guidelines:

- Refer to other classes with `\ref` if necessary. Refer to function parameters with `\c` or embed them in html TT (text-type) commands.
- Bibliographic references should be used. When possible, include the DOI link which begins with the prefix <http://dx.doi.org> (not the vendor-specific DOI link).
- Comment Doxygen documentation with `\comment` and `\endcomment`. (Yes, sometimes comments in comments are useful.)

#### Patches:

- For those who are uncomfortable with Subversion, patches are always accepted.
- Prepare patches based on the most recent version of the trunk or the appropriate branch.

#### SVN:

- Editing the trunk directly should be avoided. Most development should occur on branches, to be merged with the trunk at the appropriate time.
- Ideally the trunk should always compile and all the tests should pass.
- Communicate with the lead developer before, during, and after any non-trivial development. Communicate your ideas before development, so that you don't write many lines of code only to find that your new code will be rejected. Communicate your ideas during development to avoid conflicting changes. Communicate your ideas after development to ensure they have a chance of being implemented. Subversion is not a replacement for real communication.
- Commit often.
- Merge carefully. If you fail to merge correctly, code added by other developers will be (at least temporarily) lost.
- Branches will be merged into the trunk by the lead developer at whatever time they deem appropriate.
- Developer-specific files which are not platform-independent should not be added to the repository. Sometimes `svn:ignore` can be used to ignore these files, but this should be done sparingly.

## 38 Download O2scl

The current version is 0.910. The source distribution can be obtained from

- <http://sourceforge.net/projects/o2scl/files/>

You may also download O2scl from version from the Subversion repository. To obtain the bleeding-edge developer version, use something like

```
svn co https://o2scl.svn.sourceforge.net/svnroot/o2scl/trunk o2scl
```

The checkout process is a bit more time consuming than directly downloading the source distribution.

Version 0.910 corresponds with version 376 in the svn repository.

Version 0.909 corresponds with version 317 in the svn repository.

Version 0.908 corresponds with version 200 in the svn repository.

Version 0.907 corresponds with version 107 in the svn repository.

Version 0.906 corresponds with version 54 in the svn repository.

Version 0.905 corresponds with version 48 in the svn repository.

Version 0.904 corresponds with version 40 in the svn repository.

Version 0.903 does not exist (this number was skipped to help coordinate numbering with O2scl\_ext ).

Version 0.902 corresponds with version 37 in the svn repository.

Version 0.901 corresponds with version 31 in the svn repository.

Version 0.9 corresponds with version 26 in the svn repository.

Version 0.806 was a quick release to fix some issues with compilations in Mac OS X and does not correspond exactly with a version in the repository.

Version 0.805 corresponds with version 16 in the svn repository.



## 39 Ideas for Future Development

**Class `anneal_mt< param_t, param_vec_t, func_t, vec_t, alloc_vec_t, alloc_t, rng_t >`**

There may be a good way to remove the function indirection here to make this class a bit faster.

**File `array.h`**

Create a class which views a C-style array as a matrix and offers an `operator (, )`

**Class `array_alloc< vec_t >`**

Might it be possible to rework this so that it does range checking and ensures that the user doesn't try to allocate more or less space? I.e. `array_alloc<double[2]>` complains if you try an `allocate(x,3)`?

**Class `array_const_subvector`**

Make the member data truly const and remove the extra typecast.

**Class `bin_size`**

Finish this.

**File `cblas_base.h`**

Add float and complex versions.

There are some Level-1 BLAS functions which are already present in `vector.h`. Should we move all of them to one place or the other? The ones in `vector.h` are generic in the sense that they can use doubles or floats, but the ones here can use either `()` or `[]`.

**Class `cern_adapt< func_t, nsub >`**

Allow user to set the initial subdivisions?

- It might be interesting to directly compare the performance of this class to `gsl_inte_qag`.
- There is a fixme entry in the code which could be resolved.
- Output the point where most subdividing was required?

**Class `cern_deriv< func_t >`**

All of the coefficients appear to be fractions which could be replaced with exact representation?

Record the number of function calls?

**Class `cern_gauss< func_t >`**

Allow user to change `cst`?

**Class `cern_mroot< func_t, vec_t, alloc_vec_t, alloc_t, jfunc_t >`**

Modify this so it handles functions which return non-zero values.

Move some of the memory allocation out of `msolve()`

Give the user access to the number of function calls

Rename `nier6`, `nier7`, and `nier8` to something sensible.

It may be that the `O2scl` native Householder transformations should be used here instead of the inline version given here.

**Class `cern_mroot_root< func_t >`**

Double-check this class to make sure it cannot fail while returning 0 for success.

**Global `cern_mroot_root< func_t >::eps`**

This number should probably default to one of the GSL tolerances.

**Class `cli`**

Warn in `run_interactive()` when extra parameters are given

Include a "remove command" function

A replace command function, there's already some code in `cli.cpp` for this.

There's some code duplication between `comm_option_run()` and `run_interactive()`

Allow the user to set the tilde string

Disallow direct access to `cli::par_list` in order to ensure parameter names do not contain whitespace

**Global `cli::cli_gets` (const char \*c)**

Think about whether or not this should be protected? (Possibly not, as it's extensively used by `acolm.cpp`)

**Class `columnify`**

Move the `screenify()` functionality from `misc.h` into this class?

It might be better to allow the string table to be specified with iterators.

**Class `comp_gen_inte< func_t, lfunc_t, ufunc_t, vec_t, alloc_vec_t, alloc_t >`**

Provide an example of usage for this class.

**Class `composite_inte< func_t, vec_t, alloc_vec_t, alloc_t >`**

Create a function to set an entire array of one-dimensional integration objects at once

**Class `contour`**

Rewrite the code which adjusts the contour levels to ensure contours don't go through the data to adjust the internal copy of the data instead.

It would be nice to have a function which creates a set of closed regions to fill which represent the data. However, this likely requires a completely new algorithm, because it's not easy to simply close the contours already generated by the `calc_contours()` function. There are, for example, several cases which are difficult to handle, such as filling a region in between several closed contours.

**Global `contour::get_data` (size\_t &size\_x, size\_t &size\_y, ovector \* &x\_fun, ovector \* &y\_fun, omatrix \* &udata)**

There is probably a better way than returning pointers to the internal data.

**Class `contour_line`**

Write HDF I/O for contour lines?

Make this a subclass of `contour`.

**Class `convert_units`**

Ideally, a real C++ API for the GNU units command would be better.

**File `cx_arith.h`**

Define operators with assignment for complex + double?

**Class `deriv< func_t >`**

Improve the methods for second and third derivatives

**Class `edge_crossings`**

Write HDF I/O object for edge crossings

Make this a subclass of `contour`.

**Class `eqi_deriv< func_t, vec_t >`**

Finish the second and third derivative formulas.

**Class `err_hnd_type`**

There may be an issue associated with the string manipulations causing errors in the error handler.

**Class `expect_val`**

If `n_per_block` is nonzero and the user adds more than `n_blocks` times `n_per_block` data, set `n_per_block` to zero, allocate the `last` structure and fall back to the variable block size method.

**Page File I/O with HDF5**

Create an HDF file I/O example.

**Class `format_float`**

Handle inf's and nan's correctly.

Allow change of string for the "+" sign for the exponent

**Class `gen_inte< func_t, lfunc_t, ufunc_t, vec_t >`**

It might be interesting to construct a child class of `gen_inte` which automatically transforms variables to a hypercube and then applies a child of `multi_inte` to do the integration.

**Class `gen_test_number< tot >`**

Document what happens if `tot` is pathologically small.

**Class `gradient< func_t, vec_t >`**

Consider making an `exact_grad` class for computing exact gradients.

**Class `gsl_anneal< func_t, vec_t, alloc_vec_t, alloc_t, rng_t >`**

There's `x0`, `old_x`, `new_x`, `best_x`, and `x`? There's probably some duplication here which could be avoided.

- Implement a more general simulated annealing routine which would allow the solution of discrete problems like the - Traveling Salesman problem.

**Class `gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >`**

Compare more directly to GSL

**Class `gsl_bsimp< func_t, jac_func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t >`**

Create an example with a stiff diff eq. which requires this kind of stepper

More detailed documentation about the algorithm

Figure out if this should be a child of `ode_step` or `adapt_step`. The function `step_local()` is actually its own ODE stepper and could be reimplemented as an object of type `ode_step`.

I don't like setting `yerr` to `GSL_POSINF`, there should be a better way to force an adaptive stepper which is calling this stepper to readjust the stepsize.

The functions `deuf_kchoice()` and `compute_weights()` can be moved out of this header file

Rework internal arrays as `uvector`s?

Rework linear solver to be amenable to using a sparse matrix solver

**Global `gsl_cubic_real_coeff::gsl_poly_complex_solve_cubic2` (double a, double b, double c, gsl\_complex \*z0, gsl\_complex \*z1, gsl\_complex \*z2)**

I think the GSL function is now fixed, so we can fall back to the original GSL function here.

**Class `gsl_deriv< func_t >`**

Include the forward and backward GSL derivatives?

**Class `gsl_inte_kronrod< func_t >`**

Convert 'double \*' objects to `uvector`

**Global `gsl_inte_kronrod< func_t >::gauss_kronrod_base` (func2\_t &func, double a, double b, double \*result, double \*abserr, double \*resabs, double \*resasc)**

This function, in principle, is an integration object in and of itself, and could be implemented separately as an object of type `inte`.

**Class `gsl_inte_qag< func_t >`**

There are a few fine-tuned parameters which should be re-expressed as data members in the convergence tests.

Should QUADPACK parameters in round-off tests be subject to adjustments by the end user?

Add functions to examine the contents of the workspace to detect regions where the integrand may be problematic; possibly call these functions automatically depending on verbosity settings.

**Global `gsl_inte_qag< func_t >::qag` (func\_t &func, const double a, const double b, const double l\_epsabs, const double l\_epsrel, double \*result, double \*abserr)**

Just move this function to `integ_err()`.

**Class `gsl_inte_qawc< func_t >`**

Make `cern_cauchy` and this class consistent in the way which they require the user to provide the denominator in the integrand

Global `gsl_inte_qawo_sin< func_t >::qawo` (`func_t &func`, `const double a`, `const double epsabs`, `const double epsrel`, `gsl_inte_workspace *loc_w`, `gsl_integration_qawo_table *wf`, `double *result`, `double *abserr`)

Remove goto statements.

Class `gsl_inte_singular< func_t >`

Some of the functions inside this class could be moved out of header files?

Global `gsl_inte_singular< func_t >::extrap_table`

Move this to a new class, with `qelg()` as a method

Global `gsl_inte_singular< func_t >::extrap_table`

Move this to a new class, with `qelg()` as a method

Global `gsl_inte_singular< func_t >::qags` (`func_t &func`, `const double a`, `const double b`, `const double l_epsabs`, `const double l_epsrel`, `double *result`, `double *abserr`)

Remove goto statements. Before this is done, it might be best to add some tests which fail in the various ways.

Global `gsl_min_brent< func_t >::iterate ()`

It looks like `x_left` and `x_right` can be removed. Also, it would be great to replace the one-letter variable names with something more meaningful.

Class `gsl_min_quad_golden< func_t >`

Take common elements of this and `gsl_min_brent` and move to a generic GSL minimizer type?

Global `gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::estimate_corrmc` (`func_t &func`, `size_t ndim`, `const vec_t &xl`, `const vec_t &xu`, `size_t calls`, `double &res`, `double &err`, `const uvector &lxmlid`, `uvector &lsigma_l`, `uvector &lsigma_r`)

Remove the reference to `GSL_POSINF` and replace with a function parameter.

Class `gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >`

Double check that the updates in `gsl-1.13` are included here, and also add support for the `nmsimplex2rand` algorithm in `GSL`.

Class `gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >`

It's kind of strange that `set()` sets `jac_given` to false and `set_de()` has to reset it to true. Can this be simplified?

It might be good to make sure that we're directly testing to make sure that `GSL` and `O2SCL` are more or less identical.

Many of these minpack functions could be put in their own "minpack\_tools" class, or possibly moved to be linear algebra routines instead.

There are still some numbers in here which the user could have control over, for example, the `nslow2` threshold which indicates failure.

Class `gsl_quartic_real`

Optimize value of `cube_root_tol` and compare more clearly to `gsl_quartic_real2`

Class `gsl_quartic_real2`

Optimize value of `cube_root_tol` and compare more clearly to `gsl_quartic_real`

Class `gsl_root_brent< func_t >`

There is some duplication in the variables `x_lower`, `x_upper`, `a`, and `b`, which could be removed. Some better variable names would also be helpful.

Create a meaningful enum list for `gsl_root_brent::test_form`.

Class `gsl_root_stef< func_t, dfunc_t >`

There's some extra copying here which can probably be removed.

Compare directly to `GSL`.

This can probably be modified to shorten the step if the function goes out of bounds as in `gsl_mroot_hybrids`.

Class `gsl_series`

Move the workspaces to classes?

**Class `gsl_smooth`**

Generalize to generic vector types. (Does this require reworking the GSL linear fitting routines?) In the meantime, make a `ovector` interface.

Possibly create a new `gsl_bspline` class which replaces the GSL bspline workspace

Allow user to probe chi squared and the covariance?

**Class `gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`**

Prettify the verbose output

Allow the user to get information about the how the sampling was done, possibly by converting the bins and boxes into a structure or class.

Allow the user to change the maximum number of bins.

**Class `hdf_file`**

Automatically close groups, e.g. by storing `hid_t`'s in a stack?

**Class `hist`**

Would be nice not to have to create a new `search_vec` object in `get_bin_index()`.

Consider adding the analogs of the GSL histogram sampling functions

Add a function which computes the bin sizes?

**Class `hist_2d`**

Write a function to create a 1-d histogram from a 2-d histogram either by selecting one bin in one axis or by marginalizing over one direction.

**Global `hybrids_base::compute_df` (`size_t n`, `const vec2_t &ff_trial`, `const vec2_t &fl`, `ovector_base &dfl`)**

Replace with `daxpy`?

**Global `hybrids_base::compute_qtf` (`size_t N`, `const vec2_t &q2`, `const vec3_t &f2`, `vec4_t &qtf2`)**

This is just right-multiplication, so we could use the `O2scl cblas` routines instead.

**Global `hybrids_base::compute_trial_step` (`size_t N`, `vec2_t &xl`, `vec2_t &dxl`, `vec2_t &xx_trial`)**

Replace with `daxpy`.

**Global `hybrids_base::enorm` (`size_t N`, `const vec2_t &ff`)**

Replace this with `dnrm2` from `cblas_base.h`

**Class `inte< func_t >`**

It might be useful to have all of the integration classes report the number of function evaluations used in addition to the number of iterations which were taken

**Class `lanczos< vec_t, mat_t, alloc_vec_t, alloc_t >`**

The function `eigen_tdiag()` automatically sorts the eigenvalues, which may not be necessary.

Do something better than the naive matrix-vector product. For example, use `dgemm()` and allow user to specify column or row-major.

Rework memory allocation to perform as needed.

**Global `matrix_cx_copy_gsl` (`size_t M`, `size_t N`, `mat_t &src`, `mat2_t &dest`)**

At present this works only with complex types based directly on the GSL complex format. This could be improved.

**Global `matrix_max` (`size_t n`, `const size_t m`, `const mat_t &data`)**

Write `matrix_max_index()` and related functions similar to the way `vector_max_index()` works.

**Global `matrix_out` (`std::ostream &os`, `mat_t &A`, `size_t nrows`, `size_t ncols`)**

If all of the matrix elements are positive integers and scientific mode is not set, then we can avoid printing the extra spaces.

**Class `matrix_row< mat_t >`**

Generalize to `operator(,)`

**Page Minimization**

Plot the spring function

**Class `minimize< func_t, dfunc_t >`**

Add a class for the quad\_golden algorithm from GSL.

**Global `minimize< func_t, dfunc_t >::bracket` (double &ax, double &bx, double &cx, double &fa, double &fb, double &fc, func\_t &func)**

Improve this algorithm with the golden ratio method in gsl/min/bracketing.c?

**Class `minimize_de< func_t, dfunc_t >`**

Create a version of `gsl_mmin_conf` which implements a minimizer with this interface.

**Class `mroot< func_t, vec_t, jfunc_t >`**

Change ntrial to size\_t?

**Global `O2SCL_ASSERT` (ev)**

Make this consistent with `assert()` using `NDEBUG`?

**Global `o2scl_graph::new_graph_ticks` (TCanvas \*&c1, TPad \*&p1, TH1 \*&th1, std::string CanvasName, std::string - WindowName, std::string PadName, double lleft, double lbottom, double lright, double ltop, TGaxis \*&a1, TGaxis \*&a2, int left=0, int top=0, int right=700, int bottom=700, bool logx=false, bool logy=false)**

Modify this to just directly call `new_graph()` and add the new axes on top.

**Namespace `o2scl_linalg`**

Move this documentation to the linalg directory.

**Global `o2scl_linalg::HH_svx` (size\_t N, size\_t M, mat\_t &A, vec\_t &x)**

Handle memory allocation like the tridiagonal functions.

**Class `o2scl_linalg::linear_solver< vec_t, mat_t >`**

The test code uses a Hilbert matrix, which is known to be ill-conditioned, especially for the larger sizes. This should probably be changed.

**Global `o2scl_linalg::LU_decomp` (const size\_t N, mat\_t &A, o2scl::permutation &p, int &signum)**

The "swap rows j and i\_pivot" section could probably be made more efficient using a "matrix\_row"-like object as done in GSL. (7/16/09 - I've tried this, and it doesn't seem to improve the speed significantly.)

**Global `o2scl_linalg::LU_invert` (const size\_t N, const mat\_t &LU, const o2scl::permutation &p, mat2\_t &inverse)**

Could rewrite to avoid `mat_col_t`, (9/16/09 - However, the function may be faster if `mat_col_t` is left in, so it's unclear what's best.)

**Global `o2scl_linalg::solve_cyc_tridiag_nonsym` (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N, mem\_t &m)**

Offer an option to avoid throwing on divide by zero?

**Global `o2scl_linalg::solve_tridiag_nonsym` (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N, mem\_t &m)**

Offer an option to avoid throwing on divide by zero?

**Class `ode_bv_mshoot< func_t, mat_t, vec_t, alloc_vec_t, alloc_t, vec_int_t >`**

Make a class which performs an iterative linear solver which uses sparse matrices like `ode_it_solve`?

**Class `ode_it_solve< func_t, vec_t, mat_t, matrix_row_t, solver_vec_t, solver_mat_t >`**

Create a GSL-like `set()` and `iterate()` interface

Implement as a child of `ode_bv_solve`?

Max and average tolerance?

**Class `ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >`**

The form of `solve_final_value()` is very similar to that of `adapt_step::astep_full()`, but not quite the same. Maybe should probably be made to be consistent with each other?

Global `ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_grid` (double h, size\_t n, size\_t nsol, vec\_t &xsol, mat\_t &ysol, mat\_t &err\_sol, mat\_t &dydx\_sol, func\_t &derivs)

Consider making a version of grid which gives the same answers as solve\_final\_value(). After each proposed step, it would go back and fill in the grid points if the proposed step was past the next grid point.

Global `ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_store` (double x0, double x1, double h, size\_t n, size\_t &n\_sol, vec\_t &x\_sol, mat\_t &y\_sol, mat\_t &yerr\_sol, mat\_t &dydx\_sol, func\_t &derivs, size\_t istart=0)

It might be possible to remove some extra copying by removing the yerrl and dydx vectors

Class `ofvector< N >`

Consider making allocate() and free() functions private for this class?

Class `omatrix_col_tlate< data_t, mparent_t, vparent_t, block_t >`

Also do a umatrix constructor since we can't do that with uectors

File `omatrix_tlate.h`

The `xmatrix` class demonstrates how operator[] could return an `ovector_array` object and thus provide more bounds-checking. This would demand including a new parameter in `omatrix_view_tlate` which contains the vector type.

Class `ool_constr_mmin< func_t, dfunc_t, hfunc_t, vec_t, alloc_vec_t, alloc_t >`

Implement automatic computations of gradient and Hessian

Construct a more difficult example for the "examples" directory

Finish mmin() interface

Implement a direct computation of the hessian as the jacobian of the gradient

Class `ool_mmin_pgrad< func_t, dfunc_t, vec_t, alloc_vec_t, alloc_t >`

Replace the explicit norm computation below with the more accurate `dnrm2` from `linalg`

Replace the generic variable 'tol' with 'tolf' or 'tolx' from `multi_min`.

Class `ool_mmin_spg< func_t, dfunc_t, vec_t, alloc_vec_t, alloc_t >`

There is some memory allocation which isn't deallocated until the destructor, and should be handled a bit more elegantly.

Global `operator<< (std::ostream &os, const umatrix_cx_view_tlate< data_t, complex_t > &v)`

Make this function work even when scientific mode is not on, either by converting to scientific mode and converting back, or by leaving scientific mode off and padding with spaces

Global `operator<< (std::ostream &os, const umatrix_const_view_tlate< data_t > &v)`

This assumes that scientific mode is on and showpos is off. It'd be nice to fix this.

Global `operator<< (std::ostream &os, const omatrix_const_view_tlate< data_t, parent_t, block_t > &v)`

This assumes that scientific mode is on and showpos is off. It'd be nice to fix this.

Class `other_todos_and_bugs`

Make sure we have a `uvector_cx_alloc`, `ovector_cx_const_reverse`, `ovector_cx_const_subvector_reverse`, `uvector_reverse`, `uvector_const_reverse`, `uvector_subvector_reverse`, `uvector_const_subvector_reverse`, `omatrix_cx_diag`, `blah_const_diag`, `umatrix_diag`, and `umatrix_cx_diag`

- `ovector_cx_view::operator=(uvector_cx_view &)` is missing
- `ovector_cx::operator=(uvector_cx_view &)` is missing
- `uvector_c_view::operator+=(complex)` is missing
- `uvector_c_view::operator-=(complex)` is missing
- `uvector_c_view::operator*=(complex)` is missing

Currently, I believe the testing code requires the shared libraries and may not work if the static libraries only are installed. It would be nice to ensure the tests could be compiled in either case.

Class `ovector_alloc`

Could (or should?) the allocate() functions be adapted to return an integer error value?

**Class `ovector_const_reverse_tlate< data_t, vparent_t, block_t >`**

I think that maybe in order to ensure that this isn't created from an already reversed vector, this class has to be separated from the hierarchy altogether. However, I think this might break the smart interpolation stuff.

**File `ovector_tlate.h`**

Clean up maybe by moving, for example, ovector reverse classes to a different header file

Define ovector\_uint classes?

**Class `pinside`**

The inside() functions actually copy the points twice. This can be made more efficient.

**Class `planar_intp< vec_t, mat_t >`**

Rewrite so that it never fails unless all the points in the data set lie on a line. This would probably demand sorting all of the points by distance from desired location. (11/1/11 - Maybe not. We might be able to get away with just storing an vector which records the index j of the point in the data set which is the nearest neighbor for each point i in the data set.)

Instead of comparing den with zero, add the option of comparing it with a small number.

Allow the user to specify the scales used for x and y, instead of computing max-min every time.

The generalization to more dimensions might be straight forward.

**Class `pointer_2d_alloc< base_t >`**

There may be a slight issue here if the pointer allocation succeeds and the list insertion fails, and the user catches the exception thrown by the list insertion failure, then a memory leak will ensue. This might be partially ameliorated by counting allocations and insertions. This failure mechanism is rarely encountered in practice.

**Class `pointer_alloc< base_t >`**

There may be a slight issue here if the pointer allocation succeeds and the list insertion fails, and the user catches the exception thrown by the list insertion failure, then a memory leak will ensue. This might be partially ameliorated by counting allocations and insertions. This failure mechanism is rarely encountered in practice.

**File `poly.h`**

The quartics are tested only for a4=1, which should probably be generalized.

**Class `polylog`**

Give error estimate?

- Improve accuracy?
- Use more sophisticated interpolation?
- Add the series  $Li(n, x) = x + 2^{-n}x^2 + 3^{-n}x^3 + \dots$  for  $x \rightarrow 0$ ?
- Implement for positive arguments  $< 1.0$
- Make another polylog class which implements series acceleration?

**Global `quadratic_extremum_x (double x1, double x2, double x3, double y1, double y2, double y3)`**

Make a function quadratic\_points(double x1, double x2, double x3, double y1, double y2, double y3, double &a, double &b, double &c)?

Make a quadratic\_extremum\_xy()?

**Class `rnga`**

Consider some analog of the GSL function `gsl_rng_uniform_pos()`, i.e. as used in the GSL Monte Carlo classes.

**Global `rnga::clock_seed ()`**

Figure out a better way of computing a random seed in a platform-independent way.

**Class `root< func_t, dfunc_t >`**

Maybe consider allowing the user to specify the stream to which 'verbose' information is sent.

**Class `root_de< func_t, dfunc_t >`**

At the moment, the functions solve() and solve\_bkt() are not implemented for derivative solvers.



Global `scalar_ev::reblock_avg_stats` (`size_t new_blocks`, `double &avg`, `double &std_dev`, `double &avg_err`, `size_t &m_per_block`) `const`

Use recurrence relation for averages here rather than dividing at the end.

Class `search_vec< vec_t >`

Consider a sanity check to ensure that the cache is never larger than the vector length.

Global `search_vec< vec_t >::ordered_lookup` (`const double x0`) `const`

This function just uses the `find` functions and then adjusts the answer at the end if necessary. It might be possible to improve the speed by rewriting this from scratch.

Global `search_vec_ext< vec_t >::search_vec_ext` (`size_t nn`, `vec_t &x`)

This could be rewritten to allow vectors with only one element (5/2/11: It looks like this might have been done already?)

Class `smart_interp_vec< vec_t, svec_t, alloc_vec_t, alloc_t >`

Properly implement handling of non-monotonic regions in the derivative functions as well as the interpolation function.

Class `table`

Rewrite the `table::create_array()` and `table::insert_data()` functions for generic vector type

- Return the empty column in the `operator[]` functions as is done for the `get_column()` functions.
- A "delete rows" method to delete a range of several rows
- The present structure, `std::map<std::string, col, string_comp> atree` and `std::vector<aiter> alist`; could be replaced with `std::vector<col> list` and `std::map<std::string, int> tree` where the map just stores the index of the the column in the list.

Class `table3d`

Improve interpolation and derivative caching

Make a 'const' version of the interpolation functions

Should there be a `clear_grid()` function separate from `clear_data()` and `clear_table()`?

Class `table_units`

Make table methods virtual? (not necessary yet since `delete_column()` isn't referred to internally)

Class `tensor`

Could implement arithmetic operators + and - and some different products.

Implement copies to and from vector and matrices

Implement tensor contractions, i.e. `tensor = tensor * tensor`

Consider making a template type to replace double, e.g. `value_t`.

Could be interesting to write an iterator for this class.

Class `tensor_grid`

Only allocate space for grid if it is set

Could implement arithmetic operators + and - and some different products.

Consider creating a `set_grid()` function which takes grids from an object like `hist_grid`. Maybe make a constructor for a `tensor_grid` object which just takes as input a set of grids?

Global `tensor_grid::interpolate` (`double *vals`)

Maybe make this a template as well?

It should be straightforward to improve the scaling of this algorithm significantly by creating a "window" of local points around the point of interest. This could be done easily by constructing an initial subtensor. However, this should probably be superseded by a more generic alternative which avoids explicit use of the 1-d interpolation types.

It should be straightforward to improve the scaling of this algorithm significantly by creating a "window" of local points around the point of interest. This could be done easily by constructing an initial subtensor. However, this should probably be superseded by a more generic alternative which avoids explicit use of the 1-d interpolation types.

**Global `tensor_grid::set_grid` (`const vec_t &grid_vec`)**

Define a more generic interface for matrix types

**Class `tensor_old`**

Could implement arithmetic operators + and - and some different products.

Implement copies to and from vector and matrices

Implement `tensor_old` contractions, i.e. `tensor_old = tensor_old * tensor_old`

Consider making a template type to replace double, e.g. `value_t`.

Could be interesting to write an iterator for this class.

**Class `tensor_old_grid`**

Only allocate space for grid if it is set

Could implement arithmetic operators + and - and some different products.

Consider creating a `set_grid()` function which takes grids from an object like `hist_grid`. Maybe make a constructor for a `tensor_old_grid` object which just takes as input a set of grids?

**Global `tensor_old_grid::interpolate` (`double *vals`)**

Maybe make this a template as well?

It should be straightforward to improve the scaling of this algorithm significantly by creating a "window" of local points around the point of interest. This could be done easily by constructing an initial `subtensor_old`. However, this should probably be superseded by a more generic alternative which avoids explicit use of the 1-d interpolation types.

It should be straightforward to improve the scaling of this algorithm significantly by creating a "window" of local points around the point of interest. This could be done easily by constructing an initial `subtensor_old`. However, this should probably be superseded by a more generic alternative which avoids explicit use of the 1-d interpolation types.

**Global `tensor_old_grid::set_grid` (`const vec_t &grid`)**

Define a more generic interface for matrix types

**Class `test_mgr`**

`test_mgr::success` and `test_mgr::last_fail` should be protected, but that breaks the `operator+()` function. Can this be fixed?

**Class `twod_intp`**

Could also include mixed second/first derivatives: `deriv_xxy` and `deriv_xyy`.

Implement an improved caching system in case, for example `xfirst` is true and the last interpolation used the same value of `x`.

**Class `uvector_const_view_tlate< data_t >`**

Could allow user-defined specification of restrict keyword

**Class `uvector_cx_view_tlate< data_t, complex_t >`**

Write `lookup()` method, and possibly an `erase()` method.

**File `vec_arith.h`**

Define operators for complex vector \* real matrix

Define `==` and `!=` for complex vectors

These should be replaced by the BLAS routines where possible?

**File `vec_stats.h`**

Consider generalizing to other data types.

**File `vector.h`**

Create a matrix transpose copy function?

Create matrix swap row and column functions

**Global `vector_cx_copy_gsl` (`size_t N`, `vec_t &src`, `vec2_t &dest`)**

At present this works only with complex types based directly on the GSL complex format. This could be improved.

**Global `vector_lookup` (`size_t n`, `const vec_t &x`, `double x0`)**

Write `matrix_lookup()`.

## 40 Todo List

### Class `cli`

Long options cannot be one letter long, or else `process_args()` will fail, thus the class should throw if a long option with only one letter is given.

### Global `cli::process_args (std::string s, std::vector< cmd_line_arg > &ca, int debug=0)`

There's a typecast in this function to `(char *)` from `(const char *)` which needs reworking.

### Global `eqi_deriv< func_t, vec_t >::deriv_vector (size_t nv, double dx, const vec_t &y, vec_t &dydx)`

generalize to other values of `npoints`.

### File `givens_base.h`

Make sure `create_givens()` in `givens.h` is documented.

### Class `gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >`

Document what happens when the stepper function returns a non-zero value, as it's different now with the `ode-initval2` function.

Document count, failed\_steps, etc.

### Class `gsl_fit< func_t, vec_t, mat_t, bool_vec_t >`

Properly generalize other vector types than `ovector_base`

Allow the user to specify the derivatives

Fix so that the user can specify automatic scaling of the fitting parameters, where the initial guess are used for scaling so that the fitting parameters are near unity.

### Class `gsl_mmin_bfgs2< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >`

While BFGS does well in the `ex_mmin` example with the initial guess of  $(1, 0, 7\pi)$  it seems to converge more poorly for the spring function than the other minimizers with other initial guesses, and I think this will happen in the GSL versions too. I need to examine this more closely with some code designed to clearly show this.

### Class `gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >`

Are all the `set_all()` statements really necessary? Do they need to be executed even if memory hasn't been recently allocated?

### Class `gsl_ode_control< vec_t >`

Double check that the improvements in the `ode-initval2` routines are available here

### Class `gsl_rkf45< func_t, vec_t, alloc_vec_t, alloc_t >`

Check this because it may not give exact `dydt_out`.

### Class `gsl_smooth`

Needs a bit more error checking and more documentation.

### Class `gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`

Mode = importance only doesn't give the same answer as GSL yet.

### Global `gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::vegas_minteg_err (int stage, func_t &func, size_t ndim, const vec_t &xl, const vec_t &xu, double &res, double &err)`

Should stage be passed by reference?

There was an update between `gsl-1.12` and `1.15` which has not been implemented here yet.

### Class `hdf_file`

Error handling with HDF functions is a particular concern. Modify to throw `O2scl` exceptions when appropriate.

### Class `hist`

Check that the actions of `set_bins()`, `clear()` and other functions perform the correct actions on the `user_rep` vector. I'm a bit concerned that `set_bins_auto()` shouldn't call `user_rep.allocate()`.

More documentation and testing.

**Class `hist_ev`**

Test `set_grid_blocks()` function.

Create copy constructors as in the `scalar_ev` class.

**File `householder_base.h`**

Better documentation for the Householder functions.

**Global `matrix_cx_out_paren` (`std::ostream &os, mat_t &A, size_t nrows, size_t ncols`)**

Doesn't this only work for GSL matrices? Compare this to the corresponding vector functions

**Class `multi_min_fix< bool_vec_t >`**

Generalize to all vector types

Generalize to minimizers which require derivatives

At the moment, the user has to change `def_mmin::ntrial` instead of `multi_min_fix::ntrial`, which is a bit confusing. Fix this.

**Class `ode_bv_multishoot< func_t, vec_t, alloc_vec_t, alloc_t, vec_int_t, mat_t >`**

Improve documentation a little and create testing code

**Global `ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_final_value` (`double x0, double x1, double h, size_t n, vec_t &ystart, vec_t &yend, func_t &derivs`)**

Document if `yend` can be the same as `ystart`.

**Class `other_todos_and_bugs`**

Make sure an error message is printed to ensure users do 'make o2scl-test' and not 'make check'

- Make sure `cstdlib` is included wherever `exit()` is used [5/22/11 - Most of these are taken care of now.]

**Class `ovector_const_view_tlate< data_t, vparent_t, block_t >::const_iterator`**

Default constructor and iterator typedefs

**Class `ovector_cx_tlate< data_t, vparent_t, block_t, complex_t >`**

Add `subvector_stride`, `const_subvector_stride`

**Global `smart_interp< vec_t, svec_t >::find_subset` (`const double a, const double b, size_t sz, const vec_t &x, const vec_t &y, size_t &nsz`)**

The error handling is a bit off here, as it can return a non-zero value even with there is no real "error". We should just make a new bool reference paramter.

**Global `smart_interp< vec_t, svec_t >::interp` (`const double x0, size_t n, const vec_t &x, const vec_t &y`)**

After calling `find_subset`, I think we might need to double check that `nn` is larger than the minimum interpolation size.

**Global `smart_interp_vec< vec_t, svec_t, alloc_vec_t, alloc_t >::find_inc_subset` (`const double x0, size_t sz, const vec_t &x, const vec_t &y, size_t &nsz`)**

Variables `row` and `row` appear to be unused? (2/17/11)

**Class `table`**

Document or fix the fact that the table copy constructors do not copy the interpolation objects. Maybe `def_interp_mgr` objects can have their own copy constructors?

**Global `table::sort_column` (`std::string scol`)**

Use `vector_sort()` rather than `qsort()`.

**Global `table::sort_table` (`std::string scol`)**

Use `vector_sort()` rather than `qsort()`.

**Global `uvector_const_view_tlate< data_t >::norm () const`**

Fix this so that `norm()` is computed as in `ovector` and so that integer norms are performed separately.

**Global `vector_pvariance` (`size_t n1, const vec_t &data1, size_t n2, const vec2_t &data2`)**

Document this

## 41 Namespace Index

### 41.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

<a href="#">gsl_cgs</a>	GSL constants in CGS units	142
<a href="#">gsl_cgsm</a>	GSL constants in CGSM units	145
<a href="#">gsl_mks</a>	GSL constants in MKS units	149
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<a href="#">o2scl_graph</a>	Namespace for experimental functions for use with Root	165
<a href="#">o2scl_inte_gk_coeffs</a>	A namespace for the GSL adaptive Gauss-Kronrod integration coefficients	167
<a href="#">o2scl_inte_qng_coeffs</a>	A namespace for the quadrature coefficients for non-adaptive integration	174
<a href="#">o2scl_linalg</a>	The namespace for linear algebra classes and functions	178
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## 42 Data Structure Index

### 42.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

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<a href="#">gsl_astep_old&lt; func_t, vec_t, alloc_vec_t, alloc_t &gt;</a>	297
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hist\_ev.h

??

householder.h

??

[householder\\_base.h](#)

File for Householder transformations

673

inte.h

??

interp.h

??

jacobian.h

??

lanczos.h

??

lanczos\_base.h

??

[lib\\_settings.h](#)File for definitions for [lib\\_settings\\_class](#)

674

linear\_solver.h

??

[lu.h](#)

File for LU decomposition and associated solver

675

[lu\\_base.h](#)

File for LU decomposition and associated solver

676

mcarlo\_inte.h

??

min\_fit.h

??

[minimize.h](#)

One-dimensional minimization base class and associated functions

676

[misc.h](#)

Miscellaneous functions

678

mm\_funct.h

??

mroot.h

??

multi\_funct.h

??

multi\_inte.h

??

multi\_min.h

??

multi\_min\_fix.h

??

nonadapt\_step.h

??

ode\_bv\_mshoot.h

??

ode\_bv\_multishoot.h

??

ode\_bv\_solve.h

??

ode\_funct.h

??

ode\_it\_solve.h

??

ode\_iv\_solve.h

??

ode\_iv\_table.h

??

ode\_jac\_funct.h

??

---

ode_step.h	??
<a href="#">omatrix_cx_tlate.h</a>	
File for definitions of complex matrices	680
<a href="#">omatrix_tlate.h</a>	
File for definitions of matrices	681
ool_constr_mmin.h	??
ool_mmin_gencan.h	??
ool_mmin_pgrad.h	??
ool_mmin_spg.h	??
<a href="#">ovector_cx_tlate.h</a>	
File for definitions of complex vectors	683
<a href="#">ovector_rev_tlate.h</a>	
File for definitions of reversed vectors	685
<a href="#">ovector_tlate.h</a>	
File for definitions of vectors	686
<a href="#">permutation.h</a>	
File containing permutation class and associated functions	688
pinside.h	??
planar_intp.h	??
<a href="#">poly.h</a>	
Classes for solving polynomials	688
polylog.h	??
qr.h	??
<a href="#">qr_base.h</a>	
File for QR decomposition and associated solver	689
rnga.h	??
root.h	??
search_vec.h	??
shared_ptr.h	??
sim_anneal.h	??
<a href="#">smart_interp.h</a>	
File for "smart" interpolation routines	690
<a href="#">string_conv.h</a>	
Various string conversion functions	691
svdstep.h	??
<a href="#">svdstep_base.h</a>	
File for SVD decomposition	693
table.h	??
table3d.h	??
table_units.h	??
<a href="#">tensor.h</a>	
File for definitions of tensors	694

---

<a href="#">tensor_old.h</a>	
File for definitions of tensor_olds	694
<a href="#">test_mgr.h</a>	??
<a href="#">tridiag.h</a>	??
<a href="#">tridiag_base.h</a>	
File for solving tridiagonal systems	695
<a href="#">twod_eqi_intp.h</a>	??
<a href="#">twod_intp.h</a>	??
<a href="#">umatrix_cx_tlate.h</a>	
File for definitions of matrices	696
<a href="#">umatrix_tlate.h</a>	
File for definitions of matrices	697
<a href="#">uniform_grid.h</a>	??
<a href="#">uvector_cx_tlate.h</a>	
File for definitions of complex unit-stride vectors	699
<a href="#">uvector_tlate.h</a>	
File for definitions of unit-stride vectors	700
<a href="#">vec_arith.h</a>	
Vector and matrix arithmetic	702
<a href="#">vec_stats.h</a>	
File containing statistics template functions	712
<a href="#">vector.h</a>	
File for generic vector functions	720
<a href="#">vector_derint.h</a>	
Derivatives of integrals of functions stored in vectors with implicit fixed-size grid	727

## 45 Namespace Documentation

### 45.1 gsl\_cgs Namespace Reference

GSL constants in CGS units.

#### 45.1.1 Detailed Description

##### Note

electron, neutron, proton, and atomic mass have been updated with CODATA 2010 values. Also electron charge, gravitational constant, plancks\_constant\_hbar, are updated.

##### Variables

- const double [schwarzschild\\_radius](#) = 2.95325008e5  
*cm*
- const double [speed\\_of\\_light](#) = 2.99792458e10  
*cm / s*
- const double [gravitational\\_constant](#) = 6.67384e-8  
*cm<sup>3</sup> / g s<sup>2</sup>*
- const double [plancks\\_constant\\_h](#) = 6.62606876e-27

- $g\ cm^2/s$
- const double [plancks\\_constant\\_hbar](#) = 1.054571726e-27
- $g\ cm^2/s$
- const double [astronomical\\_unit](#) = 1.49597870691e13
- $cm$
- const double [light\\_year](#) = 9.46053620707e17
- $cm$
- const double [parsec](#) = 3.08567758135e18
- $cm$
- const double [grav\\_accel](#) = 9.80665e2
- $cm/s^2$
- const double [electron\\_volt](#) = 1.602176487e-12
- $g\ cm^2/s^2$
- const double [mass\\_electron](#) = 9.10938291e-28
- $g$
- const double [mass\\_muon](#) = 1.88353109e-25
- $g$
- const double [mass\\_proton](#) = 1.672621777e-24
- $g$
- const double [mass\\_neutron](#) = 1.674927351e-24
- $g$
- const double [rydberg](#) = 2.17987190389e-11
- $g\ cm^2/s^2$
- const double [boltzmann](#) = 1.3806503e-16
- $g\ cm^2/K\ s^2$
- const double [molar\\_gas](#) = 8.314472e7
- $g\ cm^2/K\ mol\ s^2$
- const double [standard\\_gas\\_volume](#) = 2.2710981e4
- $cm^3/mol$
- const double [minute](#) = 6e1
- $s$
- const double [hour](#) = 3.6e3
- $s$
- const double [day](#) = 8.64e4
- $s$
- const double [week](#) = 6.048e5
- $s$
- const double [inch](#) = 2.54e0
- $cm$
- const double [foot](#) = 3.048e1
- $cm$
- const double [yard](#) = 9.144e1
- $cm$
- const double [mile](#) = 1.609344e5
- $cm$
- const double [nautical\\_mile](#) = 1.852e5
- $cm$
- const double [fathom](#) = 1.8288e2
- $cm$
- const double [mil](#) = 2.54e-3
- $cm$
- const double [point](#) = 3.5277777778e-2
- $cm$
- const double [texpoint](#) = 3.51459803515e-2
- $cm$
- const double [micron](#) = 1e-4
- $cm$
- const double [angstrom](#) = 1e-8
- $cm$
- const double [hectare](#) = 1e8
- $cm^2$



- const double [acre](#) = 4.04685642241e7  
*cm<sup>2</sup>*
- const double [barn](#) = 1e-24  
*cm<sup>2</sup>*
- const double [liter](#) = 1e3  
*cm<sup>3</sup>*
- const double [us\\_gallon](#) = 3.78541178402e3  
*cm<sup>3</sup>*
- const double [quart](#) = 9.46352946004e2  
*cm<sup>3</sup>*
- const double [pint](#) = 4.73176473002e2  
*cm<sup>3</sup>*
- const double [cup](#) = 2.36588236501e2  
*cm<sup>3</sup>*
- const double [fluid\\_ounce](#) = 2.95735295626e1  
*cm<sup>3</sup>*
- const double [tablespoon](#) = 1.47867647813e1  
*cm<sup>3</sup>*
- const double [teaspoon](#) = 4.92892159375e0  
*cm<sup>3</sup>*
- const double [canadian\\_gallon](#) = 4.54609e3  
*cm<sup>3</sup>*
- const double [uk\\_gallon](#) = 4.546092e3  
*cm<sup>3</sup>*
- const double [miles\\_per\\_hour](#) = 4.4704e1  
*cm / s*
- const double [kilometers\\_per\\_hour](#) = 2.77777777778e1  
*cm / s*
- const double [knot](#) = 5.14444444444e1  
*cm / s*
- const double [pound\\_mass](#) = 4.5359237e2  
*g*
- const double [ounce\\_mass](#) = 2.8349523125e1  
*g*
- const double [ton](#) = 9.0718474e5  
*g*
- const double [metric\\_ton](#) = 1e6  
*g*
- const double [uk\\_ton](#) = 1.0160469088e6  
*g*
- const double [troy\\_ounce](#) = 3.1103475e1  
*g*
- const double [carat](#) = 2e-1  
*g*
- const double [unified\\_atomic\\_mass](#) = 1.660538921e-24  
*g*
- const double [gram\\_force](#) = 9.80665e2  
*cm g / s<sup>2</sup>*
- const double [pound\\_force](#) = 4.44822161526e5  
*cm g / s<sup>2</sup>*
- const double [kilopound\\_force](#) = 4.44822161526e8  
*cm g / s<sup>2</sup>*
- const double [poundal](#) = 1.38255e4  
*cm g / s<sup>2</sup>*
- const double [calorie](#) = 4.1868e7  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [btu](#) = 1.05505585262e10  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [therm](#) = 1.05506e15  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [horsepower](#) = 7.457e9

- $g \text{ cm}^2 / s^3$
- const double **bar** = 1e6  
 $g / \text{cm s}^2$
- const double **std\_atmosphere** = 1.01325e6  
 $g / \text{cm s}^2$
- const double **torr** = 1.33322368421e3  
 $g / \text{cm s}^2$
- const double **meter\_of\_mercury** = 1.33322368421e6  
 $g / \text{cm s}^2$
- const double **inch\_of\_mercury** = 3.38638815789e4  
 $g / \text{cm s}^2$
- const double **inch\_of\_water** = 2.490889e3  
 $g / \text{cm s}^2$
- const double **psi** = 6.89475729317e4  
 $g / \text{cm s}^2$
- const double **poise** = 1e0  
 $g / \text{cm s}$
- const double **stokes** = 1e0  
 $\text{cm}^2 / s$
- const double **stilb** = 1e0  
 $\text{cd} / \text{cm}^2$
- const double **lumen** = 1e0  
 $\text{cd sr}$
- const double **lux** = 1e-4  
 $\text{cd sr} / \text{cm}^2$
- const double **phot** = 1e0  
 $\text{cd sr} / \text{cm}^2$
- const double **footcandle** = 1.076e-3  
 $\text{cd sr} / \text{cm}^2$
- const double **lambert** = 1e0  
 $\text{cd sr} / \text{cm}^2$
- const double **footlambert** = 1.07639104e-3  
 $\text{cd sr} / \text{cm}^2$
- const double **curie** = 3.7e10  
 $1 / s$
- const double **roentgen** = 2.58e-7  
 $A s / g.$
- const double **rad** = 1e2  
 $\text{cm}^2 / s^2$
- const double **solar\_mass** = 1.98892e33  
 $g$
- const double **bohr\_radius** = 5.291772083e-9  
 $\text{cm}$
- const double **newton** = 1e5  
 $\text{cm g} / s^2$
- const double **dyne** = 1e0  
 $\text{cm g} / s^2$
- const double **joule** = 1e7  
 $g \text{ cm}^2 / s^2$
- const double **erg** = 1e0  
 $g \text{ cm}^2 / s^2$
- const double **stefan\_boltzmann\_constant** = 5.67039934436e-5  
 $g / K^4 s^3$
- const double **thomson\_cross\_section** = 6.65245853542e-25  
 $\text{cm}^2$

## 45.2 gsl\_cgsm Namespace Reference

GSL constants in CGSM units.

## Variables

- const double [schwarzschild\\_radius](#) = 2.95325008e5  
*cm*
- const double [speed\\_of\\_light](#) = 2.99792458e10  
*cm / s*
- const double [gravitational\\_constant](#) = 6.67384e-8  
*cm<sup>3</sup> / g s<sup>2</sup>*
- const double [plancks\\_constant\\_h](#) = 6.62606876e-27  
*g cm<sup>2</sup> / s*
- const double [plancks\\_constant\\_hbar](#) = 1.054571726e-27  
*g cm<sup>2</sup> / s*
- const double [astronomical\\_unit](#) = 1.49597870691e13  
*cm*
- const double [light\\_year](#) = 9.46053620707e17  
*cm*
- const double [parsec](#) = 3.08567758135e18  
*cm*
- const double [grav\\_accel](#) = 9.80665e2  
*cm / s<sup>2</sup>*
- const double [electron\\_volt](#) = 1.602176487e-12  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [mass\\_electron](#) = 9.10938291e-28  
*g*
- const double [mass\\_muon](#) = 1.88353109e-25  
*g*
- const double [mass\\_proton](#) = 1.672621777e-24  
*g*
- const double [mass\\_neutron](#) = 1.674927351e-24  
*g*
- const double [rydberg](#) = 2.17987190389e-11  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [boltzmann](#) = 1.3806503e-16  
*g cm<sup>2</sup> / K s<sup>2</sup>*
- const double [electron\\_magnetic\\_moment](#) = 9.28476362e-21  
*abamp cm<sup>2</sup>*
- const double [proton\\_magnetic\\_moment](#) = 1.410606633e-23  
*abamp cm<sup>2</sup>*
- const double [molar\\_gas](#) = 8.314472e7  
*g cm<sup>2</sup> / K mol s<sup>2</sup>*
- const double [standard\\_gas\\_volume](#) = 2.2710981e4  
*cm<sup>3</sup> / mol*
- const double [minute](#) = 6e1  
*s*
- const double [hour](#) = 3.6e3  
*s*
- const double [day](#) = 8.64e4  
*s*
- const double [week](#) = 6.048e5  
*s*
- const double [inch](#) = 2.54e0  
*cm*
- const double [foot](#) = 3.048e1  
*cm*
- const double [yard](#) = 9.144e1  
*cm*
- const double [mile](#) = 1.609344e5  
*cm*
- const double [nautical\\_mile](#) = 1.852e5  
*cm*
- const double [fathom](#) = 1.8288e2

- cm*
- const double [mil](#) = 2.54e-3
- cm*
- const double [point](#) = 3.52777777778e-2
- cm*
- const double [texpoint](#) = 3.51459803515e-2
- cm*
- const double [micron](#) = 1e-4
- cm*
- const double [angstrom](#) = 1e-8
- cm*
- const double [hectare](#) = 1e8
- cm*<sup>2</sup>
- const double [acre](#) = 4.04685642241e7
- cm*<sup>2</sup>
- const double [barn](#) = 1e-24
- cm*<sup>2</sup>
- const double [liter](#) = 1e3
- cm*<sup>3</sup>
- const double [us\\_gallon](#) = 3.78541178402e3
- cm*<sup>3</sup>
- const double [quart](#) = 9.46352946004e2
- cm*<sup>3</sup>
- const double [pint](#) = 4.73176473002e2
- cm*<sup>3</sup>
- const double [cup](#) = 2.36588236501e2
- cm*<sup>3</sup>
- const double [fluid\\_ounce](#) = 2.95735295626e1
- cm*<sup>3</sup>
- const double [tablespoon](#) = 1.47867647813e1
- cm*<sup>3</sup>
- const double [teaspoon](#) = 4.92892159375e0
- cm*<sup>3</sup>
- const double [canadian\\_gallon](#) = 4.54609e3
- cm*<sup>3</sup>
- const double [uk\\_gallon](#) = 4.546092e3
- cm*<sup>3</sup>
- const double [miles\\_per\\_hour](#) = 4.4704e1
- cm / s*
- const double [kilometers\\_per\\_hour](#) = 2.77777777778e1
- cm / s*
- const double [knot](#) = 5.14444444444e1
- cm / s*
- const double [pound\\_mass](#) = 4.5359237e2
- g*
- const double [ounce\\_mass](#) = 2.8349523125e1
- g*
- const double [ton](#) = 9.0718474e5
- g*
- const double [metric\\_ton](#) = 1e6
- g*
- const double [uk\\_ton](#) = 1.0160469088e6
- g*
- const double [troy\\_ounce](#) = 3.1103475e1
- g*
- const double [carat](#) = 2e-1
- g*
- const double [unified\\_atomic\\_mass](#) = 1.660538921e-24
- g*
- const double [gram\\_force](#) = 9.80665e2
- cm g / s*<sup>2</sup>

- const double [pound\\_force](#) = 4.44822161526e5  
*cm g / s<sup>2</sup>*
- const double [kilopound\\_force](#) = 4.44822161526e8  
*cm g / s<sup>2</sup>*
- const double [poundal](#) = 1.38255e4  
*cm g / s<sup>2</sup>*
- const double [calorie](#) = 4.1868e7  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [btu](#) = 1.05505585262e10  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [therm](#) = 1.05506e15  
*g cm<sup>2</sup> / s<sup>2</sup>*
- const double [horsepower](#) = 7.457e9  
*g cm<sup>2</sup> / s<sup>3</sup>*
- const double [bar](#) = 1e6  
*g / cm s<sup>2</sup>*
- const double [std\\_atmosphere](#) = 1.01325e6  
*g / cm s<sup>2</sup>*
- const double [torr](#) = 1.33322368421e3  
*g / cm s<sup>2</sup>*
- const double [meter\\_of\\_mercury](#) = 1.33322368421e6  
*g / cm s<sup>2</sup>*
- const double [inch\\_of\\_mercury](#) = 3.38638815789e4  
*g / cm s<sup>2</sup>*
- const double [inch\\_of\\_water](#) = 2.490889e3  
*g / cm s<sup>2</sup>*
- const double [psi](#) = 6.89475729317e4  
*g / cm s<sup>2</sup>*
- const double [poise](#) = 1e0  
*g / cm s*
- const double [stokes](#) = 1e0  
*cm<sup>2</sup> / s*
- const double [faraday](#) = 9.64853429775e3  
*abamp s / mol*
- const double [electron\\_charge](#) = 1.602176565e-20  
*abamp s*
- const double [stilb](#) = 1e0  
*cd / cm<sup>2</sup>*
- const double [lumen](#) = 1e0  
*cd sr*
- const double [lux](#) = 1e-4  
*cd sr / cm<sup>2</sup>*
- const double [phot](#) = 1e0  
*cd sr / cm<sup>2</sup>*
- const double [footcandle](#) = 1.076e-3  
*cd sr / cm<sup>2</sup>*
- const double [lambert](#) = 1e0  
*cd sr / cm<sup>2</sup>*
- const double [footlambert](#) = 1.07639104e-3  
*cd sr / cm<sup>2</sup>*
- const double [curie](#) = 3.7e10  
*1 / s*
- const double [roentgen](#) = 2.58e-8  
*abamp s / g*
- const double [rad](#) = 1e2  
*cm<sup>2</sup> / s<sup>2</sup>*
- const double [solar\\_mass](#) = 1.98892e33  
*g*
- const double [bohr\\_radius](#) = 5.291772083e-9  
*cm*
- const double [newton](#) = 1e5

- $cm\ g / s^2$
- const double [dyne](#) = 1e0
- $cm\ g / s^2$
- const double [joule](#) = 1e7
- $g\ cm^2 / s^2$
- const double [erg](#) = 1e0
- $g\ cm^2 / s^2$
- const double [stefan\\_boltzmann\\_constant](#) = 5.67039934436e-5
- $g / K^4\ s^3$
- const double [thomson\\_cross\\_section](#) = 6.65245853542e-25
- $cm^2$
- const double [bohr\\_magneton](#) = 9.27400899e-21
- $abamp\ cm^2$
- const double [nuclear\\_magneton](#) = 5.05078317e-24
- $abamp\ cm^2$

## 45.3 gsl\_mks Namespace Reference

GSL constants in MKS units.

### Variables

- const double [schwarzschild\\_radius](#) = 2.95325008e3
- $m$
- const double [speed\\_of\\_light](#) = 2.99792458e8
- $m / s$
- const double [gravitational\\_constant](#) = 6.67384e-11
- $m^3 / kg\ s^2$
- const double [plancks\\_constant\\_h](#) = 6.62606876e-34
- $kg\ m^2 / s$
- const double [plancks\\_constant\\_hbar](#) = 1.054571726e-34
- $kg\ m^2 / s$
- const double [astronomical\\_unit](#) = 1.49597870691e11
- $m$
- const double [light\\_year](#) = 9.46053620707e15
- $m$
- const double [parsec](#) = 3.08567758135e16
- $m$
- const double [grav\\_accel](#) = 9.80665e0
- $m / s^2$
- const double [electron\\_volt](#) = 1.602176487e-19
- $kg\ m^2 / s^2$
- const double [mass\\_electron](#) = 9.10938291e-31
- $kg$
- const double [mass\\_muon](#) = 1.88353109e-28
- $kg$
- const double [mass\\_proton](#) = 1.672621777e-27
- $kg$
- const double [mass\\_neutron](#) = 1.674927351e-27
- $kg$
- const double [rydberg](#) = 2.17987190389e-18
- $kg\ m^2 / s^2$
- const double [boltzmann](#) = 1.3806503e-23
- $kg\ m^2 / K\ s^2$
- const double [bohr\\_magneton](#) = 9.27400899e-24
- $A\ m^2$ .
- const double [nuclear\\_magneton](#) = 5.05078317e-27
- $A\ m^2$ .

- const double [electron\\_magnetic\\_moment](#) = 9.28476362e-24  
 $A\ m^2$ .
- const double [proton\\_magnetic\\_moment](#) = 1.410606633e-26  
 $A\ m^2$ .
- const double [molar\\_gas](#) = 8.314472e0  
 $kg\ m^2 / K\ mol\ s^2$
- const double [standard\\_gas\\_volume](#) = 2.2710981e-2  
 $m^3 / mol$
- const double [minute](#) = 6e1  
 $s$
- const double [hour](#) = 3.6e3  
 $s$
- const double [day](#) = 8.64e4  
 $s$
- const double [week](#) = 6.048e5  
 $s$
- const double [inch](#) = 2.54e-2  
 $m$
- const double [foot](#) = 3.048e-1  
 $m$
- const double [yard](#) = 9.144e-1  
 $m$
- const double [mile](#) = 1.609344e3  
 $m$
- const double [nautical\\_mile](#) = 1.852e3  
 $m$
- const double [fathom](#) = 1.8288e0  
 $m$
- const double [mil](#) = 2.54e-5  
 $m$
- const double [point](#) = 3.52777777778e-4  
 $m$
- const double [texpoint](#) = 3.51459803515e-4  
 $m$
- const double [micron](#) = 1e-6  
 $m$
- const double [angstrom](#) = 1e-10  
 $m$
- const double [hectare](#) = 1e4  
 $m^2$
- const double [acre](#) = 4.04685642241e3  
 $m^2$
- const double [barn](#) = 1e-28  
 $m^2$
- const double [liter](#) = 1e-3  
 $m^3$
- const double [us\\_gallon](#) = 3.78541178402e-3  
 $m^3$
- const double [quart](#) = 9.46352946004e-4  
 $m^3$
- const double [pint](#) = 4.73176473002e-4  
 $m^3$
- const double [cup](#) = 2.36588236501e-4  
 $m^3$
- const double [fluid\\_ounce](#) = 2.95735295626e-5  
 $m^3$
- const double [tablespoon](#) = 1.47867647813e-5  
 $m^3$
- const double [teaspoon](#) = 4.92892159375e-6  
 $m^3$
- const double [canadian\\_gallon](#) = 4.54609e-3

- $m^3$
- const double [uk\\_gallon](#) = 4.546092e-3
- $m^3$
- const double [miles\\_per\\_hour](#) = 4.4704e-1
- $m / s$
- const double [kilometers\\_per\\_hour](#) = 2.7777777778e-1
- $m / s$
- const double [knot](#) = 5.1444444444e-1
- $m / s$
- const double [pound\\_mass](#) = 4.5359237e-1
- $kg$
- const double [ounce\\_mass](#) = 2.8349523125e-2
- $kg$
- const double [ton](#) = 9.0718474e2
- $kg$
- const double [metric\\_ton](#) = 1e3
- $kg$
- const double [uk\\_ton](#) = 1.0160469088e3
- $kg$
- const double [troy\\_ounce](#) = 3.1103475e-2
- $kg$
- const double [carat](#) = 2e-4
- $kg$
- const double [unified\\_atomic\\_mass](#) = 1.660538921e-27
- $kg$
- const double [gram\\_force](#) = 9.80665e-3
- $kg\ m / s^2$
- const double [pound\\_force](#) = 4.44822161526e0
- $kg\ m / s^2$
- const double [kilopound\\_force](#) = 4.44822161526e3
- $kg\ m / s^2$
- const double [poundal](#) = 1.38255e-1
- $kg\ m / s^2$
- const double [calorie](#) = 4.1868e0
- $kg\ m^2 / s^2$
- const double [btu](#) = 1.05505585262e3
- $kg\ m^2 / s^2$
- const double [therm](#) = 1.05506e8
- $kg\ m^2 / s^2$
- const double [horsepower](#) = 7.457e2
- $kg\ m^2 / s^3$
- const double [bar](#) = 1e5
- $kg / m\ s^2$
- const double [std\\_atmosphere](#) = 1.01325e5
- $kg / m\ s^2$
- const double [torr](#) = 1.33322368421e2
- $kg / m\ s^2$
- const double [meter\\_of\\_mercury](#) = 1.33322368421e5
- $kg / m\ s^2$
- const double [inch\\_of\\_mercury](#) = 3.38638815789e3
- $kg / m\ s^2$
- const double [inch\\_of\\_water](#) = 2.490889e2
- $kg / m\ s^2$
- const double [psi](#) = 6.89475729317e3
- $kg / m\ s^2$
- const double [poise](#) = 1e-1
- $kg\ m^{-1}\ s^{-1}$
- const double [stokes](#) = 1e-4
- $m^2 / s$
- const double [faraday](#) = 9.64853429775e4
- $A\ s / mol.$



- const double [electron\\_charge](#) = 1.602176565e-19  
*A s.*
- const double [gauss](#) = 1e-4  
*kg / A s<sup>2</sup>*
- const double [stilb](#) = 1e4  
*cd / m<sup>2</sup>*
- const double [lumen](#) = 1e0  
*cd sr*
- const double [lux](#) = 1e0  
*cd sr / m<sup>2</sup>*
- const double [phot](#) = 1e4  
*cd sr / m<sup>2</sup>*
- const double [footcandle](#) = 1.076e1  
*cd sr / m<sup>2</sup>*
- const double [lambert](#) = 1e4  
*cd sr / m<sup>2</sup>*
- const double [footlambert](#) = 1.07639104e1  
*cd sr / m<sup>2</sup>*
- const double [curie](#) = 3.7e10  
*1 / s*
- const double [roentgen](#) = 2.58e-4  
*A s / kg.*
- const double [rad](#) = 1e-2  
*m<sup>2</sup> / s<sup>2</sup>*
- const double [solar\\_mass](#) = 1.98892e30  
*kg*
- const double [bohr\\_radius](#) = 5.291772083e-11  
*m*
- const double [newton](#) = 1e0  
*kg m / s<sup>2</sup>*
- const double [dyne](#) = 1e-5  
*kg m / s<sup>2</sup>*
- const double [joule](#) = 1e0  
*kg m<sup>2</sup> / s<sup>2</sup>*
- const double [erg](#) = 1e-7  
*kg m<sup>2</sup> / s<sup>2</sup>*
- const double [stefan\\_boltzmann\\_constant](#) = 5.67039934436e-8  
*kg / K<sup>4</sup> s<sup>3</sup>*
- const double [thomson\\_cross\\_section](#) = 6.65245853542e-29  
*m<sup>2</sup>*
- const double [vacuum\\_permittivity](#) = 8.854187817e-12  
*A<sup>2</sup> s<sup>4</sup> / kg m<sup>3</sup>.*
- const double [vacuum\\_permeability](#) = 1.25663706144e-6  
*kg m / A<sup>2</sup> s<sup>2</sup>*

## 45.4 gsl\_mkssa Namespace Reference

GSL constants in MKSA units.

### Variables

- const double [schwarzschild\\_radius](#) = 2.95325008e3  
*m*
- const double [speed\\_of\\_light](#) = 2.99792458e8  
*m / s*
- const double [gravitational\\_constant](#) = 6.67384e-11  
*m<sup>3</sup> / kg s<sup>2</sup>*
- const double [plancks\\_constant\\_h](#) = 6.62606876e-34

- $kg\ m^2 / s$
- const double [plancks\\_constant\\_hbar](#) = 1.054571726e-34
- $kg\ m^2 / s$
- const double [astronomical\\_unit](#) = 1.49597870691e11
- $m$
- const double [light\\_year](#) = 9.46053620707e15
- $m$
- const double [parsec](#) = 3.08567758135e16
- $m$
- const double [grav\\_accel](#) = 9.80665e0
- $m / s^2$
- const double [electron\\_volt](#) = 1.602176487e-19
- $kg\ m^2 / s^2$
- const double [mass\\_electron](#) = 9.10938291e-31
- $kg$
- const double [mass\\_muon](#) = 1.88353109e-28
- $kg$
- const double [mass\\_proton](#) = 1.672621777e-27
- $kg$
- const double [mass\\_neutron](#) = 1.674927351e-27
- $kg$
- const double [rydberg](#) = 2.17987190389e-18
- $kg\ m^2 / s^2$
- const double [boltzmann](#) = 1.3806503e-23
- $kg\ m^2 / K\ s^2$
- const double [bohr\\_magneton](#) = 9.27400899e-24
- $A\ m^2.$
- const double [nuclear\\_magneton](#) = 5.05078317e-27
- $A\ m^2.$
- const double [electron\\_magnetic\\_moment](#) = 9.28476362e-24
- $A\ m^2.$
- const double [proton\\_magnetic\\_moment](#) = 1.410606633e-26
- $A\ m^2.$
- const double [molar\\_gas](#) = 8.314472e0
- $kg\ m^2 / K\ mol\ s^2$
- const double [standard\\_gas\\_volume](#) = 2.2710981e-2
- $m^3 / mol$
- const double [minute](#) = 6e1
- $s$
- const double [hour](#) = 3.6e3
- $s$
- const double [day](#) = 8.64e4
- $s$
- const double [week](#) = 6.048e5
- $s$
- const double [inch](#) = 2.54e-2
- $m$
- const double [foot](#) = 3.048e-1
- $m$
- const double [yard](#) = 9.144e-1
- $m$
- const double [mile](#) = 1.609344e3
- $m$
- const double [nautical\\_mile](#) = 1.852e3
- $m$
- const double [fathom](#) = 1.8288e0
- $m$
- const double [mil](#) = 2.54e-5
- $m$
- const double [point](#) = 3.52777777778e-4
- $m$

- const double [texpoint](#) = 3.51459803515e-4  
*m*
- const double [micron](#) = 1e-6  
*m*
- const double [angstrom](#) = 1e-10  
*m*
- const double [hectare](#) = 1e4  
*m*<sup>2</sup>
- const double [acre](#) = 4.04685642241e3  
*m*<sup>2</sup>
- const double [barn](#) = 1e-28  
*m*<sup>2</sup>
- const double [liter](#) = 1e-3  
*m*<sup>3</sup>
- const double [us\\_gallon](#) = 3.78541178402e-3  
*m*<sup>3</sup>
- const double [quart](#) = 9.46352946004e-4  
*m*<sup>3</sup>
- const double [pint](#) = 4.73176473002e-4  
*m*<sup>3</sup>
- const double [cup](#) = 2.36588236501e-4  
*m*<sup>3</sup>
- const double [fluid\\_ounce](#) = 2.95735295626e-5  
*m*<sup>3</sup>
- const double [tablespoon](#) = 1.47867647813e-5  
*m*<sup>3</sup>
- const double [teaspoon](#) = 4.92892159375e-6  
*m*<sup>3</sup>
- const double [canadian\\_gallon](#) = 4.54609e-3  
*m*<sup>3</sup>
- const double [uk\\_gallon](#) = 4.546092e-3  
*m*<sup>3</sup>
- const double [miles\\_per\\_hour](#) = 4.4704e-1  
*m* / *s*
- const double [kilometers\\_per\\_hour](#) = 2.77777777778e-1  
*m* / *s*
- const double [knot](#) = 5.14444444444e-1  
*m* / *s*
- const double [pound\\_mass](#) = 4.5359237e-1  
*kg*
- const double [ounce\\_mass](#) = 2.8349523125e-2  
*kg*
- const double [ton](#) = 9.0718474e2  
*kg*
- const double [metric\\_ton](#) = 1e3  
*kg*
- const double [uk\\_ton](#) = 1.0160469088e3  
*kg*
- const double [troy\\_ounce](#) = 3.1103475e-2  
*kg*
- const double [carat](#) = 2e-4  
*kg*
- const double [unified\\_atomic\\_mass](#) = 1.660538921e-27  
*kg*
- const double [gram\\_force](#) = 9.80665e-3  
*kg m* / *s*<sup>2</sup>
- const double [pound\\_force](#) = 4.44822161526e0  
*kg m* / *s*<sup>2</sup>
- const double [kilopound\\_force](#) = 4.44822161526e3  
*kg m* / *s*<sup>2</sup>
- const double [poundal](#) = 1.38255e-1

- $kg\ m/s^2$
- const double [calorie](#) = 4.1868e0
- $kg\ m^2/s^2$
- const double [btu](#) = 1.05505585262e3
- $kg\ m^2/s^2$
- const double [therm](#) = 1.05506e8
- $kg\ m^2/s^2$
- const double [horsepower](#) = 7.457e2
- $kg\ m^2/s^3$
- const double [bar](#) = 1e5
- $kg/m\ s^2$
- const double [std\\_atmosphere](#) = 1.01325e5
- $kg/m\ s^2$
- const double [torr](#) = 1.33322368421e2
- $kg/m\ s^2$
- const double [meter\\_of\\_mercury](#) = 1.33322368421e5
- $kg/m\ s^2$
- const double [inch\\_of\\_mercury](#) = 3.38638815789e3
- $kg/m\ s^2$
- const double [inch\\_of\\_water](#) = 2.490889e2
- $kg/m\ s^2$
- const double [psi](#) = 6.89475729317e3
- $kg/m\ s^2$
- const double [poise](#) = 1e-1
- $kg\ m^{-1}\ s^{-1}$
- const double [stokes](#) = 1e-4
- $m^2/s$
- const double [faraday](#) = 9.64853429775e4
- $A\ s/mol.$
- const double [electron\\_charge](#) = 1.602176565e-19
- $A\ s.$
- const double [gauss](#) = 1e-4
- $kg/A\ s^2$
- const double [stilb](#) = 1e4
- $cd/m^2$
- const double [lumen](#) = 1e0
- $cd\ sr$
- const double [lux](#) = 1e0
- $cd\ sr/m^2$
- const double [phot](#) = 1e4
- $cd\ sr/m^2$
- const double [footcandle](#) = 1.076e1
- $cd\ sr/m^2$
- const double [lambert](#) = 1e4
- $cd\ sr/m^2$
- const double [footlambert](#) = 1.07639104e1
- $cd\ sr/m^2$
- const double [curie](#) = 3.7e10
- $1/s$
- const double [roentgen](#) = 2.58e-4
- $A\ s/kg.$
- const double [rad](#) = 1e-2
- $m^2/s^2$
- const double [solar\\_mass](#) = 1.98892e30
- $kg$
- const double [bohr\\_radius](#) = 5.291772083e-11
- $m$
- const double [newton](#) = 1e0
- $kg\ m/s^2$
- const double [dyne](#) = 1e-5
- $kg\ m/s^2$

- const double **joule** = 1e0  
 $\text{kg m}^2 / \text{s}^2$
- const double **erg** = 1e-7  
 $\text{kg m}^2 / \text{s}^2$
- const double **stefan\_boltzmann\_constant** = 5.67039934436e-8  
 $\text{kg} / \text{K}^4 \text{s}^3$
- const double **thomson\_cross\_section** = 6.65245853542e-29  
 $\text{m}^2$
- const double **vacuum\_permittivity** = 8.854187817e-12  
 $\text{A}^2 \text{s}^4 / \text{kg m}^3$ .
- const double **vacuum\_permeability** = 1.25663706144e-6  
 $\text{kg m} / \text{A}^2 \text{s}^2$

## 45.5 gsl\_num Namespace Reference

GSL numerical constants.

### Variables

- const double **yotta** = 1e24
- const double **zetta** = 1e21
- const double **exa** = 1e18
- const double **peta** = 1e15
- const double **tera** = 1e12
- const double **giga** = 1e9
- const double **mega** = 1e6
- const double **kilo** = 1e3
- const double **milli** = 1e-3
- const double **micro** = 1e-6
- const double **nano** = 1e-9
- const double **pico** = 1e-12
- const double **femto** = 1e-15
- const double **atto** = 1e-18
- const double **zepto** = 1e-21
- const double **yocto** = 1e-24
- const double **fine\_structure** = 7.2973525376e-3  
*Fine structure constant (updated from <http://physics.nist.gov/cuu/Constants>)*
- const double **avogadro** = 6.02214179e23  
*Avogadro's number (updated from <http://physics.nist.gov/cuu/Constants>)*

## 45.6 o2scl Namespace Reference

The main O<sub>2</sub>scl namespace.

### 45.6.1 Detailed Description

By default, all O<sub>2</sub>scl classes and functions which are not listed as being in one of O<sub>2</sub>scl's smaller specialized namespaces are in this namespace. This namespace has been removed from the documentation to simplify the formatting.

This namespace documentation is in the file [src/base/lib\\_settings.h](#)

## 45.7 o2scl\_cblas Namespace Reference

Namespace for O<sub>2</sub>scl CBLAS function templates with operator[].

## 45.7.1 Detailed Description

**Level-1 BLAS functions**

Some functionality which would otherwise appear here is already given in [vector.h](#).

- The equivalent of `dcopy()` is given in [vector\\_copy\(\)](#) except that the ordering is reversed (in [vector\\_copy\(\)](#) the source preceeds the destination in the function argument list).
- The equivalent of `dswap()` is given in [vector\\_swap\(\)](#).
- The equivalent of `idamax()` is given in [vector\\_max\\_index\(\)](#).

**Level-2 BLAS functions**

Currently only [dgemv\(\)](#), [dtrmv\(\)](#), and [dtrsv\(\)](#) are implemented.

**Level-3 BLAS functions**

Currently only [dgemm\(\)](#) is implemented.

**Helper BLAS functions**

There are several basic BLAS functions which are helpful to operate on only a part of a vector or matrix to ensure that the linear algebra routines are flexible with the types that they can handle.

The subvector functions operate only one set of adjacent vector elements. For a vector defined by with

$$\vec{x} = \begin{pmatrix} x_0 \\ x_1 \\ \cdot \\ \cdot \\ x_{ie} \\ x_{ie+1} \\ \cdot \\ \cdot \\ x_{N-1} \\ x_N \\ x_{N+1} \\ \cdot \\ \cdot \end{pmatrix}$$

the functions with suffix `subvec` operate only on elements from  $x_{ie}$  to  $x_{N-1}$  (inclusive).

The subcolumn functions operate only on a part of a column of a matrix. For a matrix defined by

$$m = \begin{pmatrix} m_{0,0} & m_{0,1} & \cdot & \cdot & m_{0,ic} & \cdot & \cdot \\ m_{1,0} & m_{1,1} & \cdot & \cdot & m_{1,ic} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & m_{ir,ic} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & m_{ir+1,ic} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & m_{N-1,ic} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & m_{N,ic} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & m_{N+1,ic} & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \end{pmatrix}$$

the functions with suffix `subcol` operate only on elements in the column from  $m_{ir,ic}$  to  $m_{N-1,ic}$  inclusive.

The subrow functions operate only on a part of a row of a matrix. For a matrix defined by

$$m = \begin{pmatrix} m_{0,0} & m_{0,1} & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ m_{1,0} & m_{1,1} & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ m_{ir,0} & \cdot & \cdot & m_{ir,ic} & m_{ir,ic+1} & \cdot & \cdot & m_{ir,N-1} & m_{ir,N} & m_{ir,N+1} & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \end{pmatrix}$$

the functions with suffix `subrow` operate only on elements in the column from  $m_{ir,ic}$  to  $m_{ir,N-1}$  inclusive.

This namespace is documented inside [src/linalg/cblas.h](#).

## Enumerations

- enum [o2cblas\\_order](#) { [o2cblas\\_RowMajor](#) = 101, [o2cblas\\_ColMajor](#) = 102 }  
*Matrix order, either column-major or row-major.*
- enum [o2cblas\\_transpose](#) { [o2cblas\\_NoTrans](#) = 111, [o2cblas\\_Trans](#) = 112, [o2cblas\\_ConjTrans](#) = 113 }  
*Transpose operations.*
- enum [o2cblas\\_uplo](#) { [o2cblas\\_Upper](#) = 121, [o2cblas\\_Lower](#) = 122 }  
*Upper- or lower-triangular.*
- enum [o2cblas\\_diag](#) { [o2cblas\\_NonUnit](#) = 131, [o2cblas\\_Unit](#) = 132 }  
*Unit or generic diagonal.*
- enum [o2cblas\\_side](#) { [o2cblas\\_Left](#) = 141, [o2cblas\\_Right](#) = 142 }  
*Left or right sided operation.*

## Functions

### Level-1 BLAS functions

- template<class vec\_t >  
double [dasum](#) (const size\_t N, const vec\_t &X)  
*Compute the absolute sum of vector elements.*
- template<class vec\_t, class vec2\_t >  
void [daxpy](#) (const double alpha, const size\_t N, const vec\_t &X, vec2\_t &Y)  
*Compute  $y = \alpha x + y$ .*
- template<class vec\_t, class vec2\_t >  
double [ddot](#) (const size\_t N, const vec\_t &X, const vec2\_t &Y)  
*Compute  $r = x \cdot y$ .*
- template<class vec\_t >  
double [dnrm2](#) (const size\_t N, const vec\_t &X)  
*Compute the norm of the vector X.*
- template<class vec\_t >  
void [dscal](#) (const double alpha, const size\_t N, vec\_t &X)  
*Compute  $x = \alpha x$ .*

### Level-2 BLAS functions

- template<class mat\_t, class vec\_t >  
void [dgemv](#) (const enum [o2cblas\\_order](#) order, const enum [o2cblas\\_transpose](#) TransA, const size\_t M, const size\_t N, const double alpha, const mat\_t &A, const vec\_t &X, const double beta, vec\_t &Y)  
*Compute  $y = \alpha [\text{op}(A)]x + \beta y$ .*
- template<class mat\_t, class vec\_t >  
void [dtrsv](#) (const enum [o2cblas\\_order](#) order, const enum [o2cblas\\_uplo](#) Uplo, const enum [o2cblas\\_transpose](#) TransA, const enum [o2cblas\\_diag](#) Diag, const size\_t M, const size\_t N, const mat\_t &A, vec\_t &X)  
*Compute  $x = \text{op}(A)^{-1}x$ .*
- template<class mat\_t, class vec\_t >  
void [dtrmv](#) (const enum [o2cblas\\_order](#) Order, const enum [o2cblas\\_uplo](#) Uplo, const enum [o2cblas\\_transpose](#) TransA, const enum [o2cblas\\_diag](#) Diag, const size\_t N, const mat\_t &A, vec\_t &x)  
*Compute  $x = \text{op}(A)x$  for the triangular matrix A.*

## Level-3 BLAS functions

- `template<class mat_t >`  
`void dgemm (const enum o2cblas_order Order, const enum o2cblas_transpose TransA, const enum o2cblas_transpose - TransB, const size_t M, const size_t N, const size_t K, const double alpha, const mat_t &A, const mat_t &B, const double beta, mat_t &C)`  
*Compute  $y = \alpha \text{op}(A)\text{op}(B) + \beta C$ .*

## Helper BLAS functions - Subvectors

- `template<class vec_t, class vec2_t >`  
`void daxpy_subvec (const double alpha, const size_t N, const vec_t &X, vec2_t &Y, const size_t ie)`  
*Compute  $y = \alpha x + y$  beginning with index  $ie$  and ending with index  $N-1$ .*
- `template<class vec_t, class vec2_t >`  
`double ddot_subvec (const size_t N, const vec_t &X, const vec2_t &Y, const size_t ie)`  
*Compute  $r = x \cdot y$  beginning with index  $ie$  and ending with index  $N-1$ .*
- `template<class vec_t >`  
`double dnrm2_subvec (const size_t N, const vec_t &X, const size_t ie)`  
*Compute the norm of the vector  $X$  beginning with index  $ie$  and ending with index  $N-1$ .*
- `template<class vec_t >`  
`void dscal_subvec (const double alpha, const size_t N, vec_t &X, const size_t ie)`  
*Compute  $x = \alpha x$  beginning with index  $ie$  and ending with index  $N-1$ .*

## Helper BLAS functions - Subcolumns of a matrix

- `template<class mat_t, class vec_t >`  
`void daxpy_subcol (const double alpha, const size_t M, const mat_t &X, const size_t ir, const size_t ic, vec_t &y)`  
*Compute  $y = \alpha x + y$  for a subcolumn of a matrix.*
- `template<class mat_t, class vec_t >`  
`double ddot_subcol (const size_t M, const mat_t &X, const size_t ir, const size_t ic, const vec_t &y)`  
*Compute  $r = x \cdot y$  for a subcolumn of a matrix.*
- `template<class mat_t >`  
`double dnrm2_subcol (const mat_t &A, const size_t ir, const size_t ic, const size_t M)`  
*Compute the norm of a subcolumn of a matrix.*
- `template<class mat_t >`  
`void dscal_subcol (mat_t &A, const size_t ir, const size_t ic, const size_t M, const double alpha)`  
*Compute  $x = \alpha x$  for a subcolumn of a matrix.*

## Helper BLAS functions - Subrows of a matrix

- `template<class mat_t, class vec_t >`  
`void daxpy_subrow (const double alpha, const size_t N, const mat_t &X, const size_t ir, const size_t ic, vec_t &Y)`  
*Compute  $y = \alpha x + y$  for a subrow of a matrix.*
- `template<class mat_t, class vec_t >`  
`double ddot_subrow (const size_t N, const mat_t &X, const size_t ir, const size_t ic, const vec_t &Y)`  
*Compute  $r = x \cdot y$  for a subrow of a matrix.*
- `template<class mat_t >`  
`double dnrm2_subrow (const mat_t &M, const size_t ir, const size_t ic, const size_t N)`  
*Compute the norm of a subrow of a matrix.*
- `template<class mat_t >`  
`void dscal_subrow (mat_t &A, const size_t ir, const size_t ic, const size_t N, const double alpha)`  
*Compute  $x = \alpha x$  for a subrow of a matrix.*

## 45.7.2 Function Documentation

45.7.2.1 `template<class vec_t > double o2scl_cblas::dasum ( const size_t N, const vec_t & X )`

If `alpha` is zero, this function returns and performs no computations.

Definition at line 84 of file `cblas_base.h`.



45.7.2.2 `template<class vec_t, class vec2_t> void o2scl_cblas::daxpy ( const double alpha, const size_t N, const vec_t & X, vec2_t & Y )`

If *alpha* is zero, this function returns and performs no computations.

Definition at line 98 of file `cblas_base.h`.

45.7.2.3 `template<class vec_t> double o2scl_cblas::dnrm2 ( const size_t N, const vec_t & X )`

#### Note

The suffix "2" on the function name indicates that this computes the "2-norm", not that the norm is squared.

If *N* is less than or equal to zero, this function returns zero without calling the error handler.

This function works only with vectors which hold `double`. For the norm of a general floating point vector, see [vector\\_norm\(\)](#).

Definition at line 156 of file `cblas_base.h`.

45.7.2.4 `template<class mat_t, class vec_t> void o2scl_cblas::dgemv ( const enum o2cblas_order order, const enum o2cblas_transpose TransA, const size_t M, const size_t N, const double alpha, const mat_t & A, const vec_t & X, const double beta, vec_t & Y )`

If *M* or *N* is zero, or if *alpha* is zero and *beta* is one, this function performs no calculations and returns without calling the error handler.

Definition at line 218 of file `cblas_base.h`.

45.7.2.5 `template<class mat_t, class vec_t> void o2scl_cblas::dtrsv ( const enum o2cblas_order order, const enum o2cblas_uplo Uplo, const enum o2cblas_transpose TransA, const enum o2cblas_diag Diag, const size_t M, const size_t N, const mat_t & A, vec_t & X )`

If *N* is zero, this function does nothing and returns zero.

Definition at line 308 of file `cblas_base.h`.

45.7.2.6 `template<class vec_t, class vec2_t> void o2scl_cblas::daxpy_subvec ( const double alpha, const size_t N, const vec_t & X, vec2_t & Y, const size_t ie )`

This function is used in [householder\\_hv\(\)](#).

If *alpha* is identical with zero or *N*==*ie*, this function will perform no calculations and return without calling the error handler.

If *ie* is greater than *N*-1 then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Definition at line 797 of file `cblas_base.h`.

45.7.2.7 `template<class vec_t, class vec2_t> double o2scl_cblas::ddot_subvec ( const size_t N, const vec_t & X, const vec2_t & Y, const size_t ie )`

This function is used in [householder\\_hv\(\)](#).

If *ie* is greater than *N*-1 then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Definition at line 834 of file `cblas_base.h`.

45.7.2.8 `template<class vec_t> double o2scl_cblas::dnrm2_subvec ( const size_t N, const vec_t & X, const size_t ie )`

Used in [householder\\_transform\(\)](#).

#### Note

The suffix "2" on the function name indicates that this computes the "2-norm", not that the norm is squared.

If *ie* is greater than *N*-1 then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Definition at line 875 of file `cblas_base.h`.

**45.7.2.9** `template<class vec_t> void o2scl_cblas::dscal_subvec ( const double alpha, const size_t N, vec_t & X, const size_t ie )`

This function is used in [householder\\_transform\(\)](#).

If *ie* is greater than *N*-1 then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Definition at line 920 of file `cblas_base.h`.

**45.7.2.10** `template<class mat_t, class vec_t> void o2scl_cblas::daxpy_subcol ( const double alpha, const size_t M, const mat_t & X, const size_t ir, const size_t ic, vec_t & y )`

Given the matrix *X*, define the vector *x* as the column with index *ic*. This function computes  $y = \alpha x + y$  for elements in the vectors *x* and *y* from row *ir* to row *M*-1 (inclusive). All other elements in *x* and *y* are not referenced.

Used in `householder_hv_sub()`.

Definition at line 959 of file `cblas_base.h`.

**45.7.2.11** `template<class mat_t, class vec_t> double o2scl_cblas::ddot_subcol ( const size_t M, const mat_t & X, const size_t ir, const size_t ic, const vec_t & y )`

Given the matrix *X*, define the vector *x* as the column with index *ic*. This function computes  $r = x \cdot y$  for elements in the vectors *x* and *y* from row *ir* to row *M*-1 (inclusive). All other elements in *x* and *y* are not referenced.

Used in `householder_hv_sub()`.

Definition at line 1001 of file `cblas_base.h`.

**45.7.2.12** `template<class mat_t> double o2scl_cblas::dnrm2_subcol ( const mat_t & A, const size_t ir, const size_t ic, const size_t M )`

Given the matrix *A*, define the vector *x* as the column with index *ic*. This function computes the norm of the part of *x* from row *ir* to row *M*-1 (inclusive). All other elements in *x* are not referenced.

if *M* is zero, then this function silently returns zero without calling the error handler.

This function is used in [householder\\_transform\\_subcol\(\)](#).

#### Note

The suffix "2" on the function name indicates that this computes the "2-norm", not that the norm is squared.

Definition at line 1044 of file `cblas_base.h`.

**45.7.2.13** `template<class mat_t> void o2scl_cblas::dscal_subcol ( mat_t & A, const size_t ir, const size_t ic, const size_t M, const double alpha )`

Given the matrix *A*, define the vector *x* as the column with index *ic*. This function computes  $x = \alpha x$  for elements in the vectors *x* from row *ir* to row *M*-1 (inclusive). All other elements in *x* are not referenced.

Used in [householder\\_transform\\_subcol\(\)](#).

Definition at line 1093 of file `cblas_base.h`.

**45.7.2.14** `template<class mat_t, class vec_t> void o2scl_cblas::daxpy_subrow ( const double alpha, const size_t N, const mat_t & X, const size_t ir, const size_t ic, vec_t & Y )`

Given the matrix *X*, define the vector *x* as the row with index *ir*. This function computes  $y = \alpha x + y$  for elements in the vectors *x* from column *ic* to column *N*-1 (inclusive). All other elements in *x* and *y* are not referenced.

If *ic* is greater than *N*-1 then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Used in `householder_hv_sub()`.

Definition at line 1138 of file `cblas_base.h`.

**45.7.2.15** `template<class mat_t, class vec_t> double o2scl_cblas::ddot_subrow ( const size_t N, const mat_t & X, const size_t ir, const size_t ic, const vec_t & Y )`

Given the matrix X, define the vector  $x$  as the row with index  $ir$ . This function computes  $r = x \cdot y$  for elements in the vectors  $x$  from column  $ic$  to column  $N-1$  (inclusive). All other elements in  $x$  and  $y$  are not referenced.

If  $ic$  is greater than  $N-1$  then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Used in `householder_hv_sub()`.

Definition at line 1184 of file `cblas_base.h`.

**45.7.2.16** `template<class mat_t> double o2scl_cblas::dnrm2_subrow ( const mat_t & M, const size_t ir, const size_t ic, const size_t N )`

Given the matrix X, define the vector  $x$  as the row with index  $ir$ . This function computes the norm of the part of  $x$  from column  $ic$  to column  $N-1$  (inclusive). All other elements in  $x$  are not referenced.

#### Note

The suffix "2" on the function name indicates that this computes the "2-norm", not that the norm is squared.

Definition at line 1223 of file `cblas_base.h`.

**45.7.2.17** `template<class mat_t> void o2scl_cblas::dscal_subrow ( mat_t & A, const size_t ir, const size_t ic, const size_t N, const double alpha )`

Given the matrix A, define the vector  $x$  as the row with index  $ir$ . This function computes  $x = \alpha x$  for elements in the vectors  $x$  from column  $ic$  to column  $N-1$  (inclusive). All other elements in  $x$  and  $y$  are not referenced.

If  $ic$  is greater than  $N-1$  then the error handler will be called if `O2SCL_NO_RANGE_CHECK` is not defined.

Definition at line 1266 of file `cblas_base.h`.

## 45.8 o2scl\_cblas\_paren Namespace Reference

Namespace for O2scl CBLAS function templates with operator()

### 45.8.1 Detailed Description

This namespace contains an identical copy of all the functions given in the [o2scl\\_cblas](#) namespace, but perform array indexing with `operator()` rather than `operator[]`. See [o2scl\\_cblas](#) for the function listing and documentation.

## 45.9 o2scl\_const Namespace Reference

O2scl constants.

### Variables

- const double **gsl\_posinf** = `GSL_POSINF`
- const double **gsl\_neginf** = `GSL_NEGINF`
- const double **pi** = `acos(-1.0)`  
 $\pi$
- const double **pi2** = `pi*pi`  
 $\pi^2$
- const double **zeta32** = `2.6123753486854883433`  
 $\zeta(3/2)$
- const double **zeta2** = `1.6449340668482264365`  
 $\zeta(2)$

- const double [zeta52](#) = 1.3414872572509171798  
 $\zeta(5/2)$
- const double [zeta3](#) = 1.2020569031595942854  
 $\zeta(3)$
- const double [zeta5](#) = 1.0369277551433699263  
 $\zeta(5)$
- const double [zeta7](#) = 1.0083492773819228268  
 $\zeta(7)$

#### Particle Physics Booklet

(see also D.E. Groom, et. al., Euro. Phys. J. C 15 (2000) 1.)

- const double [sin2\\_theta\\_weak](#) = 0.2224  
 $\sin^2 \theta_W$
- const double [mev\\_kg](#) = 1.782661731e-30  
1 MeV in kg
- const double [mev\\_cgs](#) = 1.60217733e-6  
1 MeV in  $\text{g} \cdot \text{cm}^2 / \text{s}^2$  (ergs)
- const double [boltzmann\\_mev\\_K](#) = 8.617342e-11  
1 MeV in Kelvin

From <http://physics.nist.gov/cuu/Constants> (7/27/11)

- const double [hc\\_mev\\_fm](#) = 197.3269718  
 $\hbar c$  in MeV fm
- const double [gfermi\\_gev](#) = 1.166364e-5  
Fermi coupling constant ( $G_F$ ) in  $\text{GeV}^{-2}$ .
- const double [hc\\_mev\\_cm](#) = 1.973269718e-11  
 $\hbar c$  in MeV cm

#### Squared electron charge

- const double [e2\\_gaussian](#) = [o2scl\\_const::hc\\_mev\\_fm](#)\*[gsl\\_num::fine\\_structure](#)  
Electron charge squared in Gaussian units.
- const double [e2\\_hlorentz](#) = [gsl\\_num::fine\\_structure](#)\*4.0\*pi  
Electron charge squared in Heaviside-Lorentz units where  $\hbar = c = 1$ .
- const double [e2\\_mksa](#) = [gsl\\_mksa::electron\\_charge](#)  
Electron charge squared in SI(MKSA) units.

#### 45.9.1 Variable Documentation

45.9.1.1 const double [o2scl\\_const::e2\\_gaussian](#) = [o2scl\\_const::hc\\_mev\\_fm](#)\*[gsl\\_num::fine\\_structure](#)

In Gaussian Units:

$$\vec{\nabla} \cdot \vec{E} = 4\pi\rho, \quad \vec{E} = -\vec{\nabla}\Phi, \quad \nabla^2\Phi = -4\pi\rho, \\ F = \frac{q_1 q_2}{r^2}, \quad W = \frac{1}{2} \int \rho V d^3x = \frac{1}{8\pi} \int |\vec{E}|^2 d^3x, \quad \alpha = \frac{e^2}{\hbar c} = \frac{1}{137}$$

Definition at line 952 of file constants.h.

45.9.1.2 const double [o2scl\\_const::e2\\_hlorentz](#) = [gsl\\_num::fine\\_structure](#)\*4.0\*pi

In Heaviside-Lorentz units:

$$\vec{\nabla} \cdot \vec{E} = \rho, \quad \vec{E} = -\vec{\nabla}\Phi, \quad \nabla^2\Phi = -\rho, \\ F = \frac{q_1 q_2}{4\pi r^2}, \quad W = \frac{1}{2} \int \rho V d^3x = \frac{1}{2} \int |\vec{E}|^2 d^3x, \quad \alpha = \frac{e^2}{4\pi} = \frac{1}{137}$$

Definition at line 972 of file constants.h.

## 45.9.1.3 const double o2scl\_const::e2\_mkasa = gsl\_mkasa::electron\_charge

In MKSA units:

$$\vec{\nabla} \cdot \vec{E} = \rho, \quad \vec{E} = -\vec{\nabla}\Phi, \quad \nabla^2\Phi = -\rho, \\ F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}, \quad W = \frac{1}{2} \int \rho V d^3x = \frac{\epsilon_0}{2} \int |\vec{E}|^2 d^3x, \quad \alpha = \frac{e^2}{4\pi\epsilon_0 \hbar c} = \frac{1}{137}$$

Note the conversion formulas

$$q_H L = \sqrt{4\pi} q_G = \frac{1}{\sqrt{\epsilon_0}} q_{SI}$$

as mentioned in pg. 13 of D. Griffiths Intro to Elem. Particles.

Definition at line 997 of file constants.h.

## 45.10 o2scl\_fm Namespace Reference

Constants in units of fm.

## 45.10.1 Detailed Description

In nuclear physics is frequently convenient to work in units of fm with  $\hbar = c = k_B = 1$ . Several useful constants are given here.

For example, `mev` gives 1 MeV in units of fm<sup>-1</sup> (the solution to the equation 1MeV = x fm<sup>-1</sup>). If you have a number in MeV, you can multiply by `mev` to get a number in units of fm<sup>-1</sup>. Alternatively, `mev` is a number with units MeV<sup>-1</sup> · fm<sup>-1</sup>. These can be combined, so that `erg` divided by `sec` is 1 erg/sec in units of fm<sup>-2</sup>.

/todo Make e.g. neutron mass consistent with the GSL ones somehow.

## Variables

- const double `mev` = 1.0/o2scl\_const::hc\_mev\_fm  
1 MeV in fm<sup>-1</sup>
- const double `kg` = mev\*5.60958885e29  
1 kg in fm<sup>-1</sup>
- const double `Kelvin` = 8.6173324e-11\*mev  
1 Kelvin in fm<sup>-1</sup>
- const double `joule` = kg/gsl\_mks::speed\_of\_light/gsl\_mks::speed\_of\_light  
1 Joule in fm<sup>-1</sup>
- const double `msun_per_km3` = gsl\_mks::solar\_mass/1.0e54\*kg  
1 M<sub>⊙</sub>/km<sup>3</sup> in fm<sup>-4</sup>
- const double `erg` = kg/1.0e3/gsl\_cgs::speed\_of\_light/gsl\_cgs::speed\_of\_light  
1 erg in fm<sup>-1</sup>
- const double `sec` = gsl\_mks::speed\_of\_light\*1.0e15  
1 second in fm
- const double `ec_gauss_fm2`  
1 Gauss times the electron charge in Gaussian units in fm<sup>-2</sup>
- const double `gauss2_fm4` = ec\_gauss\_fm2\*ec\_gauss\_fm2/gsl\_num::fine\_structure  
Conversion factor from Gauss<sup>2</sup> to fm<sup>-4</sup> in Gaussian units.

From <http://physics.nist.gov/cuu/index.html> (7/27/11)

- const double `mass_neutron` = 939.565379/o2scl\_const::hc\_mev\_fm  
Neutron mass in fm<sup>-1</sup>.
- const double `mass_proton` = 938.272046/o2scl\_const::hc\_mev\_fm  
Proton mass in fm<sup>-1</sup>.
- const double `mass_electron` = 0.510998928/o2scl\_const::hc\_mev\_fm  
Electron mass in fm<sup>-1</sup>.

- const double `mass_muon` = 105.6583715/o2scl\_const::hc\_mev\_fm  
*Muon mass in fm<sup>-1</sup>.*
- const double `mass_amu` = 931.494061/o2scl\_const::hc\_mev\_fm  
*Atomic mass unit in fm<sup>-1</sup>.*
- const double `mass_alpha` = 3727.379240/o2scl\_const::hc\_mev\_fm  
*Alpha particle mass in fm<sup>-1</sup>.*

#### Masses from Particle Physics Booklet

(see also D.E. Groom, et. al., Euro. Phys. J. C 15 (2000) 1.)

- const double `mass_lambda` = 1115.683/o2scl\_const::hc\_mev\_fm  
*Λ mass in fm<sup>-1</sup>*
- const double `mass_sigmam` = 1197.45/o2scl\_const::hc\_mev\_fm  
*Σ<sup>-</sup> mass in fm<sup>-1</sup>*
- const double `mass_sigma` = 1192.642/o2scl\_const::hc\_mev\_fm  
*Σ<sup>0</sup> mass in fm<sup>-1</sup>*
- const double `mass_sigmap` = 1189.37/o2scl\_const::hc\_mev\_fm  
*Σ<sup>+</sup> mass in fm<sup>-1</sup>*
- const double `mass_cascadem` = 1321.3/o2scl\_const::hc\_mev\_fm  
*Ξ<sup>-</sup> mass in fm<sup>-1</sup>*
- const double `mass_cascade` = 1314.8/o2scl\_const::hc\_mev\_fm  
*Ξ<sup>0</sup> mass in fm<sup>-1</sup>*
- const double `mass_omega` = 782.57/o2scl\_const::hc\_mev\_fm  
*ω mass in fm<sup>-1</sup>*
- const double `mass_rho` = 769.3/o2scl\_const::hc\_mev\_fm  
*ρ mass in fm<sup>-1</sup>*

#### 45.10.2 Variable Documentation

##### 45.10.2.1 const double o2scl\_fm::mass\_alpha = 3727.379240/o2scl\_const::hc\_mev\_fm

This does not include the mass of the additional two electrons which are present in a helium atom.

Definition at line 1040 of file constants.h.

##### 45.10.2.2 const double o2scl\_fm::ec\_gauss\_fm2

**Initial value:**

```
gsl_mks::electron_charge*1.0e-34/  
gsl_mks::plancks_constant_hbar
```

Definition at line 1091 of file constants.h.

##### 45.10.2.3 const double o2scl\_fm::gauss2\_fm4 = ec\_gauss\_fm2\*ec\_gauss\_fm2/gsl\_num::fine\_structure

This is useful, e.g. in converting magnetic field squared to an energy density.

Definition at line 1100 of file constants.h.

## 45.11 o2scl\_graph Namespace Reference

Namespace for experimental functions for use with Root.

#### 45.11.1 Detailed Description

This namespace contains several functions, defined in graph.cpp, which simplify plotting with Root. They require that the Root libraries have been installed and are not compiled in with the normal O2scl libraries. Some of the example plots created for the documentation are based on these functions.

## Functions

- void [arrow](#) (double x1, double y1, double x2, double y2, TLine \*&line, TPolyLine \*&poly, double size=0.1, double size2=0.8, double alpha1=0.35)  
*Draw a pretty arrow from (x1,y1) to (x2,y2)*
- int [new\\_graph](#) (TCanvas \*&c1, TPad \*&p1, TH1 \*&th1, std::string CanvasName, std::string WindowName, std::string PadName, double lleft, double lbottom, double lright, double ltop, int left=0, int top=0, int right=700, int bottom=700, bool logx=false, bool logy=false)  
*Make a canvas and pad.*
- int [new\\_graph\\_ticks](#) (TCanvas \*&c1, TPad \*&p1, TH1 \*&th1, std::string CanvasName, std::string WindowName, std::string PadName, double lleft, double lbottom, double lright, double ltop, TGaxis \*&a1, TGaxis \*&a2, int left=0, int top=0, int right=700, int bottom=700, bool logx=false, bool logy=false)  
*Make a canvas and pad with more tick marks.*
- TGraph \* [table\\_graph](#) (o2scl::table\_units &at, std::string scolx, std::string scoly, int style=1, int color=1)  
*Graph two columns from a data table.*
- TGraphErrors \* [table\\_graph\\_errors](#) (o2scl::table\_units &at, std::string scolx, std::string scoly, std::string xerr, std::string yerr, int style=1, int color=1)  
*Plot colums from a data table with error bars.*
- int [two\\_up\\_graph](#) (TCanvas \*&c1, TPad \*&p1, TPad \*&p2, TH1 \*&th1, TH1 \*&th2, std::string CanvasName, std::string WindowName, std::string Pad1Name, std::string Pad2Name, double lowx1, double highx1, double lowx2, double highx2, double lowy, double highy, int left=0, int top=0, int right=1000, int bottom=700, bool logx1=false, bool logx2=false, bool logy=false, double alpha=1.3, double margin=0.1)  
*Make a canvas with a two-up graph, side-by-side.*
- int [two\\_up\\_graphy](#) (TCanvas \*&c1, TPad \*&p1, TPad \*&p2, TH1 \*&th1, TH1 \*&th2, std::string CanvasName, std::string WindowName, std::string Pad1Name, std::string Pad2Name, double lowx, double highx, double lowy1, double highy1, double lowy2, double highy2, int left=0, int top=0, int right=1000, int bottom=700, bool logx=false, bool logy1=false, bool logy2=false, double alpha=1.3, double margin=0.1)  
*Make a canvas with two plots, one on top of the other.*

## Variables

## Some useful colors

- const int **kGray20** = kGray
- const int **kGray40** = kGray+1
- const int **kGray60** = kGray+2
- const int **kGray80** = kGray+3

## Markers

- const int **m\_small\_dot** = 1
- const int **m\_plus** = 2
- const int **m\_asterisk** = 3
- const int **m\_circle** = 4
- const int **m\_times** = 5
- const int **m\_med\_dot** = 6
- const int **m\_large\_dot** = 7
- const int **m\_fill\_circle** = 8
- const int **m\_fill\_square** = 21
- const int **m\_fill\_up\_triangle** = 22
- const int **m\_fill\_dn\_triangle** = 23
- const int **m\_open\_circle** = 24
- const int **m\_open\_square** = 25
- const int **m\_open\_up\_triangle** = 26
- const int **m\_open\_diamond** = 27
- const int **m\_open\_plus** = 28
- const int **m\_fill\_star** = 29
- const int **m\_open\_star** = 30
- const int **m\_asterisk2** = 31
- const int **m\_open\_dn\_triangle** = 32
- const int **m\_fill\_diamond** = 33
- const int **m\_fill\_plus** = 34

## 45.11.2 Function Documentation

45.11.2.1 void o2scl\_graph::arrow ( double *x1*, double *y1*, double *x2*, double *y2*, TLine \**line*, TPolyLine \**poly*, double *size* = 0.1, double *size2* = 0.8, double *alpha1* = 0.35 )

The parameter *size* determines the size of the head relative to the size of the arrow, *size2* determines the position of the niche (1.0 is no niche), and *alpha1* determines the angle of the head relative to the line (default is about 20 degrees).

45.11.2.2 int o2scl\_graph::new\_graph ( TCanvas \**c1*, TPad \**p1*, TH1 \**th1*, std::string *CanvasName*, std::string *WindowName*, std::string *PadName*, double *lleft*, double *lbottom*, double *lright*, double *ltop*, int *left* = 0, int *top* = 0, int *right* = 700, int *bottom* = 700, bool *logx* = false, bool *logy* = false )

The *CanvasName* is the default output filename for graphs and macros also. The *PadName* is the name that comes up when you right-click on the pad. When making .eps files, the Title field is set to "CanvasName.eps: Windowname". This Title field is the title that appears, e.g., in a ghostview window. The x-axis limits are given by *lleft* and *lright* and the y-axis limits are given in *lbottom* and *ltop*. The upper left corner of the canvas window is at (*left*, *top*) and the lower right corner is (*right*, *bottom*). The parameters *logx* and *logy* determine whether or not the x- or y-axes are logarithmic instead of linear (the default). The canvas and pad objects are created using *new*, and the histogram object *th1* is created with TPad::DrawFrame().

45.11.2.3 int o2scl\_graph::new\_graph\_ticks ( TCanvas \**c1*, TPad \**p1*, TH1 \**th1*, std::string *CanvasName*, std::string *WindowName*, std::string *PadName*, double *lleft*, double *lbottom*, double *lright*, double *ltop*, TGaxis \**a1*, TGaxis \**a2*, int *left* = 0, int *top* = 0, int *right* = 700, int *bottom* = 700, bool *logx* = false, bool *logy* = false )

This is the same as [new\\_graph\(\)](#), except it adds tick marks to the right and top axes, which are created with *new* and returned in *a1* and *a2* respectively).

**Idea for Future** Modify this to just directly call [new\\_graph\(\)](#) and add the new axes on top.

45.11.2.4 TGraph\* o2scl\_graph::table\_graph ( o2scl::table\_units &*at*, std::string *scolx*, std::string *scoly*, int *style* = 1, int *color* = 1 )

This function plots the function defined by (*scolx*, *scoly*) given in table *at* with line style *style* and line color *color*. A TGraph object created with *new* is returned. The name of the graph object is automatically set to be the same as the *scoly*, but this can always be changed afterwards, i.e.

```
g1=table_graph(at,scolx,scoly);
g1->SetName("Curve name");
g1->Draw();
```

45.11.2.5 int o2scl\_graph::two\_up\_graph ( TCanvas \**c1*, TPad \**p1*, TPad \**p2*, TH1 \**th1*, TH1 \**th2*, std::string *CanvasName*, std::string *WindowName*, std::string *Pad1Name*, std::string *Pad2Name*, double *lowx1*, double *highx1*, double *lowx2*, double *highx2*, double *lowy*, double *highy*, int *left* = 0, int *top* = 0, int *right* = 1000, int *bottom* = 700, bool *logx1* = false, bool *logx2* = false, bool *logy* = false, double *alpha* = 1.3, double *margin* = 0.1 )

This function creates a canvas and two pads for a side-by-side plot with two different x-axes and the same y-axis. The x-axis of the left-hand plot has limits (*lowx1*, *highx1*) and the the x-axis for the right-hand plot has limits (*lowx2*, *highx2*).

45.11.2.6 int o2scl\_graph::two\_up\_graphy ( TCanvas \**c1*, TPad \**p1*, TPad \**p2*, TH1 \**th1*, TH1 \**th2*, std::string *CanvasName*, std::string *WindowName*, std::string *Pad1Name*, std::string *Pad2Name*, double *lowx*, double *highx*, double *lowy1*, double *highy1*, double *lowy2*, double *highy2*, int *left* = 0, int *top* = 0, int *right* = 1000, int *bottom* = 700, bool *logx* = false, bool *logy1* = false, bool *logy2* = false, double *alpha* = 1.3, double *margin* = 0.1 )

The variable *p1* is on bottom and *p2* is on top

## 45.12 o2scl\_inte\_gk\_coeffs Namespace Reference

A namespace for the GSL adaptive Gauss-Kronrod integration coefficients.



## 45.12.1 Detailed Description

The storage scheme follows that of QUADPACK: symmetry about the origin permits storing only those abscissae in the interval  $[0, 1)$ . Similarly for the weights. The odd-indexed abscissae `xgk[1]`, `xgk[3]`,... belong to the low-order Gauss rule. For the full Gauss-Kronrod rule, the array `wgk[]` holds the weights corresponding to the abscissae `xgk[]`. For the low-order rule, `wg[i]` is the weight corresponding to `xgk[2*i+1]`.

**Documentation from GSL:**

Gauss quadrature weights and kronrod quadrature abscissae and weights as evaluated with 80 decimal digit arithmetic by L. W. Fullerton, Bell Labs, Nov. 1981.

**Variables**

- static const double [qk15\\_xgk](#) [8]  
*Abscissae of the 15-point Kronrod rule.*
- static const double [qk15\\_wg](#) [4]  
*Weights of the 7-point Gauss rule.*
- static const double [qk15\\_wgk](#) [8]  
*Weights of the 15-point Kronrod rule.*
- static const double [qk21\\_xgk](#) [11]  
*Abscissae of the 21-point Kronrod rule.*
- static const double [qk21\\_wg](#) [5]  
*Weights of the 10-point Gauss rule.*
- static const double [qk21\\_wgk](#) [11]  
*Weights of the 21-point Kronrod rule.*
- static const double [qk31\\_xgk](#) [16]  
*Abscissae of the 31-point Kronrod rule.*
- static const double [qk31\\_wg](#) [8]  
*Weights of the 15-point Gauss rule.*
- static const double [qk31\\_wgk](#) [16]  
*Weights of the 31-point Kronrod rule.*
- static const double [qk41\\_xgk](#) [21]  
*Abscissae of the 41-point Kronrod rule.*
- static const double [qk41\\_wg](#) [11]  
*Weights of the 20-point Gauss rule.*
- static const double [qk41\\_wgk](#) [21]  
*Weights of the 41-point Kronrod rule.*
- static const double [qk51\\_xgk](#) [26]  
*Abscissae of the 51-point Kronrod rule.*
- static const double [qk51\\_wg](#) [13]  
*Weights of the 25-point Gauss rule.*
- static const double [qk51\\_wgk](#) [26]  
*Weights of the 51-point Kronrod rule.*
- static const double [qk61\\_xgk](#) [31]  
*Abscissae of the 61-point Kronrod rule.*
- static const double [qk61\\_wg](#) [15]  
*Weights of the 30-point Gauss rule.*
- static const double [qk61\\_wgk](#) [31]  
*Weights of the 61-point Kronrod rule.*

## 45.12.2 Variable Documentation

45.12.2.1 `const double o2scl_inte_gk_coeffs::qk15_xgk[8]` [static]

**Initial value:**

```
{
    0.991455371120812639206854697526329,
    0.949107912342758524526189684047851,
    0.864864423359769072789712788640926,
    0.741531185599394439863864773280788,
    0.586087235467691130294144838258730,
    0.405845151377397166906606412076961,
    0.207784955007898467600689403773245,
    0.00000000000000000000000000000000
}
```

Definition at line 53 of file gsl\_inte\_kronrod.h.

**45.12.2.2** `const double o2scl_inte_gk_coeffs::qk15_wg[4]` `[static]`

**Initial value:**

```
{
    0.129484966168869693270611432679082,
    0.279705391489276667901467771423780,
    0.381830050505118944950369775488975,
    0.417959183673469387755102040816327
}
```

Definition at line 65 of file gsl\_inte\_kronrod.h.

**45.12.2.3** `const double o2scl_inte_gk_coeffs::qk15_wgk[8]` `[static]`

**Initial value:**

```
{
    0.022935322010529224963732008058970,
    0.063092092629978553290700663189204,
    0.104790010322250183839876322541518,
    0.140653259715525918745189590510238,
    0.169004726639267902826583426598550,
    0.190350578064785409913256402421014,
    0.204432940075298892414161999234649,
    0.209482141084727828012999174891714
}
```

Definition at line 74 of file gsl\_inte\_kronrod.h.

**45.12.2.4** `const double o2scl_inte_gk_coeffs::qk21_xgk[11]` `[static]`

**Initial value:**

```
{
    0.995657163025808080735527280689003,
    0.973906528517171720077964012084452,
    0.930157491355708226001207180059508,
    0.865063366688984510732096688423493,
    0.780817726586416897063717578345042,
    0.679409568299024406234327365114874,
    0.562757134668604683339000099272694,
    0.433395394129247190799265943165784,
    0.294392862701460198131126603103866,
    0.148874338981631210884826001129720,
    0.00000000000000000000000000000000
}
```

Definition at line 87 of file gsl\_inte\_kronrod.h.

**45.12.2.5** `const double o2scl_inte_gk_coeffs::qk21_wg[5]` `[static]`

**Initial value:**

---

```
{
  0.066671344308688137593568809893332,
  0.149451349150580593145776339657697,
  0.219086362515982043995534934228163,
  0.269266719309996355091226921569469,
  0.295524224714752870173892994651338
}
```

Definition at line 103 of file gsl\_inte\_kronrod.h.

**45.12.2.6** `const double o2scl_inte_gk_coeffs::qk21_wgk[11]` `[static]`

**Initial value:**

```
{
  0.011694638867371874278064396062192,
  0.032558162307964727478818972459390,
  0.054755896574351996031381300244580,
  0.075039674810919952767043140916190,
  0.093125454583697605535065465083366,
  0.109387158802297641899210590325805,
  0.123491976262065851077958109831074,
  0.134709217311473325928054001771707,
  0.142775938577060080797094273138717,
  0.147739104901338491374841515972068,
  0.149445554002916905664936468389821
}
```

Definition at line 113 of file gsl\_inte\_kronrod.h.

**45.12.2.7** `const double o2scl_inte_gk_coeffs::qk31_xgk[16]` `[static]`

**Initial value:**

```
{
  0.998002298693397060285172840152271,
  0.987992518020485428489565718586613,
  0.967739075679139134257347978784337,
  0.937273392400705904307758947710209,
  0.897264532344081900882509656454496,
  0.848206583410427216200648320774217,
  0.790418501442465932967649294817947,
  0.724417731360170047416186054613938,
  0.650996741297416970533735895313275,
  0.570972172608538847537226737253911,
  0.485081863640239680693655740232351,
  0.394151347077563369897207370981045,
  0.299180007153168812166780024266389,
  0.201194093997434522300628303394596,
  0.101142066918717499027074231447392,
  0.00000000000000000000000000000000
}
```

Definition at line 129 of file gsl\_inte\_kronrod.h.

**45.12.2.8** `const double o2scl_inte_gk_coeffs::qk31_wg[8]` `[static]`

**Initial value:**

```
{
  0.030753241996117268354628393577204,
  0.070366047488108124709267416450667,
  0.107159220467171935011869546685869,
  0.139570677926154314447804794511028,
  0.166269205816993933553200860481209,
  0.186161000015562211026800561866423,
  0.00000000000000000000000000000000
}
```

```

0.198431485327111576456118326443839,
0.202578241925561272880620199967519
}

```

Definition at line 150 of file gsl\_inte\_kronrod.h.

**45.12.2.9** `const double o2scl_inte_gk_coeffs::qk31_wgk[16]` `[static]`

**Initial value:**

```

{
0.005377479872923348987792051430128,
0.015007947329316122538374763075807,
0.025460847326715320186874001019653,
0.035346360791375846222037948478360,
0.044589751324764876608227299373280,
0.053481524690928087265343147239430,
0.062009567800670640285139230960803,
0.069854121318728258709520077099147,
0.0768496807577220378894432777482659,
0.083080502823133021038289247286104,
0.088564443056211770647275443693774,
0.093126598170825321225486872747346,
0.096642726983623678505179907627589,
0.099173598721791959332393173484603,
0.100769845523875595044946662617570,
0.101330007014791549017374792767493
}

```

Definition at line 163 of file gsl\_inte\_kronrod.h.

**45.12.2.10** `const double o2scl_inte_gk_coeffs::qk41_xgk[21]` `[static]`

**Initial value:**

```

{
0.998859031588277663838315576545863,
0.993128599185094924786122388471320,
0.981507877450250259193342994720217,
0.963971927277913791267666131197277,
0.940822633831754753519982722212443,
0.912234428251325905867752441203298,
0.878276811252281976077442995113078,
0.839116971822218823394529061701521,
0.795041428837551198350638833272788,
0.746331906460150792614305070355642,
0.693237656334751384805490711845932,
0.636053680726515025452836696226286,
0.575140446819710315342946036586425,
0.510867001950827098004364050955251,
0.443593175238725103199992213492640,
0.373706088715419560672548177024927,
0.301627868114913004320555356858592,
0.227785851141645078080496195368575,
0.152605465240922675505220241022678,
0.076526521133497333754640409398838,
0.00000000000000000000000000000000
}

```

Definition at line 184 of file gsl\_inte\_kronrod.h.

**45.12.2.11** `const double o2scl_inte_gk_coeffs::qk41_wg[11]` `[static]`

**Initial value:**

```

{

```

---

```

0.017614007139152118311861962351853,
0.040601429800386941331039952274932,
0.062672048334109063569506535187042,
0.083276741576704748724758143222046,
0.101930119817240435036750135480350,
0.118194531961518417312377377711382,
0.131688638449176626898494499748163,
0.142096109318382051329298325067165,
0.149172986472603746787828737001969,
0.152753387130725850698084331955098
}

```

Definition at line 210 of file gsl\_inte\_kronrod.h.

**45.12.2.12** `const double o2scl_inte_gk_coeffs::qk41_wgk[21]` [static]

**Initial value:**

```

{
0.003073583718520531501218293246031,
0.008600269855642942198661787950102,
0.014626169256971252983787960308868,
0.020388373461266523598010231432755,
0.025882133604951158834505067096153,
0.031287306777032798958543119323801,
0.036600169758200798030557240707211,
0.041668873327973686263788305936895,
0.046434821867497674720231880926108,
0.050944573923728691932707670050345,
0.055195105348285994744832372419777,
0.059111400880639572374967220648594,
0.062653237554781168025870122174255,
0.065834597133618422111563556969398,
0.068648672928521619345623411885368,
0.071054423553444068305790361723210,
0.073030690332786667495189417658913,
0.074582875400499188986581418362488,
0.075704497684556674659542775376617,
0.076377867672080736705502835038061,
0.076600711917999656445049901530102
}

```

Definition at line 225 of file gsl\_inte\_kronrod.h.

**45.12.2.13** `const double o2scl_inte_gk_coeffs::qk51_xgk[26]` [static]

**Initial value:**

```

{
0.999262104992609834193457486540341,
0.995556969790498097908784946893902,
0.988035794534077247637331014577406,
0.976663921459517511498315386479594,
0.961614986425842512418130033660167,
0.942974571228974339414011169658471,
0.920747115281701561746346084546331,
0.894991997878275368851042006782805,
0.865847065293275595448996969588340,
0.833442628760834001421021108693570,
0.797873797998500059410410904994307,
0.759259263037357630577282865204361,
0.717766406813084388186654079773298,
0.673566368473468364485120633247622,
0.626810099010317412788122681624518,
0.577662930241222967723689841612654,
0.526325284334719182599623778158010,
0.473002731445714960522182115009192,

```

```

0.417885382193037748851814394594572,
0.361172305809387837735821730127641,
0.303089538931107830167478909980339,
0.243866883720988432045190362797452,
0.183718939421048892015969888759528,
0.122864692610710396387359818808037,
0.061544483005685078886546392366797,
0.00000000000000000000000000000000
}

```

Definition at line 251 of file gsl\_inte\_kronrod.h.

**45.12.2.14** `const double o2scl_inte_gk_coeffs::qk51_wg[13]` `[static]`

**Initial value:**

```

{
0.011393798501026287947902964113235,
0.026354986615032137261901815295299,
0.040939156701306312655623487711646,
0.054904695975835191925936891540473,
0.068038333812356917207187185656708,
0.080140700335001018013234959669111,
0.091028261982963649811497220702892,
0.100535949067050644202206890392686,
0.108519624474263653116093957050117,
0.114858259145711648339325545869556,
0.119455763535784772228178126512901,
0.122242442990310041688959518945852,
0.123176053726715451203902873079050
}

```

Definition at line 282 of file gsl\_inte\_kronrod.h.

**45.12.2.15** `const double o2scl_inte_gk_coeffs::qk51_wgk[26]` `[static]`

**Initial value:**

```

{
0.001987383892330315926507851882843,
0.005561932135356713758040236901066,
0.009473973386174151607207710523655,
0.013236229195571674813656405846976,
0.016847817709128298231516667536336,
0.020435371145882835456568292235939,
0.024009945606953216220092489164881,
0.027475317587851737802948455517811,
0.030792300167387488891109020215229,
0.034002130274329337836748795229551,
0.037116271483415543560330625367620,
0.040083825504032382074839284467076,
0.042872845020170049476895792439495,
0.045502913049921788909870584752660,
0.047982537138836713906392255756915,
0.050277679080715671963325259433440,
0.052362885806407475864366712137873,
0.054251129888545490144543370459876,
0.055950811220412317308240686382747,
0.057437116361567832853582693939506,
0.058689680022394207961974175856788,
0.059720340324174059979099291932562,
0.060539455376045862945360267517565,
0.061128509717053048305859030416293,
0.061471189871425316661544131965264,
0.061580818067832935078759824240066
}

```

Definition at line 300 of file gsl\_inte\_kronrod.h.

45.12.2.16 `const double o2scl_inte_gk_coeffs::qk61_wg[15]` `[static]`

**Initial value:**

```
{
  0.007968192496166605615465883474674,
  0.018466468311090959142302131912047,
  0.028784707883323369349719179611292,
  0.038799192569627049596801936446348,
  0.048402672830594052902938140422808,
  0.057493156217619066481721689402056,
  0.065974229882180495128128515115962,
  0.073755974737705206268243850022191,
  0.080755895229420215354694938460530,
  0.086899787201082979802387530715126,
  0.092122522237786128717632707087619,
  0.096368737174644259639468626351810,
  0.099593420586795267062780282103569,
  0.101762389748405504596428952168554,
  0.102852652893558840341285636705415
}
```

Definition at line 367 of file `gsl_inte_kronrod.h`.

## 45.13 o2scl\_inte\_qng\_coeffs Namespace Reference

A namespace for the quadrature coefficients for non-adaptive integration.

### 45.13.1 Detailed Description

#### Documentation from GSL:

Gauss-Kronrod-Patterson quadrature coefficients for use in quadpack routine `qng`. These coefficients were calculated with 101 decimal digit arithmetic by L. W. Fullerton, Bell Labs, Nov 1981.

#### Variables

- static const double `x1` [5]
- static const double `w10` [5]
- static const double `x2` [5]
- static const double `w21a` [5]
- static const double `w21b` [6]
- static const double `x3` [11]
- static const double `w43a` [10]
- static const double `w43b` [12]
- static const double `x4` [22]
- static const double `w87a` [21]
- static const double `w87b` [23]

### 45.13.2 Variable Documentation

45.13.2.1 `const double o2scl_inte_qng_coeffs::x1[5]` `[static]`

**Initial value:**

```
{
  0.973906528517171720077964012084452,
  0.865063366688984510732096688423493,
  0.679409568299024406234327365114874,
```

```
0.433395394129247190799265943165784,
0.148874338981631210884826001129720
}
```

Abcissae common to the 10-, 21-, 43- and 87-point rule

Definition at line 44 of file gsl\_inte\_qng.h.

**45.13.2.2** `const double o2scl_inte_qng_coeffs::w10[5]` `[static]`

**Initial value:**

```
{
0.066671344308688137593568809893332,
0.149451349150580593145776339657697,
0.219086362515982043995534934228163,
0.269266719309996355091226921569469,
0.295524224714752870173892994651338
}
```

Weights of the 10-point formula

Definition at line 53 of file gsl\_inte\_qng.h.

**45.13.2.3** `const double o2scl_inte_qng_coeffs::x2[5]` `[static]`

**Initial value:**

```
{
0.995657163025808080735527280689003,
0.930157491355708226001207180059508,
0.780817726586416897063717578345042,
0.562757134668604683339000099272694,
0.294392862701460198131126603103866
}
```

Abcissae common to the 21-, 43- and 87-point rule

Definition at line 62 of file gsl\_inte\_qng.h.

**45.13.2.4** `const double o2scl_inte_qng_coeffs::w21a[5]` `[static]`

**Initial value:**

```
{
0.032558162307964727478818972459390,
0.075039674810919952767043140916190,
0.109387158802297641899210590325805,
0.134709217311473325928054001771707,
0.147739104901338491374841515972068
}
```

Weights of the 21-point formula for abcissae x1

Definition at line 71 of file gsl\_inte\_qng.h.

**45.13.2.5** `const double o2scl_inte_qng_coeffs::w21b[6]` `[static]`

**Initial value:**

```
{
0.011694638867371874278064396062192,
0.054755896574351996031381300244580,
0.093125454583697605535065465083366,
0.123491976262065851077958109831074,

```

---



```

    0.142775938577060080797094273138717,
    0.149445554002916905664936468389821
}

```

Weights of the 21-point formula for abscissae x2

Definition at line 80 of file gsl\_inte\_qng.h.

**45.13.2.6** `const double o2scl_inte_qng_coeffs::x3[11]` `[static]`

**Initial value:**

```

{
    0.999333360901932081394099323919911,
    0.987433402908088869795961478381209,
    0.954807934814266299257919200290473,
    0.900148695748328293625099494069092,
    0.825198314983114150847066732588520,
    0.732148388989304982612354848755461,
    0.622847970537725238641159120344323,
    0.499479574071056499952214885499755,
    0.364901661346580768043989548502644,
    0.222254919776601296498260928066212,
    0.074650617461383322043914435796506
}

```

Abscissae common to the 43- and 87-point rule

Definition at line 90 of file gsl\_inte\_qng.h.

**45.13.2.7** `const double o2scl_inte_qng_coeffs::w43a[10]` `[static]`

**Initial value:**

```

{
    0.016296734289666564924281974617663,
    0.037522876120869501461613795898115,
    0.054694902058255442147212685465005,
    0.067355414609478086075553166302174,
    0.073870199632393953432140695251367,
    0.005768556059769796184184327908655,
    0.027371890593248842081276069289151,
    0.046560826910428830743339154433824,
    0.061744995201442564496240336030883,
    0.071387267268693397768559114425516
}

```

Weights of the 43-point formula for abscissae x1, x3

Definition at line 105 of file gsl\_inte\_qng.h.

**45.13.2.8** `const double o2scl_inte_qng_coeffs::w43b[12]` `[static]`

**Initial value:**

```

{
    0.001844477640212414100389106552965,
    0.010798689585891651740465406741293,
    0.021895363867795428102523123075149,
    0.032597463975345689443882222526137,
    0.042163137935191811847627924327955,
    0.050741939600184577780189020092084,
    0.058379395542619248375475369330206,
    0.064746404951445885544689259517511,
    0.069566197912356484528633315038405,
    0.072824441471833208150939535192842,
    0.072824441471833208150939535192842,
    0.069566197912356484528633315038405,
    0.064746404951445885544689259517511,
    0.058379395542619248375475369330206,
    0.050741939600184577780189020092084,
    0.042163137935191811847627924327955,
    0.032597463975345689443882222526137,
    0.021895363867795428102523123075149,
    0.010798689585891651740465406741293,
    0.001844477640212414100389106552965
}

```

```

0.074507751014175118273571813842889,
0.074722147517403005594425168280423
}

```

Weights of the 43-point formula for abscissae x3

Definition at line 119 of file gsl\_inte\_qng.h.

**45.13.2.9** `const double o2scl_inte_qng_coeffs::x4[22]` `[static]`

**Initial value:**

```

{
0.999902977262729234490529830591582,
0.997989895986678745427496322365960,
0.992175497860687222808523352251425,
0.981358163572712773571916941623894,
0.965057623858384619128284110607926,
0.943167613133670596816416634507426,
0.915806414685507209591826430720050,
0.883221657771316501372117548744163,
0.845710748462415666605902011504855,
0.803557658035230982788739474980964,
0.757005730685495558328942793432020,
0.706273209787321819824094274740840,
0.651589466501177922534422205016736,
0.593223374057961088875273770349144,
0.531493605970831932285268948562671,
0.466763623042022844871966781659270,
0.399424847859218804732101665817923,
0.329874877106188288265053371824597,
0.258503559202161551802280975429025,
0.185695396568346652015917141167606,
0.111842213179907468172398359241362,
0.037352123394619870814998165437704
}

```

Abscissae of the 87-point rule

Definition at line 135 of file gsl\_inte\_qng.h.

**45.13.2.10** `const double o2scl_inte_qng_coeffs::w87a[21]` `[static]`

**Initial value:**

```

{
0.008148377384149172900002878448190,
0.018761438201562822243935059003794,
0.027347451050052286161582829741283,
0.033677707311637930046581056957588,
0.036935099820427907614589586742499,
0.002884872430211530501334156248695,
0.013685946022712701888950035273128,
0.023280413502888311123409291030404,
0.030872497611713358675466394126442,
0.035693633639418770719351355457044,
0.000915283345202241360843392549948,
0.005399280219300471367738743391053,
0.010947679601118931134327826856808,
0.016298731696787335262665703223280,
0.021081568889203835112433060188190,
0.025370969769253827243467999831710,
0.029189697756475752501446154084920,
0.032373202467202789685788194889595,
0.034783098950365142750781997949596,
0.036412220731351787562801163687577,
0.037253875503047708539592001191226
}

```

Weights of the 87-point formula for abscissae x1, x2, x3

Definition at line 161 of file gsl\_inte\_qng.h.

**45.13.2.11** `const double o2scl_inte_qng_coeffs::w87b[23]` `[static]`

**Initial value:**

```
{
    0.000274145563762072350016527092881,
    0.001807124155057942948341311753254,
    0.004096869282759164864458070683480,
    0.006758290051847378699816577897424,
    0.009549957672201646536053581325377,
    0.012329447652244853694626639963780,
    0.015010447346388952376697286041943,
    0.017548967986243191099665352925900,
    0.019938037786440888202278192730714,
    0.022194935961012286796332102959499,
    0.024339147126000805470360647041454,
    0.026374505414839207241503786552615,
    0.028286910788771200659968002987960,
    0.030052581128092695322521110347341,
    0.031646751371439929404586051078883,
    0.033050413419978503290785944862689,
    0.034255099704226061787082821046821,
    0.035262412660156681033782717998428,
    0.036076989622888701185500318003895,
    0.036698604498456094498018047441094,
    0.037120549269832576114119958413599,
    0.037334228751935040321235449094698,
    0.037361073762679023410321241766599
}
```

Weights of the 87-point formula for abscissae x4

Definition at line 186 of file gsl\_inte\_qng.h.

## 45.14 o2scl\_linalg Namespace Reference

The namespace for linear algebra classes and functions.

### 45.14.1 Detailed Description

This namespace documentation is in the file [src/base/lib\\_settings.h](#)

**Idea for Future** Move this documentation to the linalg directory.

### Data Structures

- class [linear\\_solver](#)  
*A generic solver for the linear system  $Ax = b$  [abstract base].*
- class [linear\\_solver\\_lu](#)  
*Generic linear solver using LU decomposition.*
- class [linear\\_solver\\_qr](#)  
*Generic linear solver using QR decomposition.*
- class [linear\\_solver\\_hh](#)  
*Generic Householder linear solver.*
- class [gsl\\_solver\\_LU](#)  
*GSL solver by LU decomposition.*

- class [gsl\\_solver\\_QR](#)  
*GSL solver by QR decomposition.*
- class [gsl\\_solver\\_HH](#)  
*GSL Householder solver.*
- class [pointer\\_2\\_mem](#)  
*Allocation object for 2 C-style arrays of equal size.*
- class [pointer\\_4\\_mem](#)  
*Allocation object for 4 C-style arrays of equal size.*
- class [pointer\\_5\\_mem](#)  
*Allocation object for 5 C-style arrays of equal size.*
- class [uvector\\_2\\_mem](#)  
*Allocation object for 2 arrays of equal size.*
- class [uvector\\_4\\_mem](#)  
*Allocation object for 4 arrays of equal size.*
- class [uvector\\_5\\_mem](#)  
*Allocation object for 5 arrays of equal size.*

## Functions

- void [create\\_givens](#) (const double a, const double b, double &c, double &s)  
*Desc.*
- template<class mat1\_t, class mat2\_t >  
void [apply\\_givens\\_qr](#) (size\_t M, size\_t N, mat1\_t &Q, mat2\_t &R, size\_t i, size\_t j, double c, double s)  
*Apply a rotation to matrices from the QR decomposition.*
- template<class mat1\_t, class mat2\_t >  
void [apply\\_givens\\_lq](#) (size\_t M, size\_t N, mat1\_t &Q, mat2\_t &L, size\_t i, size\_t j, double c, double s)  
*Apply a rotation to matrices from the LQ decomposition.*
- template<class vec\_t >  
void [apply\\_givens\\_vec](#) (vec\_t &v, size\_t i, size\_t j, double c, double s)  
*Apply a rotation to a vector;  $v \rightarrow G^T v$ .*
- template<class mat\_t, class vec\_t, class vec2\_t >  
int [HH\\_solve](#) (size\_t n, mat\_t &A, const vec\_t &b, vec2\_t &x)  
*Solve linear system after Householder decomposition.*
- template<class mat\_t, class vec\_t >  
int [HH\\_svx](#) (size\_t N, size\_t M, mat\_t &A, vec\_t &x)  
*Solve a linear system after Householder decomposition in place.*
- template<class vec\_t >  
double [householder\\_transform](#) (const size\_t n, vec\_t &v)  
*Replace the vector  $v$  with a Householder vector and a coefficient tau that annihilates  $v[1]$  through  $v[n-1]$  (inclusive)*
- template<class mat\_t >  
double [householder\\_transform\\_subcol](#) (mat\_t &A, const size\_t ir, const size\_t ic, const size\_t M)  
*Compute the Householder transform of a vector formed with  $n$  rows of a column of a matrix.*
- template<class mat\_t >  
double [householder\\_transform\\_subrow](#) (mat\_t &A, const size\_t ir, const size\_t ic, const size\_t N)  
*Compute the Householder transform of a vector formed with the last  $n$  columns of a row of a matrix.*
- template<class vec\_t, class mat\_t >  
void [householder\\_hm](#) (const size\_t M, const size\_t N, double tau, const vec\_t &v, mat\_t &A)  
*Apply a Householder transformation  $(v, \tau)$  to matrix A of size M by N.*
- template<class mat\_t >  
void [householder\\_hm\\_sub](#) (mat\_t &M, const size\_t ir, const size\_t ic, const size\_t nr, const size\_t nc, const mat\_t &M2, const size\_t ir2, const size\_t ic2, double tau)  
*Apply a Householder transformation to submatrix of a larger matrix.*
- template<class mat1\_t, class mat2\_t >  
void [householder\\_hm\\_sub2](#) (const size\_t M, const size\_t ic, double tau, const mat1\_t &mv, mat2\_t &A)  
*Special version of Householder transformation for [QR\\_unpack\(\)](#)*
- template<class vec\_t, class vec2\_t >  
void [householder\\_hv](#) (const size\_t N, double tau, const vec\_t &v, vec2\_t &w)  
*Apply a Householder transformation  $v$  to vector  $w$ .*

- template<class mat\_t, class vec\_t >  
void [householder\\_hv\\_subcol](#) (const mat\_t &A, vec\_t &w, double tau, const size\_t ie, const size\_t N)  
*Apply a Householder transformation  $v$  to vector  $w$  where  $v$  is stored as a column in a matrix  $A$ .*
- template<class mat\_t >  
void [householder\\_hm1](#) (const size\_t M, const size\_t N, double tau, mat\_t &A)  
*Apply a Householder transformation  $(v, \tau)$  to a matrix being build up from the identity matrix, using the first column of  $A$  as a - Householder vector.*
- template<class vec\_t, class mat\_t >  
void [householder\\_mh](#) (const size\_t M, const size\_t N, double tau, const vec\_t &v, mat\_t &A)  
*Apply the Householder transformation  $(v, \tau au)$  to the right-hand side of the matrix  $A$ .*
- template<class mat\_t, class mat2\_t >  
void [householder\\_mh\\_sub](#) (mat\_t &M, const size\_t ir, const size\_t ic, const size\_t nr, const size\_t nc, const mat2\_t &M2, const size\_t ir2, const size\_t ic2, double tau)  
*Apply the Householder transformation  $(v, \tau au)$  to the right-hand side of the matrix  $A$ .*
- template<size\_t N>  
int [LU\\_decomp\\_array\\_2d](#) (const size\_t n, double A[ ][N], o2scl::permutation &p, int &signum)  
*Specialized version of LU\_decomp for C-style 2D arrays.*
- template<class mat\_t >  
int [diagonal\\_has\\_zero](#) (const size\_t N, mat\_t &A)  
*Return 1 if at least one of the elements in the diagonal is zero.*
- template<class mat\_t >  
int [LU\\_decomp](#) (const size\_t N, mat\_t &A, o2scl::permutation &p, int &signum)  
*Compute the LU decomposition of the matrix  $A$ .*
- template<class mat\_t, class mat\_row\_t >  
int [LU\\_decomp\\_alt](#) (const size\_t N, mat\_t &A, o2scl::permutation &p, int &signum)
- template<class mat\_t, class vec\_t, class vec2\_t >  
int [LU\\_solve](#) (const size\_t N, const mat\_t &LU, const o2scl::permutation &p, const vec\_t &b, vec2\_t &x)  
*Solve a linear system after LU decomposition.*
- template<class mat\_t, class vec\_t >  
int [LU\\_svx](#) (const size\_t N, const mat\_t &LU, const o2scl::permutation &p, vec\_t &x)  
*Solve a linear system after LU decomposition in place.*
- template<class mat\_t, class mat2\_t, class vec\_t, class vec2\_t, class vec3\_t >  
int [LU\\_refine](#) (const size\_t N, const mat\_t &A, const mat2\_t &LU, const o2scl::permutation &p, const vec\_t &b, vec2\_t &x, vec3\_t &residual)  
*Refine the solution of a linear system.*
- template<class mat\_t, class mat2\_t, class mat\_col\_t >  
int [LU\\_invert](#) (const size\_t N, const mat\_t &LU, const o2scl::permutation &p, mat2\_t &inverse)  
*Compute the inverse of a matrix from its LU decomposition.*
- template<class mat\_t >  
double [LU\\_det](#) (const size\_t N, const mat\_t &LU, int signum)  
*Compute the determinant of a matrix from its LU decomposition.*
- template<class mat\_t >  
double [LU\\_lndet](#) (const size\_t N, const mat\_t &LU)  
*Compute the logarithm of the absolute value of the determinant of a matrix from its LU decomposition.*
- template<class mat\_t >  
int [LU\\_sgndet](#) (const size\_t N, const mat\_t &LU, int signum)  
*Compute the sign of the determinant of a matrix from its LU decomposition.*
- template<class mat\_t, class vec\_t >  
void [QR\\_decomp](#) (size\_t M, size\_t N, mat\_t &A, vec\_t &tau)  
*Compute the QR decomposition of matrix  $A$ .*
- template<class mat\_t, class vec\_t, class vec2\_t, class vec3\_t >  
void [QR\\_solve](#) (size\_t N, const mat\_t &QR, const vec\_t &tau, const vec2\_t &b, vec3\_t &x)  
*Solve the system  $Ax = b$  using the QR factorization.*
- template<class mat\_t, class vec\_t, class vec2\_t >  
void [QR\\_svx](#) (size\_t M, size\_t N, const mat\_t &QR, const vec\_t &tau, vec2\_t &x)  
*Solve the system  $Ax = b$  in place using the QR factorization.*
- template<class mat\_t, class vec\_t, class vec2\_t >  
void [QR\\_QTvec](#) (const size\_t M, const size\_t N, const mat\_t &QR, const vec\_t &tau, vec2\_t &v)  
*Form the product  $Q^T v$  from a QR factorized matrix.*

- template<class mat1\_t, class mat2\_t, class mat3\_t, class vec\_t >  
void [QR\\_unpack](#) (const size\_t M, const size\_t N, const mat1\_t &QR, const vec\_t &tau, mat2\_t &Q, mat3\_t &R)  
*Unpack the QR matrix to the individual Q and R components.*
- template<class mat1\_t, class mat2\_t, class vec1\_t, class vec2\_t >  
void [QR\\_update](#) (size\_t M, size\_t N, mat1\_t &Q, mat2\_t &R, vec1\_t &w, vec2\_t &v)  
*Update a QR factorisation for  $A = QR$ ,  $A' = A + u v^T$ .*
- template<class vec\_t, class vec2\_t >  
int [chop\\_small\\_elements](#) (size\_t N, vec\_t &d, vec2\_t &f)  
*Desc.*
- template<class vec\_t, class vec2\_t >  
double [trailing\\_eigenvalue](#) (size\_t n, const vec\_t &d, const vec\_t &f)  
*Desc.*
- int [create\\_schur](#) (double d0, double f0, double d1, double &c, double &s)  
*Desc.*
- template<class vec\_t, class vec2\_t, class mat\_t, class mat2\_t >  
int [svd2](#) (size\_t M, size\_t N, vec\_t &d, vec2\_t &f, mat\_t &U, mat2\_t &V)  
*Desc.*
- template<class vec\_t, class vec2\_t, class mat\_t >  
int [chase\\_out\\_intermediate\\_zero](#) (size\_t M, size\_t n, vec\_t &d, vec2\_t &f, mat\_t &U, size\_t k0)  
*Desc.*
- template<class vec\_t, class vec2\_t, class mat\_t >  
int [chase\\_out\\_trailing\\_zero](#) (size\_t N, size\_t n, vec\_t &d, vec2\_t &f, mat\_t &V)  
*Desc.*
- template<class vec\_t, class vec2\_t, class mat\_t, class mat2\_t >  
int [qrstep](#) (size\_t M, size\_t N, size\_t n, vec\_t &d, vec2\_t &f, mat\_t &U, mat2\_t &V)  
*Desc.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class mem\_t, class mem\_vec\_t >  
void [solve\\_tridiag\\_sym](#) (const vec\_t &diag, const vec2\_t &offdiag, const vec3\_t &b, vec4\_t &x, size\_t N, mem\_t &m)  
*Solve a symmetric tridiagonal linear system with user-specified memory.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class vec5\_t, class mem\_t, class mem\_vec\_t >  
void [solve\\_tridiag\\_nonsym](#) (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N, mem\_t &m)  
*Solve an asymmetric tridiagonal linear system with user-specified memory.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class mem\_t, class mem\_vec\_t >  
void [solve\\_cyc\\_tridiag\\_sym](#) (const vec\_t &diag, const vec2\_t &offdiag, const vec3\_t &b, vec4\_t &x, size\_t N, mem\_t &m)  
*Solve a symmetric cyclic tridiagonal linear system with user specified memory.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class vec5\_t, class mem\_t, class mem\_vec\_t >  
void [solve\\_cyc\\_tridiag\\_nonsym](#) (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N, mem\_t &m)  
*Solve an asymmetric cyclic tridiagonal linear system with user-specified memory.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t >  
void [solve\\_tridiag\\_sym](#) (const vec\_t &diag, const vec2\_t &offdiag, const vec3\_t &b, vec4\_t &x, size\_t N)  
*Solve a symmetric tridiagonal linear system.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class vec5\_t >  
void [solve\\_tridiag\\_nonsym](#) (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N)  
*Solve an asymmetric tridiagonal linear system.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t >  
void [solve\\_cyc\\_tridiag\\_sym](#) (const vec\_t &diag, const vec2\_t &offdiag, const vec3\_t &b, vec4\_t &x, size\_t N)  
*Solve a symmetric cyclic tridiagonal linear system.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class vec5\_t >  
void [solve\\_cyc\\_tridiag\\_nonsym](#) (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N)  
*Solve an asymmetric cyclic tridiagonal linear system.*

45.14.2.1 `template<class mat1_t, class mat2_t > void o2scl_linalg::apply_givens_qr ( size_t M, size_t N, mat1_t & Q, mat2_t & R, size_t i, size_t j, double c, double s )`

This performs  $Q \rightarrow QG$  and  $R \rightarrow G^T R$ .

Definition at line 58 of file `givens_base.h`.

45.14.2.2 `template<class mat1_t, class mat2_t > void o2scl_linalg::apply_givens_lq ( size_t M, size_t N, mat1_t & Q, mat2_t & L, size_t i, size_t j, double c, double s )`

This performs  $Q \rightarrow QG$  and  $L \rightarrow LG^T$ .

Definition at line 83 of file `givens_base.h`.

45.14.2.3 `template<class mat_t, class vec_t > int o2scl_linalg::HH_svx ( size_t N, size_t M, mat_t & A, vec_t & x )`

**Idea for Future** Handle memory allocation like the tridiagonal functions.

Definition at line 68 of file `hh_base.h`.

45.14.2.4 `template<class vec_t > double o2scl_linalg::householder_transform ( const size_t n, vec_t & v )`

On exit, this function returns the value of  $\tau = 2/(v^T v)$ . If  $n$  is less than or equal to 1 then this function returns zero without calling the error handler.

Definition at line 69 of file `householder_base.h`.

45.14.2.5 `template<class mat_t > double o2scl_linalg::householder_transform_subcol ( mat_t & A, const size_t ir, const size_t ic, const size_t M )`

This performs a Householder transform of a vector defined by a column of a matrix A which starts at element `A[ir][ic]` and ends at element `A[N-1][ic]`.

Used in [QR\\_decomp\(\)](#).

Definition at line 114 of file `householder_base.h`.

45.14.2.6 `template<class mat_t > double o2scl_linalg::householder_transform_subrow ( mat_t & A, const size_t ir, const size_t ic, const size_t N )`

This performs a Householder transform of a vector defined by a row of a matrix A which starts at element `A[ir][ic]` and ends at element `A[ir][N-1]`.

Definition at line 156 of file `householder_base.h`.

45.14.2.7 `template<class mat_t > void o2scl_linalg::householder_hm_sub ( mat_t & M, const size_t ir, const size_t ic, const size_t nr, const size_t nc, const mat_t & M2, const size_t ir2, const size_t ic2, double tau )`

This applies a householder transformation  $(v, \tau)$  to submatrix of M. The submatrix has `nr` rows and `nc` columns and starts at row `ir` of column `ic` of the original matrix M. The vector  $v$  is taken from a column of M2 starting at row `ir2` and column `ic2`.

This function is used in [QR\\_decomp\(\)](#).

Definition at line 237 of file `householder_base.h`.

45.14.2.8 `template<class mat_t, class vec_t > void o2scl_linalg::householder_hv_subcol ( const mat_t & A, vec_t & w, double tau, const size_t ie, const size_t N )`

Used in [QR\\_QTvec\(\)](#).

Definition at line 337 of file `householder_base.h`.

45.14.2.9 `template<class mat_t, class mat2_t> void o2scl_linalg::householder_mh_sub ( mat_t & M, const size_t ir, const size_t ic, const size_t nr, const size_t nc, const mat2_t & M2, const size_t ir2, const size_t ic2, double tau )`

This is unfinished but needed for the bidiagonalization functions.

Definition at line 446 of file `householder_base.h`.

45.14.2.10 `template<size_t N> int o2scl_linalg::LU_decomp_array_2d ( const size_t n, double A[][N], o2scl::permutation & p, int & signum )`

#### Note

Note that N and n must be equal, by no checking is done to ensure that this is the case

Definition at line 42 of file `lu.h`.

45.14.2.11 `template<class mat_t> int o2scl_linalg::LU_decomp ( const size_t N, mat_t & A, o2scl::permutation & p, int & signum )`

On output the diagonal and upper triangular part of the input matrix A contain the matrix U. The lower triangular part of the input matrix (excluding the diagonal) contains L. The diagonal elements of L are unity, and are not stored.

The permutation matrix P is encoded in the permutation p. The j-th column of the matrix P is given by the k-th column of the identity matrix, where  $k = p_j$  the j-th element of the permutation vector. The sign of the permutation is given by signum. It has the value  $(-1)^n$ , where n is the number of interchanges in the permutation.

The algorithm used in the decomposition is Gaussian Elimination with partial pivoting (Golub & Van Loan, Matrix Computations, Algorithm 3.4.1).

**Idea for Future** The "swap rows j and i\_pivot" section could probably be made more efficient using a "matrix\_row"-like object as done in GSL. (7/16/09 - I've tried this, and it doesn't seem to improve the speed significantly.)

Definition at line 86 of file `lu_base.h`.

45.14.2.12 `template<class mat_t, class vec_t, class vec2_t> int o2scl_linalg::LU_solve ( const size_t N, const mat_t & LU, const o2scl::permutation & p, const vec_t & b, vec2_t & x )`

This function solve the square system  $Ax = b$  using the LU decomposition of A into (LU, p) given by `gsl_linalg_LU_decomp` or `gsl_linalg_complex_LU_decomp`.

Definition at line 207 of file `lu_base.h`.

45.14.2.13 `template<class mat_t, class vec_t> int o2scl_linalg::LU_svx ( const size_t N, const mat_t & LU, const o2scl::permutation & p, vec_t & x )`

These functions solve the square system  $Ax = b$  in-place using the LU decomposition of A into (LU,p). On input x should contain the right-hand side b, which is replaced by the solution on output.

Definition at line 230 of file `lu_base.h`.

45.14.2.14 `template<class mat_t, class mat2_t, class vec_t, class vec2_t, class vec3_t> int o2scl_linalg::LU_refine ( const size_t N, const mat_t & A, const mat2_t & LU, const o2scl::permutation & p, const vec_t & b, vec2_t & x, vec3_t & residual )`

These functions apply an iterative improvement to x, the solution of  $Ax = b$ , using the LU decomposition of A into (LU,p). The initial residual  $r = Ax - b$  is also computed and stored in residual.

Definition at line 262 of file `lu_base.h`.

45.14.2.15 `template<class mat_t, class mat2_t, class mat_col_t> int o2scl_linalg::LU_invert ( const size_t N, const mat_t & LU, const o2scl::permutation & p, mat2_t & inverse )`

These functions compute the inverse of a matrix A from its LU decomposition (LU,p), storing the result in the matrix inverse. The inverse is computed by solving the system  $Ax = b$  for each column of the identity matrix. It is preferable to avoid direct use of the inverse whenever possible, as the linear solver functions can obtain the same result more efficiently and reliably.



**Idea for Future** Could rewrite to avoid `mat_col_t`, (9/16/09 - However, the function may be faster if `mat_col_t` is left in, so it's unclear what's best.)

Definition at line 300 of file `lu_base.h`.

**45.14.2.16** `template<class mat_t> double o2scl_linalg::LU_det ( const size_t N, const mat_t & LU, int signum )`

Compute the determinant of a matrix  $A$  from its LU decomposition,  $LU$ . The determinant is computed as the product of the diagonal elements of  $U$  and the sign of the row permutation `signum`.

Definition at line 339 of file `lu_base.h`.

**45.14.2.17** `template<class mat_t> double o2scl_linalg::LU_lndet ( const size_t N, const mat_t & LU )`

Compute the logarithm of the absolute value of the determinant of a matrix  $A$ ,  $\ln|\det(A)|$ , from its LU decomposition,  $LU$ . This function may be useful if the direct computation of the determinant would overflow or underflow.

Definition at line 361 of file `lu_base.h`.

**45.14.2.18** `template<class mat_t> int o2scl_linalg::LU_sgndet ( const size_t N, const mat_t & LU, int signum )`

Compute the sign or phase factor of the determinant of a matrix  $A$ ,  $\det(A)/|\det(A)|$ , from its LU decomposition,  $LU$ .

Definition at line 380 of file `lu_base.h`.

**45.14.2.19** `template<class mat1_t, class mat2_t, class vec1_t, class vec2_t> void o2scl_linalg::QR_update ( size_t M, size_t N, mat1_t & Q, mat2_t & R, vec1_t & w, vec2_t & v )`

The parameters  $M$  and  $N$  are the number of rows and columns of the matrix  $R$ .

```
* Q' R' = QR + u v^T
*       = Q (R + Q^T u v^T)
*       = Q (R + w v^T)
*
* where w = Q^T u.
*
* Algorithm from Golub and Van Loan, "Matrix Computations", Section
* 12.5 (Updating Matrix Factorizations, Rank-One Changes)
```

Definition at line 161 of file `qr_base.h`.

**45.14.2.20** `template<class vec_t, class vec2_t> int o2scl_linalg::chop_small_elements ( size_t N, vec_t & d, vec2_t & f )`

The parameter  $N$  is the size of  $d$ .

Definition at line 55 of file `svdstep_base.h`.

**45.14.2.21** `template<class vec_t, class vec2_t> double o2scl_linalg::trailing_eigenvalue ( size_t n, const vec_t & d, const vec_t & f )`

The parameter  $n$  is the size of the vector  $d$ .

Should be finished.

Definition at line 82 of file `svdstep_base.h`.

**45.14.2.22** `int o2scl_linalg::create_schur ( double d0, double f0, double d1, double & c, double & s )`

Should be finished.

Definition at line 117 of file `svdstep_base.h`.

45.14.2.23 `template<class vec_t, class vec2_t, class mat_t, class mat2_t> int o2scl_linalg::svd2 ( size_t M, size_t N, vec_t & d, vec2_t & f, mat_t & U, mat2_t & V )`

The parameter M is the number of rows in U and N is the number of rows in V.

Definition at line 169 of file svdstep\_base.h.

45.14.2.24 `template<class vec_t, class vec2_t, class mat_t> int o2scl_linalg::chase_out_intermediate_zero ( size_t M, size_t n, vec_t & d, vec2_t & f, mat_t & U, size_t k0 )`

Should be finished.

Definition at line 305 of file svdstep\_base.h.

45.14.2.25 `template<class vec_t, class vec2_t, class mat_t> int o2scl_linalg::chase_out_trailing_zero ( size_t N, size_t n, vec_t & d, vec2_t & f, mat_t & V )`

Should be finished.

Definition at line 352 of file svdstep\_base.h.

45.14.2.26 `template<class vec_t, class vec2_t, class mat_t, class mat2_t> int o2scl_linalg::qrstep ( size_t M, size_t N, size_t n, vec_t & d, vec2_t & f, mat_t & U, mat2_t & V )`

Should be finished.

The parameter M is the number of rows in U, N is the number of rows in V, and n is the length of the vector d.

Definition at line 402 of file svdstep\_base.h.

45.14.2.27 `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class mem_t, class mem_vec_t> void o2scl_linalg::solve_tridiag_sym ( const vec_t & diag, const vec2_t & offdiag, const vec3_t & b, vec4_t & x, size_t N, mem_t & m )`

This function solves the system  $Ax = b$  where A is a matrix of the form

```
*
*      diag[0]  offdiag[0]          0      .....
*  offdiag[0]      diag[1]  offdiag[1]  .....
*          0  offdiag[1]      diag[2]
*          0          0  offdiag[2]  .....
```

given the N diagonal elements in diag, N-1 diagonal elements in offdiag, and the N elements b from the RHS.

See [EngelnMullges96](#).

Definition at line 208 of file tridiag\_base.h.

45.14.2.28 `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class vec5_t, class mem_t, class mem_vec_t> void o2scl_linalg::solve_tridiag_nonsym ( const vec_t & diag, const vec2_t & abovediag, const vec3_t & belowdiag, const vec4_t & rhs, vec5_t & x, size_t N, mem_t & m )`

This function solves the system  $Ax = b$  where A is a matrix of the form

```
*
*      diag[0]  abovediag[0]          0      .....
*  belowdiag[0]      diag[1]  abovediag[1]  .....
*          0  belowdiag[1]      diag[2]
*          0          0  belowdiag[2]  .....
```

This function uses plain Gauss elimination, not bothering with the zeroes.

**Idea for Future** Offer an option to avoid throwing on divide by zero?

Definition at line 273 of file tridiag\_base.h.

**45.14.2.29** `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class mem_t, class mem_vec_t > void  
o2scl_linalg::solve_cyc_tridiag_sym ( const vec_t & diag, const vec2_t & offdiag, const vec3_t & b, vec4_t & x, size_t N, mem_t & m )`

This function solves the system  $Ax = b$  where  $A$  is a matrix of the form

```
*
*      diag[0]  offdiag[0]          0  .....  offdiag[N-1]
*  offdiag[0]      diag[1]  offdiag[1]  .....
*      0  offdiag[1]      diag[2]
*      0      0  offdiag[2]  .....
*      ...      ...
* offdiag[N-1]      ...
```

See [EngelnMullges96](#) .

Definition at line 331 of file tridiag\_base.h.

**45.14.2.30** `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class vec5_t, class mem_t, class mem_vec_t > void  
o2scl_linalg::solve_cyc_tridiag_nonsym ( const vec_t & diag, const vec2_t & abovediag, const vec3_t & belowdiag, const vec4_t & rhs,  
vec5_t & x, size_t N, mem_t & m )`

This function solves the system  $Ax = b$  where  $A$  is a matrix of the form

```
*
*      diag[0]  abovediag[0]          0  .....  belowdiag[N-1]
*  belowdiag[0]      diag[1]  abovediag[1]  .....
*      0  belowdiag[1]      diag[2]
*      0      0  belowdiag[2]  .....
*      ...      ...
* abovediag[N-1]      ...
```

This function solves the following system without the corner elements and then use Sherman-Morrison formula to compensate for them.

**Idea for Future** Offer an option to avoid throwing on divide by zero?

Definition at line 427 of file tridiag\_base.h.

## 45.15 o2scl\_linalg\_paren Namespace Reference

The namespace for linear algebra classes and functions with operator()

### 45.15.1 Detailed Description

This namespace contains an identical copy of all the functions given in the [o2scl\\_cblas](#) namespace, but perform array indexing with `operator()` rather than `operator[]`. See [o2scl\\_linalg](#) for the function listing and documentation.

This namespace documentation is in the file [src/base/lib\\_settings.h](#)

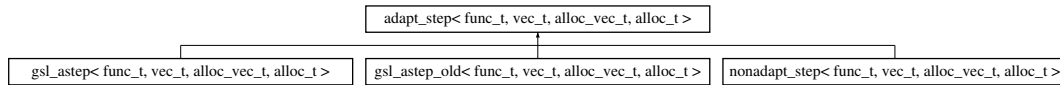
## 46 Data Structure Documentation

### 46.1 adapt\_step< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Adaptive stepper [abstract base].

```
#include <adapt_step.h>
```

Inheritance diagram for adapt\_step< func\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



#### 46.1.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>class adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >
```

The adaptive stepper routines are based on one or many applications of ordinary ODE steppers (implemented in [ode\\_step](#)). Each adaptive stepper ([gsl\\_astep](#) or [nonadapt\\_step](#)) can be used with any of the ODE stepper classes (e.g. [gsl\\_rkck](#)). By default, [gsl\\_rkck](#) is used. To modify the ODE stepper which is used, use the member function [set\\_step\(\)](#) documented below.

##### Note

If you use [gsl\\_rkck\\_fast](#) or [gsl\\_rk8pd\\_fast](#), you'll need to make sure that the argument `n` to [astep\(\)](#) or [astep\\_derivs\(\)](#) below matches the template size parameter given in the ODE stepper.

Definition at line 51 of file `adapt_step.h`.

##### Public Member Functions

- virtual int [astep](#) (double &x, double xlimit, double &h, size\_t n, vec\_t &y, vec\_t &dydx\_out, vec\_t &yerr, func\_t &derivs)=0  
*Make an adaptive integration step of the system `derivs`.*
- virtual int [astep\\_derivs](#) (double &x, double xlimit, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yerr, func\_t &derivs)=0  
*Make an adaptive integration step of the system `derivs` with derivatives.*
- virtual int [astep\\_full](#) (double x, double xlimit, double &x\_out, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)=0  
*Make an adaptive integration step of the system `derivs` with derivatives.*
- int [set\\_step](#) (ode\_step< func\_t, vec\_t > &step)  
*Set stepper.*

##### Data Fields

- int [verbose](#)  
*Set output level.*
- [gsl\\_rkck](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > [def\\_step](#)  
*The default stepper.*

##### Protected Attributes

- [ode\\_step](#)< func\_t, vec\_t > \* [stepp](#)  
*Pointer to the stepper being used.*

#### 46.1.2 Member Function Documentation

```
46.1.2.1 template<class func_t = ode.func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::astep ( double & x, double xlimit, double & h, size_t n, vec_t & y, vec_t & dydx_out,
vec_t & yerr, func_t & derivs ) [pure virtual]
```

This attempts to take a step of size  $h$  from the point  $x$  of an  $n$ -dimensional system `derivs` starting with  $y$ . On exit,  $x$  and  $y$  contain the new values at the end of the step,  $h$  contains the size of the step, `dydx_out` contains the derivative at the end of the step, and `yerr` contains the estimated error at the end of the step.

Implemented in `gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >`, `gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >`, and `nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >`.

```
46.1.2.2 template<class func_t = ode.func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::astep_derivs ( double & x, double xlimit, double & h, size_t n, vec_t & y, vec_t & dydx,
vec_t & yerr, func_t & derivs ) [pure virtual]
```

This attempts to take a step of size  $h$  from the point  $x$  of an  $n$ -dimensional system `derivs` starting with  $y$  and given the initial derivatives `dydx`. On exit,  $x$ ,  $y$  and `dydx` contain the new values at the end of the step,  $h$  contains the size of the step, `dydx` contains the derivative at the end of the step, and `yerr` contains the estimated error at the end of the step.

Implemented in `gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >`, `gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >`, and `nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >`.

```
46.1.2.3 template<class func_t = ode.func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::astep_full ( double x, double xlimit, double & x_out, double & h, size_t n, vec_t & y,
vec_t & dydx, vec_t & yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [pure virtual]
```

This function performs an adaptive integration step with the  $n$ -dimensional system `derivs` and parameter `pa`. It Begins at  $x$  with initial stepsize  $h$ , ensuring that the step goes no farther than `xlimit`. At the end of the step, the size of the step taken is  $h$  and the new value of  $x$  is in `x_out`. Initially, the function values and derivatives should be specified in  $y$  and `dydx`. The function values, derivatives, and the error at the end of the step are given in `yout`, `yerr`, and `dydx_out`. Unlike in `ode_step` objects, the objects `y`, `yout`, `dydx`, and `dydx_out` must all be distinct.

Implemented in `gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >`, `gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >`, and `nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >`.

```
46.1.2.4 template<class func_t = ode.func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int
adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::set_step ( ode_step< func_t, vec_t > & step ) [inline]
```

This sets the stepper for use in the adaptive step routine. If no stepper is specified, then the default (`def_step` of type `gsl_rkck`) is used.

Definition at line 120 of file `adapt_step.h`.

The documentation for this class was generated from the following file:

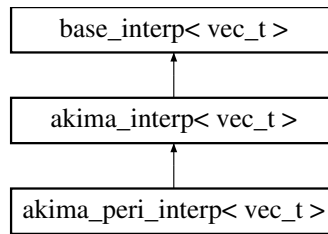
- `adapt_step.h`

## 46.2 akima\_interp< vec\_t > Class Template Reference

Akima spline interpolation (GSL)

```
#include <interp.h>
```

Inheritance diagram for `akima_interp< vec_t >`:



### 46.2.1 Detailed Description

```
template<class vec_t>class akima_interp< vec_t >
```

This class uses natural boundary conditions, where the second derivative vanishes at each end point. Extrapolation effectively assumes that the second derivative is linear outside of the endpoints. Use [akima\\_peri\\_interp](#) for perodic boundary conditions.

Definition at line 765 of file interp.h.

#### Public Member Functions

- [akima\\_interp](#) ()  
*Create a base interpolation object with or without periodic boundary conditions.*
- virtual int [allocate](#) (size\_t size)  
*Allocate memory, assuming x and y have size size.*
- virtual int [init](#) (const vec\_t &xa, const vec\_t &ya, size\_t size)  
*Initialize interpolation routine.*
- virtual int [free](#) ()  
*Free allocated memory.*
- virtual int [interp](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double x, double &y)  
*Give the value of the function  $y(x = x_0)$ .*
- virtual int [deriv](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double x, double &dydx)  
*Give the value of the derivative  $y'(x = x_0)$ .*
- virtual int [deriv2](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double x, double &d2ydx2)  
*Give the value of the second derivative  $y''(x = x_0)$ .*
- virtual int [integ](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double aa, double bb, double &result)  
*Give the value of the integral  $\int_a^b y(x) dx$ .*
- virtual const char \* [type](#) ()  
*Return the type, "akima\_interp".*

#### Protected Member Functions

- void [akima\\_calc](#) (const vec\_t &x\_array, size\_t size, double m[])  
*For initializing the interpolation.*

#### Protected Attributes

##### Storage for Akima spline interpolation

- double \* **b**
- double \* **c**
- double \* **d**
- double \* **um**

#### Private Member Functions

- [akima\\_interp](#) (const [akima\\_interp](#)< vec\_t > &)
- [akima\\_interp](#)< vec\_t > & **operator=** (const [akima\\_interp](#)< vec\_t > &)

## 46.2.2 Member Function Documentation

46.2.2.1 `template<class vec_t> virtual int akima_interp< vec_t >::init ( const vec_t & xa, const vec_t & ya, size_t size )` [inline, virtual]

Non-periodic boundary conditions

Reimplemented from [base\\_interp< vec\\_t >](#).

Reimplemented in [akima\\_peri\\_interp< vec\\_t >](#).

Definition at line 862 of file interp.h.

The documentation for this class was generated from the following file:

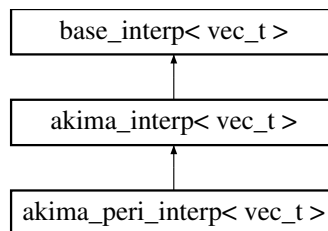
- interp.h

## 46.3 akima\_peri\_interp&lt; vec\_t &gt; Class Template Reference

Akima spline interpolation with periodic boundary conditions (GSL)

```
#include <interp.h>
```

Inheritance diagram for `akima_peri_interp< vec_t >`:



## 46.3.1 Detailed Description

```
template<class vec_t> class akima_peri_interp< vec_t >
```

Definition at line 1025 of file interp.h.

## Public Member Functions

- virtual const char \* [type](#) ()  
*Return the type, "akima\_peri\_interp".*
- virtual int [init](#) (const vec\_t &xa, const vec\_t &ya, size\_t size)  
*Initialize interpolation routine.*

## Private Member Functions

- [akima\\_peri\\_interp](#) (const [akima\\_peri\\_interp](#)< vec\_t > &)
- [akima\\_peri\\_interp](#)< vec\_t > & [operator=](#) (const [akima\\_peri\\_interp](#)< vec\_t > &)

## 46.3.2 Member Function Documentation

46.3.2.1 `template<class vec_t> virtual int akima_peri_interp< vec_t >::init ( const vec_t & xa, const vec_t & ya, size_t size )` [inline, virtual]

Periodic boundary conditions

Reimplemented from [akima\\_interp< vec\\_t >](#).

Definition at line 1039 of file `interp.h`.

The documentation for this class was generated from the following file:

- `interp.h`

## 46.4 `anneal_mt< param_t, param_vec_t, func_t, vec_t, alloc_vec_t, alloc_t, rng_t >` Class Template Reference

Multidimensional minimization by simulated annealing (Boost multi-threaded version)

```
#include <anneal_mt.h>
```

### 46.4.1 Detailed Description

```
template<class param_t, class param_vec_t = std::vector<param_t>, class func_t = multi_func_t<param_t>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class rng_t = gsl_rng> class anneal_mt< param_t, param_vec_t, func_t, vec_t, alloc_vec_t, alloc_t, rng_t >
```

This header-only class additionally requires the Boost libraries. It performs simulated annealing using an arbitrary number of processors using `boost::thread`, which is closely related to the standard Unix `pthread` library. It works very similarly to [gsl\\_anneal](#), it performs `ntrial` evaluations over each processor, then applying the metropolis algorithm to the results from all of the processors at the end.

Because `np` function calls are happening simultaneously, where `np` is the number of processors, `np` copies of the function parameters of type `param_t` must also be specified. The user-defined function to minimize must also be thread-safe, allowing multiple threads to call the function at once (albeit given different parameters). The default type for these `np` copies of the parameters of type `param_t` is `std::vector<param_t>`.

This works particularly well for functions which are not trivial to evaluate, i.e. functions where the execution time is more longer than the bookkeeping that [anneal\\_mt](#) performs between trials. For functions which satisfy this requirement, this algorithm scales nearly linearly with the number of processors.

Verbose I/O for this class happens only outside the theads unless the user places I/O in the streams in the function that is specified.

**Idea for Future** There may be a good way to remove the function indirection here to make this class a bit faster.

Definition at line 75 of file `anneal_mt.h`.

### Public Member Functions

- `virtual const char * type ()`  
*Return string denoting type ("anneal\_mt")*
- `int set_verbose_stream (std::ostream &out, std::istream &in)`  
*Set streams for verbose I/O.*
- `virtual int print_iter (size_t nv, vec_t &xx, double y, int iter, double tptr, std::string comment)`  
*Print out iteration information.*
- `template<class vec2_t>`  
`int set_step (size_t nv, vec2_t &stepv)`  
*Set the step sizes.*



## Basic usage

- virtual int **mmin** (size\_t nv, vec\_t &x0, double &fmin, func\_t &func, size\_t np, param\_vec\_t &pars)  
*Calculate the minimum  $f_{min}$  of  $func$  w.r.t the array  $x0$  of size  $nv$  using  $np$  threads.*

## Iteration control

- virtual int **next** (size\_t nv, vec\_t &x\_old, double min\_old, vec\_t &x\_new, double min\_new, double &T, size\_t n\_moves, bool &finished)  
*Determine how to change the minimization for the next iteration.*
- virtual int **start** (size\_t nv, double &T)  
*Setup initial temperature and stepsize.*

## Data Fields

- rng\_t **def\_rng**  
*The default random number generator.*

## Parameters

- double **boltz**  
*Boltzmann factor (default 1.0).*
- int **ntrial**  
*Number of iterations.*
- int **verbose**  
*Output control.*
- bool **out\_step\_changes**  
*Output step size changes (default false)*
- bool **out\_best**  
*Output best point (default false)*
- double **tolx**  
*The independent variable tolerance (default  $10^{-6}$ )*
- double **T\_start**  
*Initial temperature (default 1.0)*
- double **T\_dec**  
*Factor to decrease temperature by (default 1.5)*
- double **step\_dec**  
*Factor to decrease step size by (default 1.5)*
- double **min\_step\_ratio**  
*Ratio between minimum step size and **tolx** (default 100.0)*

## Protected Member Functions

- void **func\_wrapper** (size\_t ip)  
*The function wrapper executed by thread with index  $ip$ .*
- virtual int **allocate** (size\_t nv, size\_t np)  
*Allocate memory for a minimizer over  $n$  dimensions with stepsize  $step$ .*
- virtual int **free** (size\_t np)  
*Free allocated memory.*
- virtual int **step** (size\_t nv, vec\_t &sx)  
*Make a step to a new attempted minimum.*

## Protected Attributes

- std::ostream \* **outs**  
*Stream for verbose output.*
- std::istream \* **ins**  
*Stream for verbose input.*
- size\_t **nproc**  
*The number of threads to run.*

- param\_vec\_t \* [params](#)  
*The user-specified parameters.*
- size\_t [nvar](#)  
*The number of variables over which we minimize.*
- func\_t \* [f](#)  
*The function to minimize.*
- alloc\_t [ao](#)  
*Allocation object.*
- [ovector](#) [step\\_vec](#)  
*Vector of step sizes.*

#### Storage for present, next, and best vectors

- alloc\_vec\_t [x](#)
- alloc\_vec\_t \* [new\\_x](#)
- alloc\_vec\_t [best\\_x](#)
- alloc\_vec\_t [new\\_E](#)
- alloc\_vec\_t [old\\_x](#)

#### 46.4.2 Member Function Documentation

46.4.2.1 `template<class param_t, class param_vec_t = std::vector<param_t>, class func_t = multi_func_t<param_t>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class rng_t = gsl_rng> virtual int anneal_mt< param_t, param_vec_t, func_t, vec_t, alloc_vec_t, alloc_t, rng_t >::print_iter ( size_t nv, vec_t & xx, double y, int iter, double tptr, std::string comment ) [inline, virtual]`

Depending on the value of the variable `verbose`, this prints out the iteration information. If `verbose=0`, then no information is printed. If `verbose>0`, then after each iteration, the present values of `x` and `y` are output to `std::cout` along with the iteration number. Also, if `verbose>0`, every time a new smallest function value is found, the location and the function value is output. If `verbose>=2` then each iteration waits for a character between each trial.

Definition at line 304 of file `anneal_mt.h`.

The documentation for this class was generated from the following file:

- `anneal_mt.h`

## 46.5 array\_2d\_alloc< mat\_t > Class Template Reference

A simple class to provide an `allocate()` function for 2-dimensional arrays.

```
#include <array.h>
```

#### 46.5.1 Detailed Description

```
template<class mat_t>class array_2d_alloc< mat_t >
```

The functions here are blank, as fixed-length arrays are automatically allocated and destroyed by the compiler. This class is present to provide an analog to `pointer_2d_alloc` and `omatrix_alloc`. This class is used in `gsl_mroot_hybrids_ts.cpp`.

Definition at line 121 of file `array.h`.

#### Public Member Functions

- void [allocate](#) (mat\_t &*v*, size\_t *i*, size\_t *j*)  
*Allocate v for i elements.*
- void [free](#) (mat\_t &*v*, size\_t *i*)

*Free memory.*

The documentation for this class was generated from the following file:

- [array.h](#)

## 46.6 `array_2d_col< R, C, data_t >` Class Template Reference

Column of a 2d array.

```
#include <array.h>
```

### 46.6.1 Detailed Description

```
template<size_t R, size_t C, class data_t = double>class array_2d_col< R, C, data_t >
```

This works because two-dimensional arrays are always contiguous (as indicated in appendix C of Soustroup's book).

Definition at line 367 of file `array.h`.

#### Public Member Functions

- [array\\_2d\\_col](#) (data\_t mat[R][C], size\_t i)  
*Create an object as the *i*th column of *mat*.*
- data\_t & [operator\[\]](#) (size\_t i)  
*Array-like indexing.*
- const data\_t & [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*

#### Protected Attributes

- data\_t \* [a](#)  
*The array pointer.*

The documentation for this class was generated from the following file:

- [array.h](#)

## 46.7 `array_2d_row< array_2d_t, data_t >` Class Template Reference

Row of a 2d array.

```
#include <array.h>
```

### 46.7.1 Detailed Description

```
template<class array_2d_t, class data_t = double>class array_2d_row< array_2d_t, data_t >
```

Definition at line 401 of file `array.h`.

## Public Member Functions

- `array_2d_row` (`array_2d_t &mat`, `size_t i`)  
*Create an object as the  $i$ th row of `mat`.*
- `data_t & operator[]` (`size_t i`)  
*Array-like indexing, returns the element in the  $i$ th column of the chosen row.*
- `const data_t & operator[]` (`size_t i`) `const`  
*Array-like indexing, returns the element in the  $i$ th column of the chosen row.*

## Protected Attributes

- `data_t * a`  
*The array pointer.*

The documentation for this class was generated from the following file:

- [array.h](#)

46.8 `array_alloc< vec_t >` Class Template Reference

A simple class to provide an `allocate()` function for arrays.

```
#include <array.h>
```

## 46.8.1 Detailed Description

```
template<class vec_t>class array_alloc< vec_t >
```

The functions here are blank, as fixed-length arrays are automatically allocated and destroyed by the compiler. This class is present to provide an analog to `pointer_alloc` and `ovector_alloc`. This class is used, for example, for `sma_interp_vec`.

**Idea for Future** Might it be possible to rework this so that it does range checking and ensures that the user doesn't try to allocate more or less space? I.e. `array_alloc<double[2]>` complains if you try an `allocate(x,3)`?

Definition at line 104 of file `array.h`.

## Public Member Functions

- void `allocate` (`vec_t &v`, `size_t i`)  
*Allocate  $v$  for  $i$  elements.*
- void `free` (`vec_t &v`)  
*Free memory.*

The documentation for this class was generated from the following file:

- [array.h](#)

46.9 `array_const_reverse< sz >` Class Template Reference

A simple class which reverses the order of an array.

```
#include <array.h>
```

---

## 46.9.1 Detailed Description

```
template<size_t sz>class array_const_reverse< sz >
```

See an example of usage in `interp_ts.cpp` and `smart_interp_ts.cpp`.

Definition at line 294 of file `array.h`.

## Public Member Functions

- [array\\_const\\_reverse](#) (const double \*arr)  
*Create a reversed array from `arr` of size `sz`.*
- const double & [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*

## Protected Attributes

- double \* [a](#)  
*The array pointer.*

The documentation for this class was generated from the following file:

- [array.h](#)

## 46.10 array\_const\_subvector Class Reference

A simple subvector class for a const array (without error checking)

```
#include <array.h>
```

## 46.10.1 Detailed Description

**Idea for Future** Make the member data truly const and remove the extra typecast.

Definition at line 441 of file `array.h`.

## Public Member Functions

- [array\\_const\\_subvector](#) (const double \*arr, size\_t offset, size\_t n)  
*Create a reversed array from `arr` of size `sz`.*
- const double & [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*

## Protected Attributes

- double \* [a](#)  
*The array pointer.*
- size\_t [off](#)  
*The offset.*
- size\_t [len](#)  
*The subvector length.*

The documentation for this class was generated from the following file:

- [array.h](#)
-

## 46.11 `array_const_subvector_reverse` Class Reference

Reverse a subvector of a const array.

```
#include <array.h>
```

### 46.11.1 Detailed Description

Definition at line 519 of file `array.h`.

#### Public Member Functions

- `array_const_subvector_reverse` (const double \*arr, size\_t offset, size\_t n)  
*Create a reversed array from `arr` of size `sz`.*
- const double & `operator[]` (size\_t i) const  
*Array-like indexing.*

#### Protected Attributes

- double \* `a`  
*The array pointer.*
- size\_t `off`  
*The offset.*
- size\_t `len`  
*The subvector length.*

The documentation for this class was generated from the following file:

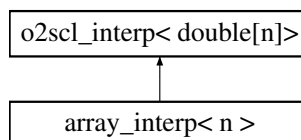
- `array.h`

## 46.12 `array_interp< n >` Class Template Reference

A specialization of `o2scl_interp` for C-style double arrays.

```
#include <interp.h>
```

Inheritance diagram for `array_interp< n >`:



### 46.12.1 Detailed Description

```
template<size_t n>class array_interp< n >
```

Definition at line 1434 of file `interp.h`.

## Public Member Functions

- [array\\_interp](#) ([base\\_interp\\_mgr](#)< double[n]> &it)  
*Create with base interpolation objects *it* and *rit*.*
- [array\\_interp](#) ()  
*Create an interpolator using the default base interpolation objects.*

The documentation for this class was generated from the following file:

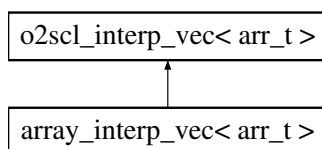
- [interp.h](#)

## 46.13 array\_interp\_vec&lt; arr\_t &gt; Class Template Reference

A specialization of [o2scl\\_interp\\_vec](#) for C-style arrays.

```
#include <interp.h>
```

Inheritance diagram for `array_interp_vec< arr_t >`:



## 46.13.1 Detailed Description

```
template<class arr_t>class array_interp_vec< arr_t >
```

Definition at line 1451 of file `interp.h`.

## Public Member Functions

- [array\\_interp\\_vec](#) ([base\\_interp\\_mgr](#)< arr\_t > &it, size\_t nv, const arr\_t &x, const arr\_t &y)  
*Create with base interpolation object *it*.*

The documentation for this class was generated from the following file:

- [interp.h](#)

## 46.14 array\_reverse&lt; sz &gt; Class Template Reference

A simple class which reverses the order of an array.

```
#include <array.h>
```

## 46.14.1 Detailed Description

```
template<size_t sz>class array_reverse< sz >
```

See an example of usage in `interp_ts.cpp` and `smart_interp_ts.cpp`.

Definition at line 257 of file `array.h`.

**Public Member Functions**

- `array_reverse` (double \*arr)  
*Create a reversed array from `arr` of size `sz`.*
- double & `operator[]` (size\_t i)  
*Array-like indexing.*
- const double & `operator[]` (size\_t i) const  
*Array-like indexing.*

**Protected Attributes**

- double \* `a`  
*The array pointer.*

The documentation for this class was generated from the following file:

- `array.h`

**46.15 `array_subvector` Class Reference**

A simple subvector class for an array (without error checking)

```
#include <array.h>
```

**46.15.1 Detailed Description**

Definition at line 322 of file `array.h`.

**Public Member Functions**

- `array_subvector` (double \*arr, size\_t offset, size\_t n)  
*Create a reversed array from `arr` of size `sz`.*
- double & `operator[]` (size\_t i)  
*Array-like indexing.*
- const double & `operator[]` (size\_t i) const  
*Array-like indexing.*

**Protected Attributes**

- double \* `a`  
*The array pointer.*
- size\_t `off`  
*The offset.*
- size\_t `len`  
*The subvector length.*

The documentation for this class was generated from the following file:

- `array.h`

**46.16 `array_subvector_reverse` Class Reference**

Reverse a subvector of an array.

```
#include <array.h>
```

---



## 46.16.1 Detailed Description

Definition at line 477 of file `array.h`.

## Public Member Functions

- `array_subvector_reverse` (`double *arr`, `size_t offset`, `size_t n`)  
Create a reversed array from `arr` of size `sz`.
- `double & operator[]` (`size_t i`)  
Array-like indexing.
- `const double & operator[]` (`size_t i`) `const`  
Array-like indexing.

## Protected Attributes

- `double * a`  
The array pointer.
- `size_t off`  
The offset.
- `size_t len`  
The subvector length.

The documentation for this class was generated from the following file:

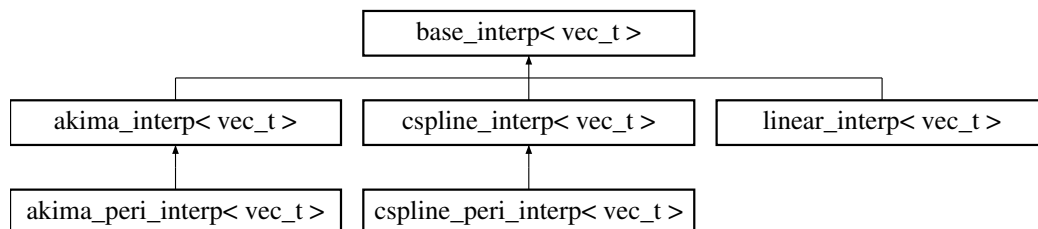
- `array.h`

46.17 `base_interp< vec_t >` Class Template Reference

Base low-level interpolation class [abstract base].

```
#include <interp.h>
```

Inheritance diagram for `base_interp< vec_t >`:



## 46.17.1 Detailed Description

```
template<class vec_t>class base_interp< vec_t >
```

For any pair of vectors `x` and `y` into which you would like to interpolate, you need to call `allocate()` and `init()` first, and then the interpolation functions, and then `free()`. If the next pair of vectors has the same size, then you need only to call `init()` before the next call to an interpolation function (you don't need to reallocate). If the `x` and `y` vectors do not change, then you may call the interpolation functions in succession.

These interpolation class work so long as the vector `x` is either monotonically increasing or monotonically decreasing. All of the descendants give identical results to the GSL interpolation routines when the vector is monotonically increasing.

Definition at line 56 of file `interp.h`.

## Public Member Functions

- virtual int `allocate` (size\_t size)  
*Allocate memory, assuming  $x$  and  $y$  have size  $size$ .*
- virtual int `free` ()  
*Free allocated memory.*
- virtual int `init` (const vec\_t &x, const vec\_t &y, size\_t size)  
*Initialize interpolation routine.*
- virtual int `interp` (const vec\_t &x, const vec\_t &y, size\_t size, double x0, double &y0)=0  
*Give the value of the function  $y(x = x_0)$ .*
- virtual int `deriv` (const vec\_t &x, const vec\_t &y, size\_t size, double x0, double &dydx)=0  
*Give the value of the derivative  $y'(x = x_0)$ .*
- virtual int `deriv2` (const vec\_t &x, const vec\_t &y, size\_t size, double x0, double &d2ydx2)=0  
*Give the value of the second derivative  $y''(x = x_0)$ .*
- virtual int `integ` (const vec\_t &x, const vec\_t &y, size\_t size, double a, double b, double &result)=0  
*Give the value of the integral  $\int_a^b y(x) dx$ .*
- virtual const char \* `type` ()  
*Return the type, "base\_interp".*

## Data Fields

- size\_t `min_size`  
*The minimum size of the vectors to interpolate between.*

## Protected Member Functions

- double `integ_eval` (double ai, double bi, double ci, double di, double xi, double a, double b)  
*An internal function to assist in computing the integral for both the cspline and Akima types.*

## Protected Attributes

- `search_vec< vec_t > * sv`  
*To perform binary searches.*
- size\_t `n_sv`  
*The size of the allocated `search_vec` object.*
- bool `mem_alloc`  
*True if memory has been allocated.*

## Private Member Functions

- `base_interp` (const `base_interp< vec_t >` &)
- `base_interp< vec_t > & operator=` (const `base_interp< vec_t >` &)

## 46.17.2 Field Documentation

46.17.2.1 `template<class vec_t> size_t base_interp< vec_t >::min_size`

This needs to be set in the constructor of the children for access by the class user

Definition at line 109 of file `interp.h`.

The documentation for this class was generated from the following file:

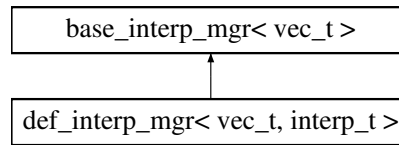
- `interp.h`

## 46.18 `base_interp_mgr< vec_t >` Class Template Reference

A base interpolation object manager [abstract base].

```
#include <interp.h>
```

Inheritance diagram for `base_interp_mgr< vec_t >`:



### 46.18.1 Detailed Description

```
template<class vec_t>class base_interp_mgr< vec_t >
```

Definition at line 1082 of file `interp.h`.

#### Public Member Functions

- virtual `base_interp< vec_t > * new_interp ()=0`  
*Create a new interpolation object.*
- virtual `int free_interp (base_interp< vec_t > *b)`  
*Deallocate an interpolation object.*

The documentation for this class was generated from the following file:

- `interp.h`

## 46.19 `bin_size` Class Reference

Determine bin size (CERNLIB)

```
#include <bin_size.h>
```

### 46.19.1 Detailed Description

This is adapted from the KERNLIB routine `binsiz.f` written by F. James.

This class computes an appropriate set of histogram bins given the upper and lower limits of the data and the maximum number of bins. The bin width is always an integral power of ten times 1, 2, 2.5 or 5. The bin width may also be specified by the user, in which case the class only computes the appropriate limits.

#### Note

This class is not working yet.

**Idea for Future** Finish this.

Definition at line 48 of file `bin_size.h`.

## Public Member Functions

- int [calc\\_bin](#) (double al, double ah, int na, double &bl, double &bh, int &nb, double &bwid)  
*Compute bin size.*

## Data Fields

- bool [cern\\_mode](#)  
*(default true)*

## 46.19.2 Member Function Documentation

## 46.19.2.1 int bin\_size::calc\_bin ( double al, double ah, int na, double &amp; bl, double &amp; bh, int &amp; nb, double &amp; bwid )

- al - Lower limit of data
- ah - Upper limit of data
- na - Maximum number of bins desired.
- bl - Lower limit (BL<=AL)
- bh - Upper limit (BH>=AH)
- nb - Number of bins determined by BINSIZ (NA/2<NB<=NA)
- bwid - Bin width (BH-BL)/NB

If na=0 or na=-1, this function always makes exactly one bin.

If na=1, this function takes bwid as input and determines only bl, hb, and nb. This is especially useful when it is desired to have the same bin width for several histograms (or for the two axes of a scatter-plot).

If al > ah, this function takes al to be the upper limit and ah to be the lower limit, so that in fact al and ah may appear in any order. They are not changed by [calc\\_bin\(\)](#). If al = ah, the lower limit is taken to be al, and the upper limit is set to al+1.

If [cern\\_mode](#) is true (which is the default) the starting guess for the number of bins is na-1. Otherwise, the starting guess for the number of bins is na.

The documentation for this class was generated from the following file:

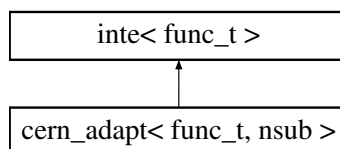
- bin\_size.h

## 46.20 cern\_adapt&lt; func\_t, nsub &gt; Class Template Reference

Adaptive integration (CERNLIB)

```
#include <cern_adapt.h>
```

Inheritance diagram for cern\_adapt< func\_t, nsub >:



## 46.20.1 Detailed Description

```
template<class func_t = func_t, size_t nsub = 100>class cern_adapt< func_t, nsub >
```

Uses a base integration object (default is [cern\\_gauss56](#)) to perform adaptive integration by automatically subdividing the integration interval. At each step, the interval with the largest absolute uncertainty is divided in half. The routine succeeds if the absolute tolerance is less than [tol\\_abs](#) or if the relative tolerance is less than [tol\\_rel](#), i.e.

$$\text{err} \leq \text{tol\_abs} \text{ or } \text{err} \leq \text{tol\_rel} \cdot |I|$$

where  $I$  is the current estimate for the integral and  $\text{err}$  is the current estimate for the uncertainty. If the number of subdivisions exceeds the template parameter `nsub`, the error handler is called, since the integration may not have been successful. The number of subdivisions used in the last integration can be obtained from [get\\_nsubdivisions\(\)](#).

The template parameter `nsub`, is the maximum number of subdivisions. It is automatically set to 100 in the original CERNLIB routine, and defaults to 100 here. The default base integration object is of type [cern\\_gauss56](#). This is the CERNLIB default, but can be modified by calling [set\\_inte\(\)](#).

This class is based on the CERNLIB routines RADAPT and DADAPT which are documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/d102/top.html>

**Idea for Future**

- Allow user to set the initial subdivisions?
- It might be interesting to directly compare the performance of this class to [gsl\\_inte\\_qag](#).
- There is a fixme entry in the code which could be resolved.
- Output the point where most subdividing was required?

Definition at line 71 of file `cern_adapt.h`.

**Public Member Functions****Basic usage**

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` giving result `res` and error `err`.*

**Protected Attributes**

- double [xlo](#) [nsub]  
*Lower end of subdivision.*
- double [xhi](#) [nsub]  
*High end of subdivision.*
- double [tval](#) [nsub]  
*Value of integral for subdivision.*
- double [ters](#) [nsub]  
*Squared error for subdivision.*
- int [prev\\_subdiv](#)  
*Previous number of subdivisions.*
- [inte](#)< func\_t > \* [it](#)  
*The base integration object.*

**Integration object**

- [cern\\_gauss56](#)< func\_t > [def\\_inte](#)  
*Default integration object.*
- int [set\\_inte](#) ([inte](#)< func\_t > &i)  
*Set the base integration object to use.*

## Subdivisions

- size\_t [nsubdiv](#)  
*Number of subdivisions.*
- size\_t [get\\_nsubdivisions](#) ()  
*Return the number of subdivisions used in the last integration.*
- int [get\\_ith\\_subdivision](#) (size\_t i, double &xlow, double &xhigh, double &value, double &errsq)  
*Return the ith subdivision.*
- template<class vec\_t >  
int [get\\_subdivisions](#) (vec\_t &xlow, vec\_t &xhigh, vec\_t &value, vec\_t &errsq)  
*Return all of the subdivisions.*

## 46.20.2 Field Documentation

46.20.2.1 `template<class func_t = func_t, size_t nsub = 100> size_t cern_adapt< func_t, nsub >::nsubdiv`

The options are

- 0: Use previous binning and do not subdivide further
- 1: Automatic - adapt until tolerance is attained (default)
- n: (n>1) split first in n equal subdivisions, then adapt until tolerance is obtained.

Definition at line 266 of file `cern_adapt.h`.

The documentation for this class was generated from the following file:

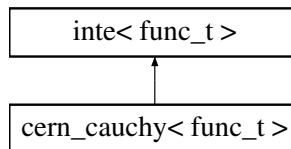
- `cern_adapt.h`

## 46.21 cern\_cauchy&lt; func\_t &gt; Class Template Reference

Cauchy principal value integration (CERNLIB)

```
#include <cern_cauchy.h>
```

Inheritance diagram for `cern_cauchy< func_t >`:



## 46.21.1 Detailed Description

```
template<class func_t> class cern_cauchy< func_t >
```

The location of the singularity must be specified before-hand in `cern_cauchy::s`, and the singularity must not be at one of the endpoints. Note that when integrating a function of the form  $\frac{f(x)}{(x-s)}$ , the denominator  $(x-s)$  must be specified in the argument `func` to `integ()`. This is different from how the `gsl_inte_qawc` operates.

The method from [Longman58](#) is used for the decomposition of the integral, and the resulting integrals are computed using a user-specified base integration object.

The uncertainty in the integral is not calculated, and is always given as zero. The default base integration object is of type `cern_gauss`. This is the CERNLIB default, but can be modified by calling `set_inte()`. If the singularity is outside the region of integration, then the result from the base integration object is returned without calling the error handler.

Possible errors for `integ()` and `integ_err()`:

- `gsl_einval` - Singularity is on an endpoint
- `gsl_efailed` - Couldn't reach requested accuracy (occurs only if `inte::err_nonconv` is true)

This function is based on the CERNLIB routines RCAUCH and DCAUCH which are documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/d104/top.html>

Definition at line 63 of file `cern_cauchy.h`.

### Public Member Functions

- `int set_inte (inte< func_t > &i)`  
*Set the base integration object to use (default is `cern_cauchy::def_inte` of type `cern_gauss`)*
- `virtual int integ_err (func_t &func, double a, double b, double &res, double &err)`  
*Integrate function `func` from `a` to `b` giving result `res` and error `err`.*
- `virtual double integ (func_t &func, double a, double b)`  
*Integrate function `func` from `a` to `b`.*

### Data Fields

- `double s`  
*The singularity (must be set before calling `integ()` or `integ_err()`)*
- `cern_gauss< func_t > def_inte`  
*Default integration object.*

### Protected Attributes

- `inte< func_t > * it`  
*The base integration object.*

### Integration constants

- `double x [12]`
- `double w [12]`

The documentation for this class was generated from the following file:

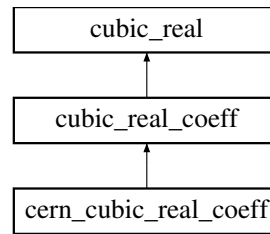
- `cern_cauchy.h`

## 46.22 cern\_cubic\_real\_coeff Class Reference

Solve a cubic with real coefficients and complex roots (CERNLIB)

```
#include <poly.h>
```

Inheritance diagram for `cern_cubic_real_coeff`:



### 46.22.1 Detailed Description

#### Note

The function [rrteq3\(\)](#) is based on the CERNLIB routine of the same name, but differs slightly. See the documtation of that function for details.

Definition at line 380 of file poly.h.

#### Public Member Functions

- virtual int [solve\\_rc](#) (const double a3, const double b3, const double c3, const double d3, double &x1, std::complex< double > &x2, std::complex< double > &x3)  
*Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the real solution  $x = x_1$  and two complex solutions  $x = x_1$ ,  $x = x_2$ , and  $x = x_3$ .*
- virtual int [rrteq3](#) (double r, double s, double t, double x[], double &d)  
*The CERNLIB-like interface.*
- const char \* [type](#) ()  
*Return a string denoting the type ("cern\_cubic\_real\_coeff")*

#### Data Fields

- double [eps](#)  
*Numerical tolerance (default  $10^{-6}$ )*
- double [delta](#)  
*Numerical tolerance (default  $10^{-15}$ )*
- bool [improve\\_scale](#)  
*Improve algorithm for poorly-scaled roots (default true)*

### 46.22.2 Member Function Documentation

#### 46.22.2.1 virtual int cern\_cubic\_real\_coeff::rrteq3 ( double r, double s, double t, double x[], double & d ) [virtual]

This function computes the roots of the cubic equation

$$x^3 + rx^2 + sx + t = 0$$

returning the value of the discriminant in d and the roots in the array x. If the discriminant is negative, then all three real roots are stored in x. Otherwise, the real root is stored in x[0] and the real and imaginary parts of the complex conjugate roots are stored in x[1] and x[2], respectively. This differs from the CERNLIB routine where the results were stored in x[1], x[2], and x[3] instead.

Another small change is that the discriminant for the resolvent cubic is evaluated slightly differently in order to improve the properties in the case where the roots are not all of order unity. The default CERNLIB behavior can be restored by setting improve\_scale to false.

The documentation for this class was generated from the following file:

- [poly.h](#)

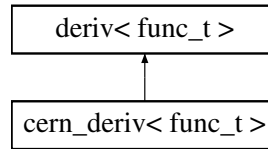


## 46.23 cern\_deriv< func\_t > Class Template Reference

Numerical differentiation routine (CERNLIB)

```
#include <cern_deriv.h>
```

Inheritance diagram for cern\_deriv< func\_t >:



### 46.23.1 Detailed Description

```
template<class func_t = funct>class cern_deriv< func_t >
```

This uses Romberg extrapolation to compute the derivative with the finite-differencing formula

$$f'(x) = [f(x+h) - f(x-h)]/(2h)$$

If `deriv::verbose` is greater than zero, then each iteration prints out the extrapolation table, and if `deriv::verbose` is greater than 1, then a keypress is required at the end of each iteration.

For sufficiently difficult functions, the derivative computation can fail, and will call the error handler and return zero with zero error.

Based on the CERNLIB routine DERIV, which was based on [Rutishauser63](#) and is documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/d401/top.html>

An example demonstrating the usage of this class is given in `examples/ex_deriv.cpp` and the [Numerical differentiation](#).

If `deriv::verbose` is greater than zero, at each iteration this class prints something similar to

```

cern_deriv, iteration: 1
(hh, a[k], derivative) list:
-4.193459e-05 4.387643e-14 8.775286e-01
-2.995402e-05 4.387792e-14 8.775585e-01
-1.048405e-05 4.387845e-14 8.775690e-01
-7.488654e-06 4.387882e-14 8.775765e-01
-2.621038e-06 4.387895e-14 8.775791e-01
-1.872173e-06 4.387905e-14 8.775810e-01
-6.552611e-07 4.387908e-14 8.775817e-01
-4.680438e-07 4.387910e-14 8.775821e-01
-1.638153e-07 4.387911e-14 8.775823e-01

```

If `deriv::verbose` is greater than 1, a keypress is required after each iteration.

#### Note

Second and third derivatives are computed by naive nested applications of the formula for the first derivative. No uncertainty for these derivatives is provided.

**Idea for Future** All of the coefficients appear to be fractions which could be replaced with exact representation?

**Idea for Future** Record the number of function calls?

Definition at line 91 of file `cern_deriv.h`.

## Public Member Functions

- virtual int [calc\\_err](#) (double x, func\_t &func, double &dwdx, double &err)  
*Calculate the first derivative of `func` w.r.t. `x` and the uncertainty.*
- virtual const char \* [type](#) ()  
*Return string denoting type ("`cern_deriv`")*

## Data Fields

- double [delta](#)  
*A scaling factor (default 1.0)*
- double [eps](#)  
*Extrapolation tolerance (default is  $5 \times 10^{14}$ )*

## Protected Member Functions

- template<class func2\_t >  
int [calc\\_base](#) (double x, func2\_t &func, double &dwdx, double &err)  
*Internal template version of the derivative function.*
- virtual int [calc\\_err\\_int](#) (double x, [func](#) &func, double &dwdx, double &err)  
*Calculate the first derivative of `func` w.r.t. `x`.*

## Protected Attributes

Storage for the fixed coefficients

- double **dx** [10]
- double **w** [10][4]

## 46.23.2 Member Function Documentation

46.23.2.1 `template<class func_t = func_t> virtual int cern_deriv< func_t >::calc_err_int ( double x, func\_t & func, double & dwdx, double & err )`  
[inline, protected, virtual]

This is an internal version of [calc\(\)](#) which is used in computing second and third derivatives

Implements [deriv< func\\_t >](#).

Definition at line 249 of file `cern_deriv.h`.

The documentation for this class was generated from the following file:

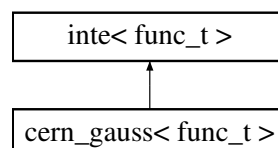
- `cern_deriv.h`

## 46.24 cern\_gauss&lt; func\_t &gt; Class Template Reference

Gaussian quadrature (CERNLIB)

```
#include <cern_gauss.h>
```

Inheritance diagram for `cern_gauss< func_t >`:



## 46.24.1 Detailed Description

```
template<class func_t = funct>class cern_gauss< func_t >
```

For any interval  $(a, b)$ , we define  $g_8(a, b)$  and  $g_{16}(a, b)$  to be the 8- and 16-point Gaussian quadrature approximations to

$$I = \int_a^b f(x) dx$$

and define

$$r(a, b) = \frac{|g_{16}(a, b) - g_8(a, b)|}{1 + g_{16}(a, b)}$$

The function `integ()` returns  $G$  given by

$$G = \sum_{i=1}^k g_{16}(x_{i-1}, x_i)$$

where  $x_0 = a$  and  $x_k = b$  and the subdivision points  $x_i$  are given by

$$x_i = x_{i-1} + \lambda(B - x_{i-1})$$

where  $\lambda$  is the first number in the sequence  $1, \frac{1}{2}, \frac{1}{4}, \dots$  for which

$$r(x_{i-1}, x_i) < \text{eps}.$$

If, at any stage, the ratio

$$q = \left| \frac{x_i - x_{i-1}}{b - a} \right|$$

is so small so that  $1 + 0.005q$  is indistinguishable from unity, then the accuracy is required is not reachable and the error handler is called.

Unless there is severe cancellation, `inte::tol_rel` may be considered as specifying a bound on the relative error of the integral in the case that  $|I| > 1$  and an absolute error if  $|I| < 1$ . More precisely, if  $k$  is the number of subintervals from above, and if

$$I_{abs} = \int_a^b |f(x)| dx$$

then

$$\frac{|G - I|}{I_{abs} + k} < \text{tol\_rel}$$

will nearly always be true when no error is returned. For functions with no singularities in the interval, the accuracy will usually be higher than this.

If the desired accuracy is not achieved, the integration functions will call the error handler and return the best guess, unless `inte::err_nonconv` is false, in which case the error handler is not called.

This function is based on the CERNLIB routines GAUSS and DGAUSS which are documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/d103/top.html>

**Idea for Future** Allow user to change `cst`?

Definition at line 93 of file `cern_gauss.h`.

## Public Member Functions

- virtual int `integ_err` (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function func from a to b giving result res and error err.*
- virtual double `integ` (func\_t &func, double a, double b)  
*Integrate function func from a to b.*

## Protected Attributes

Integration constants (Set in the constructor)

- double **x** [12]
- double **w** [12]

The documentation for this class was generated from the following file:

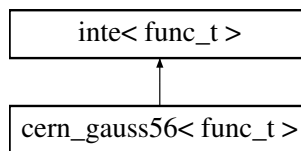
- cern\_gauss.h

## 46.25 cern\_gauss56&lt; func\_t &gt; Class Template Reference

5,6-point Gaussian quadrature (CERNLIB)

```
#include <cern_gauss56.h>
```

Inheritance diagram for cern\_gauss56< func\_t >:



## 46.25.1 Detailed Description

```
template<class func_t>class cern_gauss56< func_t >
```

If  $I_5$  is the 5-point approximation, and  $I_6$  is the 6-point approximation to the integral, then `integ_err()` returns the result  $\frac{1}{2}(I_5 + I_6)$  with uncertainty  $|I_5 - I_6|$ .

This class is based on the CERNLIB routines RGS56P and DGS56P which are documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/d106/top.html>

Definition at line 44 of file cern\_gauss56.h.

## Public Member Functions

- virtual int `integ_err` (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` giving result `res` and error `err`.*

## Protected Attributes

Integration constants

- double **x5** [5]
- double **w5** [5]
- double **x6** [6]
- double **w6** [6]

## 46.25.2 Member Function Documentation

46.25.2.1 `template<class func_t> virtual int cern_gauss56< func_t >::integ_err ( func_t & func, double a, double b, double & res, double & err ) [inline, virtual]`

This function always returns [gsl\\_success](#).

Implements [inte< func\\_t >](#).

Definition at line 79 of file `cern_gauss56.h`.

The documentation for this class was generated from the following file:

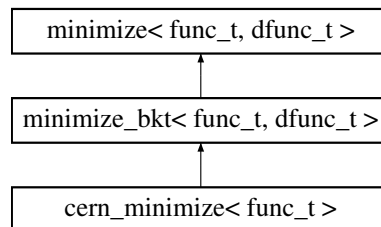
- `cern_gauss56.h`

## 46.26 cern\_minimize< func\_t > Class Template Reference

One-dimensional minimization (CERNLIB)

```
#include <cern_minimize.h>
```

Inheritance diagram for `cern_minimize< func_t >`:



### 46.26.1 Detailed Description

```
template<class func_t = funct> class cern_minimize< func_t >
```

The golden section search is applied in the interval  $(a, b)$  using a fixed number  $n$  of function evaluations where

$$n = \left\lceil 2.08 \ln(|a - b| / \text{tol\_abs}) + \frac{1}{2} \right\rceil + 1$$

The accuracy depends on the function. A choice of  $\text{tol\_abs} > 10^{-8}$  usually results in a relative error of  $\$x\$$  which is smaller than or of the order of  $\text{tol\_abs}$ .

This routine strictly searches the interval  $(a, b)$ . If the function is nowhere flat in this interval, then `min_bkt()` will return either  $a$  or  $b$  and `min_type` is set to 1. Note that if there are more than 1 local minima in the specified interval, there is no guarantee that this method will find the global minimum.

#### Note

The number of function evaluations can be quite large if `multi_min::tol_abs` is sufficiently small. If `multi_min::tol_abs` is exactly zero, then the error handler will be called.

Based on the CERNLIB routines RMINFC and DMINFC, which was based on [Fletcher87](#), and [Krabs83](#) and is documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/d503/top.html>

Definition at line 69 of file `cern_minimize.h`.

## Public Member Functions

- virtual int [min\\_bkt](#) (double &x, double a, double b, double &y, func\_t &func)  
*Calculate the minimum  $\min$  of  $func$  between  $a$  and  $b$ .*
- int [set\\_delta](#) (double d)  
*Set the value of  $\delta$ .*
- virtual const char \* [type](#) ()  
*Return string denoting type ("cern\_minimize")*

## Data Fields

- int [min\\_type](#)  
*Type of minimum found.*

## Protected Member Functions

- int [nint](#) (double x)  
*C analog of Fortran's "Nearest integer" function.*

## Protected Attributes

- double [delta](#)  
*The value of delta as specified by the user.*
- bool [delta\\_set](#)  
*True if the value of delta has been set.*

## 46.26.2 Member Function Documentation

46.26.2.1 `template<class func_t = func_t> virtual int cern_minimize< func_t >::min_bkt ( double & x, double a, double b, double & y, func_t & func ) [inline, virtual]`

The initial value of  $x$  is ignored.

If there is no minimum in the given interval, then on exit  $x$  will be equal to either  $a$  or  $b$  and [min\\_type](#) will be set to 1 instead of zero. The error handler is not called, as this need not be interpreted as an error.

Implements [minimize\\_bkt< func\\_t, dfunc\\_t >](#).

Definition at line 106 of file cern\_minimize.h.

46.26.2.2 `template<class func_t = func_t> int cern_minimize< func_t >::set_delta ( double d ) [inline]`

If this is not called before [min\\_bkt\(\)](#) is used, then the suggested value  $\delta = 10\text{tol}_a\text{bs}$  is used.

Definition at line 183 of file cern\_minimize.h.

The documentation for this class was generated from the following file:

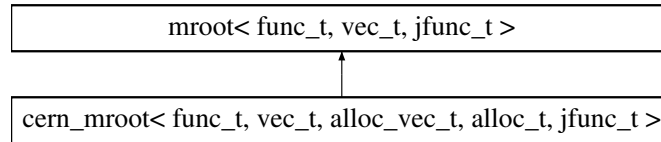
- cern\_minimize.h

## 46.27 cern\_mroot&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t, jfunc\_t &gt; Class Template Reference

Multi-dimensional mroot-finding routine (CERNLIB)

```
#include <cern_mroot.h>
```

Inheritance diagram for cern\_mroot< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, jfunc\_t >:



#### 46.27.1 Detailed Description

```
template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class jfunc_t = jac-  
func_t<vec_t,omatrix_base>>class cern_mroot< func_t, vec_t, alloc_vec_t, alloc_t, jfunc_t >
```

If  $x_i$  denotes the current iteration, and  $x'_i$  denotes the previous iteration, then the calculation is terminated if either of the following tests is successful

- 1 :  $\max |f_i(x)| \leq \text{tol\_rel}$
- 2 :  $\max |x_i - x'_i| \leq \text{tol\_abs} \times \max |x_i|$

This routine treats the functions specified as a [mm\\_func\\_t](#) object slightly differently than [gsl\\_mroot\\_hybrids](#). First the equations should be numbered (as much as is possible) in order of increasing nonlinearity. Also, instead of calculating all of the equations on each function call, only the equation specified by the `size_t` parameter needs to be calculated. If the equations are specified as

$$\begin{aligned} 0 &= f_0(x_0, x_1, \dots, x_{n-1}) \\ 0 &= f_1(x_0, x_1, \dots, x_{n-1}) \\ &\dots \\ 0 &= f_{n-1}(x_0, x_1, \dots, x_{n-1}) \end{aligned}$$

then when the `size_t` argument is given as `i`, then only the function  $f_i$  needs to be calculated.

#### Warning

This code has not been checked to ensure that it cannot fail to solve the equations without calling the error handler and returning a non-zero value. Until then, the solution may need to be checked explicitly by the caller.

There is an example for the usage of the multidimensional solver classes given in `examples/ex_mroot.cpp`, see [Multi-dimensional solver](#).

**Idea for Future** Modify this so it handles functions which return non-zero values.

**Idea for Future** Move some of the memory allocation out of `msolve()`

**Idea for Future** Give the user access to the number of function calls

**Idea for Future** Rename `nier6`, `nier7`, and `nier8` to something sensible.

**Idea for Future** It may be that the `O2scl` native Householder transformations should be used here instead of the inline version given here.

Based on the CERNLIB routines `RSNLEQ` and `DSNLEQ`, which was based on [More79](#) and [More80](#) and is documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/c201/top.html>

Definition at line 92 of file `cern_mroot.h`.

## Public Member Functions

- int [get\\_info](#) ()  
*Get the value of INFO from the last call to [msolve](#)()*
- std::string [get\\_info\\_string](#) ()  
*Get the a string corresponding to the integer returned by [cern\\_mroot::get\\_info](#)()*.
- virtual const char \* [type](#) ()  
*Return the type, "cern\_mroot".*
- virtual int [msolve](#) (size\_t nvar, vec\_t &x, func\_t &func)  
*Solve func using x as an initial guess, returning x.*

## Data Fields

- int [maxf](#)  
*Maximum number of function evaluations.*
- double [scale](#)  
*The original scale parameter from CERNLIB (default 10.0)*
- double [eps](#)  
*The smallest floating point number (default  $\sim 1.49012 \times 10^{-8}$ )*

## Protected Attributes

- alloc\_t [ao](#)  
*Memory allocator for objects of type [alloc\\_vec\\_t](#).*
- [umatrix](#) w  
*Desc.*
- int [info](#)  
*Internal storage for the value of [info](#).*
- int [mpt](#) [289]  
*Store the number of function evaluations.*

## 46.27.2 Member Function Documentation

46.27.2.1 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class jfunc_t = jac_func_t<vec_t,omatrix_base>> int cern_mroot< func_t, vec_t, alloc_vec_t, alloc_t, jfunc_t >::get_info ( ) [inline]`

The value of info is assigned according to the following list. The values 1-8 are the standard behavior from CERNLIB. 0 - The function solve() has not been called. 1 - Test 1 was successful.

2 - Test 2 was successful.

3 - Both tests were successful.

4 - Number of iterations is greater than [cern\\_mroot\\_root::maxf](#).

5 - Approximate (finite difference) Jacobian matrix is singular.

6 - Iterations are not making good progress.

7 - Iterations are diverging.

8 - Iterations are converging, but either [cern\\_mroot\\_root::tol\\_abs](#) is too small or the Jacobian is nearly singular or the variables are badly scaled.

9 - Either [root::tol\\_rel](#) or [root::tol\\_abs](#) is not greater than zero or the specified number of variables is  $\leq 0$ .

The return values returned by [msolve](#)() corresponding to the values of INFO above are 1 - [gsl\\_success](#) 2 - [gsl\\_success](#) 3 - [gsl\\_success](#) 4 - [gsl\\_emaxiter](#) 5 - [gsl\\_esing](#) 6 - [gsl\\_enoprogram](#) 7 - [gsl\\_erunaway](#) 8 - [gsl\\_efailed](#) 9 - [gsl\\_einval](#)

Definition at line 165 of file [cern\\_mroot.h](#).



## 46.27.3 Field Documentation

46.27.3.1 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class jfunc_t = jac_func_t<vec_t,omatrix_base>> int cern_mroot< func_t, vec_t, alloc_vec_t, alloc_t, jfunc_t >::maxf`

If  $\text{maxf} \leq 0$ , then  $50(nv + 3)$  (which is the CERNLIB default) is used. The default value of `maxf` is zero which then implies the default from CERNLIB.

Definition at line 200 of file `cern_mroot.h`.

46.27.3.2 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class jfunc_t = jac_func_t<vec_t,omatrix_base>> double cern_mroot< func_t, vec_t, alloc_vec_t, alloc_t, jfunc_t >::eps`

The original prescription from CERNLIB for `eps` is given below:

```
#if !defined(CERNLIB_DOUBLE)
PARAMETER (EPS = 0.84293 69702 17878 97282 52636 392E-07)
#endif
#if defined(CERNLIB_IBM)
PARAMETER (EPS = 0.14901 16119 38476 562D-07)
#endif
#if defined(CERNLIB_VAX)
PARAMETER (EPS = 0.37252 90298 46191 40625D-08)
#endif
#if (defined(CERNLIB_UNIX)) && (defined(CERNLIB_DOUBLE))
PARAMETER (EPS = 0.14901 16119 38476 600D-07)
#endif
```

Definition at line 229 of file `cern_mroot.h`.

The documentation for this class was generated from the following file:

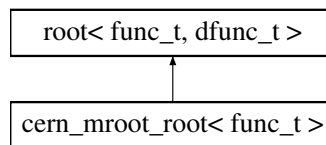
- `cern_mroot.h`

## 46.28 cern\_mroot\_root&lt; func\_t &gt; Class Template Reference

One-dimensional version of [cern\\_mroot](#).

```
#include <cern_mroot_root.h>
```

Inheritance diagram for `cern_mroot_root< func_t >`:



## 46.28.1 Detailed Description

```
template<class func_t = funct>class cern_mroot_root< func_t >
```

This one-dimensional root-finding routine, based on [cern\\_mroot](#), is probably slower than the more typical 1-d routines, but also tends to converge for a larger class of functions than [cern\\_root](#), [gsl\\_root\\_brent](#), or [gsl\\_root\\_stef](#). It has been modified from [cern\\_mroot](#) and slightly optimized, but has the same basic behavior.

If  $x_i$  denotes the current iteration, and  $x'_i$  denotes the previous iteration, then the calculation is terminated if either (or both) of the following tests is successful

$$1 : \quad \max |f_i(x)| \leq \text{tol\_rel}$$

$$2: \quad \max |x_i - x'_i| \leq \text{tol\_abs} \times \max |x_i|$$

**Note**

This code has not been checked to ensure that it cannot fail to solve the equations without calling the error handler and returning a non-zero value. Until then, the solution may need to be checked explicitly by the caller.

**Idea for Future** Double-check this class to make sure it cannot fail while returning 0 for success.

Definition at line 64 of file cern\_mroot\_root.h.

**Public Member Functions**

- int [get\\_info](#) ()  
*Get the value of INFO from the last call to [solve\(\)](#) (default 0)*
- virtual const char \* [type](#) ()  
*Return the type, "cern\_mroot\_root".*
- virtual int [solve](#) (double &ux, func\_t &func)  
*Solve func using x as an initial guess, returning x.*

**Data Fields**

- int [maxf](#)  
*Maximum number of function evaluations.*
- double [scale](#)  
*The original scale parameter from CERNLIB (default 10.0)*
- double [eps](#)  
*The smallest floating point number (default  $\sim 1.49012 \times 10^{-8}$ )*

**Protected Attributes**

- int [info](#)  
*Internal storage for the value of info.*

**46.28.2 Member Function Documentation**

**46.28.2.1** `template<class func_t = func_t> int cern_mroot_root< func_t >::get_info ( ) [inline]`

The value of info is assigned according to the following list. The values 1-8 are the standard behavior from CERNLIB. 0 - The function [solve\(\)](#) has not been called. 1 - Test 1 was successful.

2 - Test 2 was successful.

3 - Both tests were successful.

4 - Number of iterations is greater than [cern\\_mroot\\_root::maxf](#).

5 - Approximate (finite difference) Jacobian matrix is singular.

6 - Iterations are not making good progress.

7 - Iterations are diverging.

8 - Iterations are converging, but either [cern\\_mroot\\_root::tol\\_abs](#) is too small or the Jacobian is nearly singular or the variables are badly scaled.

9 - Either [root::tol\\_rel](#) or [root::tol\\_abs](#) is not greater than zero.

Definition at line 102 of file cern\_mroot\_root.h.

## 46.28.3 Field Documentation

46.28.3.1 `template<class func_t = func_t> int cern_mroot_root< func_t >::maxf`

If  $\text{maxf} \leq 0$ , then 200 (which is the CERNLIB default) is used. The default value of `maxf` is zero which then implies the default from CERNLIB.

Definition at line 110 of file `cern_mroot_root.h`.

46.28.3.2 `template<class func_t = func_t> double cern_mroot_root< func_t >::eps`

The original prescription from CERNLIB for `eps` is given below:

```
#if !defined(CERNLIB_DOUBLE)
PARAMETER (EPS = 0.84293 69702 17878 97282 52636 392E-07)
#endif
#if defined(CERNLIB_IBM)
PARAMETER (EPS = 0.14901 16119 38476 562D-07)
#endif
#if defined(CERNLIB_VAX)
PARAMETER (EPS = 0.37252 90298 46191 40625D-08)
#endif
#if (defined(CERNLIB_UNIX)) && (defined(CERNLIB_DOUBLE))
PARAMETER (EPS = 0.14901 16119 38476 600D-07)
#endif
```

**Idea for Future** This number should probably default to one of the GSL tolerances.

Definition at line 142 of file `cern_mroot_root.h`.

The documentation for this class was generated from the following file:

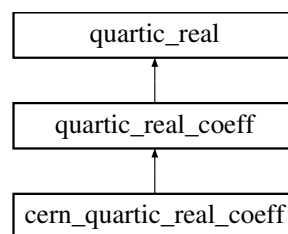
- `cern_mroot_root.h`

## 46.29 cern\_quartic\_real\_coeff Class Reference

Solve a quartic with real coefficients and complex roots (CERNLIB)

```
#include <poly.h>
```

Inheritance diagram for `cern_quartic_real_coeff`:



## 46.29.1 Detailed Description

Definition at line 440 of file `poly.h`.

## Public Member Functions

- virtual int `solve_rc` (const double a4, const double b4, const double c4, const double d4, const double e4, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3, std::complex< double > &x4)

- Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four complex solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .
- virtual int [rrteq4](#) (double a, double b, double c, double d, std::complex< double > z[], double &dc, int &mt)  
The CERNLIB-like interface.
- const char \* [type](#) ()  
Return a string denoting the type ("cern\_quartic\_real\_coeff")

#### Protected Attributes

- [cern\\_cubic\\_real\\_coeff cub\\_obj](#)  
The object to solve for the associated cubic.

The documentation for this class was generated from the following file:

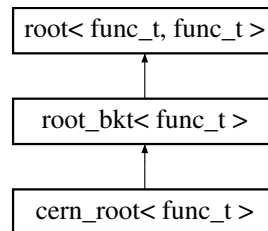
- [poly.h](#)

## 46.30 cern\_root< func\_t > Class Template Reference

One-dimensional root-finding routine (CERNLIB)

```
#include <cern_root.h>
```

Inheritance diagram for cern\_root< func\_t >:



### 46.30.1 Detailed Description

```
template<class func_t = funct>class cern_root< func_t >
```

This class attempts to find  $x_1$  and  $x_2$  in  $[a, b]$  such that  $f(x_1)f(x_2) \leq 0$ ,  $|f(x_1)| \leq |f(x_2)|$ , and  $|x_1 - x_2| \leq 2 \text{ tol\_abs} (1 + |x_0|)$ . The function [solve\\_bkt\(\)](#) requires inputs `x1` and `x2` such that  $f(x_1)f(x_2) \leq 0$ .

The variable [cern\\_root::tol\\_abs](#) defaults to  $10^{-8}$  and [cern\\_root::ntrial](#) defaults to 200.

The function [solve\\_bkt\(\)](#) returns 0 for success, [gsl\\_einval](#) if the root is not initially bracketed, and [gsl\\_emaxiter](#) if the number of function evaluations is greater than [cern\\_root::ntrial](#).

Based on the CERNLIB routines RZEROX and DZEROX, which was based on [Bus75](#) and is documented at <http://wwwasdoc.web.cern.ch/wwwasdoc/shortwrupsdir/c200/top.html>

Definition at line 58 of file `cern_root.h`.

#### Public Member Functions

- int [set\\_mode](#) (int m)  
Set mode of solution (1 or 2)
- virtual const char \* [type](#) ()  
Return the type, "cern\_root".
- virtual int [solve\\_bkt](#) (double &x1, double x2, func\_t &func)  
Solve *func* in region  $x_1 < x < x_2$  returning  $x_1$ .

## Protected Member Functions

- double [sign](#) (double a, double b)  
*FORTTRAN-like function for sign.*

## Protected Attributes

- int [mode](#)  
*Internal storage for the mode.*

## 46.30.2 Member Function Documentation

46.30.2.1 `template<class func_t = func_t> int cern_root< func_t >::set_mode ( int m ) [inline]`

- 1 should be used for simple functions where the cost is inexpensive in comparison to one iteration of [solve\\_bkt\(\)](#), or functions which have a pole near the root (this is the default).
- 2 should be used for more time-consuming functions.

If an integer other than 1 or 2 is specified, the error handler is called.

Definition at line 100 of file `cern_root.h`.

46.30.2.2 `template<class func_t = func_t> virtual int cern_root< func_t >::solve_bkt ( double & x1, double x2, func_t & func ) [inline, virtual]`

The parameters `x1` and `x2` should be set so that  $f(x_1)f(x_2) \leq 0$  before calling [solve\\_bkt\(\)](#). If this is not the case, the error handler will be called and the solver will fail.

This function converges unless the number of iterations is larger than `root::ntrial`, in which case `root::last_conv` is set to `gsl_emaxiter` and the error handler is called if `root::err_nonconv` is true.

Implements `root_bkt< func_t >`.

Definition at line 125 of file `cern_root.h`.

## 46.30.3 Field Documentation

46.30.3.1 `template<class func_t = func_t> int cern_root< func_t >::mode [protected]`

This internal variable is actually defined to be smaller by 1 than the "mode" as it is defined in the CERNLIB documentation in order to avoid needless subtraction in [solve\\_bkt\(\)](#).

Definition at line 71 of file `cern_root.h`.

The documentation for this class was generated from the following file:

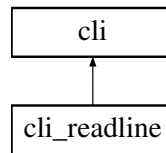
- `cern_root.h`

## 46.31 cli Class Reference

Configurable command-line interface.

```
#include <cli.h>
```

Inheritance diagram for cli:



#### 46.31.1 Detailed Description

This class is experimental.

Default commands: help, get/set, quit, exit, '!', verbose, license, warranty, alias, run.

Note that if the shell command is allowed (as it is by default) there are some potential security issues which are not solved here.

Commands which begin with a '#' character are ignored.

#### Note

In interactive mode, commands are limited to 300 characters.

**Todo** Long options cannot be one letter long, or else `process_args()` will fail, thus the class should throw if a long option with only one letter is given.

**Idea for Future** Warn in `run_interactive()` when extra parameters are given

**Idea for Future** Include a "remove command" function

**Idea for Future** A replace command function, there's already some code in cli.cpp for this.

**Idea for Future** There's some code duplication between `comm_option_run()` and `run_interactive()`

**Idea for Future** Allow the user to set the tilde string

**Idea for Future** Disallow direct access to `cli::par_list` in order to ensure parameter names do not contain whitespace

#### Concepts

As a matter of definition, the command-line arguments are simply called arguments. These arguments may be options (in which case they begin with either one dash or two) or parameters to these options. When run in interactive mode, these options are also commands.

Definition at line 230 of file cli.h.

#### Data Structures

- class `parameter`  
*Parameter for cli.*
- class `parameter_bool`  
*String parameter for cli.*
- class `parameter_double`  
*Double parameter for cli.*
- class `parameter_int`  
*Integer parameter for cli.*
- class `parameter_string`  
*String parameter for cli.*

## Public Member Functions

- int [set\\_function](#) ([comm\\_option\\_func\\_t](#) &usf)  
*Function to call when a `set` command is issued.*
- virtual char \* [cli\\_gets](#) (const char \*c)  
*The function which obtains input from the user.*
- int [call\\_args](#) (std::vector< [cmd\\_line\\_arg](#) > &ca)  
*Call functions corresponding to command-line args.*
- int [process\\_args](#) (int argv, char \*argv[], std::vector< [cmd\\_line\\_arg](#) > &ca, int debug=0)  
*Process command-line arguments from a const char array.*
- int [process\\_args](#) (std::string s, std::vector< [cmd\\_line\\_arg](#) > &ca, int debug=0)  
*Process command-line arguments from a string.*
- int [set\\_verbose](#) (int v)  
*Set verbosity.*
- int [run\\_interactive](#) ()  
*Run the interactive mode.*
- int [set\\_alias](#) (std::string alias, std::string str)  
*Set an alias `alias` for the string `str`.*
- std::string [get\\_alias](#) (std::string alias)  
*Set an alias `alias` for the string `str`.*

## Basic operation

- int [set\\_comm\\_option](#) ([comm\\_option\\_s](#) &ic)  
*Add a new command.*
- template<class vec\_t >  
int [set\\_comm\\_option\\_vec](#) (size\_t list\_size, vec\_t &option\_list)  
*Add a vector containing new commands/options.*
- int [set\\_param\\_help](#) (std::string param, std::string help)  
*Set one-line help text for a parameter named `param`.*
- int [run\\_auto](#) (int argv, char \*argv[])  
*Automatically parse arguments to main and call interactive mode if required.*

## Data Fields

- std::string [tilde\\_string](#)  
*String to replace tildes with.*
- bool [gnu\\_intro](#)  
*If true, output the usual GNU intro when [run\\_interactive\(\)](#) is called (default true).*
- bool [sync\\_verbose](#)  
*If true, then sync `cli::verbose`, with a parameter of the same name.*
- bool [shell\\_cmd\\_allowed](#)  
*If true, allow the user to use `!` to execute a shell command (default true)*
- std::string [prompt](#)  
*The prompt (default `"> "`)*
- std::string [desc](#)  
*A one- or two-line description (default is empty string)*
- std::string [cmd\\_name](#)  
*The name of the command.*
- std::string [addl\\_help\\_cmd](#)  
*Additional help text for interactive mode (default is empty string)*
- std::string [addl\\_help\\_cli](#)  
*Additional help text for command-line (default is empty string)*

## The default command objects

- [comm\\_option\\_s](#) [c\\_commands](#)
- [comm\\_option\\_s](#) [c\\_help](#)
- [comm\\_option\\_s](#) [c\\_quit](#)
- [comm\\_option\\_s](#) [c\\_exit](#)
- [comm\\_option\\_s](#) [c\\_license](#)

- `comm_option_s c_warranty`
- `comm_option_s c_set`
- `comm_option_s c_get`
- `comm_option_s c_run`
- `comm_option_s c_no_intro`
- `comm_option_s c_alias`

### Static Public Attributes

Value to indicate whether commands are also command-line options

- static const int `comm_option_command` = 0
- static const int `comm_option_cl_param` = 1
- static const int `comm_option_both` = 2

### Protected Member Functions

- int `output_param_list` ()  
*Output the parameter list.*
- int `expand_tilde` (std::vector< std::string > &sv)  
*Attempt to expand a tilde to a user's home directory.*
- int `apply_alias` (std::vector< std::string > &sv, std::string sold, std::string snw)  
*Replace all occurrences of *sold* with *snw* in *sv*.*
- int `separate` (std::string str, std::vector< std::string > &sv)  
*Separate a string into words, handling quotes.*
- bool `string_equal_dash` (std::string s1, std::string s2)  
*Compare two strings, treating dashes and underscores as equivalent.*

### The hard-coded command functions

- int `comm_option_alias` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_commands` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_get` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_help` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_license` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_no_intro` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_run` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_set` (std::vector< std::string > &sv, bool itive\_com)
- int `comm_option_warranty` (std::vector< std::string > &sv, bool itive\_com)

### Protected Attributes

- int `verbose`  
*Control screen output.*
- char `buf` [300]  
*Storage for getline.*
- `comm_option_func` \* `user_set_func`  
*Storage for the function to call after setting a parameter.*
- std::vector< `comm_option_s` > `clist`  
*List of commands.*

### Help for parameters

- std::vector< std::string > `ph_name`
- std::vector< std::string > `ph_desc`

### Parameter storage and associated iterator type

- typedef std::map< std::string, `parameter` \*, `string_comp` > ::iterator `par_t`  
*List iterator.*
- std::map< std::string, `parameter` \*, `string_comp` > `par_list`  
*Parameter list.*



## Aliases

- typedef std::map< std::string, std::string, [string\\_comp](#) > ::iterator **al\_it**
- std::map< std::string, std::string, [string\\_comp](#) > **als**

## 46.31.2 Member Function Documentation

46.31.2.1 int cli::expand\_tilde ( std::vector< std::string > & sv ) [protected]

Experimental and currently unused.

46.31.2.2 int cli::separate ( std::string str, std::vector< std::string > & sv ) [protected]

This function separates a string into words, and handles words that begin with a "</tt>" by adding more words until finding one which ends with another <tt>".

This is used to reformat command descriptions and help text for the screen width in comm\_option\_help(), to process lines read from a file in comm\_option\_run(), and to process input in [run\\_interactive\(\)](#).

## Note

This function does not understand nested quotes.

46.31.2.3 int cli::set\_comm\_option ( comm\_option\_s & ic )

Each command/option must have either a short form in [comm\\_option\\_s::shrt](#) or a long from in [comm\\_option\\_s::lng](#), which is unique from the other commands/options already present. You cannot add two commands/options with the same short form, even if they have different long forms, and vice versa.

46.31.2.4 virtual char\* cli::cli\_gets ( const char \* c ) [virtual]

**Idea for Future** Think about whether or not this should be protected? (Possibly not, as it's extensively used by acolm.cpp)

Reimplemented in [cli\\_readline](#).

46.31.2.5 int cli::process\_args ( int argv, char \* argc[], std::vector< cmd\_line\_arg > & ca, int debug = 0 )

This doesn't actually execute the functions for the corresponding options, but simply processes the parameters argv and argc and packs the information into ca.

This function assumes that argc[0] just contains the name of the command, and should thus be ignored.

46.31.2.6 int cli::process\_args ( std::string s, std::vector< cmd\_line\_arg > & ca, int debug = 0 )

**Todo** There's a typecast in this function to (char \*) from (const char \*) which needs reworking.

46.31.2.7 int cli::set\_verbose ( int v )

Most errors are output to the screen even if verbose is zero.

46.31.2.8 int cli::set\_alias ( std::string alias, std::string str )

Aliases can also be set using the command 'alias', but that version allows only one-word aliases.

46.31.2.9 std::string cli::get\_alias ( std::string alias )

Aliases can also be set using the command 'alias', but that version allows only one-word aliases.

## 46.31.3 Field Documentation

## 46.31.3.1 bool cli::gnu\_intro

In order to conform to GNU standards, this ought not be set to false by default.

Definition at line 440 of file cli.h.

The documentation for this class was generated from the following file:

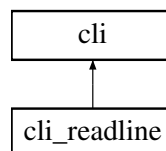
- cli.h

## 46.32 cli\_readline Class Reference

An extension to [cli](#) which uses readline.

```
#include <cli_readline.h>
```

Inheritance diagram for cli\_readline:



## 46.32.1 Detailed Description

This header-only class requires the GNU `readline` library for use, but is not referenced by `O2scl` code at the moment to make the library usable without `readline`.

Definition at line 42 of file cli\_readline.h.

## Public Member Functions

- **cli\_readline** (std::string fname=".cli\_hist", size\_t max\_size=100)
- virtual char \* [cli\\_gets](#) (const char \*c)  
*Function to get a string from the user.*

## Protected Attributes

- char \* [line\\_read](#)  
*Buffer for readline.*
- std::string [histfile](#)  
*String containing filename.*
- size\_t [msize](#)  
*Maximum history file size.*

## 46.32.2 Member Function Documentation

## 46.32.2.1 virtual char\* cli\_readline::cli\_gets ( const char \* c ) [inline, virtual]

Reimplemented from [cli](#).

Definition at line 77 of file cli\_readline.h.

The documentation for this class was generated from the following file:

- cli\_readline.h

## 46.33 cmd\_line\_arg Struct Reference

A command-line argument for [cli](#).

```
#include <cli.h>
```

### 46.33.1 Detailed Description

This is the internal structure that [cli](#) uses to package command-line arguments.

Definition at line 179 of file cli.h.

#### Data Fields

- [std::string](#) [arg](#)  
*The argument.*
- [bool](#) [is\\_option](#)  
*Is an option?*
- [bool](#) [is\\_valid](#)  
*Is a properly formatted option.*
- [std::vector< std::string >](#) [parms](#)  
*List of parameters (empty, unless it's an option)*
- [comm\\_option\\_s](#) \* [cop](#)  
*A pointer to the appropriate option (0, unless it's an option)*

The documentation for this struct was generated from the following file:

- cli.h

## 46.34 table::col\_s Struct Reference

Column structure for [table](#) [protected].

```
#include <table.h>
```

### 46.34.1 Detailed Description

This struct is used internally by [table](#) to organize the columns and need not be instantiated by the casual end-user.

Definition at line 1001 of file table.h.

#### Data Fields

- [ovector\\_base](#) \* [dat](#)  
*Pointer to column.*
  - [bool](#) [owner](#)  
*Owner of column.*
  - [int](#) [index](#)  
*Column index.*
-

The documentation for this struct was generated from the following file:

- `table.h`

## 46.35 columnify Class Reference

Create nicely formatted columns from a table of strings.

```
#include <columnify.h>
```

### 46.35.1 Detailed Description

This is a brute-force approach of order  $\text{ncols} \times \text{nrows}$ . The column widths and spacings of are computed by exhaustively examining all strings in every column.

**Idea for Future** Move the `screenify()` functionality from `misc.h` into this class?

**Idea for Future** It might be better to allow the string table to be specified with iterators.

Definition at line 51 of file `columnify.h`.

### Public Member Functions

- `template<class mat_string_t, class vec_string_t, class vec_int_t >`  
`int align (const mat_string_t &table, size_t ncols, size_t nrows, vec_string_t &ctable, vec_int_t &align_spec)`  
*Take `table` and create a new object `ctable` with appropriately formatted columns.*

### Static Public Attributes

- static const int `align_left` = 1  
*Align the left-hand sides.*
- static const int `align_right` = 2  
*Align the right-hand sides.*
- static const int `align_lmid` = 3  
*Center, slightly to the left if spacing is uneven.*
- static const int `align_rmid` = 4  
*Center, slightly to the right if spacing is uneven.*
- static const int `align_dp` = 5  
*Align with decimal points.*
- static const int `align_lnum` = 6  
*Align negative numbers to the left and use a space for positive numbers.*

### 46.35.2 Member Function Documentation

**46.35.2.1** `template<class mat_string_t, class vec_string_t, class vec_int_t > int columnify::align ( const mat_string_t & table, size_t ncols, size_t nrows, vec_string_t & ctable, vec_int_t & align_spec ) [inline]`

The table of strings should be stored in `table` in "column-major" order (`table[ncols][nrows]`), so that `table` has the interpretation of a set of columns to be aligned. Before calling `align()`, `ctable` should be allocated so that at least the first `nrows` entries can be assigned, and `align_spec` should contain `ncols` entries specifying the style of alignment for each column.

The first argument can be any type which is accessible using two applications of `operator[]`, such as `string **`, `vector<string>[]`, or `vector<vector<string>>`

Definition at line 90 of file columnify.h.

The documentation for this class was generated from the following file:

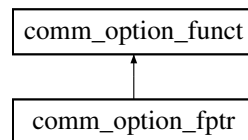
- [columnify.h](#)

## 46.36 comm\_option\_fptr Class Reference

Function pointer for [cli](#) command function.

```
#include <cli.h>
```

Inheritance diagram for comm\_option\_fptr:



### 46.36.1 Detailed Description

Definition at line 57 of file cli.h.

#### Public Member Functions

- [comm\\_option\\_fptr](#) (int(\*fp)(std::vector< std::string > &, bool))  
*Create from a member function pointer from the specified class.*
- virtual int [operator\(\)](#) (std::vector< std::string > &cstr, bool itive\_com)  
*The basic function called by [cli](#).*

#### Protected Member Functions

- [comm\\_option\\_fptr](#) & [operator=](#) (const [comm\\_option\\_fptr](#) &f)  
*Copy constructor.*

#### Protected Attributes

- int(\* [fptr](#)) (std::vector< std::string > &cstr, bool itive\_com)  
*The pointer to the member function.*

The documentation for this class was generated from the following file:

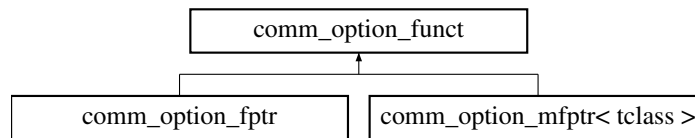
- [cli.h](#)

## 46.37 comm\_option\_func Class Reference

Base for [cli](#) command function.

```
#include <cli.h>
```

Inheritance diagram for comm\_option\_func:



#### 46.37.1 Detailed Description

See the [cli](#) class for more details.

Definition at line 43 of file cli.h.

#### Public Member Functions

- virtual int [operator\(\)](#) (std::vector< std::string > &cstr, bool itive\_com)=0  
*The basic function called by [cli](#).*

The documentation for this class was generated from the following file:

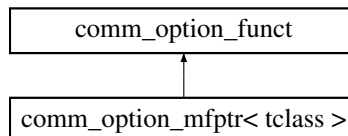
- cli.h

### 46.38 comm\_option\_mfptr< tclass > Class Template Reference

Member function pointer for [cli](#) command function.

```
#include <cli.h>
```

Inheritance diagram for comm\_option\_mfptr< tclass >:



#### 46.38.1 Detailed Description

```
template<class tclass>class comm_option_mfptr< tclass >
```

Definition at line 96 of file cli.h.

#### Public Member Functions

- [comm\\_option\\_mfptr](#) (tclass \*tp, int(tclass::\*fp)(std::vector< std::string > &, bool))  
*Create from a member function pointer from the specified class.*
- virtual int [operator\(\)](#) (std::vector< std::string > &cstr, bool itive\_com)  
*The basic function called by [cli](#).*

#### Protected Member Functions

- [comm\\_option\\_mfptr](#) (const [comm\\_option\\_mfptr](#) &f)

*Copy constructor:*

- `comm_option_mfptr` & `operator=` (const `comm_option_mfptr` &f)  
*Copy constructor:*

#### Protected Attributes

- `int(tclass::* fptr)(std::vector< std::string > &cstr, bool itive_com)`  
*The pointer to the member function.*
- `tclass * tptr`  
*The pointer to the class.*

The documentation for this class was generated from the following file:

- `cli.h`

## 46.39 comm\_option\_s Struct Reference

Command for interactive mode in `cli`.

```
#include <cli.h>
```

### 46.39.1 Detailed Description

See the `cli` class for more details.

Definition at line 151 of file `cli.h`.

#### Data Fields

- `char shrt`  
*Short option ( ' \0 ' for none, must be unique if present)*
- `std::string lng`  
*Long option (must be specified and must be unique)*
- `std::string desc`  
*Description for help.*
- `int min_parms`  
*Minimum number of parameters (0 for none, -1 for variable)*
- `int max_parms`  
*Maximum number of parameters (0 for none, -1 for variable)*
- `std::string parm_desc`  
*Description of parameters.*
- `std::string help`  
*The help description.*
- `comm_option_func * func`  
*The pointer to the function to be called (or 0 for no function)*
- `int type`  
*Type: command-line parameter, command, or both.*

The documentation for this struct was generated from the following file:

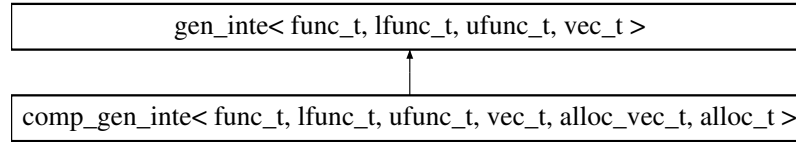
- `cli.h`

## 46.40 comp\_gen\_inte&lt; func\_t, lfunc\_t, ufunc\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Naive generalized multi-dimensional integration.

```
#include <comp_gen_inte.h>
```

Inheritance diagram for comp\_gen\_inte< func\_t, lfunc\_t, ufunc\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



## 46.40.1 Detailed Description

```
template<class func_t, class lfunc_t = func_t, class ufunc_t = func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_-alloc>class comp_gen_inte< func_t, lfunc_t, ufunc_t, vec_t, alloc_vec_t, alloc_t >
```

Naively combine several one-dimensional integration objects from class inte in order to perform a multi-dimensional integration. The integration routines are specified in the function set\_ptrs().

The integration routines are called in order of the index specified in the function [set\\_oned\\_inte\(\)](#). For  $n$ -dimensional integration,  $n$  one-dimensional integration objects should be specified, with indexes 0 through  $n-1$ . The integration routines are called in order of their index, so that the outermost integration is done by the routine specified with index 0. The integral performed is:

$$\int_{x_0=a_0}^{x_0=b_0} f(x_0) \int_{x_1=a_1(x_0)}^{x_1=b_1(x_0)} f(x_0, x_1) \dots \int_{x_{n-1}=a_{n-1}(x_0, x_1, \dots, x_{n-2})}^{x_{n-1}=b_{n-1}(x_0, x_1, \dots, x_{n-2})} f(x_0, x_1, \dots, x_{n-1}) dx_{n-1} \dots dx_1 dx_0$$

This class is particularly useful if  $f_0$  is time-consuming to evaluate, and separable from  $f_{n-1}$ .

See the discussion about the functions `func`, `lower` and `upper` in the documentation for the class [gen\\_inte](#).

No error estimate is performed. Error estimation for multiple dimension integrals is provided by the Monte Carlo integration classes (see [mcarlo\\_inte](#)).

**Idea for Future** Provide an example of usage for this class.

Definition at line 73 of file `comp_gen_inte.h`.

## Public Member Functions

- int [set\\_oned\\_inte](#) (inte< [func\\_t](#) > &it, size\_t i)  
*Set the one-dimensional integration object with index i.*
- virtual double [ginteg](#) (func\_t &func, size\_t n, func\_t &lower, func\_t &upper)  
*Integrate function  $f_{unc}$  from  $\ell_i = f_i(x_i)$  to  $u_i = g_i(x_i)$  for  $0 < i < n-1$ .*
- virtual const char \* [type](#) ()  
*Return string denoting type ("comp\_gen\_inte")*

## Data Fields

- size\_t [max\\_dim](#)  
*The maximum number of integration dimensions (default 100)*



## Protected Member Functions

- double [odfunc](#) (double x, size\_t &ix)  
*The one-dimensional integration function.*

## Protected Attributes

- alloc\_vec\_t \* [cx](#)  
*The independent variable vector.*
- lfunc\_t \* [lowerp](#)  
*The function specifying the lower limits.*
- ufunc\_t \* [upperp](#)  
*The function specifying the upper limits.*
- func\_t \* [mf](#)  
*The function to be integrated.*
- size\_t [ndim](#)  
*The number of dimensions.*
- alloc\_t [ao](#)  
*Memory allocator for objects of type alloc\_vec\_t.*
- size\_t [nint](#)  
*The size of the integration object arrays.*
- [inte](#)< [func\\_t](#) > \*\* [iptrs](#)  
*Pointers to the integration objects.*
- bool \* [tptrs](#)  
*Flag indicating if integration object has been set.*

The documentation for this class was generated from the following file:

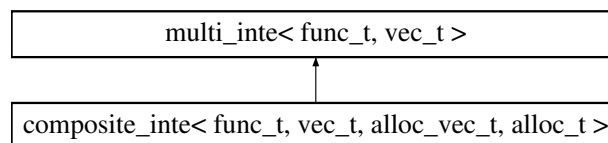
- [comp\\_gen\\_inte.h](#)

## 46.41 composite\_inte&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Naive multi-dimensional integration over a hypercube.

```
#include <composite_inte.h>
```

Inheritance diagram for composite\_inte< func\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



## 46.41.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>class composite_inte<
func_t, vec_t, alloc_vec_t, alloc_t >
```

Naively combine several one-dimensional integration objects from class [inte](#) in order to perform a multi-dimensional integration over a region defined by constant limits. For more general regions of integration, use children of the class [gen\\_inte](#).

The 1-dimensional integration routines are specified in the function [set\\_oned\\_inte\(\)](#).

The integration routines are called in order of the index specified in the function `set_oned_inte()`. For  $n$ -dimensional integration,  $n$  one-dimensional integration objects should be specified, with indexes 0 through  $n-1$ . The integration routines are called in order of their index, so that the outermost integration is done by the routine specified with index 0.

$$\int_{x_0=a_0}^{x_0=b_0} \int_{x_1=a_1}^{x_1=b_1} \dots \int_{x_{n-1}=a_{n-1}}^{x_{n-1}=b_{n-1}} f(x_0, x_1, \dots, x_n)$$

No error estimate is performed. Error estimation for multiple dimension integrals is provided by the Monte Carlo integration classes (see `mcarlo_inte`).

**Idea for Future** Create a function to set an entire array of one-dimensional integration objects at once

Definition at line 69 of file `composite_inte.h`.

#### Public Member Functions

- int `set_oned_inte` (`inte`< `func_t` > &`it`, `size_t` `i`)  
*Set the one-dimensional integration object with index  $i$ .*
- virtual int `minteg_err` (`func_t` &`func`, `size_t` `n`, const `vec_t` &`a`, const `vec_t` &`b`, double &`res`, double &`err`)  
*Integrate function `func` over the hypercube from  $x_i = a_i$  to  $x_i = b_i$  for  $0 < i < ndim-1$ .*
- virtual const char \* `type` ()  
*Return string denoting type ("composite\_inte")*

#### Data Fields

- `size_t` `max_dim`  
*The maximum number of integration dimensions (default 100)*

#### Protected Member Functions

- double `odfunc` (double `x`, `size_t` &`ix`)  
*The one-dimensional integration function.*

#### Protected Attributes

- const `vec_t` \* `ax`  
*The user-specified upper limits.*
- const `vec_t` \* `bx`  
*The user-specified lower limits.*
- `alloc_vec_t` \* `cx`  
*The independent variable vector.*
- `func_t` \* `mf`  
*The user-specified function.*
- `size_t` `ndim`  
*The user-specified number of dimensions.*
- `alloc_t` `ao`  
*Memory allocator for objects of type `alloc_vec_t`.*
- `size_t` `nint`  
*The size of the integration object arrays.*
- `inte`< `func_t` > \*\* `iptrs`  
*Pointers to the integration objects.*
- bool \* `tptrs`  
*Flag indicating if integration object has been set.*

## 46.41.2 Member Function Documentation

46.41.2.1 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int composite_inte< func_t, vec_t, alloc_vec_t, alloc_t >::minteg_err ( func_t & func, size_t n, const vec_t & a, const vec_t & b, double & res, double & err ) [inline, virtual]`

The function `set_oned_inte()` must be used first to set the one-dimensional routines to use.

Implements `multi_inte< func_t, vec_t >`.

Definition at line 155 of file `composite_inte.h`.

46.41.2.2 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double composite_inte< func_t, vec_t, alloc_vec_t, alloc_t >::odfunc ( double x, size_t & ix ) [inline, protected]`

This function to send to the integrators

Definition at line 209 of file `composite_inte.h`.

The documentation for this class was generated from the following file:

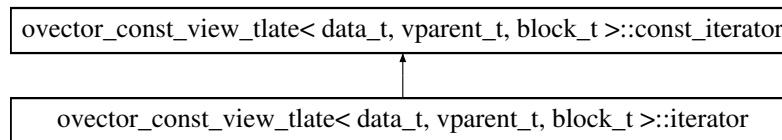
- `composite_inte.h`

## 46.42 ovector\_const\_view\_tlate&lt; data\_t, vparent\_t, block\_t &gt;::const\_iterator Class Reference

A const iterator for ovector.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_const_view_tlate< data_t, vparent_t, block_t >::const_iterator`:



## 46.42.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_view_tlate< data_t, vparent_t, block_t >::const_iterator
```

## Note

Experimental.

**Todo** Default constructor and iterator typedefs

Definition at line 123 of file `ovector_tlate.h`.

## Public Member Functions

- `const_iterator` (const `iterator` &it)  
*Copy-constructor for a const iterator.*
- bool `operator==` (const `const_iterator` &it) const  
*Equality.*
- bool `operator!=` (const `const_iterator` &it) const  
*Inequality.*

- `bool operator!= (const iterator &it) const`  
*Inequality.*
- `bool operator< (const const_iterator &it) const`  
*Less than.*
- `bool operator> (const const_iterator &it) const`  
*Greater than.*
- `const_iterator operator++ ()`  
*Prefix increment.*
- `const_iterator operator-- ()`  
*Prefix decrement.*
- `const_iterator operator++ (int)`  
*Postfix increment.*
- `const_iterator operator-- (int)`  
*Postfix decrement.*
- `const data_t operator* () const`  
*Dereference - return the corresponding vector element.*
- `const_iterator operator+= (size_t n)`  
*Move forward.*
- `const_iterator operator-= (size_t n)`  
*Move backwards.*

#### Protected Member Functions

- `const_iterator (data_t *p, size_t s)`  
*Internally create an iterator directly from a pointer.*

#### Protected Attributes

- `data_t * dp`  
*Pointer to current.*
- `size_t stride`  
*Stride.*

#### Friends

- `class ovector_const_view_tlate< data_t, vparent_t, block_t >`  
*Grant access to ovector classes for `begin()` and `end()` functions.*
- `class ovector_base_tlate< data_t, vparent_t, block_t >`  
*Grant access to ovector classes for `begin()` and `end()` functions.*

The documentation for this class was generated from the following file:

- `ovector_tlate.h`

## 46.43 contour Class Reference

Calculate contour lines from a two-dimensional data set.

```
#include <contour.h>
```

### 46.43.1 Detailed Description

#### Basic Usage

- Specify the data as a two-dimensional square grid of "heights" with `set_data()`.

- Specify the contour levels with [set\\_levels\(\)](#).
- Compute the contours with [calc\\_contours\(\)](#)

The contours are generated as a series of x- and y-coordinates, defining a line. If the contour is closed, then the first and the last set of coordinates will be equal.

The storage of the matrix to be specified in the function [set\\_data\(\)](#) and this function is designed to follow the format:

	$x_0$	$x_1$	$x_2$
$y_0$	$M_{00}$	$M_{01}$	$M_{02}$
$y_1$	$M_{10}$	$M_{11}$	$M_{12}$
$y_2$	$M_{20}$	$M_{21}$	$M_{22}$

thus the matrix should be  $M[i][j]$  where  $i$  is the y index and  $j$  is the row index. (See also the discussion in the User's guide in the section called [Rows and columns vs. x and y.](#))

The data is copied by [set\\_data\(\)](#), so changing the data will not change the contours unless [set\\_data\(\)](#) is called again. The functions [set\\_levels\(\)](#) and [calc\(\)](#) can be called several times for the same data without calling [set\\_data\(\)](#) again.

Note that in order to simplify the algorithm for computing contour lines, the [calc\\_contours\(\)](#) function will adjust the user-specified contour levels slightly in order to ensure that no contour line passes exactly through any data point on the grid. The contours are adjusted by multiplying the original contour level by 1 plus a small number ( $10^{-8}$  by default), which is specified in [lev\\_adjust](#).

Linear interpolation is used to decide whether or not a line segment and a contour cross. This choice is intentional, since (in addition to making the algorithm much simpler) it is the user (and not the class) which is likely best able to refine the data. In case a simple refinement scheme is desired, the method [regrid\\_data\(\)](#) is provided which refines the data for any interpolation type.

Since linear interpolation is used, the contour calculation implicitly assumes that there is not more than one intersection of any contour level with any line segment. For contours which do not close inside the region of interest, the results will always end at either the minimum or maximum values of the x or y grid points (no extrapolation is ever done). Note also that the points defining the contour are not necessarily equally spaced, but two neighboring points will never be farther apart than the distance across opposite corners of one cell in the grid.

#### The Algorithm:

This works by viewing the data as defining a square two-dimensional grid. The function [calc\\_contours\(\)](#) exhaustively enumerates every line segment in the grid which involves a level crossing and then organizes the points defined by the intersection of a line segment with a level curve into a full contour.

**Idea for Future** Rewrite the code which adjusts the contour levels to ensure contours don't go through the data to adjust the internal copy of the data instead.

**Idea for Future** It would be nice to have a function which creates a set of closed regions to fill which represent the data. However, this likely requires a completely new algorithm, because it's not easy to simply close the contours already generated by the [calc\\_contours\(\)](#) function. There are, for example, several cases which are difficult to handle, such as filling a region in between several closed contours.

Definition at line 172 of file contour.h.

#### Public Member Functions

##### Basic usage

- `template<class vec_t, class mat_t >`  
`int set_data (size_t sizex, size_t sizey, const vec_t &x_fun, const vec_t &y_fun, const mat_t &udata)`  
*Set the data.*
- `template<class vec_t >`  
`int set_levels (size_t nlevels, vec_t &ulevels)`  
*Set the contour levels.*
- `int calc_contours (std::vector< contour_line > &clines, bool debug=false)`  
*Calculate the contours.*

**Regrid function**

- int `regrid_data` (size\_t xfact, size\_t yfact, `base_interp_mgr`< `ovector_const_view` > &bim1, `base_interp_mgr`< `ovector_const_subvector` > &bim2)  
*Regrid the data.*

**Obtain internal data**

- int `get_data` (size\_t &size\_x, size\_t &size\_y, `ovector` \*&x\_fun, `ovector` \*&y\_fun, `omatrix` \*&udata)  
*Get the data.*
- int `get_edges` (std::vector< `edge_crossings` > &rt\_edges, std::vector< `edge_crossings` > &bm\_edges)  
*Return the edges.*
- int `print_edges` (`edge_crossings` &right, `edge_crossings` &bottom)  
*Print out the edges to cout.*

**Data Fields**

- int `verbose`  
*Verbosity parameter.*
- double `lev_adjust`  
*(default  $10^{-8}$ )*

**Protected Member Functions**

- int `find_next_point_right` (int j, int k, int &jnext, int &knext, int &dir\_next, int nsw, `edge_crossings` &right, `edge_crossings` &bottom)  
*Find next point starting from a point on a right edge.*
- int `find_next_point_bottom` (int j, int k, int &jnext, int &knext, int &dir\_next, int nsw, `edge_crossings` &right, `edge_crossings` &bottom)  
*Find next point starting from a point on a bottom edge.*
- int `find_intersections` (size\_t ilev, double &level, `edge_crossings` &right, `edge_crossings` &bottom)  
*Find all of the intersections of the edges with the contour level.*
- int `right_edges` (double level, `o2scl::sm_interp` \*si, `edge_crossings` &right)  
*Interpolate all right edge crossings.*
- int `bottom_edges` (double level, `o2scl::sm_interp` \*si, `edge_crossings` &bottom)  
*Interpolate all bottom edge crossings.*
- int `process_line` (int j, int k, int dir, `ovector` &x, `ovector` &y, bool first, `edge_crossings` &right, `edge_crossings` &bottom)  
*Create a contour line from a starting edge.*
- int `check_data` ()  
*Check to ensure the x- and y-arrays are monotonic.*

**Protected Attributes**

- std::vector< `edge_crossings` > `red`  
*Right edge list.*
- std::vector< `edge_crossings` > `bed`  
*Bottom edge list.*

**User-specified data**

- int `nx`
- int `ny`
- `ovector` `xfun`
- `ovector` `yfun`
- `omatrix` `data`

**User-specified contour levels**

- int `nlev`
- `ovector` `levels`
- bool `levels_set`

## Static Protected Attributes

## Edge direction

- static const int **dright** = 0
- static const int **dbottom** = 1

## Edge status

- static const int **empty** = 0
- static const int **edge** = 1
- static const int **contourp** = 2
- static const int **endpoint** = 3

## Edge found or not found

- static const int **efound** = 1
- static const int **enot\_found** = 0

## 46.43.2 Member Function Documentation

46.43.2.1 `template<class vec_t, class mat_t> int contour::set_data ( size_t sizex, size_t sizey, const vec_t & x_fun, const vec_t & y_fun, const mat_t & udata ) [inline]`

The types `vec_t` and `mat_t` can be any types which have `operator[]` and `operator[][]` for array and matrix indexing.

Note that this method copies all of the user-specified data to local storage so that changes in the data after calling this function will not be reflected in the contours that are generated.

Definition at line 194 of file `contour.h`.

46.43.2.2 `template<class vec_t> int contour::set_levels ( size_t nlevels, vec_t & ulevels ) [inline]`

This is separate from the function `calc_contours()` so that the user can compute the contours for different data sets using the same levels.

Definition at line 224 of file `contour.h`.

46.43.2.3 `int contour::calc_contours ( std::vector< contour_line> & clines, bool debug = false )`

The function `calc_contours()` returns the total number of contours found. Since there may be more than one disconnected contours for the same contour level, or no contours for a given level, the total number of contours may be less than or greater than the number of levels given by `set_levels()`.

If an error occurs, zero is returned.

46.43.2.4 `int contour::regrid_data ( size_t xfact, size_t yfact, base_interp_mgr< ovector_const_view> & bim1, base_interp_mgr< ovector_const_subvector> & bim2 )`

Use interpolation to refine the data set. This can be called before `calc_contours()` in order to make the contour levels smoother by providing a smaller grid size. If the original number of data points is  $(nx, ny)$ , then the new number of data points is

$$(xfact (nx - 1) + 1, yfact (ny - 1) + 1)$$

The parameters `xfact` and `yfact` must both be larger than zero and they cannot both be 1.

46.43.2.5 `int contour::get_data ( size_t & sizex, size_t & sizey, ovector *& x_fun, ovector *& y_fun, ovector *& udata ) [inline]`

This is useful to see how the data has changed after a call to `regrid_data()`.

**Idea for Future** There is probably a better way than returning pointers to the internal data.

Definition at line 280 of file `contour.h`.

The documentation for this class was generated from the following file:

- `contour.h`

## 46.44 `contour_line` Class Reference

A contour line.

```
#include <contour.h>
```

### 46.44.1 Detailed Description

The contour lines generated by the `contour` class are given as objects of this type.

**Idea for Future** Write HDF I/O for contour lines?

**Idea for Future** Make this a subclass of `contour`.

Definition at line 43 of file `contour.h`.

#### Public Member Functions

- `contour_line()`  
*Create an empty line.*
- `contour_line(const contour_line &c)`  
*Copy constructor for STL allocator.*

#### Data Fields

- double `level`  
*The contour level.*
- `ovector x`  
*The line x coordinates.*
- `ovector y`  
*The line y coordinates.*

The documentation for this class was generated from the following file:

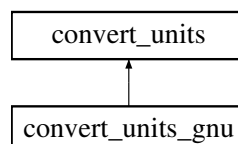
- `contour.h`

## 46.45 `convert_units` Class Reference

Convert units.

```
#include <convert_units.h>
```

Inheritance diagram for `convert_units`:





## 46.45.1 Detailed Description

Allow the user to convert between two different units after specifying a conversion factor. This class will also automatically combine two conversion factors to create a new unit conversion (but it cannot combine more than two).

Conversions are performed by the `convert()` function and the conversion factors must be specified beforehand using the `insert_cache()` function.

If the GNU units command is not in the local path, the user may modify `units_cmd_string` to specify the full pathname. One can also modify `units_cmd_string` to specify a different `units.dat` file.

Example:

```
convert_units cu;
cu.insert_cache("in", "cm", 2.54);
cout << "12 in is " << cu.convert("in", "cm", 12.0) << " cm. " << endl;
```

## Note

Combining two conversions allows for some surprising apparent contradictions from numerical precision errors. If there are two matching unit conversion pairs which give the same requested conversion factor, then one can arrange a situation where the same conversion factor is reported with slightly different values after adding a related conversion to the table. One way to fix this is to force the class not to combine two conversions by setting `combine_two_conv` to false. Alternatively, one can ensure that no combination is necessary by manually adding the desired combination conversion to the cache after it is first computed.

**Idea for Future** Ideally, a real C++ API for the GNU units command would be better.

Definition at line 78 of file `convert_units.h`.

## Data Structures

- struct `unit_t`  
*The type for caching unit conversions.*

## Public Member Functions

- virtual double `convert` (std::string from, std::string to, double val)  
*Return the value `val` after converting using units `from` and `to`.*
- int `insert_cache` (std::string from, std::string to, double conv)  
*Manually insert a unit conversion into the cache.*
- int `remove_cache` (std::string from, std::string to)  
*Manually remove a unit conversion into the cache.*
- int `print_cache` ()  
*Print the present unit cache to std::cout.*
- int `energy_conv` ()  
*Add conversion factors for energy equivalents.*

## Data Fields

- int `verbose`  
*Verbosity (default 0)*
- bool `use_gnu_units`  
*(default true)*
- bool `err_on_fail`  
*(default true)*
- bool `combine_two_conv`  
*If true, allow combinations of two conversions (default true)*
- std::string `units_cmd_string`  
*Default 'units'.*

## Protected Types

- typedef std::map< std::string, [unit\\_t](#), [string\\_comp](#) > ::iterator [miter](#)  
*The iterator type.*

## Protected Attributes

- std::map< std::string, [unit\\_t](#), [string\\_comp](#) > [mcache](#)  
*The cache where unit conversions are stored.*

The documentation for this class was generated from the following file:

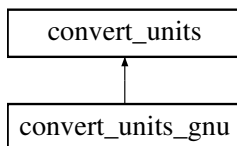
- [convert\\_units.h](#)

## 46.46 convert\_units\_gnu Class Reference

Convert units using a system call to GNU units.

```
#include <convert_units_gnu.h>
```

Inheritance diagram for `convert_units_gnu`:



## 46.46.1 Detailed Description

Experimental.

Definition at line 43 of file `convert_units_gnu.h`.

## Public Member Functions

- virtual double [convert](#) (std::string from, std::string to, double val)  
*Return the value `val` after converting using units `from` and `to`.*
- int [make\\_units\\_dat](#) (std::string fname, bool c\_1=false, bool hbar\_1=false, bool K\_1=false)  
*Make a GNU `units.dat` file from the GSL constants.*

## Data Fields

Strings to form `\c` units command

- std::string [prefix](#)
- std::string [midfix](#)
- std::string [suffix](#)

## 46.46.2 Member Function Documentation

46.46.2.1 `int convert_units_gnu::make_units_dat ( std::string fname, bool c_1 = false, bool hbar_1 = false, bool K_1 = false )`  
`[inline]`

If `c_1` is true, then the second is defined in terms of meters so that the speed of light is unitless. If `hbar_1` is true, then the kilogram is defined in terms of  $s/m^2$  so that  $\hbar$  is unitless.

## Note

Not all of the GSL constants or the canonical GNU units conversions are given here.

Definition at line 204 of file `convert_units_gnu.h`.

The documentation for this class was generated from the following file:

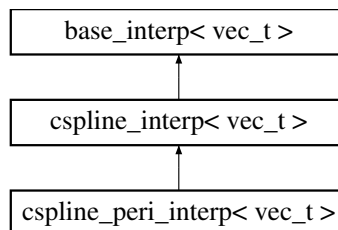
- `convert_units_gnu.h`

## 46.47 cspline\_interp&lt; vec\_t &gt; Class Template Reference

Cubic spline interpolation (GSL)

```
#include <interp.h>
```

Inheritance diagram for `cspline_interp< vec_t >`:



## 46.47.1 Detailed Description

```
template<class vec_t>class cspline_interp< vec_t >
```

By default, this class uses natural boundary conditions, where the second derivative vanishes at each end point. Extrapolation effectively assumes that the second derivative is linear outside of the endpoints.

Definition at line 300 of file `interp.h`.

## Public Member Functions

- `cspline_interp ()`  
*Create a base interpolation object with natural or periodic boundary conditions.*
- virtual int `allocate` (size\_t size)  
*Allocate memory, assuming x and y have size size.*
- virtual int `init` (const vec\_t &xa, const vec\_t &ya, size\_t size)  
*Initialize interpolation routine.*
- virtual int `free` ()  
*Free allocated memory.*
- virtual int `interp` (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double x, double &y)  
*Give the value of the function  $y(x = x_0)$ .*

- virtual int [deriv](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double x, double &dydx)  
*Give the value of the derivative  $y'(x=x_0)$ .*
- virtual int [deriv2](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double x, double &d2ydx2)  
*Give the value of the second derivative  $y''(x=x_0)$ .*
- virtual int [integ](#) (const vec\_t &x\_array, const vec\_t &y\_array, size\_t size, double a, double b, double &result)  
*Give the value of the integral  $\int_a^b y(x) dx$ .*
- virtual const char \* [type](#) ()  
*Return the type, "cspline\_interp".*

#### Protected Member Functions

- void [coeff\\_calc](#) (const double c\_array[], double dy, double dx, size\_t index, double \*b, double \*c2, double \*d)  
*Compute coefficients for cubic spline interpolation.*

#### Protected Attributes

- [o2scl\\_linalg::uvector\\_4\\_mem p4m](#)  
*Memory for the tridiagonalization.*

#### Storage for cubic spline interpolation

- double \* **c**
- double \* **g**
- double \* **diag**
- double \* **offdiag**

#### Private Member Functions

- [cspline\\_interp](#) (const [cspline\\_interp](#)< vec\_t > &)
- [cspline\\_interp](#)< vec\_t > & **operator=** (const [cspline\\_interp](#)< vec\_t > &)

#### 46.47.2 Member Function Documentation

46.47.2.1 `template<class vec_t> virtual int cspline_interp< vec_t >::init ( const vec_t & xa, const vec_t & ya, size_t size ) [inline, virtual]`

Natural boundary conditions

Reimplemented from [base\\_interp< vec\\_t >](#).

Reimplemented in [cspline\\_peri\\_interp< vec\\_t >](#).

Definition at line 383 of file `interp.h`.

The documentation for this class was generated from the following file:

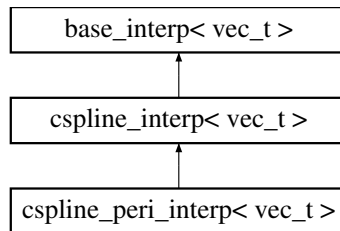
- `interp.h`

## 46.48 cspline\_peri\_interp< vec\_t > Class Template Reference

Cubic spline interpolation with periodic boundary conditions (GSL)

```
#include <interp.h>
```

Inheritance diagram for [cspline\\_peri\\_interp< vec\\_t >](#):



#### 46.48.1 Detailed Description

template<class vec\_t>class cspline\_peri\_interp< vec\_t >

Definition at line 593 of file interp.h.

##### Public Member Functions

- virtual int [allocate](#) (size\_t size)  
*Allocate memory, assuming x and y have size size.*
- virtual const char \* [type](#) ()  
*Return the type, "cspline\_peri\_interp".*
- virtual int [init](#) (const vec\_t &xa, const vec\_t &ya, size\_t size)  
*Initialize interpolation routine.*
- virtual int [free](#) ()  
*Free allocated memory.*

##### Protected Attributes

- [o2scl\\_linalg::uvector\\_5\\_mem p5m](#)  
*Desc.*

##### Private Member Functions

- [cspline\\_peri\\_interp](#) (const [cspline\\_peri\\_interp](#)< vec\_t > &)
- [cspline\\_peri\\_interp](#)< vec\_t > & [operator=](#) (const [cspline\\_peri\\_interp](#)< vec\_t > &)

#### 46.48.2 Member Function Documentation

46.48.2.1 template<class vec\_t> virtual int [cspline\\_peri\\_interp](#)< vec\_t >::init ( const vec\_t & xa, const vec\_t & ya, size\_t size )  
[inline, virtual]

Periodic boundary conditions

Natural boundary conditions

Reimplemented from [cspline\\_interp](#)< vec\_t >.

Definition at line 652 of file interp.h.

The documentation for this class was generated from the following file:

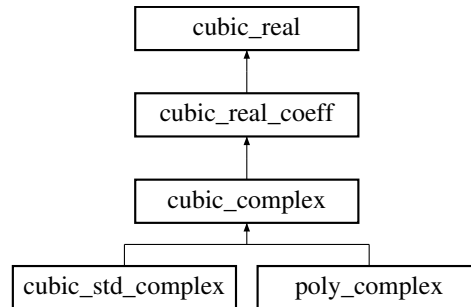
- interp.h

## 46.49 cubic\_complex Class Reference

Solve a cubic polynomial with complex coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for cubic\_complex:



## 46.49.1 Detailed Description

Definition at line 182 of file poly.h.

## Public Member Functions

- virtual int [solve\\_r](#) (const double a3, const double b3, const double c3, const double d3, double &x1, double &x2, double &x3)  
*Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the three solutions  $x = x_1$ ,  $x = x_2$ , and  $x = x_3$ .*
- virtual int [solve\\_rc](#) (const double a3, const double b3, const double c3, const double d3, double &x1, std::complex< double > &x2, std::complex< double > &x3)  
*Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the real solution  $x = x_1$  and two complex solutions  $x = x_2$  and  $x = x_3$ .*
- virtual int [solve\\_c](#) (const std::complex< double > a3, const std::complex< double > b3, const std::complex< double > c3, const std::complex< double > d3, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3)=0  
*Solves the complex polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the three complex solutions  $x = x_1$ ,  $x = x_2$ , and  $x = x_3$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("cubic\_complex")*

The documentation for this class was generated from the following file:

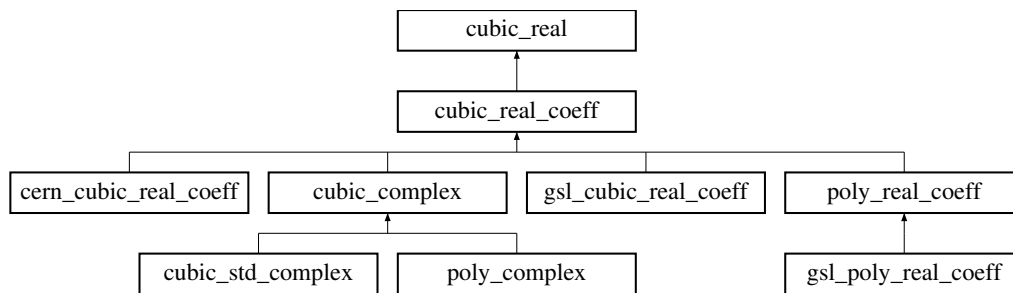
- [poly.h](#)

## 46.50 cubic\_real Class Reference

Solve a cubic polynomial with real coefficients and real roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for cubic\_real:



#### 46.50.1 Detailed Description

Definition at line 133 of file poly.h.

#### Public Member Functions

- virtual int [solve\\_r](#) (const double a3, const double b3, const double c3, const double d3, double &x1, double &x2, double &x3)=0  
*Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the three solutions  $x = x_1$ ,  $x = x_2$ , and  $x = x_3$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("cubic\_real")*

The documentation for this class was generated from the following file:

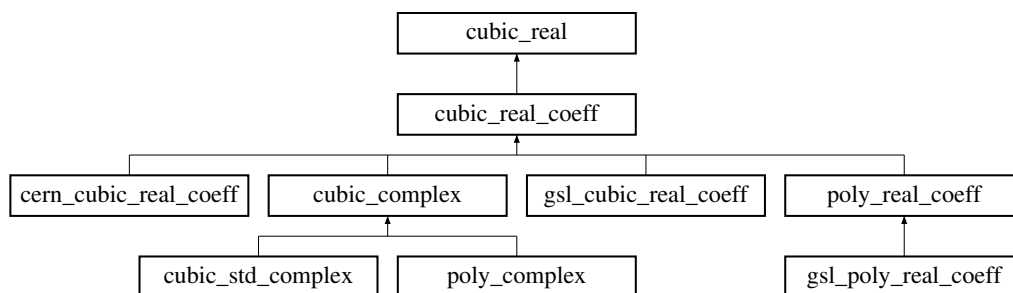
- [poly.h](#)

## 46.51 cubic\_real\_coeff Class Reference

Solve a cubic polynomial with real coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for cubic\_real\_coeff:



#### 46.51.1 Detailed Description

Definition at line 153 of file poly.h.

#### Public Member Functions

- virtual int [solve\\_r](#) (const double a3, const double b3, const double c3, const double d3, double &x1, double &x2, double &x3)

*Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the three solutions  $x = x_1$ ,  $x = x_2$ , and  $x = x_3$ .*

- virtual int [solve\\_rc](#) (const double a3, const double b3, const double c3, const double d3, double &x1, std::complex< double > &x2, std::complex< double > &x3)=0  
*Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the real solution  $x = x_1$  and two complex solutions  $x = x_2$  and  $x = x_3$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("cubic\_real\_coeff")*

The documentation for this class was generated from the following file:

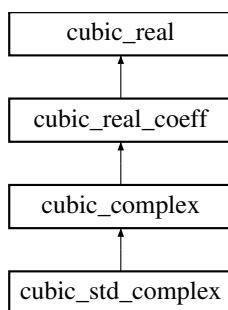
- [poly.h](#)

## 46.52 cubic\_std\_complex Class Reference

Solve a cubic with complex coefficients and complex roots.

```
#include <poly.h>
```

Inheritance diagram for cubic\_std\_complex:



### 46.52.1 Detailed Description

Definition at line 693 of file poly.h.

#### Public Member Functions

- virtual int [solve\\_c](#) (const std::complex< double > a3, const std::complex< double > b3, const std::complex< double > c3, const std::complex< double > d3, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3)  
*Solves the complex polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the three complex solutions  $x = x_1$ ,  $x = x_2$ , and  $x = x_3$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("cubic\_std\_complex")*

The documentation for this class was generated from the following file:

- [poly.h](#)

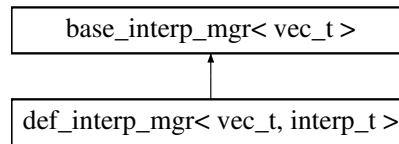
## 46.53 def\_interp\_mgr< vec\_t, interp\_t > Class Template Reference

A base interpolation object manager template.

```
#include <interp.h>
```

Inheritance diagram for def\_interp\_mgr< vec\_t, interp\_t >:





#### 46.53.1 Detailed Description

```
template<class vec_t, template< class > class interp_t>class def_interp_mgr< vec_t, interp_t >
```

Definition at line 1100 of file `interp.h`.

#### Public Member Functions

- virtual `base_interp< vec_t > * new_interp ()`  
Create a new interpolation object.

The documentation for this class was generated from the following file:

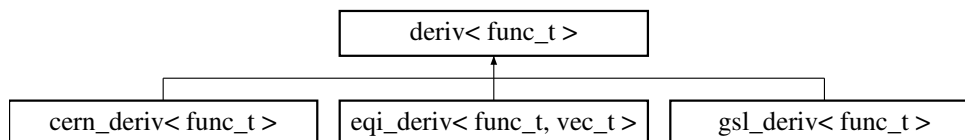
- `interp.h`

## 46.54 `deriv< func_t >` Class Template Reference

Numerical differentiation base [abstract base].

```
#include <deriv.h>
```

Inheritance diagram for `deriv< func_t >`:



#### 46.54.1 Detailed Description

```
template<class func_t = funct>class deriv< func_t >
```

This base class does not perform any actual differentiation. Use one of the children `cern_deriv`, `gsl_deriv`, or `eqi_deriv` instead.

This base class contains some code to automatically apply the first derivative routines to compute second or third derivatives. The error estimates for these will likely be underestimated.

#### Note

Because this class template aims to automatically provide second and third derivatives, one must overload either both `calc()` and `calc_int()` or both `calc_err()` and `calc_err_int()`.

**Idea for Future** Improve the methods for second and third derivatives

Definition at line 51 of file `deriv.h`.

## Data Structures

- struct [dpars](#)  
A structure for passing the function to second and third derivatives [protected].

## Public Member Functions

- virtual double [calc](#) (double x, func\_t &func)  
Calculate the first derivative of *func* w.r.t. *x*.
- virtual double [calc2](#) (double x, func\_t &func)  
Calculate the second derivative of *func* w.r.t. *x*.
- virtual double [calc3](#) (double x, func\_t &func)  
Calculate the third derivative of *func* w.r.t. *x*.
- virtual double [get\\_err](#) ()  
Get uncertainty of last calculation.
- virtual int [calc\\_err](#) (double x, func\_t &func, double &dfdx, double &err)=0  
Calculate the first derivative of *func* w.r.t. *x* and the uncertainty.
- virtual int [calc2\\_err](#) (double x, func\_t &func, double &d2fdx2, double &err)  
Calculate the second derivative of *func* w.r.t. *x* and the uncertainty.
- virtual int [calc3\\_err](#) (double x, func\_t &func, double &d3fdx3, double &err)  
Calculate the third derivative of *func* w.r.t. *x* and the uncertainty.
- virtual const char \* [type](#) ()  
Return string denoting type ("deriv")

## Data Fields

- bool [err\\_nonconv](#)  
If true, call the error handler if the routine does not "converge".
- int [verbose](#)  
Output control.

## Protected Member Functions

- virtual double [calc\\_int](#) (double x, [funct](#) &func)  
Calculate the first derivative of *func* w.r.t. *x*.
- virtual int [calc\\_err\\_int](#) (double x, [funct](#) &func, double &dfdx, double &err)=0  
Calculate the first derivative of *func* w.r.t. *x* and the uncertainty.
- double [derivfun](#) (double x, [dpars](#) &dp)  
The function for the second derivative.
- double [derivfun2](#) (double x, [dpars](#) &dp)  
The function for the third derivative.

## Protected Attributes

- bool [from\\_calc](#)  
Avoids infinite loops in case the user calls the base class version.
- double [derr](#)  
The uncertainty in the most recent derivative computation.

## 46.54.2 Member Function Documentation

46.54.2.1 `template<class func_t = funct> virtual double deriv< func_t >::calc ( double x, func_t & func ) [inline, virtual]`

After calling [calc\(\)](#), the error may be obtained from [get\\_err\(\)](#).

Definition at line 92 of file [deriv.h](#).

```
46.54.2.2  template<class func_t = funct> virtual double deriv< func_t >::calc_int ( double x, funct & func ) [inline, protected,
virtual]
```

This is an internal version of `calc()` which is used in computing second and third derivatives

Definition at line 180 of file `deriv.h`.

```
46.54.2.3  template<class func_t = funct> virtual int deriv< func_t >::calc_err_int ( double x, funct & func, double & dfdx, double & err )
[protected, pure virtual]
```

This is an internal version of `calc_err()` which is used in computing second and third derivatives

Implemented in `cern_deriv< func_t >`, `gsl_deriv< func_t >`, and `gsl_deriv< funct >`.

The documentation for this class was generated from the following file:

- `deriv.h`

## 46.55 `deriv< func_t >::dpars` Struct Reference

A structure for passing the function to second and third derivatives [protected].

```
#include <deriv.h>
```

### 46.55.1 Detailed Description

```
template<class func_t = funct> struct deriv< func_t >::dpars
```

Definition at line 60 of file `deriv.h`.

#### Data Fields

- `func_t * func`  
*The pointer to the function.*

The documentation for this struct was generated from the following file:

- `deriv.h`

## 46.56 `edge_crossings` Class Reference

Edges for the contour class.

```
#include <contour.h>
```

### 46.56.1 Detailed Description

The edge crossings generated by the `contour` class are given as objects of this type.

The `status` matrix contains one of four possible values

- 0 - empty (no edge)
- 1 - edge which has not yet been assigned to a contour
- 2 - edge assigned to contour point

- 3 - edge which has been designated as a contour endpoint

The matrices returned by `contour` are not square, their size depends on whether or not they contain the "bottom edges" or the "right edges".

**Idea for Future** Write HDF I/O object for edge crossings

**Idea for Future** Make this a subclass of `contour`.

Definition at line 82 of file `contour.h`.

#### Data Fields

- `omatrix_int status`  
*Edge status.*
- `omatrix values`  
*Edge values.*

The documentation for this class was generated from the following file:

- `contour.h`

## 46.57 `exact_jacobian< func_t, vec_t, mat_t >::ej_parms` Struct Reference

Parameter structure for passing information.

```
#include <jacobian.h>
```

### 46.57.1 Detailed Description

```
template<class func_t = mm_func<>, class vec_t = ovector_base, class mat_t = omatrix_base>struct exact_jacobian< func_t, vec_t, mat_t >::ej_parms
```

This class is primarily useful for specifying derivatives for using the `jacobian::set_deriv()` function.

Definition at line 395 of file `jacobian.h`.

#### Data Fields

- `size_t nv`  
*The number of variables.*
- `size_t xj`  
*The current x value.*
- `size_t yi`  
*The current y value.*
- `vec_t * x`  
*The x vector.*
- `vec_t * y`  
*The y vector.*

The documentation for this struct was generated from the following file:

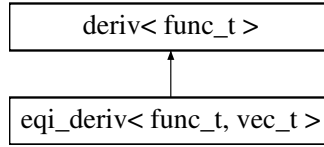
- `jacobian.h`

## 46.58 eqi\_deriv&lt; func\_t, vec\_t &gt; Class Template Reference

Derivatives for equally-spaced abscissas.

```
#include <eqi_deriv.h>
```

Inheritance diagram for eqi\_deriv< func\_t, vec\_t >:



## 46.58.1 Detailed Description

```
template<class func_t = funct, class vec_t = ovector_base>class eqi_deriv< func_t, vec_t >
```

This is an implementation of the formulas for equally-spaced abscissas as indicated below. The level of approximation is specified in `set_npoints()`. The value of  $p \times h$  can be specified in `coeff` (default is zero).

## Note

Uncertainties are not computed and the code for second and third derivatives is unfinished.

The derivatives given, for example, from the five-point formula can sometimes be more accurate than computing the derivative from the interpolation class. This is especially true near the boundaries of the interpolated region.

**Idea for Future** Finish the second and third derivative formulas.

Two-point formula (note that this is independent of p).

$$f'(x_0 + ph) = \frac{1}{h} [f_1 - f_0]$$

Three-point formula from Abramowitz and Stegun

$$f'(x_0 + ph) = \frac{1}{h} \left[ \frac{2p-1}{2} f_{-1} - 2p f_0 + \frac{2p+1}{2} f_1 \right]$$

Four-point formula from Abramowitz and Stegun

$$f'(x_0 + ph) = \frac{1}{h} \left[ -\frac{3p^2-6p+2}{6} f_{-1} + \frac{3p^2-4p-1}{2} f_0 - \frac{3p^2-2p-2}{2} f_1 + \frac{3p^2-1}{6} f_2 \right]$$

Five-point formula from Abramowitz and Stegun

$$\begin{aligned}
 f'(x_0 + ph) = & \frac{1}{h} \left[ \frac{2p^3-3p^2-p+1}{12} f_{-2} - \frac{4p^3-3p^2-8p+4}{6} f_{-1} \right. \\
 & + \frac{2p^3-5p}{2} f_0 - \frac{4p^3+3p^2-8p-4}{6} f_1 \\
 & \left. + \frac{2p^3+3p^2-p-1}{12} f_2 \right]
 \end{aligned}$$

The relations above can be confined to give formulas for second derivative formulas: Three-point formula

$$f''(x_0 + ph) = \frac{1}{h^2} [f_{-1} - 2f_0 + f_1]$$

Four-point formula:

$$f'(x_0 + ph) = \frac{1}{2h^2} [(1 - 2p)f_{-1} - (1 - 6p)f_0 - (1 + 6p)f_1 + (1 + 2p)f_2]$$

Five-point formula:

$$f'(x_0 + ph) = \frac{1}{4h^2} [(1 - 2p)^2 f_{-2} + (8p - 16p^2) f_{-1} - (2 - 24p^2) f_0 - (8p + 16p^2) f_1 + (1 + 2p)^2 f_2]$$

Six-point formula:

$$\begin{aligned} f'(x_0 + ph) = & \frac{1}{12h^2} [(2 - 10p + 15p^2 - 6p^3) f_{-2} + (3 + 14p - 57p^2 + 30p^3) f_{-1} \\ & + (-8 + 20p + 78p^2 - 60p^3) f_0 + (-2 - 44p - 42p^2 + 60p^3) f_1 \\ & + (6 + 22p + 3p^2 - 30p^3) f_2 + (-1 - 2p + 3p^2 + 6p^3) f_3] \end{aligned}$$

Seven-point formula:

$$\begin{aligned} f'(x_0 + ph) = & \frac{1}{36h^2} [(4 - 24p + 48p^2 - 36p^3 + 9p^4) f_{-3} + (12 + 12p - 162p^2 + 180p^3 - 54p^4) f_{-2} \\ & + (-15 + 120p + 162p^2 - 360p^3 + 135p^4) f_{-1} - 4(8 + 48p - 3p^2 - 90p^3 + 45p^4) f_0 \\ & + 3(14 + 32p - 36p^2 - 60p^3 + 45p^4) f_1 + (-12 - 12p + 54p^2 + 36p^3 - 54p^4) f_2 \\ & + (1 - 6p^2 + 9p^4) f_3] \end{aligned}$$

Definition at line 137 of file `eqi_deriv.h`.

#### Public Member Functions

- `int set_npoints (int npoints)`  
*Set the number of points to use for first derivatives (default 5)*
- `int set_npoints2 (int npoints)`  
*Set the number of points to use for second derivatives (default 5)*
- `virtual int calc_err (double x, func_t &func, double &dfdx, double &err)`  
*Calculate the first derivative of `func` w.r.t. `x`.*
- `virtual int calc2_err (double x, func_t &func, double &dfdx, double &err)`  
*Calculate the second derivative of `func` w.r.t. `x`.*
- `virtual int calc3_err (double x, func_t &func, double &dfdx, double &err)`  
*Calculate the third derivative of `func` w.r.t. `x`.*
- `double calc_vector (double x, double x0, double dx, size_t nx, const vec_t &y)`  
*Calculate the derivative at `x` given an array.*
- `double calc2_vector (double x, double x0, double dx, size_t nx, const vec_t &y)`  
*Calculate the second derivative at `x` given an array.*
- `double calc3_vector (double x, double x0, double dx, size_t nx, const vec_t &y)`  
*Calculate the third derivative at `x` given an array.*
- `int deriv_vector (size_t nv, double dx, const vec_t &y, vec_t &dydx)`  
*Calculate the derivative of an entire array.*
- `virtual const char * type ()`  
*Return string denoting type ("`eqi_deriv`")*

#### Data Fields

- `double h`  
*Stepsize (Default  $10^{-4}$ ).*
- `double xoff`  
*Offset (default 0.0)*

## 46.58.2 Member Function Documentation

46.58.2.1 `template<class func_t = funct, class vec_t = ovector_base> int eqi_deriv< func_t, vec_t >::set_npoints ( int npoints ) [inline]`

Acceptable values are 2-5 (see above).

Definition at line 159 of file eqi\_deriv.h.

46.58.2.2 `template<class func_t = funct, class vec_t = ovector_base> int eqi_deriv< func_t, vec_t >::set_npoints2 ( int npoints ) [inline]`

Acceptable values are 3-5 (see above).

Definition at line 185 of file eqi\_deriv.h.

46.58.2.3 `template<class func_t = funct, class vec_t = ovector_base> double eqi_deriv< func_t, vec_t >::calc_vector ( double x, double x0, double dx, size_t nx, const vec_t & y ) [inline]`

This calculates the derivative at  $x$  given a function specified in an array  $y$  of size  $nx$  with equally spaced abscissas. The first abscissa should be given as  $x_0$  and the distance between adjacent abscissas should be given as  $dx$ . The value  $x$  need not be one of the abscissas (i.e. it can lie in between an interval). The appropriate offset is calculated automatically.

Definition at line 240 of file eqi\_deriv.h.

46.58.2.4 `template<class func_t = funct, class vec_t = ovector_base> double eqi_deriv< func_t, vec_t >::calc2_vector ( double x, double x0, double dx, size_t nx, const vec_t & y ) [inline]`

This calculates the second derivative at  $x$  given a function specified in an array  $y$  of size  $nx$  with equally spaced abscissas. The first abscissa should be given as  $x_0$  and the distance between adjacent abscissas should be given as  $dx$ . The value  $x$  need not be one of the abscissas (i.e. it can lie in between an interval). The appropriate offset is calculated automatically.

Definition at line 256 of file eqi\_deriv.h.

46.58.2.5 `template<class func_t = funct, class vec_t = ovector_base> double eqi_deriv< func_t, vec_t >::calc3_vector ( double x, double x0, double dx, size_t nx, const vec_t & y ) [inline]`

This calculates the third derivative at  $x$  given a function specified in an array  $y$  of size  $nx$  with equally spaced abscissas. The first abscissa should be given as  $x_0$  and the distance between adjacent abscissas should be given as  $dx$ . The value  $x$  need not be one of the abscissas (i.e. it can lie in between an interval). The appropriate offset is calculated automatically.

Definition at line 273 of file eqi\_deriv.h.

46.58.2.6 `template<class func_t = funct, class vec_t = ovector_base> int eqi_deriv< func_t, vec_t >::deriv_vector ( size_t nv, double dx, const vec_t & y, vec_t & dydx ) [inline]`

Right now this uses  $np=5$ .

**Todo** generalize to other values of  $np$ oints.

Definition at line 286 of file eqi\_deriv.h.

The documentation for this class was generated from the following file:

- eqi\_deriv.h

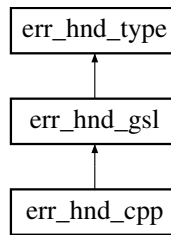
## 46.59 err\_hnd\_cpp Class Reference

Error handler to throw C++ exceptions.

```
#include <exception.h>
```

---

Inheritance diagram for `err_hnd_cpp`:



#### 46.59.1 Detailed Description

The default error handler, `def_err_hnd`, is of this type.

Definition at line 257 of file `exception.h`.

#### Public Member Functions

- virtual void `set` (const char \*reason, const char \*file, int line, int lerrno)  
*Set an error.*
- virtual const char \* `type` () const  
*Return type ("err\_hnd\_cpp")*

The documentation for this class was generated from the following file:

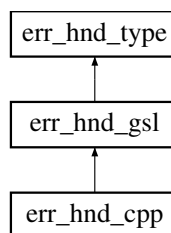
- `exception.h`

## 46.60 `err_hnd_gsl` Class Reference

The error handler.

```
#include <err_hnd.h>
```

Inheritance diagram for `err_hnd_gsl`:



#### 46.60.1 Detailed Description

An error handler for use in `O2scl` which replaces the GSL error handler

Note that the string arguments to `set()` can refer to temporary storage, since they are copied when the function is called and an error is set.

Definition at line 199 of file `err_hnd.h`.



## Public Member Functions

- virtual void `set` (const char \*reason, const char \*file, int line, int lerrno)  
*Set an error.*
- virtual void `get` (const char \*&reason, const char \*&file, int &line, int &lerrno)  
*Get the last error.*
- virtual int `get_errno` () const  
*Return the last error number.*
- virtual int `get_line` () const  
*Return the line number of the last error.*
- virtual const char \* `get_reason` () const  
*Return the reason for the last error.*
- virtual const char \* `get_file` () const  
*Return the file name of the last error.*
- virtual const char \* `get_str` ()  
*Return a string summarizing the last error.*
- virtual void `reset` ()  
*Remove last error information.*
- void `set_mode` (int m)  
*Set error handling mode.*
- int `get_mode` () const  
*Return the error handling mode.*
- virtual const char \* `type` () const  
*Return type ("err\_hnd\_gsl")*

## Data Fields

- bool `array_abort`  
*If true, call `exit()` when an array index error is set (default true)*
- size\_t `fname_size`  
*Number of characters from filename to print (default 28)*

## Protected Member Functions

- std::string `errno_to_string` (int errnox)  
*Convert an error number to a string.*

## Protected Attributes

- int `a_errno`  
*The error number.*
- int `a_line`  
*The line number.*
- int `mode`  
*The mode of error handling (default 2)*
- char \* `a_file`  
*The filename.*
- char `a_reason` [rsize]  
*The error explanation.*
- char `fullstr` [fsize]  
*A full string with explanation and line and file info.*

## Static Protected Attributes

- static const int `rsize` = 300  
*The maximum size of error explanations.*
- static const int `fsize` = 400  
*The maximum size of error explanations with the line and file info.*

## 46.60.2 Member Function Documentation

46.60.2.1 void err\_hnd\_gsl::set\_mode ( int *m* ) [inline]

- 0 - Continue execution after an error occurs
- 1 - Continue execution after an error occurs
- 2 - Abort execution after an error occurs, and print out the error information (default)

Definition at line 240 of file err\_hnd.h.

The documentation for this class was generated from the following file:

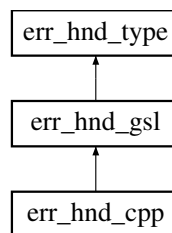
- [err\\_hnd.h](#)

## 46.61 err\_hnd\_type Class Reference

Class defining an error handler [abstract base].

```
#include <err_hnd.h>
```

Inheritance diagram for err\_hnd\_type:



## 46.61.1 Detailed Description

A global object of this type is defined, [err\\_hnd](#) .

**Idea for Future** There may be an issue associated with the string manipulations causing errors in the error handler.

Definition at line 142 of file err\_hnd.h.

## Public Member Functions

- virtual void [set](#) (const char \*reason, const char \*file, int line, int lerrno)=0  
*Set an error.*
- virtual void [get](#) (const char \*&reason, const char \*&file, int &line, int &lerrno)=0  
*Get the last error.*
- virtual int [get\\_errno](#) () const =0  
*Return the last error number.*
- virtual int [get\\_line](#) () const =0  
*Return the line number of the last error.*
- virtual const char \* [get\\_reason](#) () const =0  
*Return the reason for the last error.*
- virtual const char \* [get\\_file](#) () const =0  
*Return the file name of the last error.*
- virtual const char \* [get\\_str](#) ()=0

*Return a string summarizing the last error.*

- virtual void [reset](#) ()=0  
*Remove last error information.*
- virtual const char \* [type](#) () const =0  
*Return type.*

#### Static Public Member Functions

- static void [gsl\\_hnd](#) (const char \*reason, const char \*file, int line, int lerrno)  
*Set an error.*

#### 46.61.2 Member Function Documentation

46.61.2.1 static void `err_hnd_type::gsl_hnd ( const char * reason, const char * file, int line, int lerrno )` [`inline`, `static`]

This is separate from `set()`, since the gsl error handler needs to be a static function.

Definition at line 155 of file `err_hnd.h`.

The documentation for this class was generated from the following file:

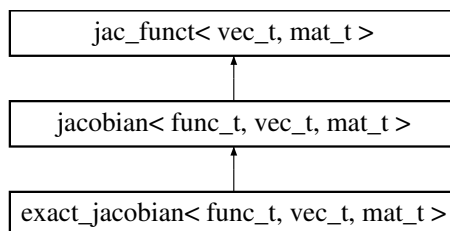
- [err\\_hnd.h](#)

## 46.62 `exact_jacobian< func_t, vec_t, mat_t >` Class Template Reference

A direct calculation of the jacobian using a [deriv](#) object.

```
#include <jacobian.h>
```

Inheritance diagram for `exact_jacobian< func_t, vec_t, mat_t >`:



#### 46.62.1 Detailed Description

```
template<class func_t = mm_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base>class exact_jacobian< func_t, vec_t, mat_t >
```

Note that it is most often wasteful to use this Jacobian in a root-finding routine and using more approximate Jacobians is more efficient. This class is mostly useful for demonstration purposes.

Definition at line 374 of file `jacobian.h`.

#### Data Structures

- struct [ej\\_parms](#)  
*Parameter structure for passing information.*

**Public Member Functions**

- int `set_deriv` (`deriv` < `funct` > &de)  
*Set the derivative object.*
- virtual int `operator()` (size\_t nv, vec\_t &x, vec\_t &y, mat\_t &jac)  
*The operator()*

**Data Fields**

- `gsl_deriv` < `funct` > `def_deriv`  
*The default derivative object.*

**Protected Member Functions**

- double `dfn` (double x, `ej_parms` &ejp)  
*Function for the derivative object.*

**Protected Attributes**

- `deriv` < `funct` > \* `dptr`  
*Pointer to the derivative object.*

The documentation for this class was generated from the following file:

- jacobian.h

**46.63 exc\_exception Class Reference**

Generic exception.

```
#include <exception.h>
```

**46.63.1 Detailed Description**

This class derives from `std::exception`.

The errors which are handled with this exception type are

- `gsl_failure` (-1) Failure
- `gsl_efailed` (5) Generic failure
- `gsl_esanity` (7) Sanity check failed
- `gsl_eunsup` (23) Requested feature is not supported by the hardware
- `gsl_eunimpl` (24) Requested feature not (yet) implemented

Definition at line 55 of file `exception.h`.

**Public Member Functions**

- [`exc\_exception\(\)`](#)  
*Create an exception.*
- virtual const char \* [`what\(\)`](#) const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [`exception.h`](#)

**46.64 `exc_invalid_argument` Class Reference**

Invalid argument exception.

```
#include <exception.h>
```

**46.64.1 Detailed Description**

This class derives from `std::invalid_argument`.

The errors which are handled with this exception type are

- `gsl_einval` (4) invalid argument supplied by user
- `gsl_ebadtol` (13) user specified an invalid tolerance
- `gsl_ebadlen` (19) matrix, vector lengths are not conformant
- `gsl_enotsqr` (20) matrix not square
- `gsl_eindex` (36) Invalid index for array or matrix

Definition at line 110 of file `exception.h`.

**Public Member Functions**

- [`exc\_invalid\_argument`](#) (const std::string &s)  
*Create an exception with description provided in `s`.*
- virtual const char \* [`what\(\)`](#) const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [`exception.h`](#)

**46.65 `exc_ios_failure` Class Reference**

I/O failure error exception.

```
#include <exception.h>
```

---

#### 46.65.1 Detailed Description

This class derives from `std::ios::failure`.

The errors which are handled with this exception type are

- `gsl_eof=32` end of file
- `gsl_efilenotfound=35` File not found

Definition at line 235 of file `exception.h`.

#### Public Member Functions

- [`exc\_ios\_failure`](#) (const std::string &s)  
*Create an exception with description provided in `s`.*
- virtual const char \* [`what`](#) () const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [exception.h](#)

## 46.66 `exc_logic_error` Class Reference

Logic error exception.

```
#include <exception.h>
```

#### 46.66.1 Detailed Description

This class derives from `std::logic_error`.

The error which is handled with this exception type is

- `gsl_ememtype (34)` Incorrect type for memory object

Definition at line 81 of file `exception.h`.

#### Public Member Functions

- [`exc\_logic\_error`](#) (const std::string &s)  
*Create an exception with description provided in `s`.*
- virtual const char \* [`what`](#) () const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [exception.h](#)

## 46.67 `exc_overflow_error` Class Reference

Overflow error runtime exception.

```
#include <exception.h>
```

---

#### 46.67.1 Detailed Description

This class derives from `std::overflow_error`.

The errors which are handled with this exception type are

- `gsl_ezerodiv` (12) tried to divide by zero
- `gsl_eovrflw` (16) overflow

Definition at line 209 of file `exception.h`.

#### Public Member Functions

- [`exc\_overflow\_error`](#) (const std::string &s)  
*Create an exception with description provided in `s`.*
- virtual const char \* [`what`](#) () const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [exception.h](#)

## 46.68 `exc_range_error` Class Reference

Range error runtime exception.

```
#include <exception.h>
```

#### 46.68.1 Detailed Description

This class derives from `std::range_error`.

The errors which are handled with this exception type are

- `gsl_edom` (1) input domain error, e.g. `sqrt(-1)`
- `gsl_erange` (2) output range error, e.g. `exp(1e100)`
- `gsl_eundrflw` (15) underflow

Definition at line 183 of file `exception.h`.

#### Public Member Functions

- [`exc\_range\_error`](#) (const std::string &s)  
*Create an exception with description provided in `s`.*
- virtual const char \* [`what`](#) () const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [exception.h](#)
-

## 46.69 `exc_runtime_error` Class Reference

Generic runtime error exception.

```
#include <exception.h>
```

### 46.69.1 Detailed Description

This class derives from `std::runtime_error`.

The errors which are handled with this exception type are

- `gsl_efault` (3) invalid pointer
- `gsl_efactor` (6) factorization failed
- `gsl_enomem` (8) malloc failed
- `gsl_ebadfunc` (9) problem with user-supplied function
- `gsl_erunaway` (10) iterative process is out of control
- `gsl_emaxiter` (11) exceeded max number of iterations
- `gsl_etol` (14) failed to reach the specified tolerance
- `gsl_eloss` (17) loss of accuracy
- `gsl_eround` (18) failed because of roundoff error
- `gsl_esing` (21) apparent singularity detected
- `gsl_ediverge` (22) integral or series is divergent
- `gsl_ecache` (25) cache limit exceeded
- `gsl_etable` (26) table limit exceeded
- `gsl_enoprog` (27) iteration is not making progress toward solution
- `gsl_enoprogj` (28) jacobian evaluations are not improving the solution
- `gsl_etolf` (29) cannot reach the specified tolerance in `f`
- `gsl_etolx` (30) cannot reach the specified tolerance in `x`
- `gsl_etolg` (31) cannot reach the specified tolerance in gradient
- `gsl_enotfound` (33) Generic "not found" result
- `gsl_outsidecons` (37) Outside constraint region

Definition at line 156 of file `exception.h`.

### Public Member Functions

- **`exc_runtime_error`** (const std::string &s)
- virtual `~exc_runtime_error` () throw ()  
*Create an exception with description provided in `s`.*
- virtual const char \* `what` () const throw ()  
*Return the error string.*

The documentation for this class was generated from the following file:

- [exception.h](#)
-

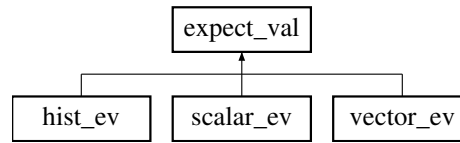


## 46.70 expect\_val Class Reference

Expectation value base class.

```
#include <expect_val.h>
```

Inheritance diagram for expect\_val:



### 46.70.1 Detailed Description

This class is experimental.

This is a base class for a set of classes useful for recording the outputs of several iterations of a numerical simulation, and summarizing the average, standard deviation, and error in the average over all iterations. After each iteration, some measurement is performed, and that measurement is added to the class with an `add()` functions (e.g. `scalar_ev::add()`). Autocorrelations are common in numerical simulations, and to handle this difficulty the measurements may be demarcated into 'blocks'. These blocks may have a variable or fixed number of measurements in each block.

The constructor needs as input the number of blocks to record (at least one) and the number of measurements per block. The number of measurements per block can be zero to indicate an unspecified number of blocks to record.

If the number of measurements per block is greater than zero, then blocks are filled one by one, moving to the next block when the requested of measurements (`n_per_block`) in the previous block has been provided. If the number of measurements per block is zero, then the blocks are filled evenly.

Current averages are always reported, though not all data is always used if there are incomplete blocks or the blocks have not yet been filled evenly. Two functions `current_avg()` and `current_avg_stats()` are provided in children. The latter provides the number of blocks and number of measurements per block used in the currently reported statistics. If only one block or one measurement is available, the standard deviation is reported as zero. If no data is available, then calls to `current_avg()` will call the error handler. See, e.g. `scalar_ev::current_avg()` and `scalar_ev::current_avg_stats()`.

If `n_per_block` is nonzero, then children call the error handler if they get more than `n_per_block` times `n_blocks` measurements.

**Idea for Future** If `n_per_block` is nonzero and the user adds more than `n_blocks` times `n_per_block` data, set `n_per_block` to zero, allocate the last structure and fall back to the variable block size method.

Definition at line 81 of file `expect_val.h`.

### Public Member Functions

- `expect_val()`  
*Create with one block of unspecified size.*
- `expect_val(const expect_val &ev)`  
*Copy constructor.*
- `expect_val & operator= (const expect_val &ev)`  
*Copy constructor.*
- `expect_val(size_t n_blocks, size_t n_per_block)`  
*Create with n\_blocks blocks and n\_per\_block points per block.*
- virtual void `set_blocks(size_t n_blocks, size_t n_per_block)`  
*Reset for n\_blocks blocks and n\_per\_block points per block.*

- virtual void [get\\_blocks](#) (size\_t &n\_blocks, size\_t &n\_per\_block) const  
*Get the number of blocks and the number of points per block.*
- virtual void [free](#) ()  
*Free allocated data.*
- virtual void [reset](#) ()  
*Clear all the data.*
- virtual void [get\\_block\\_indices](#) (size\_t &i\_block, size\_t &i\_curr\_block) const  
*Get the block index and the index within the current block.*
- virtual bool [finished](#) () const  
*Returns true if all blocks have been stored.*
- virtual double [progress](#) () const  
*Report progress as a fraction between zero to one (inclusive)*

#### Data Fields

- std::string [name](#)  
*The name of the expectation value.*
- std::string [short\\_name](#)  
*The shortened name.*

#### Protected Attributes

- size\_t [iblock](#)  
*Index denoting the current block number.*
- size\_t [i](#)  
*Index for the number of values in the current block (or blocks)*
- size\_t [nblocks](#)  
*Total number of blocks (default 1)*
- size\_t [nperblock](#)  
*Number of measurements per block (default 0)*

### 46.70.2 Constructor & Destructor Documentation

#### 46.70.2.1 expect\_val::expect\_val ( size\_t n\_blocks, size\_t n\_per\_block )

If this is called with a value of zero for `n_blocks`, then the error handler is called.

### 46.70.3 Member Function Documentation

#### 46.70.3.1 virtual void expect\_val::set\_blocks ( size\_t n\_blocks, size\_t n\_per\_block ) [virtual]

This function resets the currently stored data to zero by calling [reset\(\)](#). If this is called with a value of zero for `n_blocks`, then the value 1 is assumed.

Reimplemented in [scalar\\_ev](#).

#### 46.70.3.2 virtual bool expect\_val::finished ( ) const [virtual]

If `n_per_block` is greater than zero, then this reports true only when all `n_blocks` times `n_per_block` data points have been added.

Otherwise, this reports true whenever the last addition of data filled up the last block.

46.70.3.3 `virtual double expect_val::progress ( ) const` `[virtual]`

When `n_per_block` is zero, this reports the progress in having filled a round of blocks (i.e. whenever the last addition of data filled up the last block). This reports zero if no data has been added.

When `n_per_block` is nonzero, this reports the total progress on all blocks, reporting 1.0 only when all `n_blocks` times `n_per_block` data points have been added.

#### 46.70.4 Field Documentation

46.70.4.1 `size_t expect_val::nblocks` `[protected]`

This should never be zero.

Definition at line 95 of file `expect_val.h`.

46.70.4.2 `size_t expect_val::nperblock` `[protected]`

This is zero to indicate blocks of unspecified size

Definition at line 101 of file `expect_val.h`.

The documentation for this class was generated from the following file:

- `expect_val.h`

## 46.71 `gsl_inte_singular< func_t >::extrapolation_table` Struct Reference

A structure for extrapolation for [gsl\\_inte\\_qags](#).

```
#include <gsl_inte_singular.h>
```

### 46.71.1 Detailed Description

```
template<class func_t>struct gsl_inte_singular< func_t >::extrapolation_table
```

**Idea for Future** Move this to a new class, with [qelg\(\)](#) as a method

Definition at line 59 of file `gsl_inte_singular.h`.

#### Data Fields

- `size_t n`  
*Index of new element in the first column.*
- `double rlist2 [52]`  
*Lower diagonals of the triangular epsilon table.*
- `size_t nres`  
*Number of calls.*
- `double res3la [3]`  
*Three most recent results.*

The documentation for this struct was generated from the following file:

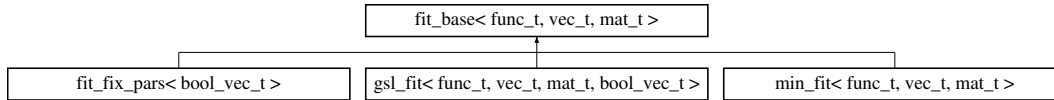
- `gsl_inte_singular.h`

46.72 `fit_base< func_t, vec_t, mat_t >` Class Template Reference

Non-linear least-squares fitting [abstract base].

```
#include <fit_base.h>
```

Inheritance diagram for `fit_base< func_t, vec_t, mat_t >`:



## 46.72.1 Detailed Description

```
template<class func_t = fit_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base> class fit_base< func_t, vec_t, mat_t >
```

Definition at line 185 of file `fit_base.h`.

## Public Member Functions

- virtual int `print_iter` (size\_t nv, vec\_t &x, double y, int iter, double value=0.0, double limit=0.0)  
*Print out iteration information.*
- virtual int `fit` (size\_t ndat, vec\_t &xdat, vec\_t &ydat, vec\_t &yerr, size\_t npar, vec\_t &par, mat\_t &covar, double &chi2, func\_t &fitfun)=0  
*Fit the data specified in (xdat,ydat) to the function fitfun with the parameters in par.*
- virtual const char \* `type` ()  
*Return string denoting type ("fit\_base")*

## Data Fields

- int `verbose`  
*An integer describing the verbosity of the output.*
- size\_t `n_dat`  
*The number of data points.*
- size\_t `n_par`  
*The number of parameters.*

## 46.72.2 Member Function Documentation

46.72.2.1 `template<class func_t = fit_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base> virtual int fit_base< func_t, vec_t, mat_t >::print_iter ( size_t nv, vec_t &x, double y, int iter, double value = 0.0, double limit = 0.0 ) [inline, virtual]`

Depending on the value of the variable `verbose`, this prints out the iteration information. If `verbose=0`, then no information is printed, while if `verbose>1`, then after each iteration, the present values of `x` and `y` are output to `std::cout` along with the iteration number. If `verbose>=2` then each iteration waits for a character.

Definition at line 204 of file `fit_base.h`.

46.72.2.2 `template<class func_t = fit_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base> virtual int fit_base< func_t, vec_t, mat_t >::fit ( size_t ndat, vec_t &xdat, vec_t &ydat, vec_t &yerr, size_t npar, vec_t &par, mat_t &covar, double &chi2, func_t &fitfun ) [pure virtual]`

The covariance matrix for the parameters is returned in `covar` and the value of  $\chi^2$  is returned in `chi2`.

Implemented in `gsl_fit< func_t, vec_t, mat_t, bool_vec_t >`, and `min_fit< func_t, vec_t, mat_t >`.

The documentation for this class was generated from the following file:

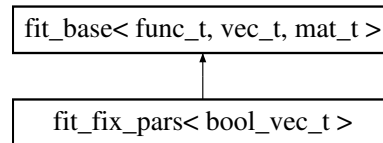
- fit\_base.h

## 46.73 fit\_fix\_pars< bool\_vec\_t > Class Template Reference

Multidimensional fitting fixing some parameters and varying others.

```
#include <fit_fix.h>
```

Inheritance diagram for fit\_fix\_pars< bool\_vec\_t >:



### 46.73.1 Detailed Description

```
template<class bool_vec_t>class fit_fix_pars< bool_vec_t >
```

Definition at line 37 of file fit\_fix.h.

#### Public Member Functions

- [fit\\_fix\\_pars](#) ()  
*Specify the member function pointer.*
- virtual int [fit](#) (size\_t ndat, [ovector\\_base](#) &xdat, [ovector\\_base](#) &ydat, [ovector\\_base](#) &yerr, size\_t npar, [ovector\\_base](#) &par, [omatrix\\_base](#) &covar, double &chi2, [fit\\_func](#)<> &fitfun)  
*Fit the data specified in (xdat,ydat) to the function `fitfun` with the parameters in `par`.*
- virtual int [fit\\_fix](#) (size\_t ndat, [ovector\\_base](#) &xdat, [ovector\\_base](#) &ydat, [ovector\\_base](#) &yerr, size\_t npar, [ovector\\_base](#) &par, [bool\\_vec\\_t](#) &fix, [omatrix\\_base](#) &covar, double &chi2, [fit\\_func](#)<> &fitfun)  
*Fit function `func` while fixing some parameters as specified in `fix`.*
- int [set\\_fit](#) ([fit\\_base](#)< [fit\\_func\\_mfptr](#)< [fit\\_fix\\_pars](#)< [bool\\_vec\\_t](#) > > > &fitter)  
*Change the base minimizer.*

#### Data Fields

- [gsl\\_fit](#)< [fit\\_func\\_mfptr](#) < [fit\\_fix\\_pars](#)< [bool\\_vec\\_t](#) > > > [def\\_fit](#)  
*The default base minimizer.*

#### Protected Member Functions

- virtual double [fit\\_func](#) (size\_t nv, const [ovector\\_base](#) &x, double xx)  
*The new function to send to the minimizer.*

#### Protected Attributes

- [fit\\_base](#)< [fit\\_func\\_mfptr](#) < [fit\\_fix\\_pars](#)< [bool\\_vec\\_t](#) > > > \* [fitp](#)  
*The minimizer.*
- [fit\\_func](#) \* [funcp](#)  
*The user-specified function.*

- `size_t unv`  
*The user-specified number of variables.*
- `size_t nv_new`  
*The new number of variables.*
- `bool_vec_t * fixp`  
*Specify which parameters to fix.*
- `ovector_base * xp`  
*The user-specified initial vector.*

#### Private Member Functions

- `fit_fix_pars` (const `fit_fix_pars` &)
- `fit_fix_pars` & `operator=` (const `fit_fix_pars` &)

#### 46.73.2 Member Function Documentation

46.73.2.1 `template<class bool_vec_t> virtual int fit_fix_pars< bool_vec_t >::fit ( size_t ndat, ovector_base & xdat, ovector_base & ydat, ovector_base & yerr, size_t npar, ovector_base & par, omatrix_base & covar, double & chi2, fit_func<> & fitfun )`  
[inline, virtual]

The covariance matrix for the parameters is returned in `covar` and the value of  $\chi^2$  is returned in `chi2`.

Definition at line 61 of file `fit_fix.h`.

The documentation for this class was generated from the following file:

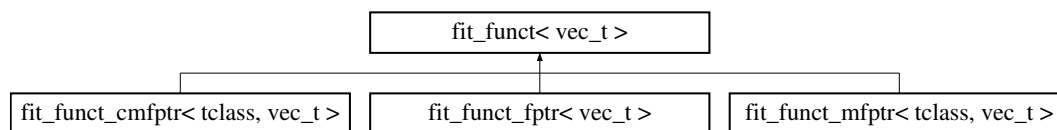
- `fit_fix.h`

## 46.74 `fit_func< vec_t >` Class Template Reference

Fitting function [abstract base].

`#include <fit_base.h>`

Inheritance diagram for `fit_func< vec_t >`:



#### 46.74.1 Detailed Description

`template<class vec_t = ovector_base> class fit_func< vec_t >`

Definition at line 35 of file `fit_base.h`.

#### Public Member Functions

- virtual double `operator()` (size\_t np, const `vec_t` &p, double x)=0  
*Using parameters in `p`, predict `y` given `x`.*

## Private Member Functions

- `fit_func_t` (const `fit_func_t` &)
- `fit_func_t` & `operator=` (const `fit_func_t` &)

The documentation for this class was generated from the following file:

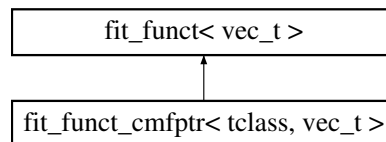
- `fit_base.h`

46.75 `fit_func_t_cmfp`< `tclass`, `vec_t` > Class Template Reference

Const member function pointer fitting function.

```
#include <fit_base.h>
```

Inheritance diagram for `fit_func_t_cmfp`< `tclass`, `vec_t` >:



## 46.75.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class fit_func_t_cmfp< tclass, vec_t >
```

Definition at line 139 of file `fit_base.h`.

## Public Member Functions

- `fit_func_t_cmfp` (`tclass` \*`tp`, double(`tclass`::\*`fp`)(`size_t` `np`, const `vec_t` &`p`, double `x`) const)  
*Specify the member function pointer.*
- virtual double `operator()` (`size_t` `np`, const `vec_t` &`p`, double `x`)  
*Using parameters in `p`, predict `y` given `x`.*

## Protected Attributes

- double(`tclass`::\* `fptr`)(`size_t` `np`, const `vec_t` &`p`, double `x`) const  
*Storage for the user-specified function pointer.*
- `tclass` \* `tptr`  
*Storage for the class pointer.*

## Private Member Functions

- `fit_func_t_cmfp` (const `fit_func_t_cmfp` &)
- `fit_func_t_cmfp` & `operator=` (const `fit_func_t_cmfp` &)

The documentation for this class was generated from the following file:

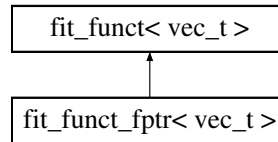
- `fit_base.h`

46.76 `fit_funcnt_fptr< vec_t >` Class Template Reference

Function pointer fitting function.

```
#include <fit_base.h>
```

Inheritance diagram for `fit_funcnt_fptr< vec_t >`:



## 46.76.1 Detailed Description

```
template<class vec_t = ovector_base>class fit_funcnt_fptr< vec_t >
```

Definition at line 58 of file `fit_base.h`.

## Public Member Functions

- `fit_funcnt_fptr` (double(\*fp)(size\_t np, const vec\_t &p, double x))  
*Specify a fitting function by a function pointer.*
- virtual double `operator()` (size\_t np, const vec\_t &p, double x)  
*Using parameters in  $p$ , predict  $y$  given  $x$ .*

## Protected Member Functions

- `fit_funcnt_fptr` (const `fit_funcnt_fptr` &)
- `fit_funcnt_fptr` & `operator=` (const `fit_funcnt_fptr` &)

## Protected Attributes

- double(\* `fptr`) (size\_t np, const vec\_t &p, double x)  
*Storage for the user-specified function pointer.*

The documentation for this class was generated from the following file:

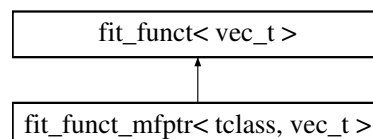
- `fit_base.h`

46.77 `fit_funcnt_mfptr< tclass, vec_t >` Class Template Reference

Member function pointer fitting function.

```
#include <fit_base.h>
```

Inheritance diagram for `fit_funcnt_mfptr< tclass, vec_t >`:





## 46.77.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class fit_funct_mfptr< tclass, vec_t >
```

Definition at line 96 of file `fit_base.h`.

## Public Member Functions

- `fit_funct_mfptr` (`tclass *tp`, `double(tclass::*fp)(size_t np, const vec_t &p, double x)`)  
*Specify the member function pointer.*
- virtual `double operator()` (`size_t np`, `const vec_t &p`, `double x`)  
*Using parameters in `p`, predict `y` given `x`.*

## Protected Attributes

- `double(tclass::* fptr)` (`size_t np`, `const vec_t &p`, `double x`)  
*Storage for the user-specified function pointer.*
- `tclass * tptr`  
*Storage for the class pointer.*

## Private Member Functions

- `fit_funct_mfptr` (`const fit_funct_mfptr &`)
- `fit_funct_mfptr & operator=` (`const fit_funct_mfptr &`)

The documentation for this class was generated from the following file:

- `fit_base.h`

46.78 `format_float` Class Reference

Format a floating point number into a Latex or HTML string.

```
#include <format_float.h>
```

## 46.78.1 Detailed Description

This class formats floating point strings into something useful for HTML or Latex documents. For basic use, simply call either `html_mode()` or `latex_mode()` and then use `convert()`.

The base-10 logarithm of the smallest and largest numbers to be represented without a string akin to "times 10 to the nth power" can be specified in `set_exp_limits()`. The number of significant figures can be specified with `set_sig_figs()` (the default is 5).

To force `convert()` to add zeros to the right side of the mantissa to guarantee that the requested number of significant digits is given, call `set_pad_zeros()` with a `true` argument.

To force scientific notation for all numbers, set the maximum exponent to be smaller than the minimum exponent.

## Note

This function does not warn the user if the number of significant figures requested is larger than the machine precision. If the absolute magnitude for either the minimum or maximum exponent is larger than or equal to the number of significant figures, then rounding will automatically occur.

The format for a normal number is

```
prefix (sign-string) number suffix
```

and in scientific notation is

```
sci-prefix (sci-sign-string) number times-string
exp-prefix (exp-sign-string) exponent exp-suffix sci-suffix
```

## Examples

The code

```
format_float fd;
fd.latex_mode();
cout << fd.convert(-sqrt(2.0)*1.0e-5) << endl;
cout << fd.convert(sqrt(2.0)*1.0e-2) << endl;
cout << fd.convert(-sqrt(2.0)*1.0e-1) << endl;
```

outputs

```
$-$1.4142 $\times 10^{-5}$
0.014142
$-$0.14142
```

and the code

```
format_float fd;
fd.html_mode();
fd.set_sig_figs(7);
fd.set_pad_zeros(true);
cout << fd.convert(1.414e-5) << endl;
cout << fd.convert(1.414e-2) << endl;
```

outputs

```
1.414000 &times; 10<sup>-5</sup>
0.01414000
```

**Idea for Future** Handle `inf`'s and `nan`'s correctly.

**Idea for Future** Allow change of string for the "+" sign for the exponent

Definition at line 110 of file `format_float.h`.

## Public Member Functions

### Basic usage

- int `html_mode()`  
*Set HTML mode.*
- int `latex_mode()`  
*Set Latex mode.*
- int `c_mode()`  
*C-like mode.*
- std::string `convert` (double x, bool debug=false)  
*Convert a floating point number to a string.*

### Set text settings

These are modified by the functions `html_mode()` and `latex_mode()`

- `int set_prefix (std::string prefix)`  
*set prefix*
- `int set_suffix (std::string suffix)`  
*Set suffix.*
- `int set_sci_prefix (std::string sci_prefix)`  
*Set prefix for scientific notation.*
- `int set_sci_suffix (std::string sci_suffix)`  
*Set suffix for scientific notation.*
- `int set_exp_prefix (std::string exp_prefix)`  
*Set prefix for exponent.*
- `int set_exp_suffix (std::string exp_suffix)`  
*Set suffix for exponent.*
- `int set_sign (std::string sign)`  
*Set sign.*
- `int set_exp_sign (std::string exp_sign)`  
*Set sign for exponent.*
- `int set_show_exp_sign (bool b)`  
*Set policy for showing positive exponent sign.*
- `int set_sci_sign (std::string sci_sign)`  
*Set sign for scientific notation.*
- `int set_times (std::string times)`  
*Set times.*
- `int set_zero (std::string zero)`  
*Set zero.*
- `int set_not_finite (std::string not_finite)`  
*Set string for numbers which are not finite.*

### Set other settings

These are not modified by the functions `html_mode()` and `latex_mode()`

- `int set_exp_limits (int min, int max)`  
*Set the exponent limits.*
- `int set_sig_figs (size_t sig_figs)`  
*Set the number of significant figures (argument has maximum of 15 and cannot be zero)*
- `int set_pad_zeros (bool pad)`  
*Set pad zeros.*
- `int set_dec_point (std::string dec_point)`  
*Set decimal point.*
- `int set_exp_digits (size_t d)`  
*Set minimum number of digits in the exponent.*

### Get text settings

These are modified by the functions `html_mode()` and `latex_mode()`

- `std::string get_prefix ()`  
*Get prefix.*
- `std::string get_suffix ()`  
*Get suffix.*
- `std::string get_sci_prefix ()`  
*Get prefix for scientific notation.*
- `std::string get_sci_suffix ()`  
*Get suffix for scientific notation.*
- `std::string get_exp_prefix ()`  
*Get prefix for exponent.*
- `std::string get_exp_suffix ()`  
*Get suffix for exponent.*
- `std::string get_sign ()`  
*Get sign.*

- `std::string get_exp_sign ()`  
*Get sign for exponent.*
- `std::string get_sci_sign ()`  
*Get sign for scientific notation.*
- `std::string get_times ()`  
*Get times.*
- `std::string get_zero ()`  
*Get zero.*
- `std::string get_not_finite ()`  
*Get string for numbers which are not finite.*

#### Get other settings

These are not modified by the functions `html_mode()` and `latex_mode()`

- `int get_exp_min ()`  
*Get minimum exponent.*
- `int get_exp_max ()`  
*Get maximum exponent.*
- `size_t get_sig_figs ()`  
*Get sig\_figs.*
- `bool get_pad_zeros ()`  
*Get pad\_zeros.*
- `std::string get_dec_point ()`  
*Get decimal point.*

#### Protected Member Functions

- `int remove_zeros_dpt (std::string &s)`  
*Remove extra zeros and decimal point from mantisaa.*

#### Protected Attributes

##### Base text settings

- `std::string prefix`  
*Prefix (default "")*
- `std::string suffix`  
*Suffix (default "")*
- `std::string sgn`  
*Sign string (default "-")*
- `std::string sci_sgn`  
*Sign string in scientific mode (default "-")*
- `std::string exp_sgn`  
*Sign string for exponent in scientific mode (default "-")*
- `std::string sci_prefix`  
*Prefix in scientific mode (default "")*
- `std::string sci_suffix`  
*Suffix in scientific mode (default "")*
- `std::string exp_prefix`  
*Exponent prefix (default "")*
- `std::string exp_suffix`  
*Exponent suffix (default "")*
- `std::string times`  
*Times symbol for scientific mode (default "x")*
- `std::string not_finte`  
*String for numbers which are not finite (default "Nan")*
- `std::string zeros`  
*String for zeros (default "0")*

## Other settings

- `size_t sig_fgs`  
*Number of significant figures (default 5)*
- `size_t exp_dgs`  
*Number of digits in exponent (default 0 which prints the minimum)*
- `int ex_mn`  
*Lower limit for automatic mode (default -2)*
- `int ex_mx`  
*Upper limit for automatic mode (default 3)*
- `bool pad_zeros`  
*If true, pad with zeros (default false)*
- `bool show_exp_sgn`  
*If true, show the sign of the exponent when it's positive (default false)*
- `std::string dpt`  
*The decimal point (default ' . ')*

## 46.78.2 Member Function Documentation

46.78.2.1 `int format_float::html_mode ( )`

This function is equivalent to the settings:

```
set_prefix("");
set_sign("-");
set_suffix("");
set_sci_prefix("");
set_times(" &times; ");
set_exp_prefix("10<sup>");
set_exp_sign("-");
set_sci_sign("-");
set_exp_suffix("</sup>");
set_sci_suffix("");
set_not_finite("Nan");
set_zero("0");
set_exp_digits(0);
set_show_exp_sign(false);
```

46.78.2.2 `int format_float::latex_mode ( )`

This function is equivalent to the settings:

```
set_prefix("");
set_sign("$-$");
set_suffix("");
set_sci_prefix("");
set_times("$\\times ");
set_exp_prefix("10^{");
set_exp_sign("-");
set_sci_sign("$-$");
set_exp_suffix("}");
set_sci_suffix("");
set_not_finite("Nan");
set_zero("0");
set_exp_digits(0);
set_show_exp_sign(false);
```

## Note

This setting assumes that the user is not in LaTeX's "math mode" already.

46.78.2.3 `int format_float::c.mode ( )`

This reproduces the default settings of `cout` in automatic mode. Obviously it is faster to use `iostreams` than to format numbers with this class. Nevertheless, this mode is very useful for testing to ensure that this class processes the numbers correctly at the requested precision.

This function is equivalent to the settings:

```
set_prefix("");
set_sign("-");
set_suffix("");
set_sci_prefix("");
set_times("e");
set_exp_prefix("");
set_exp_sign("-");
set_sci_sign("-");
set_exp_suffix("");
set_sci_suffix("");
set_not_finite("NaN");
set_zero("0");
set_exp_limits(-4, 5);
set_exp_digits(2);
set_show_exp_sign(true);
```

The documentation for this class was generated from the following file:

- `format_float.h`

46.79 `gsl_fit< func_t, vec_t, mat_t, bool_vec_t >::func_par` Struct Reference

A structure for passing to the functions `func()`, `dfunc()`, and `fdfunc()`

```
#include <gsl_fit.h>
```

## 46.79.1 Detailed Description

```
template<class func_t = fit_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base, class bool_vec_t = bool *>struct gsl_fit< func_t, vec_t, mat_t, bool_vec_t >::func_par
```

Definition at line 433 of file `gsl_fit.h`.

## Data Fields

- `func_t & f`  
*The function object.*
- `int ndat`  
*The number.*
- `vec_t * xdat`  
*The x values.*
- `vec_t * ydat`  
*The y values.*
- `vec_t * yerr`  
*The y uncertainties.*
- `int npar`  
*The number of parameters.*

The documentation for this struct was generated from the following file:

- `gsl_fit.h`

## 46.80 min\_fit< func\_t, vec\_t, mat\_t >::func\_par Struct Reference

A structure for passing information to the GSL functions for the [min\\_fit](#) class.

```
#include <min_fit.h>
```

### 46.80.1 Detailed Description

```
template<class func_t = fit.func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base>struct min_fit< func_t, vec_t, mat_t >::func_par
```

This structure is given so that the user can specify the minimizer to use.

Definition at line 75 of file min\_fit.h.

#### Data Fields

- [func\\_t](#) & [f](#)  
*The fitting function.*
- int [ndat](#)  
*The number of data.*
- [vec\\_t](#) \* [xdat](#)  
*The x values.*
- [vec\\_t](#) \* [ydat](#)  
*The y values.*
- [vec\\_t](#) \* [yerr](#)  
*The y uncertainties.*
- int [npar](#)  
*The number of fitting parameters.*

The documentation for this struct was generated from the following file:

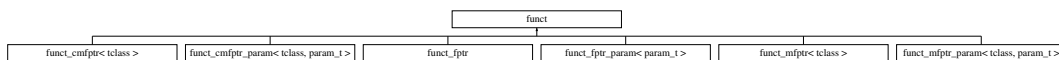
- min\_fit.h

## 46.81 funct Class Reference

One-dimensional function [abstract base].

```
#include <funct.h>
```

Inheritance diagram for funct:



### 46.81.1 Detailed Description

This class generalizes a one-dimensional function  $y(x)$ .

This class is one of a large number of function object classes in O<sub>2</sub>scl designed to provide a mechanism for the user to supply functions to solvers, minimizers, integrators, etc. See [Function Objects](#) for a general description.

Definition at line 41 of file funct.h.

## Public Member Functions

- virtual double `operator()` (double x)=0  
*Compute the function at point x, with result y.*

The documentation for this class was generated from the following file:

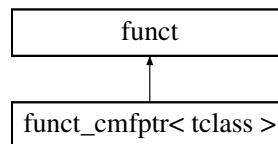
- `funct.h`

46.82 `funct_cmfp< tclass >` Class Template Reference

Const member function pointer to a one-dimensional function.

```
#include <funct.h>
```

Inheritance diagram for `funct_cmfp< tclass >`:



## 46.82.1 Detailed Description

```
template<class tclass>class funct_cmfp< tclass >
```

## Note

While this is designed to accept a pointer to a const member function, the choice of whether the class pointer given in the template type `tclass` is const or not is up to the user.

Definition at line 260 of file `funct.h`.

## Public Member Functions

- `funct_cmfp` (tclass \*tp, double(tclass::\*fp)(double x) const)  
*Specify the member function pointer.*
- virtual double `operator()` (double x)  
*Compute the function at point x, with result y.*

## Protected Member Functions

- `funct_cmfp` (const `funct_cmfp` &f)  
*Copy constructor.*
- `funct_cmfp` & `operator=` (const `funct_cmfp` &f)  
*Copy constructor.*

## Protected Attributes

- double(tclass::\* `fptr`)(double x) const  
*Storage for the const member function pointer.*
- tclass \* `tptr`



*Store the pointer to the class instance.*

The documentation for this class was generated from the following file:

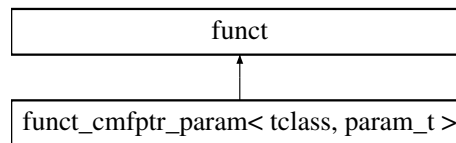
- `funct.h`

## 46.83 `funct_cmfp_ptr_param< tclass, param_t >` Class Template Reference

Const member function pointer to a one-dimensional function with a parameter.

```
#include <funct.h>
```

Inheritance diagram for `funct_cmfp_ptr_param< tclass, param_t >`:



### 46.83.1 Detailed Description

```
template<class tclass, class param_t>class funct_cmfp_ptr_param< tclass, param_t >
```

#### Note

While this is designed to accept a pointer to a const member function, the choice of whether the class pointer given in the template type `tclass` is const or not is up to the user.

Definition at line 315 of file `funct.h`.

#### Public Member Functions

- `funct_cmfp_ptr_param` (`tclass *tp`, `double(tclass::*fp)(double x, param_t &pa) const`, `param_t &pa`)  
*Specify the member function pointer.*
- virtual `double operator()` (`double x`, `param_t &pa`)  
*Compute the function at point  $x$ , with result  $y$ .*

#### Protected Member Functions

- `funct_cmfp_ptr_param` (`const funct_cmfp_ptr_param &f`)  
*Copy constructor.*
- `funct_cmfp_ptr_param & operator=` (`const funct_cmfp_ptr_param &f`)  
*Copy constructor.*

#### Protected Attributes

- `double(tclass::* fptr)` (`double x`, `param_t &pa`) `const`  
*Storage for the const member function pointer.*
- `tclass * tptr`  
*Store the pointer to the class instance.*
- `param_t * pp`  
*The parameter.*

The documentation for this class was generated from the following file:

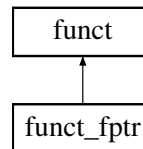
- `funct.h`

## 46.84 `funct_ptr` Class Reference

Function pointer to a function.

```
#include <funct.h>
```

Inheritance diagram for `funct_ptr`:



### 46.84.1 Detailed Description

Definition at line 61 of file `funct.h`.

#### Public Member Functions

- `funct_ptr` (`double(*fp)(double)`)  
*Specify the function pointer.*
- virtual `double operator()` (`double x`)  
*Compute the function at point  $x$ , with result  $y$ .*

#### Protected Member Functions

- `funct_ptr` (`const funct_ptr &f`)  
*Copy constructor.*
- `funct_ptr & operator=` (`const funct_ptr &f`)  
*Copy constructor.*

#### Protected Attributes

- `double(* fptr)` (`double x`)  
*Function pointer.*

The documentation for this class was generated from the following file:

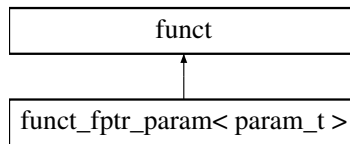
- `funct.h`

## 46.85 `funct_ptr_param< param_t >` Class Template Reference

Function pointer to a function with a parameter.

```
#include <funct.h>
```

Inheritance diagram for `funct_ptr_param< param_t >`:



#### 46.85.1 Detailed Description

`template<class param_t>class funct_fptr_param< param_t >`

Definition at line 103 of file `funct.h`.

#### Public Member Functions

- `funct_fptr_param` (`double(*fp)(double, param_t &), param_t &pa`)  
*Specify the function pointer.*
- virtual `double operator()` (`double x`)  
*Compute the function at point  $x$ , with result  $y$ .*

#### Protected Member Functions

- `funct_fptr_param` (`const funct_fptr_param &f`)  
*Copy constructor.*
- `funct_fptr_param & operator=` (`const funct_fptr_param &f`)  
*Copy constructor.*

#### Protected Attributes

- `double(* fptr)` (`double x, param_t &pa`)  
*The function pointer.*
- `param_t * pp`  
*The parameter.*

The documentation for this class was generated from the following file:

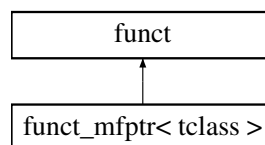
- `funct.h`

## 46.86 `funct_mfptr< tclass >` Class Template Reference

Member function pointer to a one-dimensional function.

```
#include <funct.h>
```

Inheritance diagram for `funct_mfptr< tclass >`:



## 46.86.1 Detailed Description

```
template<class tclass>class funct_mfptr< tclass >
```

Definition at line 149 of file `funct.h`.

## Public Member Functions

- `funct_mfptr` (`tclass *tp`, `double(tclass::*fp)(double x)`)  
*Specify the member function pointer.*
- virtual `double operator()` (`double x`)  
*Compute the function at point  $x$ , with result  $y$ .*

## Protected Member Functions

- `funct_mfptr` (`const funct_mfptr &f`)  
*Copy constructor.*
- `funct_mfptr &operator=` (`const funct_mfptr &f`)  
*Copy constructor.*

## Protected Attributes

- `double(tclass::* fptr)` (`double x`)  
*Storage for the member function pointer.*
- `tclass * tptr`  
*Store the pointer to the class instance.*

The documentation for this class was generated from the following file:

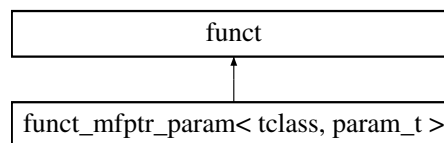
- `funct.h`

46.87 `funct_mfptr_param< tclass, param_t >` Class Template Reference

Member function pointer to a one-dimensional function with a parameter.

```
#include <funct.h>
```

Inheritance diagram for `funct_mfptr_param< tclass, param_t >`:



## 46.87.1 Detailed Description

```
template<class tclass, class param_t>class funct_mfptr_param< tclass, param_t >
```

Definition at line 198 of file `funct.h`.

## Public Member Functions

- [func\\_t\\_mfptr\\_param](#) (tclass \*tp, double(tclass::\*fp)(double x, param\_t &pa), param\_t &pa)  
*Specify the member function pointer.*
- virtual double [operator\(\)](#) (double x)  
*Compute the function at point x, with result y.*

## Protected Member Functions

- [func\\_t\\_mfptr\\_param](#) (const [func\\_t\\_mfptr\\_param](#) &f)  
*Copy constructor.*
- [func\\_t\\_mfptr\\_param](#) & [operator=](#) (const [func\\_t\\_mfptr\\_param](#) &f)  
*Copy constructor.*

## Protected Attributes

- double(tclass::\* [fptr](#))(double x, param\_t &pa)  
*Storage for the member function pointer.*
- tclass \* [tptr](#)  
*Store the pointer to the class instance.*
- param\_t \* [pp](#)  
*The parameter.*

The documentation for this class was generated from the following file:

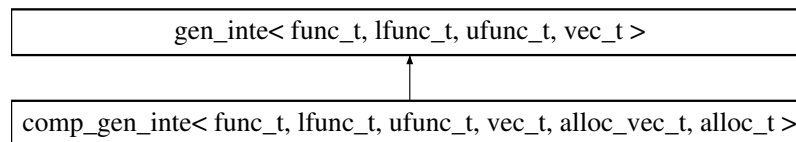
- [funct.h](#)

## 46.88 gen\_inte&lt; func\_t, lfunc\_t, ufunc\_t, vec\_t &gt; Class Template Reference

Generalized multi-dimensional integration [abstract base].

```
#include <gen_inte.h>
```

Inheritance diagram for `gen_inte< func_t, lfunc_t, ufunc_t, vec_t >`:



## 46.88.1 Detailed Description

```
template<class func_t, class lfunc_t, class ufunc_t, class vec_t = ovector_base>class gen_inte< func_t, lfunc_t, ufunc_t, vec_t >
```

Perform the generalized multi-dimensional integral:

$$\int_{x_0=a_0}^{x_0=b_0} f(x_0) \int_{x_1=a_1(x_0)}^{x_1=b_1(x_0)} f(x_0, x_1) \dots \int_{x_{n-1}=a_{n-1}(x_0, x_1, \dots, x_{n-2})}^{x_{n-1}=b_{n-1}(x_0, x_1, \dots, x_{n-2})} f(x_0, x_1, \dots, x_{n-1}) dx_{n-1} \dots dx_1 dx_0$$

The functions  $a_i$  and  $b_i$  are specified in the arguments `a` and `b` to the function [ginteg\(\)](#) or [ginteg\\_err\(\)](#).

In order to allow the user to specify only three functions (for the integrand, the lower limits, and the upper limits) the first argument to the limit and integrand functions is used to distinguish among the limits for each separate integral. So first argument to `a` for  $a_0()$

is 0, and the first argument to `a` for  $a_1()$  is 1, etc., and similarly for the upper limits specified in `b` and the integrands specified in `func`.

At present, the only implementation of this abstract base is in `comp_gen_inte`.

**Idea for Future** It might be interesting to construct a child class of `gen_inte` which automatically transforms variables to a hypercube and then applies a child of `multi_inte` to do the integration.

Definition at line 62 of file `gen_inte.h`.

#### Public Member Functions

- virtual double `ginteg` (func\_t &func, size\_t ndim, lfunc\_t &a, ufunc\_t &b)=0  
*Integrate function `func` from  $x_i = a_i(x_i)$  to  $x_i = b_i(x_i)$  for  $0 < i < \text{ndim} - 1$ .*
- virtual int `ginteg_err` (func\_t &func, size\_t ndim, lfunc\_t &a, ufunc\_t &b, double &res, double &err)  
*Integrate function `func` from  $x_i = a_i(x_i)$  to  $x_i = b_i(x_i)$  for  $0 < i < \text{ndim} - 1$ .*
- double `get_error` ()  
*Return the error in the result from the last call to `ginteg()` or `ginteg_err()`*
- const char \* `type` ()  
*Return string denoting type ("`gen_inte`")*

#### Data Fields

- int `verbose`  
*Verbosity.*
- double `tol_rel`  
*The maximum "uncertainty" in the value of the integral.*
- bool `err_nonconv`  
*If true, call the error handler if the routine does not "converge".*

#### Protected Attributes

- double `interror`  
*The uncertainty for the last integration computation.*

#### 46.88.2 Member Function Documentation

46.88.2.1 `template<class func_t, class lfunc_t, class ufunc_t, class vec_t = ovector_base> double gen_inte< func_t, lfunc_t, ufunc_t, vec_t >::get_error( ) [inline]`

This will quietly return zero if no integrations have been performed.

Definition at line 108 of file `gen_inte.h`.

The documentation for this class was generated from the following file:

- `gen_inte.h`

#### 46.89 gen\_test\_number< tot > Class Template Reference

Generate number sequence for testing.

```
#include <misc.h>
```

## 46.89.1 Detailed Description

```
template<size_t tot>class gen_test_number< tot >
```

A class which generates `tot` numbers from -1 to 1, making sure to include -1, 1, 0, and numbers near -1, 0 and 1 (so long as `tot` is sufficiently large). If `gen()` is called more than `tot` times, it just recycles through the list again.

This class is used to generate combinations of coefficients for testing the polynomial solvers.

For example, the first 15 numbers generated by an object of type `gen_test_number<10>` are:

```
0  -1.000000e+00
1  -9.975274e-01
2  -8.807971e-01
3  -1.192029e-01
4  -2.472623e-03
5  +0.000000e+00
6  +2.472623e-03
7  +1.192029e-01
8  +8.807971e-01
9  +1.000000e+00
10 -1.000000e+00
11 -9.975274e-01
12 -8.807971e-01
13 -1.192029e-01
14 -2.472623e-03
```

This function is used in `src/other/poly_ts.cpp` which tests the polynomial solvers.

**Idea for Future** Document what happens if `tot` is pathologically small.

Definition at line 219 of file `misc.h`.

## Public Member Functions

- double `gen()`  
*Return the next number in the sequence.*

## Protected Attributes

- int `n`  
*Count number of numbers generated.*
- double `fact`  
*A constant factor for the argument to `tanh()`, equal to `tot` divided by 20.*

The documentation for this class was generated from the following file:

- `misc.h`

46.90 `grad_funct< vec_t >` Class Template Reference

Array of multi-dimensional functions [abstract base].

```
#include <multi_min.h>
```

Inheritance diagram for `grad_funct< vec_t >`:



### 46.90.1 Detailed Description

`template<class vec_t = ovector_base>class grad_funct< vec_t >`

This class generalizes `nv` functions of `nv` variables, i.e.  $y_j(x_0, x_1, \dots, x_{nv-1})$  for  $0 \leq j \leq nv - 1$ .

This class is one of a large number of function object classes in `O2scl` designed to provide a mechanism for the user to supply functions to solvers, minimizers, integrators, etc. See [Function Objects](#) for a general description.

#### Note

This class is different from `mm_funct` in that the first vector argument is not `const`.

Definition at line 49 of file `multi_min.h`.

#### Public Member Functions

- virtual int `operator()` (size\_t `nv`, vec\_t &`x`, vec\_t &`y`)=0  
Compute `nv` functions, `y`, of `nv` variables stored in `x` with parameter `pa`.

The documentation for this class was generated from the following file:

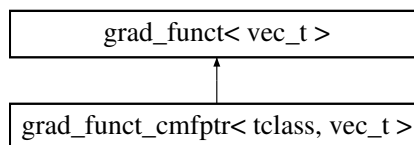
- `multi_min.h`

## 46.91 `grad_funct_cmfptr< tclass, vec_t >` Class Template Reference

Const member function pointer to an array of multi-dimensional functions.

```
#include <multi_min.h>
```

Inheritance diagram for `grad_funct_cmfptr< tclass, vec_t >`:



### 46.91.1 Detailed Description

`template<class tclass, class vec_t = ovector_base>class grad_funct_cmfptr< tclass, vec_t >`

Definition at line 303 of file `multi_min.h`.

#### Public Member Functions

- `grad_funct_cmfptr` ()  
Empty constructor.
- `grad_funct_cmfptr` (tclass \*`tp`, int(tclass::\*`fp`)(size\_t `nv`, vec\_t &`x`, vec\_t &`y`) const)



*Specify the member function pointer.*

- int [set\\_function](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y) const)

*Specify the member function pointer.*

- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &y)

*Compute nv functions, y, of nv variables stored in x with parameter pa.*

#### Protected Attributes

- int(tclass::\* [fptr](#))(size\_t nv, vec\_t &x, vec\_t &y) const

*The member function pointer.*

- tclass \* [tptr](#)

*The class pointer.*

#### Private Member Functions

- [grad\\_funct\\_cmfp](#) (const [grad\\_funct\\_cmfp](#) &)
- [grad\\_funct\\_cmfp](#) & [operator=](#) (const [grad\\_funct\\_cmfp](#) &)

The documentation for this class was generated from the following file:

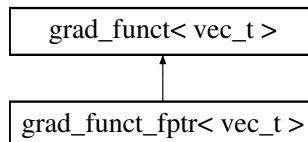
- multi\_min.h

## 46.92 grad\_funct\_fptr< vec\_t > Class Template Reference

Function pointer to array of multi-dimensional functions.

```
#include <multi_min.h>
```

Inheritance diagram for grad\_funct\_fptr< vec\_t >:



### 46.92.1 Detailed Description

```
template<class vec_t = ovector_base>class grad_funct_fptr< vec_t >
```

Definition at line 74 of file multi\_min.h.

#### Public Member Functions

- [grad\\_funct\\_fptr](#) (int(\*fp)(size\_t nv, vec\_t &x, vec\_t &y))

*Specify the function pointer.*

- int [set\\_function](#) (int(\*fp)(size\_t nv, vec\_t &x, vec\_t &y))

*Specify the function pointer.*

- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &y)

*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- `int(* fptr)(size_t nv, vec_t &x, vec_t &y)`  
*The function pointer to the user-supplied function.*

## Private Member Functions

- `grad_funct_fptr` (const `grad_funct_fptr` &)
- `grad_funct_fptr` & `operator=` (const `grad_funct_fptr` &)

The documentation for this class was generated from the following file:

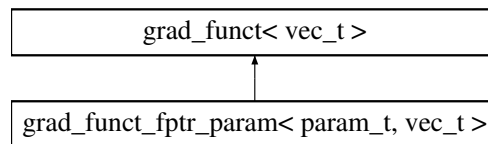
- `multi_min.h`

## 46.93 grad\_funct\_fptr\_param&lt; param\_t, vec\_t &gt; Class Template Reference

Function pointer to array of multi-dimensional functions.

```
#include <multi_min.h>
```

Inheritance diagram for `grad_funct_fptr_param< param_t, vec_t >`:



## 46.93.1 Detailed Description

```
template<class param_t, class vec_t = ovector_base>class grad_funct_fptr_param< param_t, vec_t >
```

Definition at line 123 of file `multi_min.h`.

## Public Member Functions

- `grad_funct_fptr_param` (int(\*fp)(size\_t nv, vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the function pointer.*
- `int set_function` (int(\*fp)(size\_t nv, vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the function pointer.*
- `virtual int operator()` (size\_t nv, vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- `int(* fptr)(size_t nv, vec_t &x, vec_t &y, param_t &)`  
*The function pointer to the user-supplied function.*
- `param_t * pp`  
*The parameter.*

## Private Member Functions

- `grad_func_tfp_ptr_param` (const `grad_func_tfp_ptr_param` &)
- `grad_func_tfp_ptr_param` & `operator=` (const `grad_func_tfp_ptr_param` &)

The documentation for this class was generated from the following file:

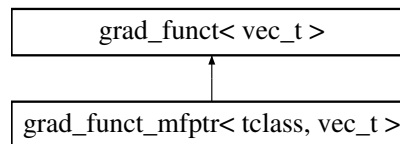
- `multi_min.h`

46.94 `grad_func_tmfptr< tclass, vec_t >` Class Template Reference

Member function pointer to an array of multi-dimensional functions.

```
#include <multi_min.h>
```

Inheritance diagram for `grad_func_tmfptr< tclass, vec_t >`:



## 46.94.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class grad_func_tmfptr< tclass, vec_t >
```

Definition at line 181 of file `multi_min.h`.

## Public Member Functions

- `grad_func_tmfptr` ()  
*Empty constructor.*
- `grad_func_tmfptr` (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y))  
*Specify the member function pointer.*
- int `set_function` (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y))  
*Specify the member function pointer.*
- virtual int `operator()` (size\_t nv, vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- int(tclass::\* `fptr`)(size\_t nv, vec\_t &x, vec\_t &y)  
*The member function pointer.*
- tclass \* `tptr`  
*The class pointer.*

## Private Member Functions

- `grad_func_tmfptr` (const `grad_func_tmfptr` &)
- `grad_func_tmfptr` & `operator=` (const `grad_func_tmfptr` &)

The documentation for this class was generated from the following file:

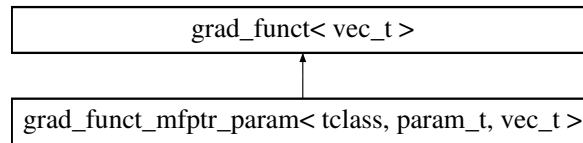
- `multi_min.h`

## 46.95 grad\_funct\_mfptr\_param&lt; tclass, param\_t, vec\_t &gt; Class Template Reference

Member function pointer to an array of multi-dimensional functions.

```
#include <multi_min.h>
```

Inheritance diagram for grad\_funct\_mfptr\_param< tclass, param\_t, vec\_t >:



## 46.95.1 Detailed Description

```
template<class tclass, class param_t, class vec_t = ovector_base>class grad_funct_mfptr_param< tclass, param_t, vec_t >
```

Definition at line 239 of file multi\_min.h.

## Public Member Functions

- [grad\\_funct\\_mfptr\\_param](#) ()  
*Empty constructor.*
- [grad\\_funct\\_mfptr\\_param](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the member function pointer.*
- int [set\\_function](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the member function pointer.*
- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- int(tclass::\* [fptr](#)) (size\_t nv, vec\_t &x, vec\_t &y, param\_t &pa)  
*The member function pointer.*
- tclass \* [tptr](#)  
*The class pointer.*
- param\_t \* [pp](#)  
*Parameter.*

## Private Member Functions

- [grad\\_funct\\_mfptr\\_param](#) (const [grad\\_funct\\_mfptr\\_param](#) &)
- [grad\\_funct\\_mfptr\\_param](#) & [operator=](#) (const [grad\\_funct\\_mfptr\\_param](#) &)

The documentation for this class was generated from the following file:

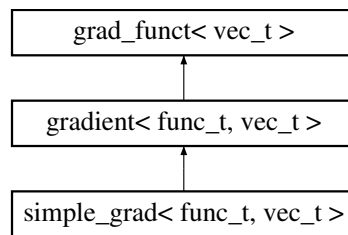
- multi\_min.h

## 46.96 gradient&lt; func\_t, vec\_t &gt; Class Template Reference

Class for automatically computing gradients [abstract base].

```
#include <multi_min.h>
```

Inheritance diagram for gradient< func\_t, vec\_t >:



#### 46.96.1 Detailed Description

```
template<class func_t, class vec_t = ovector_base>class gradient< func_t, vec_t >
```

Default template arguments

- func\_t - (no default)
- vec\_t - [ovector\\_base](#)

**Idea for Future** Consider making an exact\_grad class for computing exact gradients.

Definition at line 368 of file multi\_min.h.

#### Public Member Functions

- virtual int [set\\_function](#) (func\_t &f)  
*Set the function to compute the gradient of.*
- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &g)=0  
*Compute the gradient g at the point x.*

#### Protected Attributes

- func\_t \* [func](#)  
*A pointer to the user-specified function.*

The documentation for this class was generated from the following file:

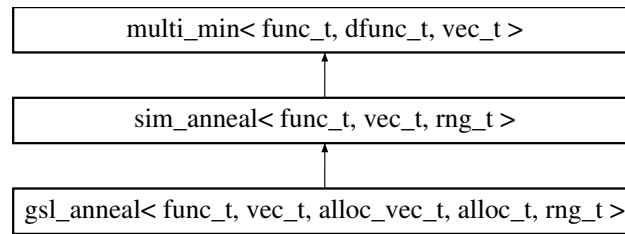
- multi\_min.h

## 46.97 gsl\_anneal< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, rng\_t > Class Template Reference

Multidimensional minimization by simulated annealing (GSL)

```
#include <gsl_anneal.h>
```

Inheritance diagram for gsl\_anneal< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, rng\_t >:



#### 46.97.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class rng_t = gsl-
rnga>class gsl_anneal< func_t, vec_t, alloc_vec_t, alloc_t, rng_t >
```

This class is a modification of simulated annealing as implemented in GSL in the function `gsl_siman_solve()`. It acts as a generic multidimensional minimizer for any function given a generic temperature schedule specified by the user.

There are a large variety of strategies for choosing the temperature evolution. To offer the user the largest possible flexibility, the temperature evolution is controlled by the virtual functions `start()` and `next()` which can be freely changed by creating a child class which overwrites these functions.

The simulated annealing algorithm proposes a displacement of one coordinate of the previous point by

$$x_{i,\text{new}} = \text{step\_size}_i(2u_i - 1) + x_{i,\text{old}}$$

where the  $u_i$  are random numbers between 0 and 1. The displacement is accepted or rejected based on the Metropolis method. The random number generator is set in the parent, `sim_anneal`.

The default behavior is as follows: Initially, the step sizes are chosen to be 1.0 (or whatever was recently specified in `set_step()`) and the temperature to be `T_start` (default 1.0). Each iteration decreases the temperature by a factor of `T_dec` (default 1.5) for each step, and the minimizer is finished when the next decrease would bring the temperature below `multi_min::tol_abs`. If none of the `multi_min::ntrial` steps in a particular iteration changes the value of the minimum, and the step sizes are greater than `min_step_ratio` (default 100) times `multi_min::tol_abs`, then the step sizes are decreased by a factor of `step_dec` (default 1.5) for the next iteration.

If `multi_min::verbose` is greater than zero, then `mmin()` will print out information and/or request a keypress after the function iterations for each temperature.

An example demonstrating the usage of this class is given in `examples/ex_anneal.cpp` and in the [Simulated annealing](#).

The form of the user-specified function is as in `multi_func` has a "function value" which is the value of the function (given in the third argument as a number of type `double`), and a "return value" (the integer return value). The initial function evaluation which is performed at the user-specified initial guess must give 0 as the return value. If subsequent function evaluations have a non-zero return value, then the resulting point is ignored and a new point is selected.

This class thus can sometimes handle constrained minimization problems. If the user ensures that the function's return value is non-zero when the function is evaluated outside the allowed region, the minimizer will not accept any steps which take the minimizer outside the allowed region. Note that this should be done with care, however, as this approach may cause convergence problems with sufficiently difficult functions or constraints.

See also a multi-threaded version of this class in [anneal\\_mt](#).

**Idea for Future** There's `x0`, `old_x`, `new_x`, `best_x`, and `x`? There's probably some duplication here which could be avoided.

**Idea for Future** • Implement a more general simulated annealing routine which would allow the solution of discrete problems like the Traveling Salesman problem.

Definition at line 134 of file `gsl_anneal.h`.

## Public Member Functions

- virtual int `mmin` (size\_t nvar, vec\_t &x0, double &fmin, func\_t &func)  
*Calculate the minimum  $f_{min}$  of  $func$  w.r.t the array  $x_0$  of size  $nvar$ .*
- virtual const char \* `type` ()  
*Return string denoting type ("gsl\_anneal")*
- template<class vec2\_t >  
int `set_step` (size\_t nv, vec2\_t &stepv)  
*Set the step sizes.*

## Data Fields

- double `boltz`  
*Boltzmann factor (default 1.0).*
- double `T_start`  
*Initial temperature (default 1.0)*
- double `T_dec`  
*Factor to decrease temperature by (default 1.5)*
- double `step_dec`  
*Factor to decrease step size by (default 1.5)*
- double `min_step_ratio`  
*Ratio between minimum step size and `tol_abs` (default 100.0)*

## Protected Member Functions

- virtual int `next` (size\_t nvar, vec\_t &x\_old, double min\_old, vec\_t &x\_new, double min\_new, double &T, size\_t n\_moves, bool &finished)  
*Determine how to change the minimization for the next iteration.*
- virtual int `start` (size\_t nvar, double &T)  
*Setup initial temperature and stepsize.*
- virtual int `allocate` (size\_t n, double boltz\_factor=1.0)  
*Allocate memory for a minimizer over  $n$  dimensions with stepsize  $step$  and Boltzmann factor  $boltz\_factor$ .*
- virtual int `free` ()  
*Free allocated memory.*
- virtual int `step` (vec\_t &sx, int nvar)  
*Make a step to a new attempted minimum.*

## Protected Attributes

- alloc\_t `ao`  
*Allocation object.*
- ovector `step_vec`  
*Vector of step sizes.*

## Storage for present, next, and best vectors

- alloc\_vec\_t `x`
- alloc\_vec\_t `new_x`
- alloc\_vec\_t `best_x`
- alloc\_vec\_t `old_x`

The documentation for this class was generated from the following file:

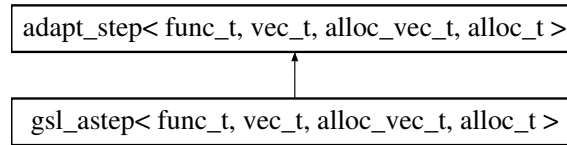
- `gsl_anneal.h`

**46.98 `gsl_aste< func_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference**

Adaptive ODE stepper (GSL)

```
#include <gsl_aste.h>
```

Inheritance diagram for `gsl_aste< func_t, vec_t, alloc_vec_t, alloc_t >`:

**46.98.1 Detailed Description**

```
template<class func_t = ode_func<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_aste< func_t,
vec_t, alloc_vec_t, alloc_t >
```

This class performs an adaptive step of a system of ODEs. To modify the ODE stepper which is used, use the function [adapt\\_step::set\\_step\(\)](#).

Note, this has been updated to correspond to the `ode-initval2` functions in GSL.

There is an example for the usage of this class in `examples/ex_ode.cpp` documented in the [Ordinary differential equations](#) section.

**Todo** Document what happens when the stepper function returns a non-zero value, as it's different now with the `ode-initval2` function.

Document count, failed\_steps, etc.

**Idea for Future** Compare more directly to GSL

Default template arguments

- `func_t` - [ode\\_func](#)
- `vec_t` - [ovector\\_base](#)
- `alloc_vec_t` - [ovector](#)
- `alloc_t` - [ovector\\_alloc](#)

Definition at line 259 of file `gsl_aste.h`.

**Public Member Functions**

- virtual int [aste](#)(double &x, double xmax, double &h, size\_t n, vec\_t &y, vec\_t &dydx\_out, vec\_t &yerr, func\_t &derivs)  
*Make an adaptive integration step of the system `derivs`.*
- virtual int [aste\\_derivs](#)(double &x, double xmax, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yerr, func\_t &derivs)  
*Make an adaptive integration step of the system `derivs` with derivatives.*
- virtual int [aste\\_full](#)(double x, double xmax, double &x\_out, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Make an adaptive integration step of the system `derivs`.*



## Data Fields

- [gsl\\_ode\\_control](#)< vec\_t > [con](#)  
*Control specification.*

## Protected Member Functions

- [int evolve\\_apply](#) (double t0, double t1, double &t, double &h, size\_t nvar, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Apply the evolution for the next adaptive step.*

## Protected Attributes

- [alloc\\_t ao](#)  
*Memory allocator for objects of type alloc\_vec\_t.*
- [alloc\\_vec\\_t yout\\_int](#)  
*Temporary storage for yout.*
- [alloc\\_vec\\_t dydx\\_int](#)  
*Internal storage for dydx.*
- [double last\\_step](#)  
*The size of the last step.*
- [unsigned long int count](#)  
*The number of steps.*
- [unsigned long int failed\\_steps](#)  
*The number of failed steps.*
- [size\\_t msize](#)  
*The size of the allocated vectors.*

## 46.98.2 Member Function Documentation

46.98.2.1 `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >::evolve_apply ( double t0, double t1, double & t, double & h, size_t nvar, vec_t & y, vec_t & dydx, vec_t & yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [inline, protected]`

This function is based on `gsl_odeiv2_evolve_apply`.

## Note

This function requires that `y`, `yout`, `dydx` and `dydx_out` are all distinct vectors.

Definition at line 293 of file `gsl_astep.h`.

46.98.2.2 `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >::astep ( double & x, double xmax, double & h, size_t n, vec_t & y, vec_t & dydx_out, vec_t & yerr, func_t & derivs ) [inline, virtual]`

This attempts to take a step of size `h` from the point `x` of an `n`-dimensional system `derivs` starting with `y`. On exit, `x` and `y` contain the new values at the end of the step, `h` contains the size of the step, `dydx_out` contains the derivative at the end of the step, and `yerr` contains the estimated error at the end of the step.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 452 of file `gsl_astep.h`.

```
46.98.2.3 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
    gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >::astep_derivs ( double & x, double xmax, double & h, size_t n, vec_t & y, vec_t & dydx,
    vec_t & yerr, func_t & derivs ) [inline, virtual]
```

This attempts to take a step of size `h` from the point `x` of an `n`-dimensional system `derivs` starting with `y` and given the initial derivatives `dydx`. On exit, `x`, `y` and `dydx` contain the new values at the end of the step, `h` contains the size of the step, `dydx` contains the derivative at the end of the step, and `yerr` contains the estimated error at the end of the step.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 497 of file `gsl_astep.h`.

```
46.98.2.4 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
    gsl_astep< func_t, vec_t, alloc_vec_t, alloc_t >::astep_full ( double x, double xmax, double & x_out, double & h, size_t n, vec_t & y,
    vec_t & dydx, vec_t & yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [inline, virtual]
```

This function performs an adaptive integration step with the `n`-dimensional system `derivs` and parameter `pa`. It Begins at `x` with initial stepsize `h`, ensuring that the step goes no farther than `xmax`. At the end of the step, the size of the step taken is `h` and the new value of `x` is in `x_out`. Initially, the function values and derivatives should be specified in `y` and `dydx`. The function values, derivatives, and the error at the end of the step are given in `yout`, `yerr`, and `dydx_out`. Unlike in [ode\\_step](#) objects, the objects `y`, `yout`, `dydx`, and `dydx_out` must all be distinct.

This adaptive stepper function is faster than [astep\(\)](#) or [astep\\_derivs\(\)](#) because it does not require any copying of vectors.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 548 of file `gsl_astep.h`.

The documentation for this class was generated from the following file:

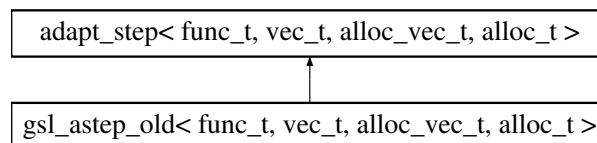
- `gsl_astep.h`

## 46.99 `gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference

Adaptive ODE stepper (GSL)

```
#include <gsl_astep_old.h>
```

Inheritance diagram for `gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >`:



### 46.99.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>class gsl_astep_old<
func_t, vec_t, alloc_vec_t, alloc_t >
```

[This is the stepper from O2scl version 0.908 which is kept around for diagnostic purposes and some legacy code.]

This class performs an adaptive step of a system of ODEs. To modify the ODE stepper which is used, use the function [adapt\\_step::set\\_step\(\)](#).

There is an example for the usage of this class in `examples/ex_ode.cpp` documented in the [Ordinary differential equations](#) section.

Default template arguments

- [func\\_t](#) - [ode\\_func\\_t](#)
- [vec\\_t](#) - [ovector\\_base](#)
- [alloc\\_vec\\_t](#) - [ovector](#)
- [alloc\\_t](#) - [ovector\\_alloc](#)

Definition at line 78 of file `gsl_astep_old.h`.

#### Public Member Functions

- virtual int [astep\\_derivs](#) (double &x, double xmax, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yerr, func\_t &derivs)  
*Make an adaptive integration step of the system `derivs` with derivatives.*
- virtual int [astep\\_full](#) (double x, double xmax, double &x\_out, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout2, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Make an adaptive integration step of the system `derivs`.*
- virtual int [astep](#) (double &x, double xmax, double &h, size\_t n, vec\_t &y, vec\_t &dydx\_out, vec\_t &yerr, func\_t &derivs)  
*Make an adaptive integration step of the system `derivs`.*

#### Data Fields

- [gsl\\_ode\\_control](#)< vec\_t > [con](#)  
*Control specification.*

#### Protected Member Functions

- int [evolve\\_apply](#) (double t0, double &t, double &h, double t1, size\_t nvar, vec\_t &y, vec\_t &dydx, vec\_t &yout2, vec\_t &yerr, vec\_t &dydx\_out2, func\_t &derivs)  
*Apply the evolution for the next adaptive step.*

#### Protected Attributes

- [alloc\\_t](#) [ao](#)  
*Memory allocator for objects of type `alloc_vec_t`.*
- [alloc\\_vec\\_t](#) [yout](#)  
*Temporary storage for `yout`.*
- [alloc\\_vec\\_t](#) [dydx\\_int](#)  
*Internal storage for `dydx`.*
- double [last\\_step](#)  
*The size of the last step.*
- unsigned long int [count](#)  
*The number of steps.*
- unsigned long int [failed\\_steps](#)  
*The number of failed steps.*
- size\_t [msize](#)  
*The size of the allocated vectors.*

### 46.99.2 Member Function Documentation

**46.99.2.1** `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >::astep_derivs ( double & x, double xmax, double & h, size_t n, vec_t & y, vec_t & dydx, vec_t & yerr, func_t & derivs ) [inline, virtual]`

This attempts to take a step of size `h` from the point `x` of an `n`-dimensional system `derivs` starting with `y` and given the initial derivatives `dydx`. On exit, `x`, `y` and `dydx` contain the new values at the end of the step, `h` contains the size of the step, `dydx` contains the derivative at the end of the step, and `yerr` contains the estimated error at the end of the step.

If the base stepper returns a non-zero value, the step is aborted and `y` is unmodified. The error handler is never called.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 209 of file `gsl_astep_old.h`.

```
46.99.2.2 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >::astep_full( double x, double xmax, double & x_out, double & h, size_t n, vec_t &
y, vec_t & dydx, vec_t & yout2, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [inline, virtual]
```

This function performs an adaptive integration step with the `n`-dimensional system `derivs` and parameter `pa`. It Begins at `x` with initial stepsize `h`, ensuring that the step goes no farther than `xmax`. At the end of the step, the size of the step taken is `h` and the new value of `x` is in `x_out`. Initially, the function values and derivatives should be specified in `y` and `dydx`. The function values, derivatives, and the error at the end of the step are given in `yout`, `yerr`, and `dydx_out`. Unlike in [ode\\_step](#) objects, the objects `y`, `yout`, `dydx`, and `dydx_out` must all be distinct.

If the base stepper returns a non-zero value, the step is aborted. The error handler is never called.

This adaptive stepper function is faster than [astep\(\)](#) or [astep\\_derivs\(\)](#) because it does not require any copying of vectors.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 263 of file `gsl_astep_old.h`.

```
46.99.2.3 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual
int gsl_astep_old< func_t, vec_t, alloc_vec_t, alloc_t >::astep( double & x, double xmax, double & h, size_t n, vec_t & y, vec_t &
dydx_out, vec_t & yerr, func_t & derivs ) [inline, virtual]
```

This attempts to take a step of size `h` from the point `x` of an `n`-dimensional system `derivs` starting with `y`. On exit, `x` and `y` contain the new values at the end of the step, `h` contains the size of the step, `dydx_out` contains the derivative at the end of the step, and `yerr` contains the estimated error at the end of the step.

If the system `derivs` or the base stepper return a non-zero value, the adaptive step is aborted and `y` is unmodified. The error handler is never called.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 298 of file `gsl_astep_old.h`.

The documentation for this class was generated from the following file:

- `gsl_astep_old.h`

## 46.100 gsl\_bsimp< func\_t, jac\_func\_t, vec\_t, alloc\_vec\_t, alloc\_t, mat\_t, alloc\_mat\_t, mat\_alloc\_t > Class Template Reference

Bulirsch-Stoer implicit ODE stepper (GSL)

```
#include <gsl_bsimp.h>
```

### 46.100.1 Detailed Description

```
template<class func_t, class jac_func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_
base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc> class gsl_bsimp< func_t, jac_func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t,
mat_alloc_t >
```

Bader-Deuffhard implicit extrapolative stepper ([Bader83](#)).

## Note

The variable `h_next` was defined in the original GSL version has been removed here, as it was unused by the stepper routine. At the moment, this class retains the GSL approach to handling non-integer return values in the user-specified derivative function. If the user-specified function returns `gsl_efailed`, then the stepper attempts to decrease the stepsize to continue. If the user-specified function returns a non-zero value other than `gsl_efailed`, or if the Jacobian evaluation returns any non-zero value, then the stepper aborts and returns the error value without calling the error handler. This behavior may change in the future.

**Idea for Future** Create an example with a stiff diff eq. which requires this kind of stepper

**Idea for Future** More detailed documentation about the algorithm

**Idea for Future** Figure out if this should be a child of `ode_step` or `adapt_step`. The function `step_local()` is actually its own ODE stepper and could be reimplemented as an object of type `ode_step`.

**Idea for Future** I don't like setting `yerr` to `GSL_POSINF`, there should be a better way to force an adaptive stepper which is calling this stepper to readjust the stepsize.

**Idea for Future** The functions `deuf_kchoice()` and `compute_weights()` can be moved out of this header file

**Idea for Future** Rework internal arrays as uvectors?

**Idea for Future** Rework linear solver to be amenable to using a sparse matrix solver

Definition at line 102 of file `gsl_bsimp.h`.

## Public Member Functions

- int `reset()`  
*Reset stepper.*
- virtual int `step` (double x, double h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs, jac\_func\_t &jac)  
*Perform an integration step.*

## Protected Member Functions

- int `compute_weights` (const double y[], double w[], size\_t n)  
*Compute weights.*
- size\_t `deuf_kchoice` (double eps2, size\_t dimension)  
*Calculate a choice for the "order" of the method, using the Deuffhard criteria.*
- int `poly_extrap` (`gsl_matrix` \*dloc, const double x[], const unsigned int i\_step, const double x\_i, const vec\_t &y\_i, vec\_t &y\_0, vec\_t &y\_0\_err, double work[])  
*Polynomial extrapolation.*
- int `step_local` (const double t0, const double h\_total, const unsigned int n\_step, const double y[], const double yp\_loc[], const vec\_t &dfdt\_loc, const mat\_t &dfdy\_loc, vec\_t &y\_out)  
*Basic implicit Bulirsch-Stoer step.*
- int `allocate` (size\_t n)  
*Allocate memory for a system of size n.*
- void `free()`  
*Free allocated memory.*

## Protected Attributes

- size\_t **dim**  
*Size of allocated vectors.*
- alloc\_t **ao**  
*Memory allocator for objects of type alloc\_vec\_t.*
- mat\_alloc\_t **mo**  
*Memory allocator for objects of type alloc\_mat\_t.*
- func\_t \* **funcp**  
*Function specifying derivatives.*
- jac\_func\_t \* **jfuncp**  
*Jacobian.*
- gsl\_matrix \* **d**  
*Workspace for extrapolation.*
- gsl\_matrix \* **a\_mat**  
*Workspace for linear system matrix.*
- double **ex\_wk** [sequence\_max]  
*Workspace for extrapolation.*
- size\_t **order**  
*Order of last step.*

## State info

- size\_t **k\_current**
- size\_t **k\_choice**
- double **eps**

## Workspace for extrapolation step

- double \* **yp**
- double \* **y\_save**
- double \* **yerr\_save**
- double \* **y\_extrap\_save**
- alloc\_vec\_t **y\_extrap\_sequence**
- double \* **extrap\_work**
- alloc\_vec\_t **dfdt**
- alloc\_vec\_t **y\_temp**
- alloc\_vec\_t **delta\_temp**
- double \* **weight**
- alloc\_mat\_t **dfdy**

## Workspace for the basic stepper

- alloc\_vec\_t **rhs\_temp**
- double \* **delta**

## Static Protected Attributes

- static const int **sequence\_count** = 8  
*Number of entries in the Bader-Deufllhard extrapolation sequence.*
- static const int **sequence\_max** = 7  
*Largest index of the Bader-Deufllhard extrapolation sequence.*

## 46.100.2 Member Function Documentation

46.100.2.1 `template<class func_t, class jac_func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc> size_t gsl_bsimp< func_t, jac_func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t >::deuf_kchoice ( double eps2, size_t dimension ) [inline, protected]`

Used in the `allocate()` function.

Definition at line 189 of file `gsl_bsimp.h`.

```
46.100.2.2 template<class func_t, class jac_func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t
= omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc> int gsl_bsimp< func_t, jac_func_t, vec_t, alloc_vec_t,
alloc_t, mat_t, alloc_mat_t, mat_alloc_t >::poly_extrap ( gsl_matrix * dloc, const double x[], const unsigned int i_step, const double
x_i, const vec_t & y_i, vec_t & y_0, vec_t & y_0_err, double work[] ) [inline, protected]
```

Compute the step of index `i_step` using polynomial extrapolation to evaluate functions by fitting a polynomial to estimates (`x_i`, `y_i`) and output the result to `y_0` and `y_0_err`.

The index `i_step` begins with zero.

Definition at line 244 of file `gsl_bsimp.h`.

```
46.100.2.3 template<class func_t, class jac_func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t
= omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc> int gsl_bsimp< func_t, jac_func_t, vec_t, alloc_vec_t,
alloc_t, mat_t, alloc_mat_t, mat_alloc_t >::step_local ( const double t0, const double h_total, const unsigned int n_step, const double y[],
const double yp_loc[], const vec_t & dfdt_loc, const mat_t & dfdy_loc, vec_t & y_out ) [inline, protected]
```

Divide the step `h_total` into `n_step` smaller steps and do the Bader-Deufhard semi-implicit iteration. This function starts at `t0` with function values `y`, derivatives `yp_loc`, and information from the Jacobian to compute the final value `y_out`.

Definition at line 293 of file `gsl_bsimp.h`.

```
46.100.2.4 template<class func_t, class jac_func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class
mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc> virtual int gsl_bsimp< func_t, jac_func_t, vec_t,
alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t >::step ( double x, double h, size_t n, vec_t & y, vec_t & dydx, vec_t & yout, vec_t &
yerr, vec_t & dydx_out, func_t & derivs, jac_func_t & jac ) [inline, virtual]
```

Given initial value of the `n`-dimensional function in `y` and the derivative in `dydx` (which must generally be computed beforehand) at the point `x`, take a step of size `h` giving the result in `yout`, the uncertainty in `yerr`, and the new derivative in `dydx_out` (at `x+h`) using function `derivs` to calculate derivatives. Implementations which do not calculate `yerr` and/or `dydx_out` do not reference these variables so that a blank `vec_t` can be given. All of the implementations allow `yout=y` and `dydx_out=dydx` if necessary.

Definition at line 504 of file `gsl_bsimp.h`.

#### 46.100.3 Field Documentation

```
46.100.3.1 template<class func_t, class jac_func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class
mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc> double gsl_bsimp< func_t, jac_func_t, vec_t,
alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t >::ex_wk[sequence_max] [protected]
```

(This state variable was named 'x' in GSL.)

Definition at line 139 of file `gsl_bsimp.h`.

The documentation for this class was generated from the following file:

- `gsl_bsimp.h`

## 46.101 gsl\_chebapp Class Reference

Chebyshev approximation (GSL)

```
#include <gsl_chebapp.h>
```

## 46.101.1 Detailed Description

Approximate a function on a finite interval using a Chebyshev series:

$$f(x) = \sum_n c_n T_n(x) \quad \text{where} \quad T_n(x) = \cos(n \arccos x)$$

Definition at line 44 of file `gsl_chebapp.h`.

## Public Member Functions

- `gsl_chebapp` (const `gsl_chebapp` &gc)  
*Copy constructor.*
- `gsl_chebapp & operator=` (const `gsl_chebapp` &gc)  
*Copy constructor.*

## Initialization methods

- template<class func\_t >  
int `init` (func\_t &func, size\_t ord, double a1, double b1)  
*Initialize a Chebyshev approximation of the function `func` over the interval from `a1` to `b1`.*
- template<class vec\_t >  
int `init` (double a1, double b1, size\_t ord, vec\_t &v)  
*Create an approximation from a vector of coefficients.*
- template<class vec\_t >  
int `init_func_values` (double a1, double b1, size\_t ord, vec\_t &fval)  
*Create an approximation from a vector of function values.*

## Evaluation methods

- double `eval` (double x) const  
*Evaluate the approximation.*
- double `operator()` (double x) const  
*Evaluate the approximation.*
- double `eval_n` (size\_t n, double x) const  
*Evaluate the approximation to a specified order.*
- int `eval_err` (double x, double &result, double &abserr)  
*Evaluate the approximation and give the uncertainty.*
- int `eval_n_err` (size\_t n, double x, double &result, double &abserr)  
*Evaluate the approximation to a specified order and give the uncertainty.*

## Manipulating coefficients and endpoints

- double `get_coefficient` (size\_t ix) const  
*Get a coefficient.*
- int `set_coefficient` (size\_t ix, double co)  
*Set a coefficient.*
- int `get_endpoints` (double &la, double &lb)  
*Return the endpoints of the approximation.*
- template<class vec\_t >  
int `get_coefficients` (size\_t n, vec\_t &v) const  
*Get the coefficients.*
- template<class vec\_t >  
int `set_coefficients` (size\_t n, const vec\_t &v)  
*Set the coefficients.*

## Derivatives and integrals

- int `deriv` (`gsl_chebapp` &gc) const  
*Make `gc` an approximation to the derivative.*
- int `integ` (`gsl_chebapp` &gc) const  
*Make `gc` an approximation to the integral.*



## Protected Attributes

- [uvector c](#)  
*Coefficients.*
- [size\\_t order](#)  
*Order of the approximation.*
- [double a](#)  
*Lower end of the interval.*
- [double b](#)  
*Upper end of the interval.*
- [size\\_t order\\_sp](#)  
*Single precision order.*
- [uvector f](#)  
*Function evaluated at Chebyshev points.*
- [bool init\\_called](#)  
*True if init has been called.*

## 46.101.2 Member Function Documentation

46.101.2.1 `template<class func_t > int gsl_chebapp::init( func_t & func, size_t ord, double a1, double b1 )` `[inline]`

The interval must be specified so that  $a < b$ , so a and b are swapped if this is not the case.

Definition at line 107 of file `gsl_chebapp.h`.

46.101.2.2 `double gsl_chebapp::get_coefficient( size_t ix ) const` `[inline]`

Legal values of the argument are 0 to `order` (inclusive)

Definition at line 326 of file `gsl_chebapp.h`.

46.101.2.3 `int gsl_chebapp::set_coefficient( size_t ix, double co )` `[inline]`

Legal values of the argument are 0 to `order` (inclusive)

Definition at line 340 of file `gsl_chebapp.h`.

The documentation for this class was generated from the following file:

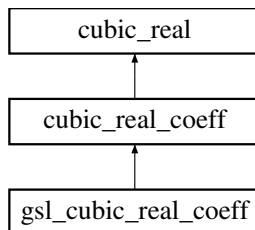
- `gsl_chebapp.h`

## 46.102 gsl\_cubic\_real\_coeff Class Reference

Solve a cubic with real coefficients and complex roots (GSL)

```
#include <poly.h>
```

Inheritance diagram for `gsl_cubic_real_coeff`:



## 46.102.1 Detailed Description

Definition at line 495 of file `poly.h`.

## Public Member Functions

- virtual int `solve_rc` (const double a3, const double b3, const double c3, const double d3, double &x1, std::complex< double > &x2, std::complex< double > &x3)  
Solves the polynomial  $a_3x^3 + b_3x^2 + c_3x + d_3 = 0$  giving the real solution  $x = x_1$  and two complex solutions  $x = x_2$  and  $x = x_3$ .
- const char \* `type` ()  
Return a string denoting the type ("`gsl_cubic_real_coeff`")
- int `gsl_poly_complex_solve_cubic2` (double a, double b, double c, gsl\_complex \*z0, gsl\_complex \*z1, gsl\_complex \*z2)  
An alternative to `gsl_poly_complex_solve_cubic()`

## 46.102.2 Member Function Documentation

46.102.2.1 int `gsl_cubic_real_coeff::gsl_poly_complex_solve_cubic2` ( double a, double b, double c, gsl\_complex \* z0, gsl\_complex \* z1, gsl\_complex \* z2 )

This is an alternative to the function `gsl_poly_complex_solve_cubic()` with some small corrections to ensure finite values for some cubics. See `src/other/poly_ts.cpp` for more.

**Idea for Future** I think the GSL function is now fixed, so we can fall back to the original GSL function here.

The documentation for this class was generated from the following file:

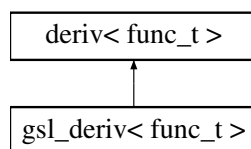
- `poly.h`

46.103 `gsl_deriv< func_t >` Class Template Reference

Numerical differentiation (GSL)

```
#include <gsl_deriv.h>
```

Inheritance diagram for `gsl_deriv< func_t >`:



## 46.103.1 Detailed Description

```
template<class func_t = funct>class gsl_deriv< func_t >
```

This class computes the numerical derivative of a function. The stepsize `h` should be specified before use. If similar functions are being differentiated in succession, the user may be able to increase the speed of later derivatives by setting the new stepsize equal to the optimized stepsize from the previous differentiation, by setting `h` to `h_opt`.

The derivative computation will never fail, but the results will be incorrect for sufficiently difficult functions or if the step size is not properly chosen.

Some successive derivative computations can be made more efficient by using the optimized stepsize in `gsl_deriv::h_opt`, which is set by the most recent last derivative computation.

Setting `deriv::verbose` to a number greater than zero results in output for each call to `central_deriv()` which looks like:

```
gsl_deriv:
step: 1.000000e-04
abscissas: 4.999500e-01 4.999000e-01 5.000500e-01 5.001000e-01
ordinates: 4.793377e-01 4.793816e-01 4.794694e-01 4.795132e-01
res: 8.775825e-01 trc: 1.462163e-09 rnd: 7.361543e-12
```

where the last line contains the result (`res`), the truncation error (`trc`) and the rounding error (`rnd`). If `deriv::verbose` is greater than 1, a keypress is required after each iteration.

Computing first derivatives requires either 1 or 2 calls to `central_deriv()` and thus either 4 or 8 function calls. This class never calls the error handler.

#### Note

Second and third derivatives are computed by naive nested applications of the formula for the first derivative. No uncertainty for these derivatives is provided.

An example demonstrating the usage of this class is given in `examples/ex_deriv.cpp` and the [Numerical differentiation](#).

**Idea for Future** Include the forward and backward GSL derivatives?

Definition at line 105 of file `gsl_deriv.h`.

#### Public Member Functions

- virtual int `calc_err` (double x, func\_t &func, double &dfdx, double &err)  
*Calculate the first derivative of `func` w.r.t. `x` and uncertainty.*
- virtual const char \* `type` ()  
*Return string denoting type ("`gsl_deriv`")*

#### Data Fields

- double `h`  
*Initial stepsize.*
- double `h_opt`  
*The last value of the optimized stepsize.*

#### Protected Member Functions

- template<class func2\_t >  
int `calc_base` (double x, func\_t &func, double &dfdx, double &err)  
*Internal template version of the derivative function.*
- virtual int `calc_err_int` (double x, func\_t &func, double &dfdx, double &err)  
*Internal version of `calc_err()` for second and third derivatives.*
- template<class func2\_t >  
int `central_deriv` (double x, double hh, double &result, double &abserr\_round, double &abserr\_trunc, func2\_t &func)  
*Compute derivative using 5-point rule.*

## 46.103.2 Member Function Documentation

46.103.2.1 `template<class func_t = funct> template<class func2_t > int gsl_deriv< func_t >::central_deriv ( double x, double hh, double & result, double & abserr_round, double & abserr_trunc, func2_t & func ) [inline, protected]`

Compute the derivative using the 5-point rule (x-h, x-h/2, x, x+h/2, x+h) and the error using the difference between the 5-point and the 3-point rule (x-h,x,x+h). Note that the central point is not used for either.

This must be a class template because it is used by both [calc\\_err\(\)](#) and [calc\\_err\\_int\(\)](#).

Definition at line 207 of file `gsl_deriv.h`.

## 46.103.3 Field Documentation

46.103.3.1 `template<class func_t = funct> double gsl_deriv< func_t >::h`

This should be specified before a call to [calc\(\)](#) or [calc\\_err\(\)](#). If it is zero, then  $x10^{-4}$  will used, or if x is zero, then  $10^{-4}$  will be used.

Definition at line 122 of file `gsl_deriv.h`.

46.103.3.2 `template<class func_t = funct> double gsl_deriv< func_t >::h_opt`

This is initialized to zero in the constructor and set by [calc\\_err\(\)](#) to the most recent value of the optimized stepsize.

Definition at line 129 of file `gsl_deriv.h`.

The documentation for this class was generated from the following file:

- `gsl_deriv.h`

## 46.104 gsl\_fft Class Reference

Real mixed-radix fast Fourier transform.

```
#include <gsl_fft.h>
```

## 46.104.1 Detailed Description

This is a simple wrapper for the GSL FFT functions which automatically allocates the necessary memory.

Definition at line 40 of file `gsl_fft.h`.

## Public Member Functions

- int [transform](#) (int n, double \*x)  
*Perform the FFT transform.*
- int [inverse\\_transform](#) (int n, double \*x)  
*Perform the inverse FFT transform.*

## Protected Member Functions

- int [mem\\_resize](#) (int new\_size)  
*Reallocate memory.*

## Protected Attributes

- `int mem_size`  
*The current memory size.*
- `gsl_fft_real_workspace * work`  
*The GSL workspace.*
- `gsl_fft_real_wavetable * real`  
*The table for the forward transform.*
- `gsl_fft_halfcomplex_wavetable * hc`  
*The table for the inverse transform.*

The documentation for this class was generated from the following file:

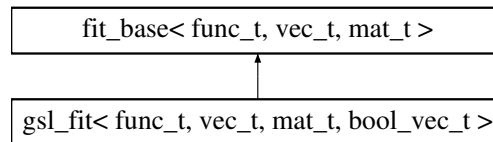
- `gsl_fft.h`

46.105 `gsl_fit< func_t, vec_t, mat_t, bool_vec_t >` Class Template Reference

Non-linear least-squares fitting class (GSL)

```
#include <gsl_fit.h>
```

Inheritance diagram for `gsl_fit< func_t, vec_t, mat_t, bool_vec_t >`:



## 46.105.1 Detailed Description

```
template<class func_t = fit_func<>, class vec_t = ovector_base, class mat_t = omatrix_base, class bool_vec_t = bool *> class gsl_fit< func_t, vec_t, mat_t, bool_vec_t >
```

The GSL-based fitting class using a Levenberg-Marquardt type algorithm. The algorithm stops when

$$|dx_i| < \text{epsabs} + \text{epsrel} \times |x_i|$$

where  $dx$  is the last step and  $x$  is the current position. If `test_gradient` is true, then additionally `fit()` requires that

$$\sum_i |g_i| < \text{epsabs}$$

where  $g_i$  is the  $i$ -th component of the gradient of the function  $\Phi(x)$  where

$$\Phi(x) = ||F(x)||^2$$

## Default template arguments

- `func_t` - `fit_func<>`
- `vec_t` - `ovector_base`
- `alloc_vec_t` - `ovector`
- `bool_vec_t` - `bool *`

**Todo** Properly generalize other vector types than ovector\_base

Allow the user to specify the derivatives

Fix so that the user can specify automatic scaling of the fitting parameters, where the initial guess are used for scaling so that the fitting parameters are near unity.

Definition at line 91 of file gsl\_fit.h.

## Data Structures

- struct [func\\_par](#)  
*A structure for passing to the functions [func\(\)](#), [dfunc\(\)](#), and [fdfunc\(\)](#)*

## Public Member Functions

- virtual int [fit](#) (size\_t ndat, vec\_t &xdat, vec\_t &ydat, vec\_t &yerr, size\_t npar, vec\_t &par, mat\_t &covar, double &chi2, func\_t &fitfun)  
*Fit the data specified in (xdat,ydat) to the function `fitfun` with the parameters in `par`.*
- virtual const char \* [type](#) ()  
*Return string denoting type ("gsl\_fit")*

## Data Fields

- int [max\\_iter](#)  
*(default 500)*
- double [epsabs](#)  
*(default 1.0e-4)*
- double [epsrel](#)  
*(default 1.0e-4)*
- bool [test\\_gradient](#)  
*If true, test the gradient also (default false)*
- bool [use\\_scaled](#)  
*Use the scaled routine if true (default true)*

## Protected Member Functions

- virtual int [print\\_iter](#) (size\_t nv, gsl\_vector \*x, int iter, double val, double lim)  
*Print the progress in the current iteration.*

## Static Protected Member Functions

- static int [func](#) (const gsl\_vector \*x, void \*pa, gsl\_vector \*f)  
*Evaluate the function.*
- static int [dfunc](#) (const gsl\_vector \*x, void \*pa, [gsl\\_matrix](#) \*jac)  
*Evaluate the jacobian.*
- static int [fdfunc](#) (const gsl\_vector \*x, void \*pa, gsl\_vector \*f, [gsl\\_matrix](#) \*jac)  
*Evaluate the function and the jacobian.*

## 46.105.2 Member Function Documentation

**46.105.2.1** `template<class func_t = fit_func<>, class vec_t = ovector_base, class mat_t = omatrix_base, class bool_vec_t = bool *> virtual int gsl_fit< func_t, vec_t, mat_t, bool_vec_t >::fit ( size_t ndat, vec_t & xdat, vec_t & ydat, vec_t & yerr, size_t npar, vec_t & par, mat_t & covar, double & chi2, func_t & fitfun ) [inline, virtual]`

The covariance matrix for the parameters is returned in `covar` and the value of  $\chi^2$  is returned in `chi2`.

Implements [fit\\_base< func\\_t, vec\\_t, mat\\_t >](#).

Definition at line 261 of file `gsl_fit.h`.

The documentation for this class was generated from the following file:

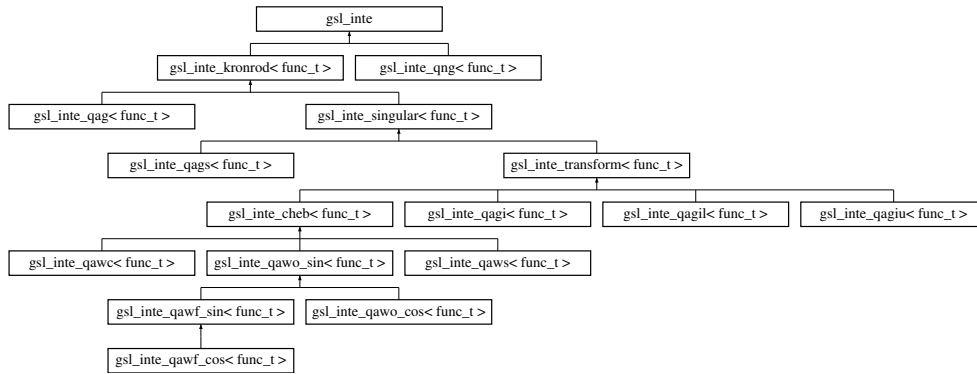
- `gsl_fit.h`

## 46.106 gsl\_inte Class Reference

GSL integration base.

```
#include <gsl_inte.h>
```

Inheritance diagram for `gsl_inte`:



### 46.106.1 Detailed Description

This base class does not perform any actual integration, but just provides functions to be used in the integration classes based on GSL.

Definition at line 56 of file `gsl_inte.h`.

#### Protected Member Functions

- double [rescale\\_error](#) (double *err*, const double *result\_abs*, const double *result\_asc*)  
*QUADPACK's nonlinear rescaling of the absolute-error estimate.*

### 46.106.2 Member Function Documentation

#### 46.106.2.1 double `gsl_inte::rescale_error ( double err, const double result_abs, const double result_asc )` `[inline, protected]`

The values  $\rho_{\text{abs}}$  (stored in `result_abs`) and  $\rho_{\text{asc}}$  (stored in `result_asc`) are assumed to be

$$\begin{aligned}\rho_{\text{abs}} &= \int_a^b |f| dx, \\ \rho_{\text{asc}} &= \int_a^b |f - \mu(f)| dx, \quad \mu(f) = \frac{1}{b-a} \int_a^b f dx,\end{aligned}$$

all of which are computed from the best (i.e., finest-grid) approximation of the integrals. The rescaled error,  $\sigma_{\text{err}}$ , is computed from the raw error, `err`, by

$$\sigma_{\text{err}} = \rho_{\text{asc}} \cdot \min \left\{ 1, \left( \frac{200|\text{err}|}{\rho_{\text{asc}}} \right)^{3/2} \right\},$$

or

$$\sigma_{\text{err}} = 50 \cdot \epsilon_{\text{mach}} \cdot \rho_{\text{abs}},$$

whichever of the two is greater. The value  $\epsilon_{\text{mach}}$  denotes "machine epsilon." (In the case that the second value underflows, the first value is automatically accepted.)

This function is used in `gsl_inte_qng` and `gsl_inte_kronrod::gauss_kronrod_base()`.

Definition at line 100 of file `gsl_inte.h`.

The documentation for this class was generated from the following file:

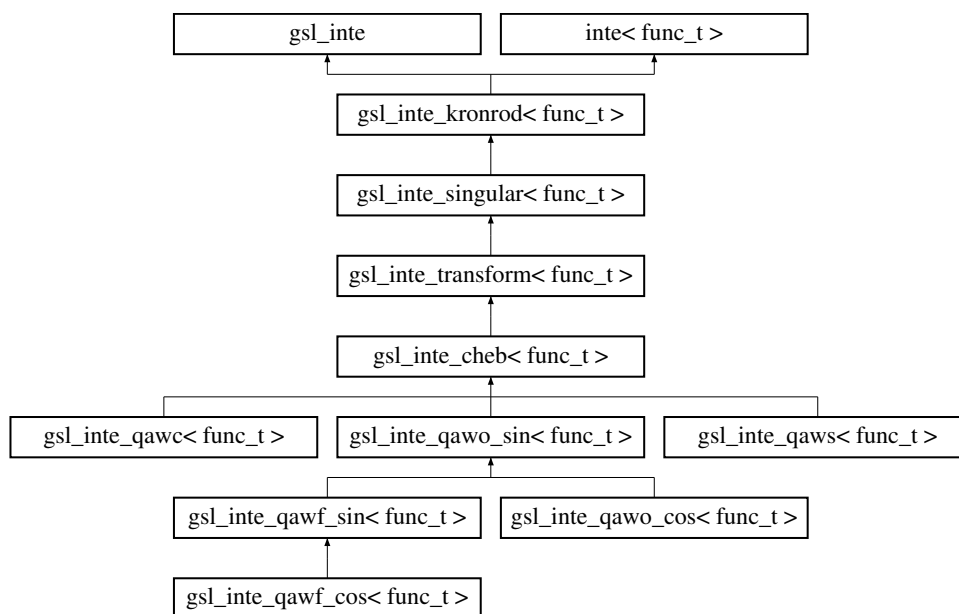
- `gsl_inte.h`

## 46.107 `gsl_inte_cheb< func_t >` Class Template Reference

Chebyshev integration base class (GSL)

```
#include <gsl_inte_qawc.h>
```

Inheritance diagram for `gsl_inte_cheb< func_t >`:



### 46.107.1 Detailed Description

```
template<class func_t>class gsl_inte_cheb< func_t >
```

This class provides the basic Chebyshev integration functions for use in the GSL-based integration classes which require them. See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 42 of file `gsl_inte_qawc.h`.

#### Protected Member Functions

- void `compute_moments` (double cc, double \*moment)  
*Compute the Chebyshev moments.*



- `template<class func2_t>`  
`void inte\_cheb\_series (func2_t &f, double a, double b, double *cheb12, double *cheb24)`  
*Compute Chebyshev series expansion using a FFT method.*

#### 46.107.2 Member Function Documentation

46.107.2.1 `template<class func_t> template<class func2_t> void gsl\_inte\_cheb< func_t >::inte_cheb_series ( func2_t &f, double a, double b, double *cheb12, double *cheb24 )` [`inline`, `protected`]

The Chebyshev coefficients for the truncated expansions,

$$f(x) = \frac{a_0}{2}T_0(x) + \frac{a_d}{2}T_d(x) + \sum_{k=1}^{d-1} a_k^{(d)}T_k(x),$$

are computed for  $d = 12$  and  $d = 24$  using an FFT algorithm from [Tolstov62](#) that is adapted so that the both sets of coefficients are computed simultaneously.

Given the function specified in `f`, this function computes the 13 Chebyshev coefficients,  $C_k^{12}$  of degree 12 and 25 Chebyshev coefficients of degree 24,  $C_k^{24}$ , for the interval  $[a, b]$  using a FFT method.

These coefficients are constructed to approximate the original function with

$$f = \sum_{k=1}^{13} C_k^{12} T_{k-1}(x)$$

and

$$f = \sum_{k=1}^{25} C_k^{24} T_{k-1}(x)$$

where  $T_{k-1}(x)$  is the Chebyshev polynomial of degree  $k - 1$  evaluated at the point  $x$ .

It is assumed that memory for `cheb12` and `cheb24` has been allocated beforehand.

Originally written in QUADPACK by R. Piessens and E. de Doncker, translated into C for GSL by Brian Gough, and then rewritten for O<sub>2</sub>scl.

Definition at line 111 of file `gsl_inte_qawc.h`.

The documentation for this class was generated from the following file:

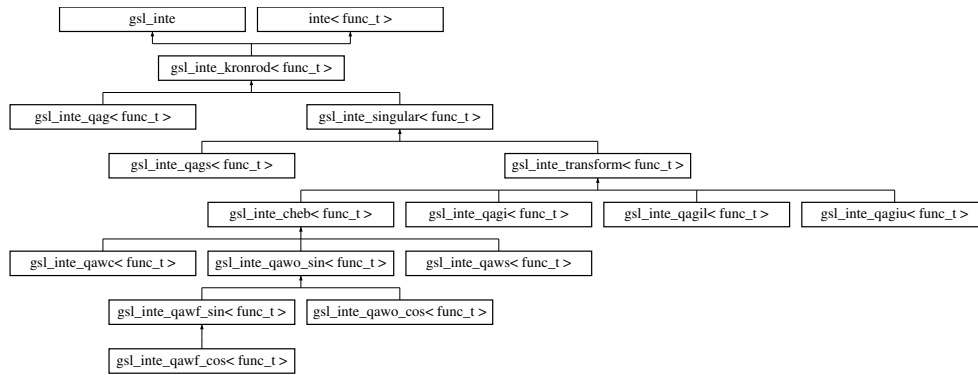
- `gsl_inte_qawc.h`

#### 46.108 gsl\_inte\_kronrod< func\_t > Class Template Reference

Basic Gauss-Kronrod integration class (GSL)

`#include <gsl_inte_kronrod.h>`

Inheritance diagram for `gsl_inte_kronrod< func_t >`:



### 46.108.1 Detailed Description

`template<class func_t>class gsl_inte_kronrod< func_t >`

This class provides the basic Gauss-Kronrod integration function and integration workspace for some of the GSL-based integration classes.

The main function of interest is `set_rule()`, which sets the integration rule for the GSL integration classes which inherit from this base class. The argument to set rule should be selected from the following list:

- 1: 15-point Gauss-Kronrod integration rule (default)
- 2: 21-point rule
- 3: 31-point rule
- 4: 41-point rule
- 5: 51-point rule
- 6: 61-point rule Any value other than 1-6 forces the error handler to be called. All classes default to the 15-point rule, except for `gsl_inte_qags` which defaults to the 21-point rule for singularities.

The integration coefficients for use with this class and associated children are stored in the `o2scl_inte_gk_coeffs` namespace.

**Idea for Future** Convert 'double \*' objects to uvector

Definition at line 610 of file `gsl_inte_kronrod.h`.

#### Public Member Functions

- `int get_rule ()`  
*Get the Gauss-Kronrod integration rule.*
- `void set_rule (int rule)`  
*Set the Gauss-Kronrod integration rule to be used.*
- `int set_limit (size_t lim)`  
*Set the limit for the number of subdivisions of the integration region (default 1000)*
- `template<class func2_t >`  
`void gauss_kronrod_base (func2_t &func, double a, double b, double *result, double *abserr, double *resabs, double *resasc)`  
*The base Gauss-Kronrod integration function template.*
- `virtual void gauss_kronrod (func_t &func, double a, double b, double *result, double *abserr, double *resabs, double *resasc)`  
*Integration wrapper for user-specified function type.*

## Protected Attributes

- `gsl_inte_workspace * w`  
*The integration workspace.*
- `int n_gk`  
*Size of Gauss-Kronrod arrays.*
- `const double * x_gk`  
*Gauss-Kronrod abscissae pointer.*
- `const double * w_g`  
*Gauss weight pointer.*
- `const double * w_gk`  
*Gauss-Kronrod weight pointer.*
- `double * f_v1`  
*Scratch space.*
- `double * f_v2`  
*Scratch space.*

## 46.108.2 Member Function Documentation

46.108.2.1 `template<class func_t> int gsl_inte_kronrod< func_t >::get_rule ( ) [inline]`

This returns the index of the GSL integration rule a number between 1 and 6 (inclusive)

Definition at line 659 of file `gsl_inte_kronrod.h`.

46.108.2.2 `template<class func_t> int gsl_inte_kronrod< func_t >::set_limit ( size_t lim ) [inline]`

If the value of `size` is zero, the error handler will be called.

Definition at line 741 of file `gsl_inte_kronrod.h`.

46.108.2.3 `template<class func_t> template<class func2_t> void gsl_inte_kronrod< func_t >::gauss_kronrod_base ( func2_t & func, double a, double b, double * result, double * abserr, double * resabs, double * resasc ) [inline]`

Given abscissas and weights, this performs the integration of `func` between `a` and `b`, providing a result with uncertainties.

The Gauss-Kronrod rule uses  $2m + 1$  abscissae  $x_1, \dots, x_{2m+1} \in (a, b)$  to estimate the integral of a function as a linear combination of values,

$$\int_a^b f dx \approx Q_m^{GK} f \equiv \sum_{k=1}^{2m+1} \beta_k f(x_k),$$

where the weights  $\beta_1, \dots, \beta_{2m+1}$  are intrinsic to the abscissae. The data are designed so that the even-indexed abscissae yield a coarser estimate,

$$Q_m^G f \equiv \sum_{j=1}^m \alpha_j f(x_{2j}),$$

and their difference  $|Q_m^G f - Q_m^{GK} f|$  is the "raw" error estimate. The various quantities that the function computes are

$$\begin{aligned} \text{result} &= Q_m^{GK} f, \\ \text{resabs} &= Q_m^{GK} |f|, \\ \text{resasc} &= Q_m^{GK} (|f| - \mu), \quad \mu \equiv \frac{Q_m^{GK} f}{b-a}. \end{aligned}$$

The "absolute" error `abserr` is computed from the raw error value using the function `gsl_inte::rescale_error`.

This function is designed for use with the values given in the `o2scl_inte_gk_coeffs` namespace.

This function never calls the error handler.

**Idea for Future** This function, in principle, is an integration object in and of itself, and could be implemented separately as an object of type `inte`.

Definition at line 794 of file `gsl_inte_kronrod.h`.

The documentation for this class was generated from the following file:

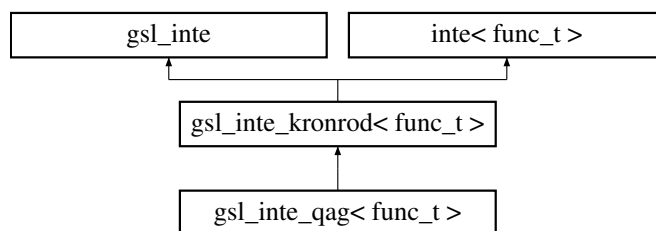
- `gsl_inte_kronrod.h`

## 46.109 `gsl_inte_qag< func_t >` Class Template Reference

Adaptive numerical integration of a function (without singularities) on a bounded interval (GSL)

```
#include <gsl_inte_qag.h>
```

Inheritance diagram for `gsl_inte_qag< func_t >`:



### 46.109.1 Detailed Description

```
template<class func_t = funct>class gsl_inte_qag< func_t >
```

Adaptive integration of a univariate function requires two main procedures: approximating the integral on a bounded interval, and estimating the approximation error. The algorithm recursively refines the interval, computing the integral and its error estimate on each subinterval, until the total error estimate over **all** subintervals falls within the user-specified tolerance. The value returned is the sum of the (approximated) integrals over all subintervals.

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

**Idea for Future** There are a few fine-tuned parameters which should be re-expressed as data members in the convergence tests.

**Idea for Future** Should QUADPACK parameters in round-off tests be subject to adjustments by the end user?

**Idea for Future** Add functions to examine the contents of the workspace to detect regions where the integrand may be problematic; possibly call these functions automatically depending on verbosity settings.

Definition at line 78 of file `gsl_inte_qag.h`.

### Public Member Functions

- `gsl_inte_qag ()`  
*Create an integrator with the specified rule.*
- virtual int `integ_err` (`func_t &func`, double `a`, double `b`, double `&res`, double `&err`)  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*
- const char \* `type ()`  
*Return string denoting type ("`gsl_inte_qag`")*

## Protected Member Functions

- int [qag](#) (func\_t &func, const double a, const double b, const double l\_epsabs, const double l\_epsrel, double \*result, double \*abserr)  
*Perform an adaptive integration given the coefficients, and returning result.*

## 46.109.2 Member Function Documentation

46.109.2.1 `template<class func_t = func_t> int gsl_inte_qag< func_t >::qag ( func_t & func, const double a, const double b, const double l_epsabs, const double l_epsrel, double * result, double * abserr ) [inline, protected]`

**Idea for Future** Just move this function to [integ\\_err\(\)](#).

Definition at line 107 of file `gsl_inte_qag.h`.

The documentation for this class was generated from the following file:

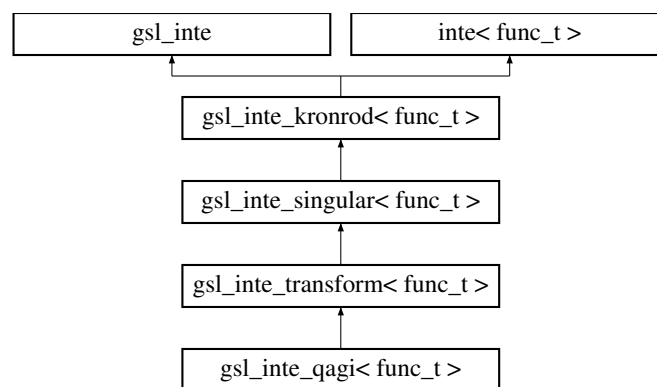
- `gsl_inte_qag.h`

## 46.110 gsl\_inte\_qagi&lt; func\_t &gt; Class Template Reference

Integrate a function over the interval  $(-\infty, \infty)$  (GSL)

```
#include <gsl_inte_qagi.h>
```

Inheritance diagram for `gsl_inte_qagi< func_t >`:



## 46.110.1 Detailed Description

```
template<class func_t = func_t>class gsl_inte_qagi< func_t >
```

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 40 of file `gsl_inte_qagi.h`.

## Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function func from  $-\infty$  to  $\infty$  giving result res and error err.*

## Protected Member Functions

- virtual double [transform](#) (double t, func\_t &func)  
*Transformation to  $t \in (0, 1]$ .*

## 46.110.2 Member Function Documentation

46.110.2.1 `template<class func_t = funct> virtual int gsl_inte_qagi< func_t >::integ_err ( func_t & func, double a, double b, double & res, double & err ) [inline, virtual]`

The values a and b are ignored

Implements [inte< func\\_t >](#).

Definition at line 50 of file `gsl_inte_qagi.h`.

The documentation for this class was generated from the following file:

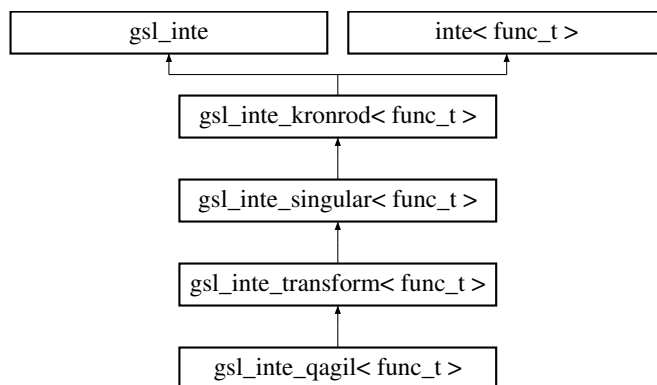
- `gsl_inte_qagi.h`

## 46.111 gsl\_inte\_qagil&lt; func\_t &gt; Class Template Reference

Integrate a function over the interval  $(-\infty, b]$  (GSL)

`#include <gsl_inte_qagil.h>`

Inheritance diagram for `gsl_inte_qagil< func_t >`:



## 46.111.1 Detailed Description

`template<class func_t = funct> class gsl_inte_qagil< func_t >`

The integral on the unbounded interval is rewritten over the semi-open interval  $(0, 1]$  via a variable transformation,

$$\int_{-\infty}^b f(x) dx = \int_0^1 f(b - (1-t)/t) t^{-2} dt,$$

and the right hand side is evaluated with [gsl\\_inte\\_qags](#).

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 48 of file `gsl_inte_qagil.h`.

## Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from  $-\infty$  to `b` and place the result in `res` and the error in `err`.*

## Protected Member Functions

- virtual double [transform](#) (double t, func\_t &func)  
*Transform to  $t \in (0, 1]$ .*

## Protected Attributes

- double [upper\\_limit](#)  
*The upper limit.*

## 46.111.2 Member Function Documentation

46.111.2.1 `template<class func_t = func_t> virtual int gsl_inte_qagil< func_t >::integ_err ( func_t &func, double a, double b, double &res, double &err ) [inline, virtual]`

The value given in `a` is ignored.

Implements [inte< func\\_t >](#).

Definition at line 67 of file `gsl_inte_qagil.h`.

The documentation for this class was generated from the following file:

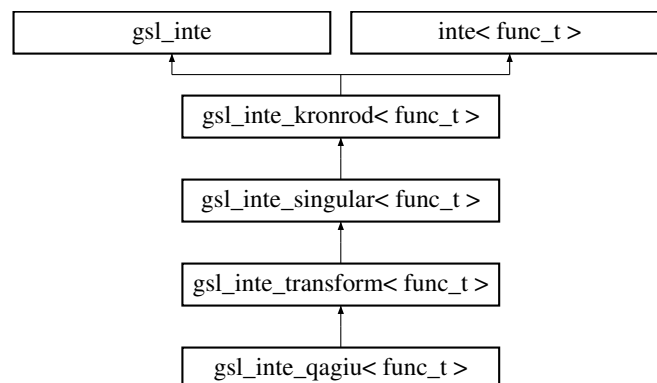
- `gsl_inte_qagil.h`

## 46.112 gsl\_inte\_qagiu&lt; func\_t &gt; Class Template Reference

Integrate a function over the interval  $[a, \infty)$  (GSL)

`#include <gsl_inte_qagiu.h>`

Inheritance diagram for `gsl_inte_qagiu< func_t >`:



## 46.112.1 Detailed Description

```
template<class func_t = func_t>class gsl_inte_qagi< func_t >
```

The integral on the unbounded interval is rewritten over the semi-open interval  $(0, 1]$  via a variable transformation,

$$\int_a^\infty f(x) dx = \int_0^1 f(a + (1-t)/t) t^{-2} dt,$$

and the right hand side is evaluated with [gsl\\_inte\\_qags](#).

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 48 of file `gsl_inte_qagi.h`.

#### Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate a function over the interval  $[a, \infty)$  giving result `res` and error `err`.*

#### Protected Member Functions

- virtual double [transform](#) (double t, func\_t &func)  
*Transform to  $t \in (0, 1]$ .*

#### Protected Attributes

- double [lower\\_limit](#)  
*The lower limit.*

#### 46.112.2 Member Function Documentation

46.112.2.1 `template<class func_t = func_t> virtual int gsl_inte_qagi< func_t >::integ_err ( func_t & func, double a, double b, double & res, double & err ) [inline, virtual]`

The value `b` is ignored.

Implements [inte< func\\_t >](#).

Definition at line 67 of file `gsl_inte_qagi.h`.

The documentation for this class was generated from the following file:

- `gsl_inte_qagi.h`

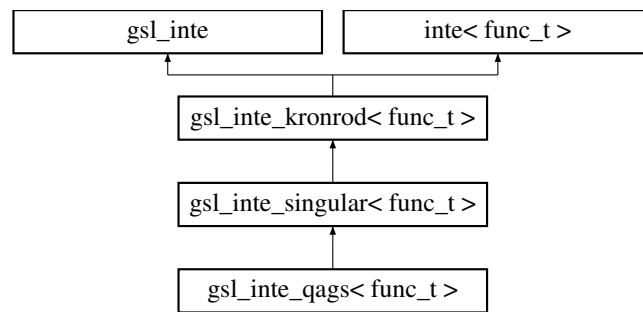
#### 46.113 `gsl_inte_qags< func_t >` Class Template Reference

Integrate a function with a singularity (GSL)

```
#include <gsl_inte_qags.h>
```

Inheritance diagram for `gsl_inte_qags< func_t >`:





#### 46.113.1 Detailed Description

```
template<class func_t = funct>class gsl_inte_qags< func_t >
```

If a function is unbounded but has a finite integral, using the adaptive algorithm described for [gsl\\_inte\\_qag](#) to compute that integral (up to specified tolerance) will converge very slowly. The integration routine of this class remedies this by combining the adaptive algorithm with a series-acceleration method.

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 53 of file `gsl_inte_qags.h`.

#### Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*

The documentation for this class was generated from the following file:

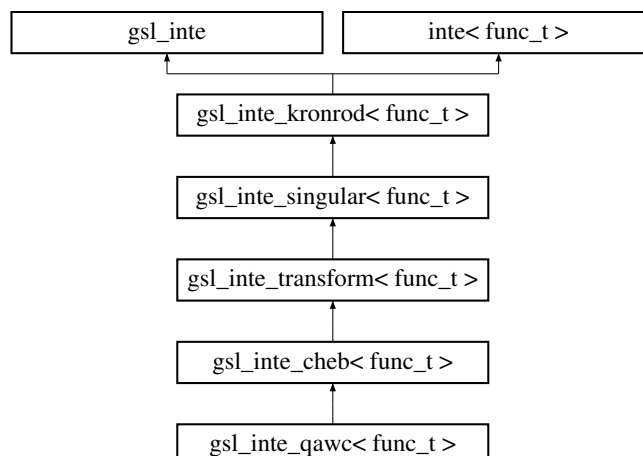
- `gsl_inte_qags.h`

#### 46.114 `gsl_inte_qawc< func_t >` Class Template Reference

Adaptive Cauchy principal value integration (GSL)

```
#include <gsl_inte_qawc.h>
```

Inheritance diagram for `gsl_inte_qawc< func_t >`:



## 46.114.1 Detailed Description

```
template<class func_t>class gsl_inte_qawc< func_t >
```

The Cauchy principal value of the integral of

$$\int_a^b \frac{f(x)}{x-c} dx = \lim_{\varepsilon \rightarrow 0^+} \left\{ \int_a^{c-\varepsilon} \frac{f(x)}{x-c} dx + \int_{c+\varepsilon}^b \frac{f(x)}{x-c} dx \right\}.$$

over  $(a, b)$ , with a singularity at  $c$ , is computed. The adaptive refinement algorithm described for [gsl\\_inte\\_qag](#) is used with modifications to ensure that subdivisions do not occur at the singular point  $x = c$ . When a subinterval contains the point  $x = c$  or is close to it, a special 25-point modified Clenshaw-Curtis rule is used to control the singularity. Further away from the singularity the algorithm uses a Gauss-Kronrod integration rule.

The location of the singularity must be specified before-hand in [gsl\\_inte\\_qawc::s](#), and the singularity must not be at one of the endpoints. Note that when integrating a function of the form  $\frac{f(x)}{(x-s)}$ , the denominator  $(x-s)$  must not be specified in the argument `func` to [integ\(\)](#). Note that this is different from how the [cern\\_cauchy](#) operates.

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

**Idea for Future** Make [cern\\_cauchy](#) and this class consistent in the way which they require the user to provide the denominator in the integrand

Definition at line 347 of file `gsl_inte_qawc.h`.

## Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*

## Data Fields

- double [s](#)  
*The singularity.*

## Protected Member Functions

- int [qawc](#) (func\_t &func, const double a, const double b, const double c, const double epsabs, const double epsrel, double \*result, double \*abserr)  
*The full GSL integration routine called by [integ\\_err\(\)](#)*
- void [qc25c](#) (func\_t &func, double a, double b, double c, double \*result, double \*abserr, int \*err\_reliable)  
*25-point quadrature for Cauchy principal values*
- virtual double [transform](#) (double t, func\_t &func)  
*Add the singularity to the function.*
- const char \* [type](#) ()  
*Return string denoting type ("gsl\_inte\_qawc")*

The documentation for this class was generated from the following file:

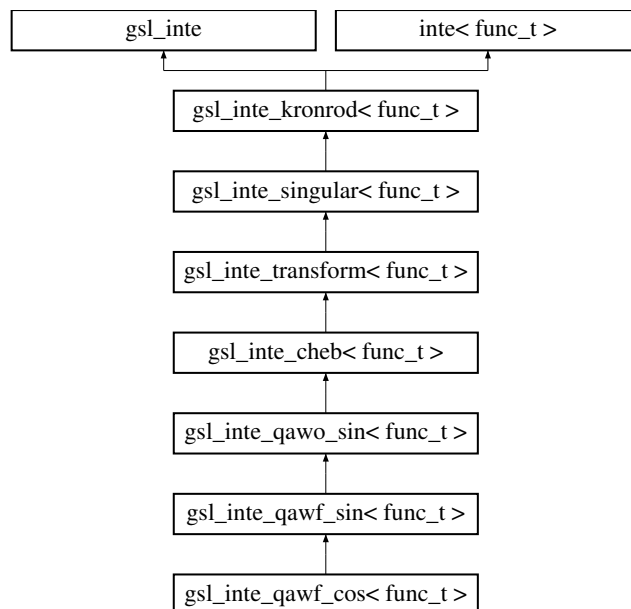
- `gsl_inte_qawc.h`

## 46.115 gsl\_inte\_qawf\_cos&lt; func\_t &gt; Class Template Reference

Adaptive integration a function with finite limits of integration (GSL)

```
#include <gsl_inte_qawf.h>
```

Inheritance diagram for gsl\_inte\_qawf\_cos< func\_t >:



## 46.115.1 Detailed Description

```
template<class func_t>class gsl_inte_qawf_cos< func_t >
```

The Fourier integral

$$\int_a^\infty f(x) \cos(\omega x) dx$$

is computed for some frequency parameter  $\omega$ .

This class is exactly analogous to [gsl\\_inte\\_qawf\\_sin](#). See that class documentation for more details.

Definition at line 385 of file `gsl_inte_qawf.h`.

## Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*

## Protected Member Functions

- virtual double [transform](#) (double t, func\_t &func)  
*Add the oscillating part to the integrand.*
- const char \* [type](#) ()  
*Return string denoting type ("`gsl_inte_qawf_cos`")*

The documentation for this class was generated from the following file:

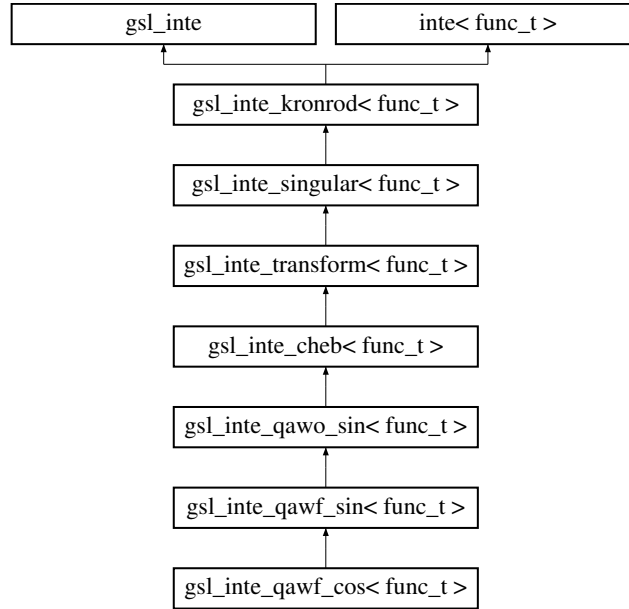
- `gsl_inte_qawf.h`

## 46.116 gsl\_inte\_qawf\_sin&lt; func\_t &gt; Class Template Reference

Adaptive integration for oscillatory integrals (GSL)

```
#include <gsl_inte_qawf.h>
```

Inheritance diagram for gsl\_inte\_qawf\_sin< func\_t >:



## 46.116.1 Detailed Description

```
template<class func_t>class gsl_inte_qawf_sin< func_t >
```

The Fourier integral

$$\int_a^\infty f(x) \sin(\omega x) dx$$

is computed for some frequency parameter  $\omega$ , stored in `gsl_inte_qawo_sin::omega`.

The integral is computed using the same method as `gsl_inte_qawo_sin` and `gsl_inte_qawo_cos` over each of the subintervals,

$$\begin{aligned} C_1 &= [a, a+c] \\ C_2 &= [a+c, a+2c] \\ &\vdots \\ C_k &= [a+(k-1)c, a+kc], \end{aligned}$$

where  $c = (2\text{floor}(|\omega|) + 1)\pi/|\omega|$ . This width is chosen to cover an odd number of periods so that the contributions from the intervals alternate in sign and are monotonically decreasing when  $f$  is positive and monotonically decreasing. The sum of this sequence of contributions is accelerated using the  $\varepsilon$  algorithm.

The algorithm uses zero for the relative tolerance `inte::tol_rel` and attempts to compute the integral to an overall absolute tolerance set by `inte::tol_abs`. The following strategy is used: on each interval  $C_k$ , the algorithm tries to achieve the tolerance

$$\text{TOL}_k = u_k \cdot \varepsilon_{\text{abs}}$$

where  $u_k = (1-p)p^{k-1}$  and  $p = 0.9$ . The sum of the geometric series of contributions from each interval gives an overall tolerance of  $\varepsilon_{\text{abs}}$ . If the integration of a subinterval leads to difficulties then the accuracy requirement for subsequent intervals is relaxed,

$$\text{TOL}_k = u_k \cdot \max\{\varepsilon_{\text{abs}}, E_1, \dots, E_{k-1}\}$$

where  $E_k$  is the estimated error on the interval  $C_k$ .

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

When verbose output is enabled, this class outputs information from both the subintegrations performed by [gsl\\_inte\\_qawo\\_sin](#) and the overall integration progress in this class.

Definition at line 88 of file `gsl_inte_qawf.h`.

#### Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*

#### Protected Member Functions

- int [qawf](#) (func\_t &func, const double a, const double epsabs, double \*result, double \*abserr)  
*The full GSL integration routine called by [integ\\_err\(\)](#)*
- virtual double [transform](#) (double t, func\_t &func)  
*Add the oscillating part to the integrand.*
- const char \* [type](#) ()  
*Return string denoting type ("`gsl_inte_qawf_sin`")*

#### Protected Attributes

- [gsl\\_inte\\_workspace](#) \* [cyclew](#)  
*The integration workspace.*

The documentation for this class was generated from the following file:

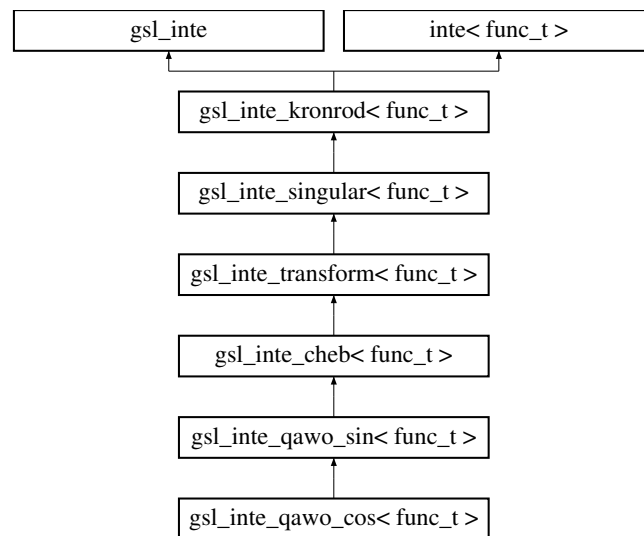
- `gsl_inte_qawf.h`

## 46.117 `gsl_inte_qawo_cos< func_t >` Class Template Reference

Adaptive integration a function with finite limits of integration (GSL)

```
#include <gsl_inte_qawo.h>
```

Inheritance diagram for `gsl_inte_qawo_cos< func_t >`:



#### 46.117.1 Detailed Description

```
template<class func_t>class gsl_inte_qawo_cos< func_t >
```

The integral

$$\int_a^b f(x) \cos(\omega x) dx$$

is computed for some frequency parameter  $\omega$ .

This class is exactly analogous to [gsl\\_inte\\_qawo\\_sin](#). See that class documentation for more details.

Definition at line 645 of file `gsl_inte_qawo.h`.

#### Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*

#### Protected Member Functions

- virtual double [transform](#) (double t, func\_t &func)  
*Add the oscillating part to the integrand.*
- const char \* [type](#) ()  
*Return string denoting type ("`gsl_inte_qawo_cos`")*

The documentation for this class was generated from the following file:

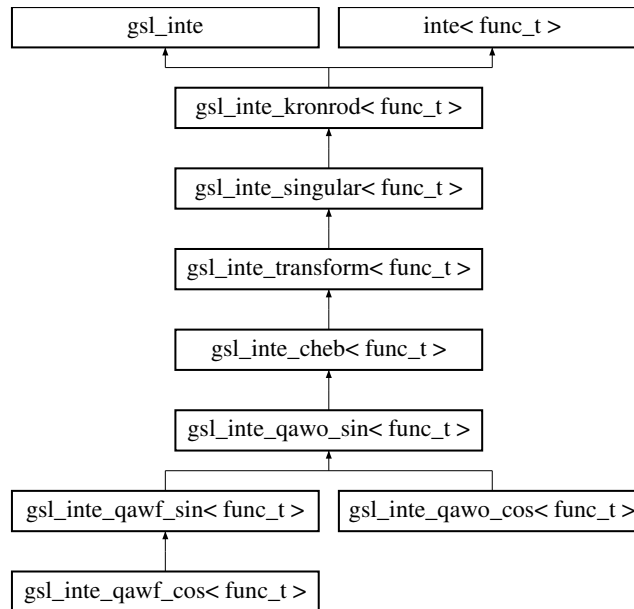
- `gsl_inte_qawo.h`

## 46.118 gsl\_inte\_qawo\_sin< func\_t > Class Template Reference

Adaptive integration for oscillatory integrals (GSL)

```
#include <gsl_inte_qawo.h>
```

Inheritance diagram for `gsl_inte_qawo_sin< func_t >`:



#### 46.118.1 Detailed Description

template<class func\_t>class gsl\_inte\_qawo\_sin< func\_t >

The integral

$$\int_a^b f(x) \sin(\omega x) dx$$

is computed for some frequency parameter  $\omega$ , stored in [gsl\\_inte\\_qawo\\_sin::omega](#).

An adaptive algorithm together with an series-acceleration method like that of [gsl\\_inte\\_qags](#) is used. Those subintervals with "large" widths  $d \equiv b - a$  where  $d\omega > 4$  are computed using a 25-point Clenshaw-Curtis integration rule to handle the oscillatory behavior. In order to work efficiently, the Chebyshev moments for the particular weight function  $W$  are computed in advance.

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 54 of file `gsl_inte_qawo.h`.

#### Public Member Functions

- virtual int [integ\\_err](#) (func\_t &func, double a, double b, double &res, double &err)  
Integrate function *func* from *a* to *b* and place the result in *res* and the error in *err*.

#### Data Fields

- double [omega](#)  
The user-specified frequency (default 1.0)
- size\_t [n\\_levels](#)  
The number of bisection levels (default 10)

#### Protected Member Functions

- int [qawo](#) (func\_t &func, const double a, const double epsabs, const double epsrel, [gsl\\_inte\\_workspace](#) \*loc\_w, [gsl\\_integration\\_qawo\\_table](#) \*wf, double \*result, double \*abserr)  
The full GSL integration routine called by [integ\\_err\(\)](#)

- void [qc25f](#) (func\_t &func, double a, double b, gsl\_integration\_qawo\_table \*wf, size\_t level, double \*result, double \*abserr, double \*resabs, double \*resasc)  
*25-point quadrature for oscillating functions*
- virtual double [transform](#) (double t, func\_t &func)  
*Add the oscillating part to the integrand.*
- const char \* [type](#) ()  
*Return string denoting type ("gsl\_inte\_qawo\_sin")*

#### Protected Attributes

- gsl\_integration\_qawo\_table \* [otable](#)  
*The integration workspace.*

#### 46.118.2 Member Function Documentation

46.118.2.1 `template<class func_t> int gsl_inte_qawo_sin< func_t >::qawo ( func_t &func, const double a, const double epsabs, const double epsrel, gsl_inte_workspace *loc_w, gsl_integration_qawo_table *wf, double *result, double *abserr ) [inline, protected]`

**Idea for Future** Remove goto statements.

Definition at line 102 of file `gsl_inte_qawo.h`.

The documentation for this class was generated from the following file:

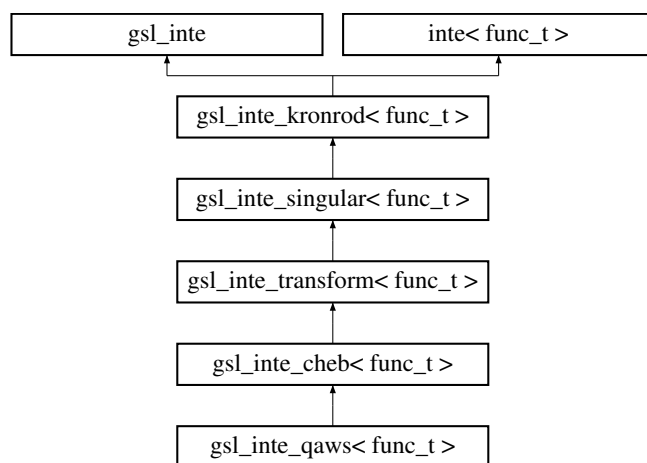
- `gsl_inte_qawo.h`

### 46.119 gsl\_inte\_qaws< func\_t > Class Template Reference

Adaptive integration with with algebraic-logarithmic singularities at the end-points (GSL)

```
#include <gsl_inte_qaws.h>
```

Inheritance diagram for `gsl_inte_qaws< func_t >`:



#### 46.119.1 Detailed Description



```
template<class func_t = func_t>class gsl_inte_qaws< func_t >
```

This class computes the weighted integral

$$\int_a^b f(x)(x-a)^\alpha (b-x)^\beta \log^\mu(x-a) \log^\nu(b-x) dx$$

where the parameters of the weight function must satisfy

$$\alpha > -1, \quad \beta > -1, \quad \mu \in \{0, 1\}, \quad \nu \in \{0, 1\},$$

and which are set by `set_weight()`. Note that setting  $\mu = 0$  or  $\nu = 0$  removes the respective factor  $\log^\mu u(\dots)$  or  $\log^\nu(\dots)$  from the weight.

The adaptive refinement algorithm described for `gsl_inte_qag` is used. When a subinterval contains one of the endpoints, a special 25-point modified Clenshaw-Curtis rule is used to control the singularities. For subintervals which do not include the endpoints, a Gauss-Kronrod integration rule is used.

See [GSL-based integration routines](#) in the User's guide for general information about the GSL integration classes.

Definition at line 77 of file `gsl_inte_qaws.h`.

#### Public Member Functions

- `gsl_inte_qaws()`  
*Initialize the adptive workspace as with the constructor `gsl_inte_qag::gsl_inte_qag`.*
- `int set_weight(double u_alpha, double u_beta, int u_mu, int u_nu)`  
*Sets the exponents of singularities of the weight function.*
- `void get_weight(double &u_alpha, double &u_beta, int &u_mu, int &u_nu)`  
*Returns the current values (via reference) of the weight-function's parameters.*
- `virtual int integ_err(func_t &func, double a, double b, double &result, double &abserr)`  
*Integrate the function `func` on the interval  $(a, b)$  returning the `result` and error estimate `abserr`.*
- `const char * type()`  
*Return string denoting type ("gsl\_inte\_qaws")*

#### Protected Member Functions

- `void initialise_qaws_table()`  
*Set the array values `ri`, `rj`, `rg`, `rh` from the current values `alpha` and `beta`.*
- `virtual double transform(double t, func_t &func)`  
*Weighted integrand.*
- `void qc25s(func_t &func, double a, double b, double a1, double b1, double &result, double &abserr, int &err_reliable)`  
*Clenshaw-Curtis 25-point integration and error estimator for functions with an algebraic-logarithmic singularity at the endpoint(s).*
- `void compute_result(double *r, double *cheb12, double *cheb24, double &result12, double &result24)`  
*Compute the 13-point and 25-point approximations from the Chebyshev moments and coefficients.*

#### Protected Attributes

- `bool fn_qaws_R`  
*True if algebraic-logarithmic singularity is present at the right endpoint in the definition `f_trans`.*
- `bool fn_qaws_L`  
*True if algebraic-logarithmic singularity is present at the left endpoint in the definition `f_trans`.*
- `double left_endpoint`  
*Left endpoint in definition of `f_trans`.*
- `double right_endpoint`  
*Right endpoint in definition of `f_trans`.*

Data from \c gsl\_integration\_qaws\_table

- double **alpha**
- double **beta**
- int **mu**
- int **nu**
- double **ri** [25]
- double **rj** [25]
- double **rg** [25]
- double **rh** [25]

#### 46.119.2 Constructor & Destructor Documentation

46.119.2.1 `template<class func_t = funct> gsl_inte_qaws< func_t >::gsl_inte_qaws( ) [inline]`

The default paramters  $\alpha, \beta, \mu, \nu$  of the weight function are all zero.

Definition at line 367 of file `gsl_inte_qaws.h`.

#### 46.119.3 Member Function Documentation

46.119.3.1 `template<class func_t = funct> void gsl_inte_qaws< func_t >::initialise_qaws_table( ) [inline, protected]`

This is the function from the GSL source code `integration/qmomo.c` that initializes `gsl_integration_qaws_table`.

Definition at line 104 of file `gsl_inte_qaws.h`.

46.119.3.2 `template<class func_t = funct> int gsl_inte_qaws< func_t >::set_weight( double u.alpha, double u.beta, int u.mu, int u.nu ) [inline]`

The parameters determine the exponents of the weight function

$$W(x) = (x-a)^\alpha (b-x)^\beta \log^\mu(x-a) \log^\nu(b-x),$$

and must satisfy

$$\alpha > -1, \quad \beta > -1, \quad \mu \in \{0, 1\}, \quad \nu \in \{0, 1\}.$$

In order for the adaptive algorithm to run quickly, a table of Chebyshev weights for the particular parameters are computed in advance.

Definition at line 388 of file `gsl_inte_qaws.h`.

The documentation for this class was generated from the following file:

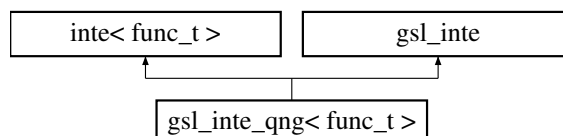
- `gsl_inte_qaws.h`

## 46.120 gsl\_inte\_qng< func\_t > Class Template Reference

Non-adaptive integration from a to b (GSL)

```
#include <gsl_inte_qng.h>
```

Inheritance diagram for `gsl_inte_qng< func_t >`:



## 46.120.1 Detailed Description

```
template<class func_t = funct>class gsl_inte_qng< func_t >
```

The function `integ()` uses 10-point, 21-point, 43-point, and 87-point Gauss-Kronrod integration successively until the integral is returned within the accuracy specified by `inte::tol_abs` and `inte::tol_rel`. The 10-point rule is only used to estimate the error for the 21-point rule. The result of the 21-point calculation is used to estimate the error for the 43-point rule, and so forth.

The error handler is called if the 87-point integration fails to produce the desired accuracy. If `inte::err_nonconv` is false (the default is true), then the error handler is never called and when the desired accuracy is not obtained the result of the 87-point integration is returned along with the associated error.

The return value of the function to be integrated is ignored.

The integration fails and the error handler is called if the tolerances are too small, i.e. if either  $\text{tol}_{\text{abs}} \leq 0$  or if  $\text{tol}_{\text{rel}} < 50 \cdot \epsilon_{\text{double}}$  where  $\epsilon_{\text{double}} \approx 1.11 \times 10^{-14}$ .

The integration coefficients are stored in the `o2scl_inte_qng_coeffs` namespace.

Definition at line 251 of file `gsl_inte_qng.h`.

## Public Member Functions

- virtual int `integ_err` (func\_t &func, double a, double b, double &res, double &err2)  
*Integrate function `func` from `a` to `b` giving result `res` and error `err`.*
- const char \* `type` ()  
*Return string denoting type ("`gsl_inte_qng`")*

## Data Fields

- size\_t `feval`  
*The number of function evaluations for the last integration.*
- double `min_rel_tol`  
*Minimum relative tolerance for integration (default  $5 \times 10^{-29}$ )*

## 46.120.2 Field Documentation

## 46.120.2.1 template&lt;class func\_t = funct&gt; size\_t gsl\_inte\_qng&lt; func\_t &gt;::feval

Set to either 0, 21, 43, or 87, depending on the number of function evaluations that were used. This variable is zero if an error occurs before any function evaluations were performed and is never equal 10, since in the 10-point method, the 21-point result is used to estimate the error. If the function fails to achieve the desired precision, `feval` is 87.

Definition at line 270 of file `gsl_inte_qng.h`.

The documentation for this class was generated from the following file:

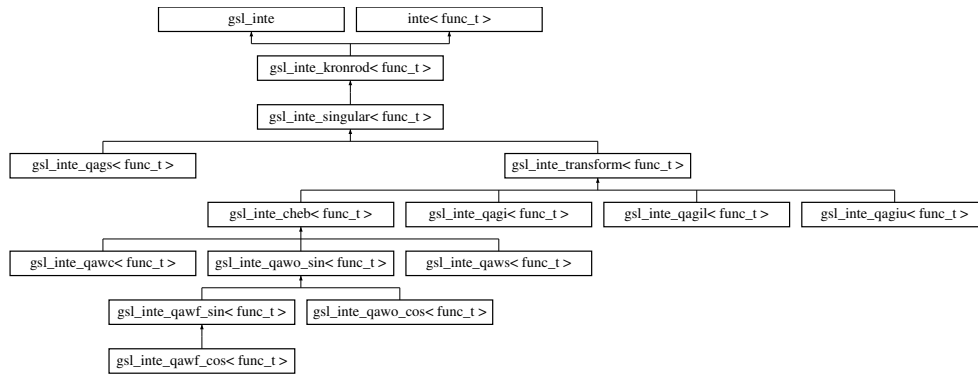
- `gsl_inte_qng.h`

## 46.121 gsl\_inte\_singular&lt; func\_t &gt; Class Template Reference

Base class for integrating a function with a singularity (GSL)

```
#include <gsl_inte_singular.h>
```

Inheritance diagram for `gsl_inte_singular< func_t >`:



### 46.121.1 Detailed Description

`template<class func_t>class gsl_inte_singular< func_t >`

This class contains the extrapolation table mechanics and the base integration function for singular integrals from GSL. The casual end-user should use the classes explained in the [Integration](#) section of the User's guide.

**Idea for Future** Some of the functions inside this class could be moved out of header files?

Definition at line 50 of file `gsl_inte_singular.h`.

#### Data Structures

- struct [extrapolation\\_table](#)  
A structure for extrapolation for `gsl_inte_qags`.

#### Public Types

- typedef struct [gsl\\_inte\\_singular::extrapolation\\_table](#) `extrap_table`  
A structure for extrapolation for `gsl_inte_qags`.

#### Protected Member Functions

- void [initialise\\_table](#) (struct [extrapolation\\_table](#) \*table)  
Initialize the table.
- void [append\\_table](#) (struct [extrapolation\\_table](#) \*table, double y)  
Append a result to the table.
- int [test\\_positivity](#) (double result, double resabs)  
Test if the integrand satisfies  $f = |f|$ .
- void [qelg](#) (struct [extrapolation\\_table](#) \*table, double \*result, double \*abserr)  
Determines the limit of a given sequence of approximations.
- int [large\\_interval](#) ([gsl\\_inte\\_workspace](#) \*workspace)  
Determine if an interval is large.
- void [reset\\_nrmx](#) ([gsl\\_inte\\_workspace](#) \*workspace)  
Reset workspace to work on the interval with the largest error.
- int [increase\\_nrmx](#) ([gsl\\_inte\\_workspace](#) \*workspace)  
Increase workspace.
- int [qags](#) (func\_t &func, const double a, const double b, const double l\_epsabs, const double l\_epsrel, double \*result, double \*abserr)  
Integration function.

## 46.121.2 Member Typedef Documentation

46.121.2.1 `template<class func_t> typedef struct gsl_inte_singular::extrapolation_table gsl_inte_singular< func_t >::extrap_table`

**Idea for Future** Move this to a new class, with `qelg()` as a method

## 46.121.3 Member Function Documentation

46.121.3.1 `template<class func_t> void gsl_inte_singular< func_t >::qelg ( struct extrapolation_table * table, double * result, double * abserr ) [inline, protected]`

For certain convergent series  $\sum_k a_k$  whose error term  $E_n = \sum_{k=n}^{\infty} a_k$  is well behaved, it is possible to find a transformation of the sequence that yields a faster converging series to the same limit. This method of extrapolation applies to some sequences of adaptive-approximation and error-estimation for numerical integration. This function implements the  $\varepsilon$ -algorithm (Wynn56, Piessens83) for an extrapolation table stored in `table`.

Quadpack documentation

```
c
c  list of major variables
c  -----
c  e0      - the 4 elements on which the computation of a new
c  e1      element in the epsilon table is based
c  e2
c  e3      e0
c          e3  e1  new
c          e2
c  newelm - number of elements to be computed in the new
c          diagonal
c  error  - error = abs(e1-e0)+abs(e2-e1)+abs(new-e2)
c  result - the element in the new diagonal with least value
c          of error
c
c  machine dependent constants
c  -----
c
c  epmach is the largest relative spacing.
c  oflow is the largest positive magnitude.
c  limexp is the maximum number of elements the epsilon
c  table can contain. if this number is reached, the upper
c  diagonal of the epsilon table is deleted.
c
```

Definition at line 136 of file `gsl_inte_singular.h`.

46.121.3.2 `template<class func_t> int gsl_inte_singular< func_t >::qags ( func_t & func, const double a, const double b, const double l_epsabs, const double l_epsrel, double * result, double * abserr ) [inline, protected]`

**Idea for Future** Remove goto statements. Before this is done, it might be best to add some tests which fail in the various ways.

Definition at line 344 of file `gsl_inte_singular.h`.

The documentation for this class was generated from the following file:

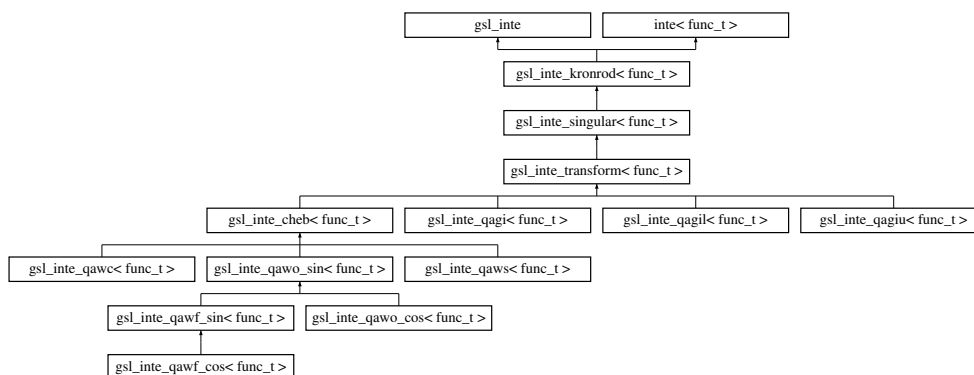
- `gsl_inte_singular.h`

## 46.122 gsl\_inte\_transform&lt; func\_t &gt; Class Template Reference

Integrate a function with a singularity (GSL) [abstract base].

```
#include <gsl_inte_singular.h>
```

Inheritance diagram for `gsl_inte_transform< func_t >`:



#### 46.122.1 Detailed Description

```
template<class func_t = funct>class gsl_inte_transform< func_t >
```

This class contains the GSL-based integration function for applying transformations to the user-defined integrand. The casual end-user should use the classes explained in the [Integration](#) section of the User's guide.

Definition at line 752 of file `gsl_inte_singular.h`.

#### Public Member Functions

- virtual double [transform](#) (double t, func\_t &func)=0  
*The transformation to apply to the user-supplied function.*
- virtual void [gauss\\_kronrod](#) (func\_t &func, double a, double b, double \*result, double \*abserr, double \*resabs, double \*resasc)

*Integration wrapper for internal transformed function type.*

The documentation for this class was generated from the following file:

- `gsl_inte_singular.h`

## 46.123 gsl\_inte\_workspace Class Reference

Integration workspace for the GSL integrators.

```
#include <gsl_inte_kronrod.h>
```

#### 46.123.1 Detailed Description

This is a simple rewrite of `gsl_integration_workspace` into a class.

QUADPACK workspace documentation:

```

c    parameters (meaning at output)
c    limit      - integer
c                maximum number of error estimates the list
c                can contain
c    last       - integer
c                number of error estimates currently in the list
c    maxerr     - integer
  
```

```

c          maxerr points to the nrmax-th largest error
c          estimate currently in the list
c      ermax  - double precision
c              nrmax-th largest error estimate
c              ermax = elist(maxerr)
c      elist  - double precision
c              vector of dimension last containing
c              the error estimates
c      iord   - integer
c              vector of dimension last, the first k elements
c              of which contain pointers to the error
c              estimates, such that
c              elist(iord(1)), ..., elist(iord(k))
c              form a decreasing sequence, with
c              k = last if last.le.(limit/2+2), and
c              k = limit+1-last otherwise
c      nrmax  - integer
c      maxerr = iord(nrmax)

c      alist  - real
c              vector of dimension at least limit, the first
c              last elements of which are the left
c              end points of the subintervals in the partition
c              of the given integration range (a,b)
c      blist  - real
c              vector of dimension at least limit, the first
c              last elements of which are the right
c              end points of the subintervals in the partition
c              of the given integration range (a,b)
c      rlist  - real
c              vector of dimension at least limit, the first
c              last elements of which are the
c              integral approximations on the subintervals
c      elist  - real
c              vector of dimension at least limit, the first
c              last elements of which are the moduli of the
c              absolute error estimates on the subintervals
c      iord   - integer
c              vector of dimension at least limit, the first k
c              elements of which are pointers to the
c              error estimates over the subintervals,
c              such that elist(iord(1)), ...,
c              elist(iord(k)) form a decreasing sequence,
c              with k = last if last.le.(limit/2+2), and
c              k = limit+1-last otherwise
c      last   - integer
c              number of subintervals actually produced in the
c              subdivision process

```

Definition at line 494 of file `gsl_inte_kronrod.h`.

## Public Member Functions

- [int allocate](#) (size\_t sz)  
*Allocate a workspace.*
- [int free](#) ()  
*Free allocated workspace memory.*
- [int initialise](#) (double a, double b)  
*Initialize the workspace for an integration with limits a and b.*
- [int set\\_initial\\_result](#) (double result, double error)  
*Update the workspace with the result and error from the first integration.*
- [int retrieve](#) (double \*a, double \*b, double \*r, double \*e) const  
*Retrieve the ith result from the workspace stack.*

- int [qpsrt](#) ()  
*Sort the workspace stack.*
- int [update](#) (double a1, double b1, double area1, double error1, double a2, double b2, double area2, double error2)  
*Determine which new subinterval to add to the workspace stack and perform update.*
- double [sum\\_results](#) ()  
*Add up all of the contributions to construct the final result.*
- int [subinterval\\_too\\_small](#) (double a1, double a2, double b2)  
*Test whether the proposed subdivision falls before floating-point precision.*
- void [append\\_interval](#) (double a1, double b1, double area1, double error1)  
*Push a new interval to the workspace stack.*

## Data Fields

- size\_t [limit](#)  
*Maximum number of subintervals allocated.*
- size\_t [size](#)  
*Current number of subintervals being used.*
- size\_t [nrmax](#)  
*Counter for extrapolation routine.*
- size\_t [i](#)  
*Index of current subinterval.*
- size\_t [maximum\\_level](#)  
*Depth of subdivisions reached.*
- double \* [alist](#)  
*Left endpoints of subintervals.*
- double \* [blist](#)  
*Right endpoints of subintervals.*
- double \* [rlist](#)  
*Integral approximations on subintervals.*
- double \* [elist](#)  
*Integral error estimates.*
- size\_t \* [order](#)  
*Linear ordering vector for sort routine.*
- size\_t \* [level](#)  
*Numbers of subdivisions made.*

## 46.123.2 Member Function Documentation

### 46.123.2.1 int gsl\_inte\_workspace::retrieve ( double \* a, double \* b, double \* r, double \* e ) const

The workspace variable `i` is used to specify which interval is requested.

### 46.123.2.2 int gsl\_inte\_workspace::qpsrt ( )

This routine maintains the descending ordering in the list of the local error estimated resulting from the interval subdivision process. at each call two error estimates are inserted using the sequential search method, top-down for the largest error estimate and bottom-up for the smallest error estimate.

Originally written in QUADPACK by R. Piessens and E. de Doncker, translated into C for GSL by Brian Gough, and then rewritten for O<sub>2</sub>scl .

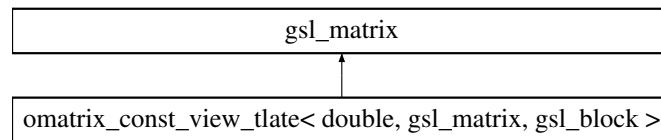
The documentation for this class was generated from the following file:

- `gsl_inte_kronrod.h`



## 46.124 gsl\_matrix Class Reference

Inheritance diagram for `gsl_matrix`:



The documentation for this class was generated from the following file:

- [omatrix\\_tlate.h](#)

## 46.125 gsl\_matrix\_int Class Reference

Inherited by [omatrix\\_const\\_view\\_tlate< int, gsl\\_matrix\\_int, gsl\\_block\\_int >](#).

The documentation for this class was generated from the following file:

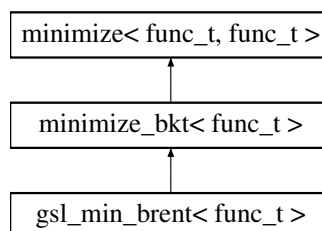
- [omatrix\\_tlate.h](#)

## 46.126 gsl\_min\_brent&lt; func\_t &gt; Class Template Reference

One-dimensional minimization using Brent's method (GSL)

```
#include <gsl_min_brent.h>
```

Inheritance diagram for `gsl_min_brent< func_t >`:



## 46.126.1 Detailed Description

```
template<class func_t = funct>class gsl_min_brent< func_t >
```

The minimization in the function [min\\_bkt\(\)](#) is complete when the bracketed interval is smaller than  $\text{tol} = \text{tol\_abs} + \text{tol\_rel} \cdot \text{min}$ , where  $\text{min} = \min(|\text{lower}|, |\text{upper}|)$ .

Note that this algorithm requires that the initial guess already brackets the minimum, i.e.  $x_1 < x_2 < x_3$ ,  $f(x_1) > f(x_2)$  and  $f(x_3) > f(x_2)$ . This is different from [cern\\_minimize](#), where the initial value of the first parameter to [cern\\_minimize::min\\_bkt\(\)](#) is ignored.

The set functions throw an error if the initial bracket is not correctly specified. The function [iterate\(\)](#) never calls the error handler. The function [min\\_bkt\(\)](#) calls the error handler if the tolerances are negative or if the number of iterations is insufficient to give the specified tolerance.

Setting [minimize::err\\_nonconv](#) to false will force [min\\_bkt\(\)](#) not to call the error handler when the number of iterations is insufficient.

Note that if there are more than 1 local minima in the specified interval, there is no guarantee that this method will find the global minimum.

See also [gsl\\_root\\_brent](#) for a similar algorithm applied as a solver rather than a minimizer.

#### Note

There was a bug in this minimizer which was fixed for GSL-1.11 which has also been fixed here.

Definition at line 87 of file `gsl_min_brent.h`.

#### Public Member Functions

- `int set` (`func_t` &`func`, `double` `xmin`, `double` `lower`, `double` `upper`)  
*Set the function and the initial bracketing interval.*
- `int set_with_values` (`func_t` &`func`, `double` `xmin`, `double` `fmin`, `double` `lower`, `double` `fl`, `double` `upper`, `double` `fu`)  
*Set the function, the initial bracketing interval, and the corresponding function values.*
- `int iterate` ()  
*Perform an iteration.*
- `virtual int min_bkt` (`double` &`x2`, `double` `x1`, `double` `x3`, `double` &`fmin`, `func_t` &`func`)  
*Calculate the minimum  $f_{min}$  of `func` with `x2` bracketed between `x1` and `x3`.*
- `virtual const char * type` ()  
*Return string denoting type ("gsl\_min\_brent")*

#### Data Fields

- `double x_minimum`  
*Location of minimum.*
- `double x_lower`  
*Lower bound.*
- `double x_upper`  
*Upper bound.*
- `double f_minimum`  
*Minimum value.*
- `double f_lower`  
*Value at lower bound.*
- `double f_upper`  
*Value at upper bound.*

#### Protected Member Functions

- `int compute_f_values` (`func_t` &`func`, `double` `xminimum`, `double` &`fminimum`, `double` `xlower`, `double` &`f_lower`, `double` `xupper`, `double` &`f_upper`)  
*Compute the function values at the various points.*

#### Protected Attributes

- `func_t * uf`  
*The function.*

#### Temporary storage

- `double d`
- `double e`
- `double v`
- `double w`
- `double f_v`
- `double f_w`

## 46.126.2 Member Function Documentation

46.126.2.1 `template<class func_t = funct> int gsl_min_brent< func_t >::iterate ( ) [inline]`

**Idea for Future** It looks like `x_left` and `x_right` can be removed. Also, it would be great to replace the one-letter variable names with something more meaningful.

Definition at line 198 of file `gsl_min_brent.h`.

46.126.2.2 `template<class func_t = funct> virtual int gsl_min_brent< func_t >::min_bkt ( double & x2, double x1, double x3, double & fmin, func_t & func ) [inline, virtual]`

Note that this algorithm requires that the initial guess already brackets the minimum, i.e.  $x_1 < x_2 < x_3$ ,  $f(x_1) > f(x_2)$  and  $f(x_3) > f(x_2)$ . This is different from `cern_minimize`, where the initial value of the first parameter to `cern_minimize::min_bkt()` is ignored.

Implements `minimize_bkt< func_t >`.

Definition at line 332 of file `gsl_min_brent.h`.

The documentation for this class was generated from the following file:

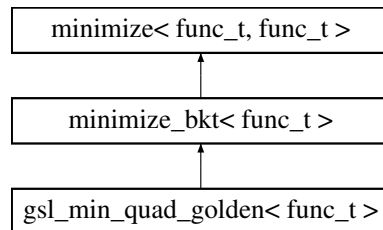
- `gsl_min_brent.h`

## 46.127 gsl\_min\_quad\_golden&lt; func\_t &gt; Class Template Reference

Minimization of a function using the safeguarded step-length algorithm of Gill and Murray [GSL].

```
#include <gsl_min_quad_golden.h>
```

Inheritance diagram for `gsl_min_quad_golden< func_t >`:



## 46.127.1 Detailed Description

```
template<class func_t = funct> class gsl_min_quad_golden< func_t >
```

This class is unfinished.

Documentation from GSL:

This algorithm performs univariate minimization (i.e., line search). It requires only objective function values  $g(x)$  to compute the minimum. The algorithm maintains an interval of uncertainty  $[a, b]$  and a point  $x$  in the interval  $[a, b]$  such that  $a < x < b$ , and  $g(a) > g(x)$  and  $g(x) < g(b)$ . The algorithm also maintains the three points with the smallest objective values  $x$ ,  $v$  and  $w$  such that  $g(x) < g(v) < g(w)$ . The algorithm terminates when  $\max(x-a, b-x) < 2(r|x| + t)$  where  $r$  and  $t$  are small positive reals. At a given iteration, the algorithm first fits a quadratic through the three points  $(x, g(x))$ ,  $(v, g(v))$  and  $(w, g(w))$  and computes the location of the minimum  $u$  of the resulting quadratic. If  $u$  is in the interval  $[a, b]$  then  $g(u)$  is

computed. If  $u$  is not in the interval  $[a,b]$ , and either  $v < x$  and  $w < x$ , or  $v > x$  and  $w > x$  (i.e., the quadratic is extrapolating), then a point  $u'$  is computed using a safeguarding procedure and  $g(u')$  is computed. If  $u$  is not in the interval  $[a,b]$ , and the quadratic is not extrapolating, then a point  $u''$  is computed using approximate golden section and  $g(u'')$  is computed. After evaluating  $g()$  at the appropriate new point,  $a$ ,  $b$ ,  $x$ ,  $v$ , and  $w$  are updated and the next iteration is performed. The algorithm is based on work presented in the following references.

Algorithms for Minimization without derivatives  
Richard Brent  
Prentice-Hall Inc., Englewood Cliffs, NJ, 1973

Safeguarded Steplength Algorithms for Optimization using Descent Methods  
Philip E. Gill and Walter Murray  
Division of Numerical Analysis and Computing  
National Physical Laboratory, Teddington, United Kingdom  
NPL Report NAC 37, August 1974

**Idea for Future** Take common elements of this and `gsl_min_brent` and move to a generic GSL minimizer type?

Definition at line 100 of file `gsl_min_quad_golden.h`.

#### Public Member Functions

- `int set (func_t &func, double xmin, double lower, double upper)`  
*Set the function and the initial bracketing interval.*
- `int set_with_values (func_t &func, double xmin, double fmin, double lower, double fl, double upper, double fu)`  
*Set the function, the initial bracketing interval, and the corresponding function values.*
- `int iterate ()`  
*Perform an iteration.*
- `virtual int min_bkt (double &x2, double x1, double x3, double &fmin, func_t &func)`  
*Calculate the minimum  $f_{min}$  of  $func$  with  $x_2$  bracketed between  $x_1$  and  $x_3$ .*
- `virtual const char * type ()`  
*Return string denoting type ("gsl\_min\_quad\_golden")*

#### Data Fields

- `double x_minimum`  
*Location of minimum.*
- `double x_lower`  
*Lower bound.*
- `double x_upper`  
*Upper bound.*
- `double f_minimum`  
*Minimum value.*
- `double f_lower`  
*Value at lower bound.*
- `double f_upper`  
*Value at upper bound.*

#### Protected Member Functions

- `int compute_f_values (func_t &func, double xminimum, double *fminimum, double xlower, double *flower, double xupper, double *fupper)`  
*Compute the function values at the various points.*

## Protected Attributes

- `func_t * uf`  
*The function.*
- double `x_prev_small`
- double `f_prev_small`
- double `x_small`
- double `f_small`
- double `step_size`
- double `stored_step`
- double `prev_stored_step`
- size\_t `num_iter`
- double `rel_err_val`
- double `abs_err_val`
- double `golden_mean`
- double `golden_ratio`

## 46.127.2 Member Function Documentation

46.127.2.1 `template<class func_t = func_t> virtual int gsl_min_quad_golden< func_t >::min_bkt ( double & x2, double x1, double x3, double & fmin, func_t & func ) [inline, virtual]`

Note that this algorithm requires that the initial guess already brackets the minimum, i.e.  $x_1 < x_2 < x_3$ ,  $f(x_1) > f(x_2)$  and  $f(x_3) > f(x_2)$ . This is different from `cern_minimize`, where the initial value of the first parameter to `cern_minimize::min_bkt()` is ignored.

Implements `minimize_bkt< func_t >`.

Definition at line 399 of file `gsl_min_quad_golden.h`.

The documentation for this class was generated from the following file:

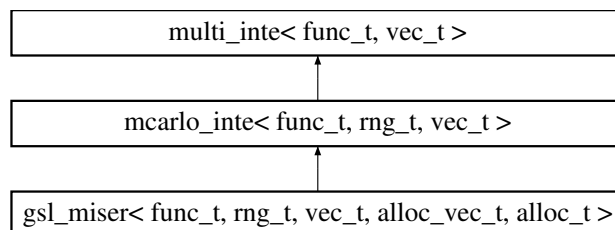
- `gsl_min_quad_golden.h`

46.128 `gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference

Multidimensional integration using the MISER Monte Carlo algorithm (GSL)

```
#include <gsl_miser.h>
```

Inheritance diagram for `gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`:



## 46.128.1 Detailed Description

```
template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_
alloc>class gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >
```

This class uses recursive stratified sampling to estimate the value of an integral over a hypercubic region.

By default the minimum number of calls to estimate the variance is 16 times the number of dimensions. This ratio is stored in `calls_per_dim`. By default the minimum number of calls per bisection is 32 times `calls_per_dim` times the number of dimensions. This ratio is stored in `bisection_ratio`. These ratios are employed by `minteg_err()`.

Alternatively, the user can directly set these minimums by `set_min_calls()` and `set_min_calls_per_bisection()` and use `miser_minteg_err()` which ignores `calls_per_dim` and `bisection_ratio`.

If `mcarlo_inte::verbose` is greater than zero, then the status of the integration is output at every level of bisection less than `n_levels_out`. If it is greater than 1, then the boundaries of the current region are also output. Finally, if it is greater than 2, a keypress is required after each output.

Based on [Press90](#).

Definition at line 88 of file `gsl_miser.h`.

### Public Member Functions

- `int set_min_calls (size_t &mc)`  
*Minimum number of calls to estimate the variance.*
- `int set_min_calls_per_bisection (size_t &mcb)`  
*Minimum number of calls required to proceed with bisection.*
- `virtual int allocate (size_t ldim)`  
*Allocate memory.*
- `virtual int free ()`  
*Free allocated memory.*
- `virtual int miser_minteg_err (func_t &func, size_t ndim, const vec_t &xl, const vec_t &xu, size_t calls, size_t level, double &res, double &err)`  
*Integrate function `func` over the hypercube from  $x_i = xl_i$  to  $x_i = xu_i$  for  $0 < i < ndim-1$ .*
- `virtual int minteg_err (func_t &func, size_t ndim, const vec_t &a, const vec_t &b, double &res, double &err)`  
*Integrate function `func` from  $x=a$  to  $x=b$ .*
- `virtual double minteg (func_t &func, size_t ndim, const vec_t &a, const vec_t &b)`  
*Integrate function `func` over the hypercube from  $x_i = a_i$  to  $x_i = b_i$  for  $0 < i < ndim-1$ .*
- `virtual const char * type ()`  
*Return string denoting type ("gsl\_miser")*

### Data Fields

- `size_t calls_per_dim`  
*Number of calls per dimension (default 16)*
- `size_t bisection_ratio`  
*Factor to set `min_calls_per_bisection` (default 32)*
- `double dither`  
*Introduce random variation into bisection (default 0.0)*
- `double estimate_frac`  
*Specify fraction of function calls for estimating variance (default 0.1)*
- `double alpha`  
*How estimated variances for two sub-regions are combined (default 2.0)*
- `size_t n_levels_out`  
*The number of recursive levels to output when verbose is greater than zero (default 5)*

### Protected Member Functions

- `virtual int estimate_corrmc (func_t &func, size_t ndim, const vec_t &xl, const vec_t &xu, size_t calls, double &res, double &err, const uvector &lsmid, uvector &lsigma_l, uvector &lsigma_r)`  
*Estimate the variance.*

## Protected Attributes

- `size_t min_calls`  
*Minimum number of calls to estimate the variance.*
- `size_t min_calls_per_bisection`  
*Minimum number of calls required to proceed with bisection.*
- `size_t dim`  
*The number of dimensions of memory allocated.*
- `alloc_t ao`  
*Memory allocator.*
- `alloc_vec_t x`  
*The most recent integration point.*

## Arrays which contain a value for each dimension

- `uvector xmid`  
*The current midpoint.*
- `uvector sigma_l`  
*The left variance.*
- `uvector sigma_r`  
*The right variance.*
- `uvector fmax_l`  
*The maximum function value in the left half.*
- `uvector fmax_r`  
*The maximum function value in the right half.*
- `uvector fmin_l`  
*The minimum function value in the left half.*
- `uvector fmin_r`  
*The minimum function value in the right half.*
- `uvector fsum_l`  
*The sum in the left half.*
- `uvector fsum_r`  
*The sum in the right half.*
- `uvector fsum2_l`  
*The sum of the squares in the left half.*
- `uvector fsum2_r`  
*The sum of the squares in the right half.*
- `uvector_size_t hits_l`  
*The number of evaluation points in the left half.*
- `uvector_size_t hits_r`  
*The number of evaluation points in the right half.*

## 46.128.2 Member Function Documentation

46.128.2.1 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::set_min_calls ( size_t & mc ) [inline]`

This is set by `minteg()` and `minteg_err()` to be `calls_per_dim` times the number of dimensions in the problem. The default value of `calls_per_dim` is 16 (which is the GSL default).

From GSL documentation:

This parameter specifies the minimum number of function calls required for each estimate of the variance. If the number of function calls allocated to the estimate using ESTIMATE\_FRAC falls below MIN\_CALLS then MIN\_CALLS are used instead. This ensures that each estimate maintains a reasonable level of accuracy.

Definition at line 167 of file `gsl_miser.h`.

```
46.128.2.2 template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t =
ovector_alloc> int gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::set_min_calls_per_bisection ( size_t & mcb ) [inline]
```

This is set by [minteg\(\)](#) and [minteg\\_err\(\)](#) to be [calls\\_per\\_dim](#) times [bisection\\_ratio](#) times the number of dimensions in the problem. The default values give 512 times the number of dimensions (also the GSL default).

From GSL documentation:

```
This parameter specifies the minimum number of function calls
required to proceed with a bisection step. When a recursive step
has fewer calls available than MIN_CALLS_PER_BISECTION it performs
a plain Monte Carlo estimate of the current sub-region and
terminates its branch of the recursion.
```

Definition at line 188 of file `gsl_miser.h`.

```
46.128.2.3 template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t =
ovector_alloc> virtual int gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::estimate_corrmc ( func_t & func, size_t ndim, const
vec_t & xl, const vec_t & xu, size_t calls, double & res, double & err, const uvector & lxmid, uvector & lsigma_l, uvector & lsigma_r
) [inline, protected, virtual]
```

**Idea for Future** Remove the reference to `GSL_POSINF` and replace with a function parameter.

Definition at line 246 of file `gsl_miser.h`.

```
46.128.2.4 template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t =
ovector_alloc> virtual int gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::miser_minteg_err ( func_t & func, size_t ndim, const
vec_t & xl, const vec_t & xu, size_t calls, size_t level, double & res, double & err ) [inline, virtual]
```

#### Note

The values of [min\\_calls](#) and [min\\_calls\\_per\\_bisection](#) should be set before calling this function. The default values if not set are 100 and 3000 respectively, which correspond to the GSL default setting for a 6 dimensional problem.

Definition at line 428 of file `gsl_miser.h`.

```
46.128.2.5 template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t =
ovector_alloc> virtual int gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::minteg_err ( func_t & func, size_t ndim, const vec_t &
a, const vec_t & b, double & res, double & err ) [inline, virtual]
```

This function is just a wrapper to [miser\\_minteg\\_err\(\)](#) which allocates the memory if necessary, sets [min\\_calls](#) and [min\\_calls\\_per\\_bisection](#), calls [miser\\_minteg\\_err\(\)](#), and then frees the previously allocated memory.

Implements [multi\\_inte< func\\_t, vec\\_t >](#).

Definition at line 693 of file `gsl_miser.h`.

```
46.128.2.6 template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t =
ovector_alloc> virtual double gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::minteg ( func_t & func, size_t ndim, const vec_t &
a, const vec_t & b ) [inline, virtual]
```

This function is just a wrapper to [minteg\\_err\(\)](#) which allocates the memory, sets [min\\_calls](#) and [min\\_calls\\_per\\_bisection](#), calls [miser\\_minteg\\_err\(\)](#), and then frees the previously allocated memory.

Reimplemented from [multi\\_inte< func\\_t, vec\\_t >](#).

Definition at line 716 of file `gsl_miser.h`.



46.128.3.1 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::dither`

From GSL documentation:

This parameter introduces a random fractional variation of size DITHER into each bisection, which can be used to break the symmetry of integrands which are concentrated near the exact center of the hypercubic integration region. The default value of dither is zero, so no variation is introduced. If needed, a typical value of DITHER is 0.1.

Definition at line 113 of file `gsl_miser.h`.

46.128.3.2 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::estimate_frac`

From GSL documentation:

This parameter specifies the fraction of the currently available number of function calls which are allocated to estimating the variance at each recursive step. The default value is 0.1.

Definition at line 125 of file `gsl_miser.h`.

46.128.3.3 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::alpha`

The error handler will be called if this is less than zero.

From GSL documentation:

This parameter controls how the estimated variances for the two sub-regions of a bisection are combined when allocating points. With recursive sampling the overall variance should scale better than  $1/N$ , since the values from the sub-regions will be obtained using a procedure which explicitly minimizes their variance. To accommodate this behavior the MISER algorithm allows the total variance to depend on a scaling parameter  $\alpha$ ,

$$\text{Var}(f) = \{\sigma_a \text{ over } N_a^\alpha\} + \{\sigma_b \text{ over } N_b^\alpha\}.$$

The authors of the original paper describing MISER recommend the value  $\alpha = 2$  as a good choice, obtained from numerical experiments, and this is used as the default value in this implementation.

Definition at line 150 of file `gsl_miser.h`.

The documentation for this class was generated from the following file:

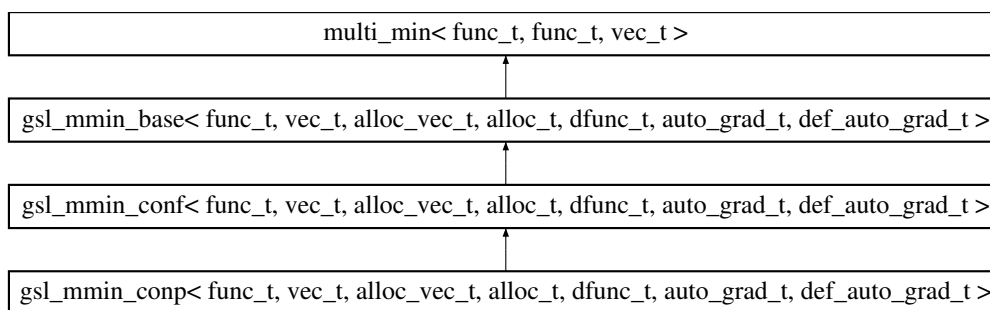
- `gsl_miser.h`

## 46.129 `gsl_mmin_base< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >` Class Template Reference

Base minimization routines for [gsl\\_mmin\\_conf](#) and [gsl\\_mmin\\_conp](#).

```
#include <gsl_mmin_conf.h>
```

Inheritance diagram for `gsl_mmin_base< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >`:



#### 46.129.1 Detailed Description

`template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> class gsl_mmin_base< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >`

This class is used by the `gsl_mmin_conf` and `gsl_mmin_conp` minimizers to perform the line minimization along a specified direction. It is not intended for a casual end-user.

Default template arguments

- `func_t` - `multi_func_t< ovector_base >`
- `vec_t` - `ovector_base`
- `alloc_vec_t` - `ovector`
- `alloc_t` - `ovector_alloc`
- `dfunc_t` - `mm_func_t< ovector_base >`
- `auto_grad_t` - `gradient<func_t, ovector_base >`
- `def_auto_grad_t` - `simple_grad<func_t,ovector_base >`

Definition at line 61 of file `gsl_mmin_conf.h`.

#### Public Member Functions

- `int base_set (func_t &ufunc, auto_grad_t &u_def_grad)`  
*Set the function.*
- `int base_set_de (func_t &ufunc, dfunc_t &udfunc)`  
*Set the function and the gradient .*
- `int base_allocate (size_t nn)`  
*Allocate memory.*
- `int base_free ()`  
*Clear allocated memory.*

#### Data Fields

- `double deriv_h`  
*Stepsize for finite-differencing ( default  $10^{-4}$  )*
- `int nmaxiter`  
*Maximum iterations for line minimization (default 10)*
- `def_auto_grad_t def_grad`  
*Default automatic gradient object.*

## Protected Member Functions

- void [take\\_step](#) (const vec\_t &x, const vec\_t &px, double stepx, double lambda, vec\_t &x1x, vec\_t &dx)  
*Take a step.*
- void [intermediate\\_point](#) (const vec\_t &x, const vec\_t &px, double lambda, double pg, double stepa, double stepc, double fa, double fc, vec\_t &x1x, vec\_t &dx, vec\_t &gradient, double \*stepx, double \*f)  
*Line minimization.*
- void [minimize](#) (const vec\_t &x, const vec\_t &xp, double lambda, double stepa, double stepb, double stepc, double fa, double fb, double fc, double xtol, vec\_t &x1x, vec\_t &dx1x, vec\_t &x2x, vec\_t &dx2x, vec\_t &gradient, double \*xstep, double \*f, double \*gnorm\_u)  
*Perform the minimization.*

## Protected Attributes

- func\_t \* [func](#)  
*User-specified function.*
- dfunc\_t \* [grad](#)  
*User-specified gradient.*
- auto\_grad\_t \* [agrad](#)  
*Automatic gradient object.*
- bool [grad\\_given](#)  
*If true, a gradient has been specified.*
- size\_t [dim](#)  
*Memory size.*
- alloc\_t [ao](#)  
*Memory allocation.*

## 46.129.2 Member Function Documentation

46.129.2.1 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> void gsl_mmin_base< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >::intermediate_point ( const vec_t &x, const vec_t &px, double lambda, double pg, double stepa, double stepc, double fa, double fc, vec_t &x1x, vec_t &dx, vec_t &gradient, double *stepx, double *f ) [inline, protected]`

Do a line minimisation in the region (xa,fa) (xc,fc) to find an intermediate (xb,fb) satisfying  $fa > fb < fc$ . Choose an initial xb based on parabolic interpolation.

Definition at line 105 of file `gsl_mmin_conf.h`.

46.129.2.2 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> void gsl_mmin_base< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >::minimize ( const vec_t &x, const vec_t &xp, double lambda, double stepa, double stepb, double stepc, double fa, double fb, double fc, double xtol, vec_t &x1x, vec_t &dx1x, vec_t &x2x, vec_t &dx2x, vec_t &gradient, double *xstep, double *f, double *gnorm_u ) [inline, protected]`

Starting at (x0, f0) move along the direction p to find a minimum  $f(x_0 - \lambda p)$ , returning the new point  $x_1 = x_0 - \lambda p$ ,  $f_1 = f(x_1)$  and  $g_1 = \text{grad}(f)$  at  $x_1$ .

Definition at line 178 of file `gsl_mmin_conf.h`.

The documentation for this class was generated from the following file:

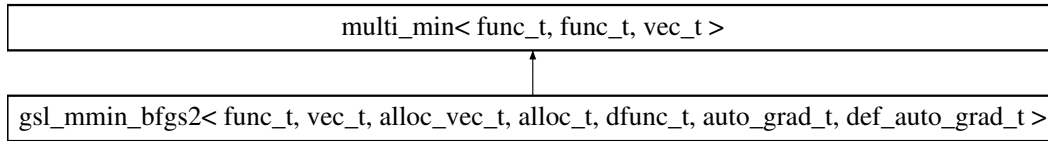
- `gsl_mmin_conf.h`

## 46.130 gsl\_mmin\_bfgs2&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t, dfunc\_t, auto\_grad\_t, def\_auto\_grad\_t &gt; Class Template Reference

Multidimensional minimization by the BFGS algorithm (GSL)

```
#include <gsl_mmin_bfgs2.h>
```

Inheritance diagram for gsl\_mmin\_bfgs2< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, dfunc\_t, auto\_grad\_t, def\_auto\_grad\_t >:



## 46.130.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> class gsl_mmin_bfgs2< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >
```

The functions `mmin()` and `mmin_de()` minimize a given function until the gradient is smaller than the value of `multi_min::tol_rel` (which defaults to  $10^{-4}$ ).

See an example for the usage of this class in [Multidimensional minimizer](#).

This class includes the optimizations from the GSL minimizer `vector_bfgs2`.

Default template arguments

- `func_t` - `multi_func_t< ovector_base >`
- `vec_t` - `ovector_base`
- `alloc_vec_t` - `ovector`
- `alloc_t` - `ovector_alloc`
- `dfunc_t` - `mm_func_t< ovector_base >`
- `auto_grad_t` - `gradient<func_t, ovector_base >`
- `def_auto_grad_t` - `simple_grad<func_t,ovector_base >`

**Todo** While BFGS does well in the `ex_mmin` example with the initial guess of  $(1, 0, 7\pi)$  it seems to converge more poorly for the spring function than the other minimizers with other initial guesses, and I think this will happen in the GSL versions too. I need to examine this more closely with some code designed to clearly show this.

Definition at line 375 of file `gsl_mmin_bfgs2.h`.

## Public Member Functions

- virtual int `iterate()`  
*Perform an iteration.*
- virtual const char \* `type()`  
*Return string denoting type("gsl\_mmin\_bfgs2")*
- virtual int `allocate(size_t n)`  
*Allocate the memory.*
- virtual int `free()`

*Free the allocated memory.*

- int `restart()`  
*Reset the minimizer to use the current point as a new starting point.*
- virtual int `set`(vec\_t &x, double u\_step\_size, double tol\_u, func\_t &ufunc)  
*Set the function and initial guess.*
- virtual int `set_de`(vec\_t &x, double u\_step\_size, double tol\_u, func\_t &ufunc, dfunc\_t &udfunc)  
*Set the function, the gradient, and the initial guess.*
- virtual int `mmin`(size\_t nn, vec\_t &xx, double &fmin, func\_t &ufunc)  
*Calculate the minimum `min` of `func` w.r.t the array `x` of size `nn`.*
- virtual int `mmin_de`(size\_t nn, vec\_t &xx, double &fmin, func\_t &ufunc, dfunc\_t &udfunc)  
*Calculate the minimum `min` of `func` w.r.t the array `x` of size `nn`.*

#### Data Fields

- double `step_size`  
*The size of the first trial step (default 0.01)*
- double `lmin_tol`  
*The tolerance for the 1-dimensional minimizer.*
- def\_auto\_grad\_t `def_grad`  
*Default automatic gradient object.*

#### Protected Attributes

- `gsl_mmin_linmin2` lm  
*The line minimizer.*
- size\_t `dim`  
*Memory size.*
- alloc\_t `ao`  
*Memory allocation.*
- auto\_grad\_t \* `agrad`  
*Automatic gradient object.*

#### The original variables from the GSL state structure

- int `iter`
- double `step`
- double `g0norm`
- double `pnorm`
- double `delta_f`
- double `fp0`
- alloc\_vec\_t `x0`
- alloc\_vec\_t `g0`
- alloc\_vec\_t `p`
- alloc\_vec\_t `dx0`
- alloc\_vec\_t `dg0`
- `gsl_mmin_wrapper`< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, dfunc\_t, auto\_grad\_t > `wrap`
- double `rho`
- double `sigma`
- double `tau1`
- double `tau2`
- double `tau3`
- int `order`

Store the arguments to `set()` so we can use them for `iterate()`

- vec\_t \* `st_x`
- alloc\_vec\_t `st_dx`
- alloc\_vec\_t `st_grad`
- double `st_f`

The documentation for this class was generated from the following file:

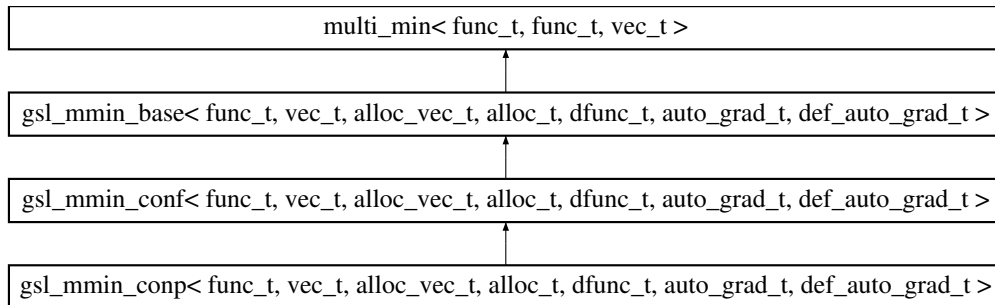
- `gsl_mmin_bfgs2.h`

## 46.131 gsl\_mmin\_conf&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t, dfunc\_t, auto\_grad\_t, def\_auto\_grad\_t &gt; Class Template Reference

Multidimensional minimization by the Fletcher-Reeves conjugate gradient algorithm (GSL)

```
#include <gsl_mmin_conf.h>
```

Inheritance diagram for gsl\_mmin\_conf< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, dfunc\_t, auto\_grad\_t, def\_auto\_grad\_t >:



## 46.131.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> class gsl_mmin_conf< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >
```

This class performs multidimensional minimization by the Fletcher-Reeves conjugate gradient algorithm (GSL). The functions [mmin\(\)](#) and [mmin\\_de\(\)](#) minimize a given function until the gradient is smaller than the value of [multi\\_min::tol\\_rel](#) (which defaults to  $10^{-4}$ ).

This class has a high-level interface using [mmin\(\)](#) or [mmin\\_de\(\)](#) which automatically performs the memory allocation and minimization, or a GSL-like interface using [allocate\(\)](#), [free\(\)](#), [iterate\(\)](#) and [set\(\)](#) or [set\\_simplex\(\)](#).

See an example for the usage of this class in [Multidimensional minimizer](#).

Default template arguments

- func\_t - [multi\\_func\\_t< ovector\\_base >](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)
- dfunc\_t - [grad\\_func\\_t< ovector\\_base >](#)
- auto\_grad\_t - [gradient<func\\_t, ovector\\_base >](#)
- def\_auto\_grad\_t - [simple\\_grad<func\\_t, ovector\\_base >](#)

Note that the state variable `max_iter` has not been included here, because it was not really used in the original GSL code for these minimizers.

Definition at line 401 of file `gsl_mmin_conf.h`.

## Public Member Functions

- virtual const char \* [type](#) ()  
Return string denoting type("gsl\_mmin\_conf")

## GSL-like lower level interface

- virtual int `iterate` ()  
*Perform an iteration.*
- virtual int `allocate` (size\_t n)  
*Allocate the memory.*
- virtual int `free` ()  
*Free the allocated memory.*
- int `restart` ()  
*Reset the minimizer to use the current point as a new starting point.*
- virtual int `set` (vec\_t &x, double u\_step\_size, double tol\_u, func\_t &ufunc)  
*Set the function and initial guess.*
- virtual int `set_de` (vec\_t &x, double u\_step\_size, double tol\_u, func\_t &ufunc, dfunc\_t &udfunc)  
*Set the function and initial guess.*

## Basic usage

- virtual int `mmin` (size\_t nn, vec\_t &xx, double &fmin, func\_t &ufunc)  
*Calculate the minimum  $\min$  of  $func$  w.r.t the array  $x$  of size  $nvar$ .*
- virtual int `mmin_de` (size\_t nn, vec\_t &xx, double &fmin, func\_t &ufunc, dfunc\_t &udfunc)  
*Calculate the minimum  $\min$  of  $func$  w.r.t the array  $x$  of size  $nvar$ .*

## Data Fields

- double `lmin_tol`  
*Tolerance for the line minimization (default  $10^{-4}$ )*
- double `step_size`  
*Size of the initial step (default 0.01)*

## Protected Attributes

## The original variables from the GSL state structure

- int `iter`  
*Iteration number.*
- double `step`  
*Stepsize.*
- double `tol`  
*Tolerance.*
- alloc\_vec\_t `x1`  
*Desc.*
- alloc\_vec\_t `dx1`  
*Desc.*
- alloc\_vec\_t `x2`  
*Desc.*
- double `pnorm`  
*Desc.*
- alloc\_vec\_t `p`  
*Desc.*
- double `g0norm`  
*Desc.*
- alloc\_vec\_t `g0`  
*Desc.*

## Store the arguments to set() so we can use them for iterate()

- alloc\_vec\_t `ugx`  
*Proposed minimum.*
- alloc\_vec\_t `ugg`  
*Gradient.*
- alloc\_vec\_t `udx`  
*Proposed step.*
- double `it_min`  
*Desc.*

## 46.131.2 Member Function Documentation

46.131.2.1 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> virtual int gsl_mmin_conf< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >::set ( vec_t & x, double u_step_size, double tol_u, func_t & ufunc ) [inline, virtual]`

Evaluate the function and its gradient

Definition at line 614 of file `gsl_mmin_conf.h`.

The documentation for this class was generated from the following file:

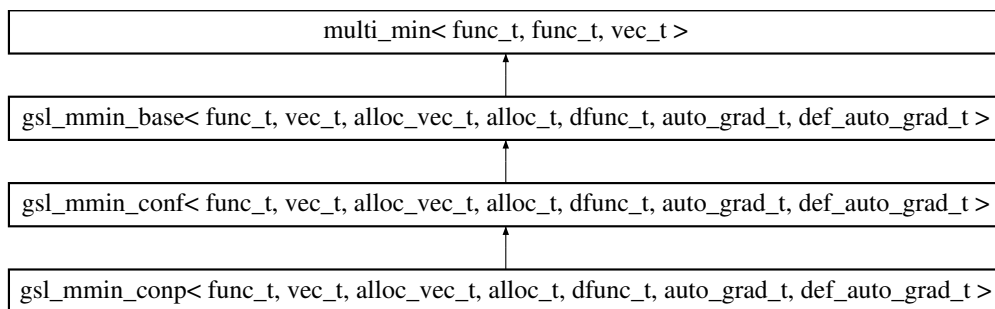
- `gsl_mmin_conf.h`

46.132 `gsl_mmin_conp< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >` Class Template Reference

Multidimensional minimization by the Polak-Ribiere conjugate gradient algorithm (GSL)

```
#include <gsl_mmin_conp.h>
```

Inheritance diagram for `gsl_mmin_conp< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >`:



## 46.132.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func_t<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>, class def_auto_grad_t = simple_grad<func_t,ovector_base>> class gsl_mmin_conp< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t, def_auto_grad_t >
```

The functions `mmin()` and `mmin_de()` minimize a given function until the gradient is smaller than the value of `multi_min::tol_rel` (which defaults to  $10^{-4}$ ).

See an example for the usage of this class in [Multidimensional minimizer](#).

Definition at line 49 of file `gsl_mmin_conp.h`.

## Public Member Functions

- virtual int `iterate` ()  
*Perform an iteration.*
- virtual const char \* `type` ()  
*Return string denoting type("gsl\_mmin\_conp")*

The documentation for this class was generated from the following file:

- `gsl_mmin_conp.h`



## 46.133 gsl\_mmin\_linmin2 Class Reference

The line minimizer for [gsl\\_mmin\\_bfgs2](#).

```
#include <gsl_mmin_bfgs2.h>
```

### 46.133.1 Detailed Description

Definition at line 286 of file `gsl_mmin_bfgs2.h`.

#### Public Member Functions

- `int minimize (gsl_mmin_wrap_base &wrap, double rho, double sigma, double tau1, double tau2, double tau3, int order, double alpha1, double *alpha_new)`  
*The line minimization.*

#### Protected Member Functions

- `double interp_quad (double f0, double fp0, double f1, double zl, double zh)`  
*Minimize the interpolating quadratic.*
- `double cubic (double c0, double c1, double c2, double c3, double z)`  
*Minimize the interpolating cubic.*
- `void check_extremum (double c0, double c1, double c2, double c3, double z, double *zmin, double *fmin)`  
*Test to see curvature is positive.*
- `double interp_cubic (double f0, double fp0, double f1, double fp1, double zl, double zh)`  
*Interpolate using a cubic.*
- `double interpolate (double a, double fa, double fpa, double b, double fb, double fpb, double xmin, double xmax, int order)`  
*Perform the interpolation.*

### 46.133.2 Member Function Documentation

**46.133.2.1** `double gsl_mmin_linmin2::interp_quad ( double f0, double fp0, double f1, double zl, double zh )` [protected]

Find a minimum in  $x=[0,1]$  of the interpolating quadratic through  $(0,f_0)$   $(1,f_1)$  with derivative  $fp_0$  at  $x=0$ . The interpolating polynomial is  $q(x)=f_0 + fp_0 * x + (f_1-f_0-fp_0) * x^2$

**46.133.2.2** `double gsl_mmin_linmin2::cubic ( double c0, double c1, double c2, double c3, double z )` [protected]

Find a minimum in  $x=[0,1]$  of the interpolating cubic through  $(0,f_0)$   $(1,f_1)$  with derivatives  $fp_0$  at  $x=0$  and  $fp_1$  at  $x=1$ .

The interpolating polynomial is:

$$c(x)=f_0 + fp_0 * x + \eta * x^2 + \xi * x^3$$

where  $\eta=3*(f_1-f_0)-2*fp_0-fp_1$ ,  $\xi=fp_0+fp_1-2*(f_1-f_0)$ .

**46.133.2.3** `int gsl_mmin_linmin2::minimize ( gsl_mmin_wrap_base &wrap, double rho, double sigma, double tau1, double tau2, double tau3, int order, double alpha1, double *alpha_new )`

Recommended values from [Fletcher87](#) are  $\rho=0.01$ ,  $\sigma=0.1$ ,  $\tau_1=9$ ,  $\tau_2=0.05$ ,  $\tau_3=0.5$

The documentation for this class was generated from the following file:

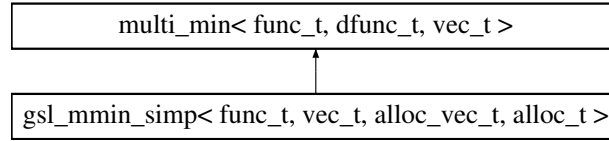
- `gsl_mmin_bfgs2.h`

## 46.134 gsl\_mmin\_simp&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Multidimensional minimization by the Simplex method (GSL)

```
#include <gsl_mmin_simp.h>
```

Inheritance diagram for gsl\_mmin\_simp< func\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



## 46.134.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>class gsl_mmin_simp<
func_t, vec_t, alloc_vec_t, alloc_t >
```

This class minimizes a function using Nelder and Mead's Simplex algorithm. A simplex in a N-dimensional space is defined as a set of N+1 points which describe an N-dimensional volume surrounding the minimum. The algorithm proceeds by shifting the simplex points until the simplex is sufficiently small and thus the minimum is known with sufficient accuracy.

For a slightly improved method, see [gsl\\_mmin\\_simp2](#).

This class has a high-level interface using [mmin\(\)](#), [mmin\\_twovec\(\)](#) or [mmin\\_simplex\(\)](#) which automatically performs the memory allocation and minimization, or a GSL-like interface using [allocate\(\)](#), [free\(\)](#), [iterate\(\)](#) and [set\(\)](#) or [set\\_simplex\(\)](#).

The simplex can be completely specified by the user (see [mmin\\_simplex\(\)](#) and [set\\_simplex\(\)](#)). Alternatively, the simplex is automatically specified given initial guess  $x_j$  and a step size vector  $s_k$  for  $0 \leq k < n_s$ . The simplex  $p_{ij}$  with  $0 \leq i \leq n$  and  $0 \leq j < n$  is chosen with  $p_{0j} = x_j$  and

$$\begin{aligned}
 p_{i+1,j} &= x_j \quad \text{for } i \neq j \\
 p_{i+1,j} &= x_j + s_{j \bmod n_s} \quad \text{for } i = j
 \end{aligned}$$

for  $0 < i < n$ . The step size vector  $s$  is set by the [set\\_step\(\)](#) member function. The presence of mod in the recipe above just indicates that elements of the step size vector are automatically re-used if there are less step sizes than dimensions in the minimization problem.

## Note

It is important that the initial simplex contains sufficient variation in every direction of the parameter space over which one is minimizing. For example, if all three points in a simplex for minimizing over a two-dimensional space contain nearly the same value for the second parameter, then the minimizer may only minimize the function with respect to the first parameter.

## Default template arguments

- func\_t - [multi\\_func\\_t<>](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)

Based on [Nelder65](#).

Definition at line 106 of file [gsl\\_mmin\\_simp.h](#).

## Public Member Functions

- template<class vec2\_t >  
int [set\\_step](#) (size\_t nv, vec2\_t &step)  
*Set the step sizes for each independent variable.*
- virtual int [mmin](#) (size\_t nn, vec\_t &xx, double &fmin, func\_t &ufunc)  
*Calculate the minimum  $\min$  of  $func$  w.r.t the array  $x$  of size  $nvar$ .*
- virtual int [mmin\\_twovec](#) (size\_t nn, vec\_t &xx, vec\_t &xx2, double &fmin, func\_t &ufunc)  
*Calculate the minimum  $\min$  of  $func$  w.r.t the array  $x$  of size  $nvar$ , using  $xx$  and  $xx2$  to specify the simplex.*
- template<class mat\_t >  
int [mmin\\_simplex](#) (size\_t nn, mat\_t &sx, double &fmin, func\_t &ufunc)  
*Calculate the minimum  $\min$  of  $func$  w.r.t the array  $x$  of size  $nvar$ , given an initial simplex.*
- virtual int [allocate](#) (size\_t n)  
*Allocate the memory.*
- virtual int [free](#) ()  
*Free the allocated memory.*
- virtual int [set](#) (func\_t &ufunc, size\_t n, vec\_t &ax, vec\_t &step\_size)  
*Set the function and initial guess.*
- template<class mat\_t >  
int [set\\_simplex](#) (func\_t &ufunc, mat\_t &sx)  
*Set the function and initial simplex.*
- virtual int [iterate](#) ()  
*Perform an iteration.*
- virtual int [print\\_iter](#) (size\_t nv, vec\_t &xx, alloc\_vec\_t \*simp, double y, int iter, double value, double limit, std::string comment)  
*Print out iteration information.*
- virtual const char \* [type](#) ()  
*Return string denoting type("gsl\_mmin\_simp")*

## Data Fields

- double [size](#)  
*Size of current simplex computed by [iterate\(\)](#)*
- alloc\_vec\_t [x](#)  
*Present minimum vector computed by [iterate\(\)](#)*
- double [fval](#)  
*Function value at minimum computed by [iterate\(\)](#)*
- int [print\\_simplex](#)  
*Print simplex information in [print\\_iter\(\)](#) (default 0)*

## Protected Member Functions

- int [nmsimplex\\_calc\\_center](#) (vec\_t &mp)  
*Compute the center of the simplex and store in  $mp$ .*
- double [nmsimplex\\_size](#) ()  
*Compute the size of the simplex.*
- virtual int [move\\_corner\\_err](#) (const double coeff, size\_t corner, vec\_t &xc, func\_t &f, size\_t nvar, double &newval)  
*Move a corner of a simplex.*
- virtual int [contract\\_by\\_best](#) (size\_t best, vec\_t &xc, func\_t &f, size\_t nvar)  
*Contract the simplex towards the best point.*

## Protected Attributes

- alloc\_vec\_t \* [x1](#)  
*An array of  $n+1$  vectors containing the simplex.*
- [ovector](#) [y1](#)  
*The  $n+1$  function values at the simplex points.*

- alloc\_vec\_t [ws1](#)  
*Workspace vector 1.*
- alloc\_vec\_t [ws2](#)  
*Workspace vector 2.*
- alloc\_vec\_t [ws3](#)  
*Workspace vector 3.*
- size\_t [dim](#)  
*Number of variables to be minimized over.*
- func\_t \* [func](#)  
*Function.*
- bool [set\\_called](#)  
*True if `set()` has been called.*
- ovector [step\\_vec](#)  
*Vector of step sizes.*
- alloc\_t [ao](#)  
*Vector allocator.*
- bool [avoid\\_nonzero](#)  
*If true, try to automatically avoid regions where the function returns a non-zero value (default false)*

#### 46.134.2 Member Function Documentation

**46.134.2.1** `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::nmsimplex_size ( ) [inline, protected]`

Calculates simplex size as average sum of length of vectors from simplex center to corner points:

$$(1/n) \sum ||y - y_{\text{middlepoint}}||$$

Definition at line 161 of file `gsl_mmin_simp.h`.

**46.134.2.2** `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::move_corner_err ( const double coeff, size_t corner, vec_t & xc, func_t & f,  
size_t nvar, double & newval ) [inline, protected, virtual]`

Moves a simplex corner scaled by `coeff` (negative value represents mirroring by the middle point of the "other" corner points) and gives new corner in `xc` and function value at `xc` in `newval`.

Definition at line 182 of file `gsl_mmin_simp.h`.

**46.134.2.3** `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::contract_by_best ( size_t best, vec_t & xc, func_t & f, size_t nvar )  
[inline, protected, virtual]`

Function contracts the simplex in respect to best valued corner. All corners besides the best corner are moved.

The vector, `xc`, is used as work space.

Definition at line 212 of file `gsl_mmin_simp.h`.

**46.134.2.4** `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::print_iter ( size_t nv, vec_t & xx, alloc_vec_t * simp, double y, int iter, double  
value, double limit, std::string comment ) [inline, virtual]`

Depending on the value of the variable `verbose`, this prints out the iteration information. If `verbose=0`, then no information is printed, while if `verbose>1`, then after each iteration, the present values of `x` and `y` are output to `std::cout` along with the iteration number. If `verbose>=2` then each iteration waits for a character.

Definition at line 763 of file `gsl_mmin_simp.h`.

#### 46.134.3 Field Documentation

46.134.3.1 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> ovector  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::y1` [protected]

Definition at line 129 of file `gsl_mmin_simp.h`.

46.134.3.2 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> bool  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::avoid_nonzero` [protected]

#### Note

This option doesn't work yet, so I've made the variable protected to prevent the user from changing it.

Definition at line 288 of file `gsl_mmin_simp.h`.

46.134.3.3 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int  
gsl_mmin_simp< func_t, vec_t, alloc_vec_t, alloc_t >::print_simplex`

If this is 1 and `verbose` is greater than 0, then `print_iter()` will print the function values at all the simplex points. If this is 2 and `verbose` is greater than 0, then `print_iter()` will print the simplex coordinates in addition to the function values.

Definition at line 334 of file `gsl_mmin_simp.h`.

The documentation for this class was generated from the following file:

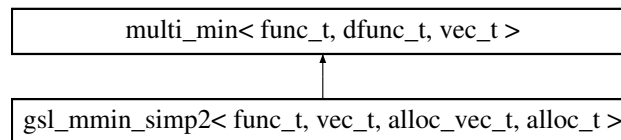
- `gsl_mmin_simp.h`

## 46.135 gsl\_mmin\_simp2< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Multidimensional minimization by the Simplex method (v2) (GSL)

```
#include <gsl_mmin_simp2.h>
```

Inheritance diagram for `gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >`:



### 46.135.1 Detailed Description

```
template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_mmin_simp2<  
func_t, vec_t, alloc_vec_t, alloc_t >
```

This class minimizes a function using Nelder and Mead's Simplex algorithm. A simplex in a N-dimensional space is defined as a set of N+1 points which describe an N-dimensional volume surrounding the minimum. The algorithm proceeds by shifting the simplex points until the simplex is sufficiently small and thus the minimum is known with sufficient accuracy.

For the earlier method used in GSL, see `gsl_mmin_simp`.

This class has a high-level interface using `mmin()`, `mmin_twovec()` or `mmin_simplex()` which automatically performs the memory allocation and minimization, or a GSL-like interface using `allocate()`, `free()`, `iterate()` and `set()` or `set_simplex()`.

The simplex can be completely specified by the user (see `mmin_simplex()` and `set_simplex()`). Alternatively, the simplex is automatically specified given initial guess  $x_j$  and a step size vector  $s_k$  for  $0 \leq k < n_s$ . The simplex  $p_{ij}$  with  $0 \leq i \leq n$  and  $0 \leq j < n$  is chosen with  $p_{0j} = x_j$  and

$$p_{i+1,j} = x_j \quad \text{for } i \neq j$$

$$p_{i+1,j} = x_j + s_{j \bmod n_s} \quad \text{for } i = j$$

for  $0 < i < n$ . The step size vector  $s$  is set by the [set\\_step\(\)](#) member function. The presence of mod in the recipe above just indicates that elements of the step size vector are automatically re-used if there are less step sizes than dimensions in the minimization problem.

#### Note

It is important that the initial simplex contains sufficient variation in every direction of the parameter space over which one is minimizing. For example, if all three points in a simplex for minimizing over a two-dimensional space contain nearly the same value for the second parameter, then the minimizer may only minimize the function with respect to the first parameter.

See an example for the usage of this class in [Multidimensional minimizer](#) .

#### Default template arguments

- param\_t - no default
- func\_t - [multi\\_func](#)<param\_t>
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)

Based on [Nelder65](#) .

A variable `count` originally defined in the GSL simplex state is not present here, because it was unused.

**Idea for Future** Double check that the updates in gsl-1.13 are included here, and also add support for the `nmsimplex2rand` algorithm in GSL.

Definition at line 120 of file `gsl_mmin_simp2.h`.

#### Public Member Functions

- template<class vec2\_t >  
int [set\\_step](#) (size\_t nv, vec2\_t &step)  
*Set the step sizes for each independent variable.*
- virtual int [mmin](#) (size\_t nn, vec\_t &xx, double &fmin, func\_t &ufunc)  
*Calculate the minimum min of func w.r.t the array x of size nvar.*
- virtual int [mmin\\_twovec](#) (size\_t nn, vec\_t &xx, vec\_t &xx2, double &fmin, func\_t &ufunc)  
*Calculate the minimum min of func w.r.t the array x of size nvar, using xx and xx2 to specify the simplex.*
- template<class mat\_t >  
int [mmin\\_simplex](#) (size\_t nn, mat\_t &sx, double &fmin, func\_t &ufunc)  
*Calculate the minimum min of func w.r.t the array x of size nvar, given an initial simplex.*
- virtual int [allocate](#) (size\_t n)  
*Allocate the memory.*
- virtual int [free](#) ()  
*Free the allocated memory.*
- virtual int [set](#) (func\_t &ufunc, size\_t n, vec\_t &ax, vec\_t &step\_size)  
*Set the function and initial guess.*
- template<class mat\_t >  
int [set\\_simplex](#) (func\_t &ufunc, mat\_t &sx)  
*Set the function and initial simplex.*
- virtual int [iterate](#) ()  
*Perform an iteration.*
- virtual int [print\\_iter](#) (size\_t nv, vec\_t &xx, alloc\_vec\_t \*simp, double y, int iter, double value, double limit, std::string comment)  
*Print out iteration information.*
- virtual const char \* [type](#) ()  
*Return string denoting type("gsl\_mmin\_simp2")*

## Data Fields

- double `size`  
*Size of current simplex computed by `iterate()`*
- `alloc_vec_t` `x`  
*Present minimum vector computed by `iterate()`*
- double `fval`  
*Function value at minimum computed by `iterate()`*
- int `print_simplex`  
*Print simplex information in `print_iter()` (default 0)*

## Protected Member Functions

- int `compute_center` ()  
*Compute the center of the simplex.*
- double `compute_size` ()  
*Compute the size of the simplex.*
- virtual int `try_corner_move` (const double coeff, size\_t corner, vec\_t &xc, func\_t &f, size\_t nvar, double &newval)  
*Move a corner of a simplex.*
- virtual int `update_point` (size\_t i, vec\_t &xx, double val)  
*Update point *i* in the simplex with values *xx*.*
- virtual int `contract_by_best` (size\_t best, func\_t &f, size\_t nvar)  
*Contract the simplex towards the best point.*

## Protected Attributes

- `alloc_vec_t` \* `x1`  
*An array of *n+1* vectors containing the simplex.*
- `ovector` `y1`  
*The *n+1* function values at the simplex points.*
- `alloc_vec_t` `ws1`  
*Workspace vector 1.*
- `alloc_vec_t` `ws2`  
*Workspace vector 2.*
- `alloc_vec_t` `ws3`  
*Workspace vector 3.*
- `alloc_vec_t` `center`  
*Center of simplex.*
- `alloc_vec_t` `delta`  
*Desc.*
- `alloc_vec_t` `xmc`  
*Distance of vector from center.*
- double `S2`  
*Squared simplex size.*
- size\_t `dim`  
*Number of variables to be minimized over.*
- `func_t` \* `func`  
*Function.*
- bool `set_called`  
*True if `set()` has been called.*
- `ovector` `step_vec`  
*Vector of step sizes.*
- `alloc_t` `ao`  
*Vector allocator.*
- bool `avoid_nonzero`  
*If true, try to automatically avoid regions where the function returns a non-zero value (default false)*

## 46.135.2 Member Function Documentation

46.135.2.1 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::compute_size ( ) [inline, protected]`

Calculates simplex size as average sum of length of vectors from simplex center to corner points:

$$(1/n) \sum ||y - y_{\text{center}}||$$

Definition at line 183 of file `gsl_mmin_simp2.h`.

46.135.2.2 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::try_corner_move ( const double coeff, size_t corner, vec_t & xc, func_t & f,  
size_t nvar, double & newval ) [inline, protected, virtual]`

Moves a simplex corner scaled by `coeff` (negative value represents mirroring by the middle point of the "other" corner points) and gives new corner in `xc` and function value at `xc` in `newval`.

Definition at line 207 of file `gsl_mmin_simp2.h`.

46.135.2.3 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::contract_by_best ( size_t best, func_t & f, size_t nvar ) [inline,  
protected, virtual]`

Function contracts the simplex in respect to best valued corner. All corners besides the best corner are moved.

Definition at line 279 of file `gsl_mmin_simp2.h`.

46.135.2.4 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::print_iter ( size_t nv, vec_t & xx, alloc_vec_t * simp, double y, int iter, double  
value, double limit, std::string comment ) [inline, virtual]`

Depending on the value of the variable `verbose`, this prints out the iteration information. If `verbose=0`, then no information is printed, while if `verbose>1`, then after each iteration, the present values of `x` and `y` are output to `std::cout` along with the iteration number. If `verbose>=2` then each iteration waits for a character.

Definition at line 842 of file `gsl_mmin_simp2.h`.

## 46.135.3 Field Documentation

46.135.3.1 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> ovector  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::y1 [protected]`

Definition at line 143 of file `gsl_mmin_simp2.h`.

46.135.3.2 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> bool  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::avoid_nonzero [protected]`

## Note

This option doesn't work yet, so I've made the variable `protected` to prevent the casual user from changing it.

Definition at line 365 of file `gsl_mmin_simp2.h`.

46.135.3.3 `template<class func_t = multi_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int  
gsl_mmin_simp2< func_t, vec_t, alloc_vec_t, alloc_t >::print_simplex`

If this is 1 and `verbose` is greater than 0, then `print_iter()` will print the function values at all the simplex points. If this is 2 and `verbose` is greater than 0, then `print_iter()` will print the simplex coordinates in addition to the function values.



Definition at line 411 of file `gsl_mmin_simp2.h`.

The documentation for this class was generated from the following file:

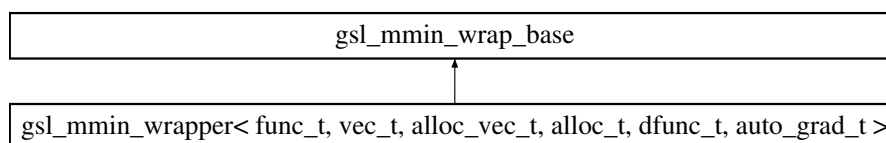
- `gsl_mmin_simp2.h`

## 46.136 gsl\_mmin\_wrap\_base Class Reference

Virtual base for the `gsl_mmin_bfgs2` wrapper.

```
#include <gsl_mmin_bfgs2.h>
```

Inheritance diagram for `gsl_mmin_wrap_base`:



### 46.136.1 Detailed Description

This class is useful so that the `gsl_mmin_linmin` class doesn't need to depend on any template parameters, even though it will need a wrapping object as an argument for the `gsl_mmin_linmin::minimize()` function.

Definition at line 43 of file `gsl_mmin_bfgs2.h`.

#### Public Member Functions

- virtual double `wrap_f` (double alpha)=0  
*Function.*
- virtual double `wrap_df` (double alpha)=0  
*Derivative.*
- virtual void `wrap_fdf` (double alpha, double \*f, double \*df)=0  
*Function and derivative.*

The documentation for this class was generated from the following file:

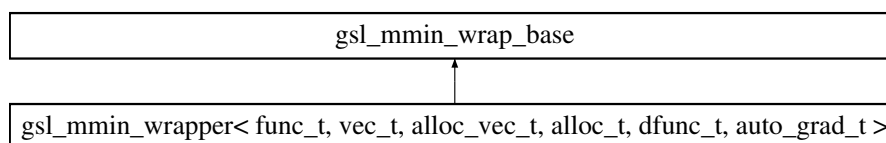
- `gsl_mmin_bfgs2.h`

## 46.137 gsl\_mmin\_wrapper< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, dfunc\_t, auto\_grad\_t > Class Template Reference

Wrapper class for the `gsl_mmin_bfgs2` minimizer.

```
#include <gsl_mmin_bfgs2.h>
```

Inheritance diagram for `gsl_mmin_wrapper< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t >`:



### 46.137.1 Detailed Description

```
template<class func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_funct<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>> class gsl_mmin_wrapper< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t >
```

This is a reimplmentation of the internal GSL wrapper for function calls in the BFGS minimizer.

Definition at line 63 of file `gsl_mmin_bfgs2.h`.

#### Public Member Functions

- void `prepare_wrapper` (func\_t &ufunc, dfunc\_t \*udfunc, vec\_t &t\_x, double f, vec\_t &t\_g, vec\_t &t\_p, auto\_grad\_t \*ag)  
*Initialize wrapper.*
- void `update_position` (double alpha, vec\_t &t\_x, double \*t\_f, vec\_t &t\_g)  
*Update position.*
- void `change_direction` ()  
*Convert cache values to the new minimizer direction.*

#### Data Fields

- alloc\_vec\_t `av_x_alpha`  
*Temporary storage.*
- alloc\_vec\_t `av_g_alpha`  
*Temporary storage.*
- size\_t `dim`  
*Number of minimization dimensions.*

#### Protected Member Functions

- void `moveto` (double alpha)  
*Move to a new point, using the cached value if possible.*
- double `slope` ()  
*Compute the slope.*
- virtual double `wrap_f` (double alpha)  
*Evaluate the function.*
- virtual double `wrap_df` (double alpha)  
*Evaluate the derivative.*
- virtual void `wrap_fdf` (double alpha, double \*f, double \*df)  
*Evaluate the function and the derivative.*

#### Protected Attributes

- func\_t \* `func`  
*Function.*
- dfunc\_t \* `dfunc`  
*Derivative.*
- auto\_grad\_t \* `agrad`  
*The automatic gradient object.*
- bool `grad_given`  
*True if the gradient was given by the user.*

#### fixed values

- vec\_t \* `x`
  - vec\_t \* `g`
  - vec\_t \* `p`
-

cached values, for  $x(\alpha)=x + \alpha * p$

- double **f\_alpha**
- double **df\_alpha**

cache keys

- double **f\_cache\_key**
- double **df\_cache\_key**
- double **x\_cache\_key**
- double **g\_cache\_key**

#### 46.137.2 Member Function Documentation

46.137.2.1 `template<class func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class dfunc_t = grad_func<ovector_base>, class auto_grad_t = gradient<func_t,ovector_base>> void gsl_mmin_wrapper< func_t, vec_t, alloc_vec_t, alloc_t, dfunc_t, auto_grad_t >::change_direction ( ) [inline]`

Convert the cache values from the end of the current minimisation to those needed for the start of the next minimisation,  $\alpha=0$

Definition at line 259 of file `gsl_mmin_bfgs2.h`.

The documentation for this class was generated from the following file:

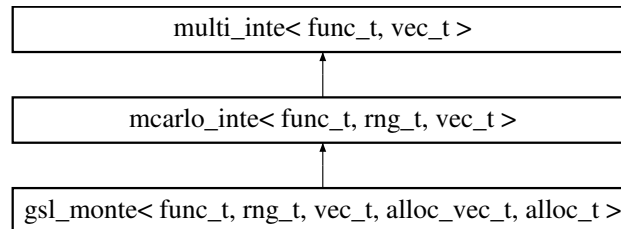
- `gsl_mmin_bfgs2.h`

### 46.138 gsl\_monte< func\_t, rng\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Multidimensional integration using plain Monte Carlo (GSL)

```
#include <gsl_monte.h>
```

Inheritance diagram for `gsl_monte< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`:



#### 46.138.1 Detailed Description

```
template<class func_t = multi_func<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>
class gsl_monte< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >
```

Definition at line 60 of file `gsl_monte.h`.

#### Public Member Functions

- virtual int [minteg\\_err](#) (func\_t &func, size\_t ndim, const vec\_t &a, const vec\_t &b, double &res, double &err)  
*Integrate function `func` from  $x=a$  to  $x=b$ .*
- virtual double [minteg](#) (func\_t &func, size\_t ndim, const vec\_t &a, const vec\_t &b)  
*Integrate function `func` over the hypercube from  $x_i = a_i$  to  $x_i = b_i$  for  $0 < i < ndim-1$ .*
- virtual const char \* [type](#) ()

*Return string denoting type ("gsl\_monte")*

The documentation for this class was generated from the following file:

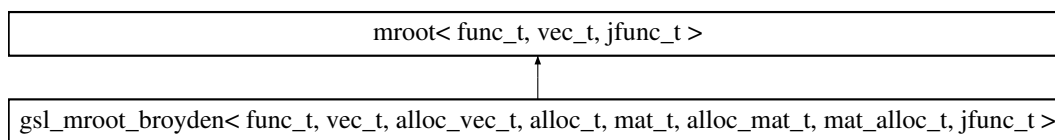
- `gsl_monte.h`

## 46.139 gsl\_mroot\_broyden< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, mat\_t, alloc\_mat\_t, mat\_alloc\_t, jfunc\_t > Class Template - Reference

Multidimensional root-finding using Broyden's method (GSL)

```
#include <gsl_mroot_broyden.h>
```

Inheritance diagram for `gsl_mroot_broyden< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >`:



### 46.139.1 Detailed Description

```
template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix_alloc, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_func_t<vec_t,mat_t>> class gsl_mroot_broyden< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >
```

Experimental.

See [Broyden65](#).

Definition at line 45 of file `gsl_mroot_broyden.h`.

### Public Member Functions

- void [allocate](#) (size\_t n)  
*Allocate memory.*
- double [enorm](#) (size\_t nvar, const vec\_t &ff)  
*Euclidean norm.*
- void [set](#) (func\_t &func, size\_t nvar, vec\_t &x, vec\_t &f, vec\_t &dx)  
*Set the function, initial guess, and provide vectors to store function values and stepsize.*
- int [iterate](#) ()  
*Perform an iteration.*
- virtual int [msolve](#) (size\_t n, vec\_t &x, func\_t &func)  
*Desc.*
- void [free](#) ()  
*Desc.*

### Data Fields

- [simple\\_jacobian](#)< func\_t, vec\_t, mat\_t, alloc\_vec\_t, alloc\_t > [def\\_jac](#)  
*Default Jacobian object.*

## Protected Member Functions

- void `clear` ()  
*Clear allocated vectors and matrices.*

## Protected Attributes

- `omatrix` `H`  
*Desc.*
- `omatrix` `lu`  
*LU decomposition.*
- `permutation` `perm`  
*Permutation object for the LU decomposition.*
- `ovector` `v`  
*Desc.*
- `ovector` `w`  
*Desc.*
- `ovector` `y`  
*Desc.*
- `ovector` `p`  
*Desc.*
- `ovector` `fnew`  
*Desc.*
- `ovector` `x_trial`  
*Desc.*
- double `phi`  
*Desc.*
- `alloc_t` `ao`  
*Memory allocation object.*
- `alloc_vec_t` `dx_int`  
*Stepsize vector.*
- `alloc_vec_t` `f_int`  
*Function value vector.*
- `func_t` \* `user_func`  
*A pointer to the user-specified function.*
- `vec_t` \* `user_f`  
*Function values.*
- `vec_t` \* `user_x`  
*Initial guess and current solution.*
- `vec_t` \* `user_dx`  
*Initial and current step.*
- `size_t` `user_nvar`  
*Number of variables.*
- `size_t` `mem_size`  
*Size of memory allocated.*
- `jacobian`< `func_t`, `vec_t`, `mat_t` > \* `ajac`  
*Jacobian.*

## 46.139.2 Member Function Documentation

46.139.2.1 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_func_t<vec_t,mat_t>> void gsl_mroot_broyden< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >::clear ( ) [inline, protected]`

This function is called by `set()` before each solve.

Definition at line 113 of file `gsl_mroot_broyden.h`.

---

```
46.139.2.2 template<class func_t = mm_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class
mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_funct<vec_t,mat_t>>> void
gsl_mroot_broyden< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >::set ( func_t & func, size_t nvar,
vec_t & x, vec_t & f, vec_t & dx ) [inline]
```

The initial values of `f` and `dx` are ignored.

Definition at line 187 of file `gsl_mroot_broyden.h`.

The documentation for this class was generated from the following file:

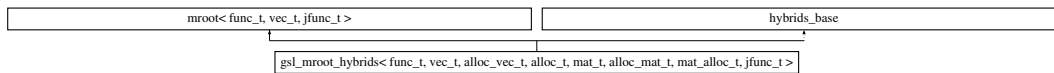
- `gsl_mroot_broyden.h`

## 46.140 gsl\_mroot\_hybrids< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, mat\_t, alloc\_mat\_t, mat\_alloc\_t, jfunc\_t > Class Template - Reference

Multidimensional root-finding algorithm using Powell's Hybrid method (GSL)

```
#include <gsl_mroot_hybrids.h>
```

Inheritance diagram for `gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >`:



### 46.140.1 Detailed Description

```
template<class func_t = mm_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_
base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_funct<vec_t,mat_t>>>class gsl_mroot_hybrids< func_t, vec_t,
alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >
```

This is a recasted version of the GSL routines which use a modified version of Powell's Hybrid method as implemented in the HYBRJ algorithm in MINPACK ([Garbow80](#)). Both the scaled and unscaled options are available by setting [int\\_scaling](#) (the scaled version is the default). If derivatives are not provided, they will be computed automatically. This class provides the GSL-like interface using [allocate\(\)](#), [set\(\)](#) (or [set\\_de\(\)](#) in case where derivatives are available), [iterate\(\)](#), and [free\(\)](#) and higher-level interfaces, [msolve\(\)](#) and [msolve\\_de\(\)](#), which perform the solution and the memory allocation automatically. Some additional checking is performed in case the user calls the functions out of order (i.e. [set\(\)](#) without [allocate\(\)](#)).

The functions [msolve\(\)](#) and [msolve\\_de\(\)](#) use the condition  $\sum_i |f_i| < \text{mroot::tol\_rel}$  to determine if the solver has succeeded.

The original GSL algorithm has been modified to shrink the stepsize if a proposed step causes the function to return a non-zero value. This allows the routine to automatically try to avoid regions where the function is not defined. To return to the default GSL behavior, set [shrink\\_step](#) to false.

The default method for numerically computing the Jacobian is from [simple\\_jacobian](#). This default is identical to the GSL approach, except that the default value of [simple\\_jacobian::epsmin](#) is non-zero. See [simple\\_jacobian](#) for more details.

There is an example for the usage of the multidimensional solver classes given in `examples/ex_mroot.cpp`, see the [Multi-dimensional solver](#).

**Todo** Are all the `set_all()` statements really necessary? Do they need to be executed even if memory hasn't been recently allocated?

**Idea for Future** It's kind of strange that `set()` sets `jac_given` to false and `set_de()` has to reset it to true. Can this be simplified?

**Idea for Future** It might be good to make sure that we're directly testing to make sure that GSL and O2SCL are more or less identical.

**Idea for Future** Many of these minpack functions could be put in their own "minpack\_tools" class, or possibly moved to be linear algebra routines instead.

**Idea for Future** There are still some numbers in here which the user could have control over, for example, the `nslow2` threshold which indicates failure.

Definition at line 485 of file `gsl_mroot_hybrids.h`.

#### Public Member Functions

- virtual int `set_jacobian` (`jacobian`< `func_t`, `vec_t`, `mat_t` > &j)  
*Set the automatic Jacobian object.*
- int `iterate` ()  
*Perform an iteration.*
- int `allocate` (size\_t n)  
*Allocate the memory.*
- int `free` ()  
*Free the allocated memory.*
- virtual const char \* `type` ()  
*Return the type, "gsl\_mroot\_hybrids".*
- virtual int `msolve_de` (size\_t nn, `vec_t` &xx, `func_t` &ufunc, `jfunc_t` &dfunc)  
*Solve func with derivatives dfunc using x as an initial guess, returning x.*
- virtual int `msolve` (size\_t nn, `vec_t` &xx, `func_t` &ufunc)  
*Solve ufunc using xx as an initial guess, returning xx.*
- int `set` (size\_t nn, `vec_t` &ax, `func_t` &ufunc)  
*Set the function, the parameters, and the initial guess.*
- int `set_de` (size\_t nn, `vec_t` &ax, `func_t` &ufunc, `jfunc_t` &dfunc)  
*Set the function, the Jacobian, the parameters, and the initial guess.*

#### Data Fields

- bool `shrink_step`  
*If true, `iterate()` will shrink the step-size automatically if the function returns a non-zero value (default true)*
- bool `int_scaling`  
*If true, use the internal scaling method (default true)*
- `simple_jacobian`< `func_t`, `vec_t`, `mat_t`, `alloc_vec_t`, `alloc_t` > `def_jac`  
*Default automatic Jacobian object.*
- `alloc_vec_t` `f`  
*The value of the function at the present iteration.*
- `alloc_vec_t` `x`  
*The present solution.*

#### Protected Member Functions

- int `solve_set` (size\_t nn, `vec_t` &xx, `func_t` &ufunc)  
*Finish the solution after `set()` or `set_de()` has been called.*

#### Protected Attributes

- int `iter`  
*Number of iterations.*
  - size\_t `ncfail`  
*Compute the number of failures.*
  - size\_t `ncsuc`  
*Compute the number of successes.*
  - size\_t `nslow1`
-

The number of times the actual reduction is less than 0.001.

- size\_t [nslow2](#)

The number of times the actual reduction is less than 0.1.

- double [fnorm](#)

The norm of the current function value.

- double [delta](#)

The limit of the Nuclidean norm.

- alloc\_mat\_t [J](#)

Jacobian.

- omatrix [q](#)

Q matrix from QR decomposition.

- omatrix [r](#)

R matrix from QR decomposition.

- ovector [tau](#)

The tau vector from QR decomposition.

- ovector [diag](#)

The diagonal elements.

- ovector [qtf](#)

The value of  $Q^T f$ .

- ovector [newton](#)

The Newton direction.

- ovector [gradient](#)

The gradient direction.

- ovector [df](#)

The change in the function value.

- ovector [qtdf](#)

The value of  $Q^T \cdot df$ .

- ovector [rdx](#)

The value of  $R \cdot dx$ .

- ovector [w](#)

The value of  $w = (Q^T df - Rdx)/|dx|$ .

- ovector [v](#)

The value of  $v = D^2 dx/|dx|$ .

- jfunc\_t \* [jac](#)

The user-specified Jacobian.

- jacobian< func\_t, vec\_t, mat\_t > \* [ajac](#)

The automatic Jacobian.

- alloc\_t [ao](#)

Memory allocator for objects of type `alloc_vec_t`.

- mat\_alloc\_t [am](#)

Memory allocator for objects of type `alloc_mat_t`.

- alloc\_vec\_t [dx](#)

The value of the derivative.

- alloc\_vec\_t [x\\_trial](#)

Trial root.

- alloc\_vec\_t [f\\_trial](#)

Trial function value.

- size\_t [dim](#)

The number of equations and unknowns.

- bool [jac\\_given](#)

True if the jacobian has been given.

- func\_t \* [fnewp](#)

The user-specified function.

- bool [set\\_called](#)

True if "set" has been called.



## 46.140.2 Member Function Documentation

46.140.2.1 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_func_t<vec_t,mat_t>> int  
gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >::iterate ( ) [inline]`

At the end of the iteration, the current value of the solution is stored in `x`.

Definition at line 675 of file `gsl_mroot_hybrids.h`.

46.140.2.2 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_func_t<vec_t,mat_t>> virtual int  
gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >::msolve_de ( size_t nn, vec_t & xx,  
func_t & ufunc, jfunc_t & dfunc ) [inline, virtual]`

Reimplemented from `mroot< func_t, vec_t, jfunc_t >`.

Definition at line 972 of file `gsl_mroot_hybrids.h`.

## 46.140.3 Field Documentation

46.140.3.1 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_func_t<vec_t,mat_t>> bool  
gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >::shrink_step`

The original GSL behavior can be obtained by setting this to `false`.

Definition at line 644 of file `gsl_mroot_hybrids.h`.

46.140.3.2 `template<class func_t = mm_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class mat_t = omatrix_base, class alloc_mat_t = omatrix, class mat_alloc_t = omatrix_alloc, class jfunc_t = jac_func_t<vec_t,mat_t>> alloc_vec_t  
gsl_mroot_hybrids< func_t, vec_t, alloc_vec_t, alloc_t, mat_t, alloc_mat_t, mat_alloc_t, jfunc_t >::f`

Definition at line 665 of file `gsl_mroot_hybrids.h`.

The documentation for this class was generated from the following file:

- `gsl_mroot_hybrids.h`

## 46.141 gsl\_ode\_control&lt; vec\_t &gt; Class Template Reference

Control structure for `gsl_astep`.

```
#include <gsl_astep.h>
```

## 46.141.1 Detailed Description

```
template<class vec_t = ovector_base>class gsl_ode_control< vec_t >
```

This class implements both the "standard" and "scaled" step control methods from GSL. The standard control method is the default. To use the scaled control, set `standard` to `false` and set the scale for each component using `set_scale()`.

The control object is a four parameter heuristic based on absolute and relative errors `eps_abs` and `eps_rel`, and scaling factors `a_y` and `a_dydt` for the system state  $y(t)$  and derivatives  $y'(t)$  respectively.

The step-size adjustment procedure for this method begins by computing the desired error level  $D_i$  for each component. In the unscaled version,

$$D_i = \text{eps\_abs} + \text{eps\_rel} \times (a\_y|y_i| + a\_dydt h|y'_i|)$$

while in the scaled version the user specifies the scale for each component,  $s_i$ ,

$$D_i = \text{eps\_abs } s_i + \text{eps\_rel} \times (\text{a\_y}|y_i| + \text{a\_dydt } h|y'_i|)$$

The desired error level  $D_i$  is compared to then observed error  $E_i = |\text{yerr}_i|$ . If the observed error  $E$  exceeds the desired error level  $D$  by more than 10 percent for any component then the method reduces the step-size by an appropriate factor,

$$h_{\text{new}} = S h_{\text{old}} \left( \frac{E}{D} \right)^{-1/q}$$

where  $q$  is the consistency order of the method (e.g.  $q = 4$  for 4(5) embedded RK), and  $S$  is a safety factor of 0.9. The ratio  $E/D$  is taken to be the maximum of the ratios  $E_i/D_i$ .

If the observed error  $E$  is less than 50 percent of the desired error level  $D$  for the maximum ratio  $E_i/D_i$  then the algorithm takes the opportunity to increase the step-size to bring the error in line with the desired level,

$$h_{\text{new}} = S h_{\text{old}} \left( \frac{E}{D} \right)^{-1/(q+1)}$$

This encompasses all the standard error scaling methods. To avoid uncontrolled changes in the stepsize, the overall scaling factor is limited to the range 1/5 to 5.

If the user specified fewer scaling parameters than the number of ODEs, then the scaling parameters are reused as follows. If there are  $N$  ODEs and  $M$  scaling parameters, then for  $i > M$ , the  $i$ th scaling parameter  $s_i$  is set to be  $s_{i \% M}$ . If the user selects the scaled control by setting `standard` to `false` and no scale parameters are specified, this class reverts to the standard control.

**Todo** Double check that the improvements in the ode-initval2 routines are available here

Definition at line 122 of file `gsl_astep.h`.

## Public Member Functions

- `template<class svec_t>`  
`int set_scale (size_t nscal, const svec_t &scale)`  
*Set the scaling for each differential equation.*
- `virtual int hadjust (size_t dim, unsigned int ord, const vec_t &y, vec_t &yerr, vec_t &yp, double &h)`  
*Automatically adjust step-size.*

## Data Fields

- `double eps_abs`  
*Absolute precision (default  $10^{-6}$ )*
- `double eps_rel`  
*Relative precision (default 0)*
- `double a_y`  
*Function scaling factor (default 1)*
- `double a_dydt`  
*Derivative scaling factor (default 0)*
- `bool standard`  
*Use standard or scaled algorithm (default true)*

## Static Public Attributes

### Adjustment specification

- `static const size_t hadj_nil = 0`  
*No adjustment required.*
- `static const size_t hadj_dec = 1`  
*Recommend step decrease.*
- `static const size_t hadj_inc = 2`  
*Recommend step increase.*

## Protected Attributes

- [uvector scale\\_abs](#)  
*Scalings.*

The documentation for this class was generated from the following file:

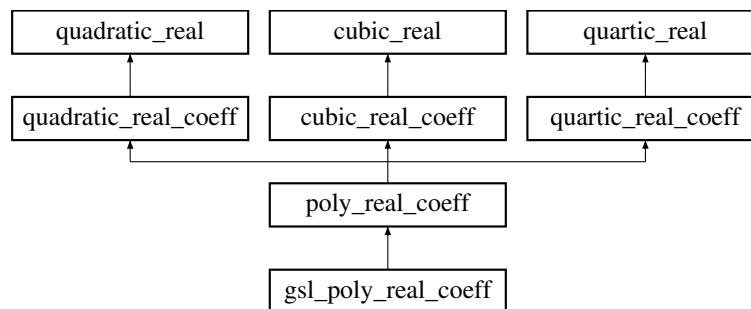
- `gsl_astep.h`

## 46.142 gsl\_poly\_real\_coeff Class Reference

Solve a general polynomial with real coefficients (GSL)

```
#include <poly.h>
```

Inheritance diagram for `gsl_poly_real_coeff`:



## 46.142.1 Detailed Description

Definition at line 606 of file `poly.h`.

## Public Member Functions

- virtual int [solve\\_rc](#) (int n, const double co[], std::complex< double > ro[])  
*Solve a generic polynomial given  $n+1$  coefficients.*
- virtual int [solve\\_rc](#) (const double a3, const double b3, const double c3, const double d3, double &x1, std::complex< double > &x2, std::complex< double > &x3)  
*Solve a cubic polynomial with real coefficients.*
- virtual int [solve\\_rc](#) (const double a2, const double b2, const double c2, std::complex< double > &x1, std::complex< double > &x2)  
*Solve a quadratic polynomial with real coefficients.*
- virtual int [solve\\_rc](#) (const double a4, const double b4, const double c4, const double d4, const double e4, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3, std::complex< double > &x4)  
*Solve a quartic polynomial with real coefficients.*
- const char \* [type](#) ()  
*Return a string denoting the type ("gsl\_poly\_real\_coeff")*

## Protected Attributes

- `gsl_poly_complex_workspace * w2`  
*Workspace for quadratic polynomials.*
- `gsl_poly_complex_workspace * w3`  
*Workspace for cubic polynomials.*

- `gsl_poly_complex_workspace * w4`  
*Workspace for quartic polynomials.*
- `gsl_poly_complex_workspace * wgen`  
*Workspace for general polynomials.*
- `int gen_size`  
*The size of the workspace wgen.*

#### 46.142.2 Member Function Documentation

46.142.2.1 `virtual int gsl_poly_real_coeff::solve_rc ( int n, const double co[], std::complex< double > ro[] ) [virtual]`

##### Note

In order to be consistent with the other `solve_rc()` functions, the ordering of the coefficients is reversed with respect to `gsl_poly_complex_solve()`. The leading coefficient is stored in `co[0]` and the constant term is stored in `co[n]`.

Implements `poly_real_coeff`.

The documentation for this class was generated from the following file:

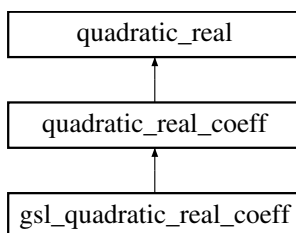
- `poly.h`

### 46.143 gsl\_quadratic\_real\_coeff Class Reference

Solve a quadratic with real coefficients and complex roots (GSL)

```
#include <poly.h>
```

Inheritance diagram for `gsl_quadratic_real_coeff`:



#### 46.143.1 Detailed Description

Definition at line 476 of file `poly.h`.

##### Public Member Functions

- `virtual int solve_rc (const double a2, const double b2, const double c2, std::complex< double > &x1, std::complex< double > &x2)`  
*Solves the polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two complex solutions  $x = x_1$  and  $x = x_2$ .*
- `const char * type ()`  
*Return a string denoting the type ("gsl\_quadratic\_real\_coeff")*

The documentation for this class was generated from the following file:

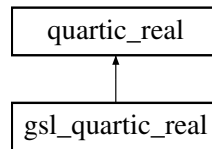
- `poly.h`

46.144 `gsl_quartic_real` Class Reference

Solve a quartic with real coefficients and real roots (GSL)

```
#include <poly.h>
```

Inheritance diagram for `gsl_quartic_real`:



## 46.144.1 Detailed Description

This class internally uses the GSL functions to solve the resolvent cubic and associated quadratics, while [gsl\\_quartic\\_real2](#) contains explicit code to solve them instead.

**Idea for Future** Optimize value of `cube_root_tol` and compare more clearly to [gsl\\_quartic\\_real2](#)

Definition at line 539 of file `poly.h`.

## Public Member Functions

- virtual int [solve\\_r](#) (const double a4, const double b4, const double c4, const double d4, const double e4, double &x1, double &x2, double &x3, double &x4)  
*Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four real solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("gsl\_quartic\_real")*

## Data Fields

- double [cube\\_root\\_tol](#)  
*A tolerance for determining the proper cube root (default  $10^{-4}$ )*

The documentation for this class was generated from the following file:

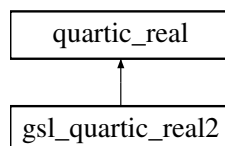
- [poly.h](#)

46.145 `gsl_quartic_real2` Class Reference

Solve a quartic with real coefficients and real roots (GSL)

```
#include <poly.h>
```

Inheritance diagram for `gsl_quartic_real2`:



## 46.145.1 Detailed Description

This class directly solves resolvent cubic and associated quadratics without using the GSL functions (as done in [gsl\\_quartic\\_real](#)).

**Idea for Future** Optimize value of `cube_root_tol` and compare more clearly to [gsl\\_quartic\\_real](#)

Definition at line 576 of file `poly.h`.

## Public Member Functions

- virtual int [solve\\_r](#) (const double a4, const double b4, const double c4, const double d4, const double e4, double &x1, double &x2, double &x3, double &x4)  
Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four real solutions  $x = x_1$  ,  $x = x_2$  ,  $x = x_3$  , and  $x = x_4$  .
- const char \* [type](#) ()  
Return a string denoting the type ("`gsl_quartic_real2`")

## Data Fields

- double [cube\\_root\\_tol](#)  
A tolerance for determining the proper cube root (default  $10^{-7}$  )

The documentation for this class was generated from the following file:

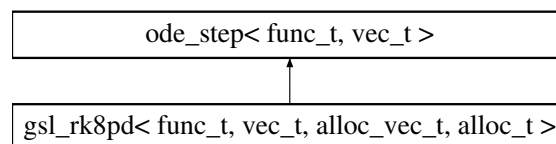
- [poly.h](#)

46.146 `gsl_rk8pd< func_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference

Embedded Runge-Kutta Prince-Dormand ODE stepper (GSL)

```
#include <gsl_rk8pd.h>
```

Inheritance diagram for `gsl_rk8pd< func_t, vec_t, alloc_vec_t, alloc_t >`:



## 46.146.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_rk8pd< func_t,
vec_t, alloc_vec_t, alloc_t >
```

Based on [Prince81](#) .

There is an example for the usage of this class in `examples/ex_ode.cpp` documented in the [Ordinary differential equations](#) section.

Definition at line 62 of file `gsl_rk8pd.h`.

## Public Member Functions

- virtual int [step](#) (double x, double h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Perform an integration step.*

## Protected Attributes

- size\_t [ndim](#)  
*Size of allocated vectors.*
- alloc\_t [ao](#)  
*Memory allocator for objects of type alloc\_vec\_t.*

## Storage for the intermediate steps

- alloc\_vec\_t **k2**
- alloc\_vec\_t **k3**
- alloc\_vec\_t **k4**
- alloc\_vec\_t **k5**
- alloc\_vec\_t **k6**
- alloc\_vec\_t **k7**
- alloc\_vec\_t **vtmp**
- alloc\_vec\_t **k8**
- alloc\_vec\_t **k9**
- alloc\_vec\_t **k10**
- alloc\_vec\_t **k11**
- alloc\_vec\_t **k12**
- alloc\_vec\_t **k13**

## Storage for the coefficients

- double **Abar** [13]
- double **A** [12]
- double **ah** [10]
- double **b21**
- double **b3** [2]
- double **b4** [3]
- double **b5** [4]
- double **b6** [5]
- double **b7** [6]
- double **b8** [7]
- double **b9** [8]
- double **b10** [9]
- double **b11** [10]
- double **b12** [11]
- double **b13** [12]

## 46.146.2 Member Function Documentation

46.146.2.1 `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int gsl_rk8pd< func_t, vec_t, alloc_vec_t, alloc_t >::step ( double x, double h, size_t n, vec_t &y, vec_t &dydx, vec_t &yout, vec_t &yerr, vec_t &dydx_out, func_t &derivs ) [inline, virtual]`

Given initial value of the n-dimensional function in y and the derivative in dydx (which must be computed beforehand) at the point x, take a step of size h giving the result in yout, the uncertainty in yerr, and the new derivative in dydx\_out using function derivs to calculate derivatives. The parameters yout and y and the parameters dydx\_out and dydx may refer to the same object.

If derivs always returns zero, then this function will also return zero. If not, `step()` will return the first non-zero value which was obtained in a call to derivs. The error handler is never called.

Implements `ode_step< func_t, vec_t >`.

Definition at line 256 of file `gsl_rk8pd.h`.

The documentation for this class was generated from the following file:

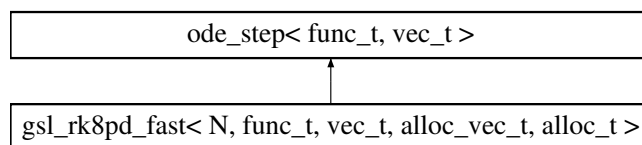
- `gsl_rk8pd.h`

## 46.147 `gsl_rk8pd_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference

Faster embedded Runge-Kutta Prince-Dormand ODE stepper (GSL)

```
#include <gsl_rk8pd.h>
```

Inheritance diagram for `gsl_rk8pd_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >`:



### 46.147.1 Detailed Description

```
template<size_t N, class func_t = ode_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_rk8pd-
_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >
```

This is a fast version of `gsl_rk8pd`, which is a stepper for a fixed number of ODEs. It ignores the error values returned by the `derivs` argument. The argument `n` to `step()` should always be equal to the template parameter `N`, and the vector parameters to `step` must have space allocated for at least `N` elements. No error checking is performed to ensure that this is the case.

Based on [Prince81](#).

Definition at line 427 of file `gsl_rk8pd.h`.

### Public Member Functions

- virtual int `step` (double `x`, double `h`, size\_t `n`, vec\_t &`y`, vec\_t &`dydx`, vec\_t &`yout`, vec\_t &`yerr`, vec\_t &`dydx_out`, func\_t &`derivs`)  
*Perform an integration step.*

### Protected Attributes

- alloc\_t `ao`  
*Memory allocator for objects of type `alloc_vec_t`.*

### Storage for the intermediate steps

- alloc\_vec\_t `k2`
- alloc\_vec\_t `k3`
- alloc\_vec\_t `k4`
- alloc\_vec\_t `k5`
- alloc\_vec\_t `k6`
- alloc\_vec\_t `k7`
- alloc\_vec\_t `ytmp`
- alloc\_vec\_t `k8`
- alloc\_vec\_t `k9`
- alloc\_vec\_t `k10`
- alloc\_vec\_t `k11`
- alloc\_vec\_t `k12`
- alloc\_vec\_t `k13`



## Storage for the coefficients

- double **Abar** [13]
- double **A** [12]
- double **ah** [10]
- double **b21**
- double **b3** [2]
- double **b4** [3]
- double **b5** [4]
- double **b6** [5]
- double **b7** [6]
- double **b8** [7]
- double **b9** [8]
- double **b10** [9]
- double **b11** [10]
- double **b12** [11]
- double **b13** [12]

## 46.147.2 Member Function Documentation

46.147.2.1 `template<size_t N, class func_t = ode_func<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>  
virtual int gsl_rk8pd_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >::step ( double x, double h, size_t n, vec_t & y, vec_t & dydx, vec_t  
& yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [inline, virtual]`

Given initial value of the n-dimensional function in `y` and the derivative in `dydx` (which must be computed beforehand) at the point `x`, take a step of size `h` giving the result in `yout`, the uncertainty in `yerr`, and the new derivative in `dydx_out` using function `derivs` to calculate derivatives. The parameters `yout` and `y` and the parameters `dydx_out` and `dydx` may refer to the same object.

## Note

The value of the parameter `n` should be equal to the template parameter `N`.

Implements [ode\\_step< func\\_t, vec\\_t >](#).

Definition at line 628 of file `gsl_rk8pd.h`.

The documentation for this class was generated from the following file:

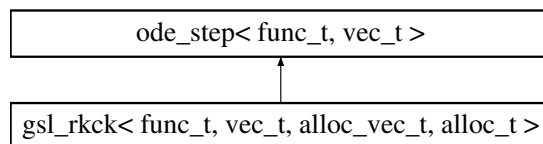
- `gsl_rk8pd.h`

## 46.148 gsl\_rkck&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Cash-Karp embedded Runge-Kutta ODE stepper (GSL)

```
#include <gsl_rkck.h>
```

Inheritance diagram for `gsl_rkck< func_t, vec_t, alloc_vec_t, alloc_t >`:



## 46.148.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_rkck< func_t,
vec_t, alloc_vec_t, alloc_t >
```

Based on [Cash90](#) .

There is an example for the usage of this class in `examples/ex_ode.cpp` documented in the [Ordinary differential equations](#) section.

Definition at line 63 of file `gsl_rkck.h`.

#### Public Member Functions

- virtual int [step](#) (double x, double h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Perform an integration step.*

#### Protected Attributes

- size\_t [ndim](#)  
*Size of allocated vectors.*
- alloc\_t [ao](#)  
*Memory allocator for objects of type `alloc_vec_t`.*

#### Storage for the intermediate steps

- alloc\_vec\_t **k2**
- alloc\_vec\_t **k3**
- alloc\_vec\_t **k4**
- alloc\_vec\_t **k5**
- alloc\_vec\_t **k6**
- alloc\_vec\_t **ytmp**

#### Storage for the coefficients

- double **ah** [5]
- double **b3** [2]
- double **b4** [3]
- double **b5** [4]
- double **b6** [5]
- double **ec** [7]
- double **b21**
- double **c1**
- double **c3**
- double **c4**
- double **c6**

#### 46.148.2 Member Function Documentation

46.148.2.1 `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int gsl_rkck< func_t, vec_t, alloc_vec_t, alloc_t >::step( double x, double h, size_t n, vec_t &y, vec_t &dydx, vec_t &yout, vec_t &yerr, vec_t &dydx_out, func_t &derivs ) [inline, virtual]`

Given initial value of the n-dimensional function in `y` and the derivative in `dydx` (which must be computed beforehand) at the point `x`, take a step of size `h` giving the result in `yout`, the uncertainty in `yerr`, and the new derivative in `dydx_out` using function `derivs` to calculate derivatives. The parameters `yout` and `y` and the parameters `dydx_out` and `dydx` may refer to the same object.

If `derivs` always returns zero, then this function will also return zero. If not, `step()` will return the first non-zero value which was obtained in a call to `derivs`. The error handler is never called.

Implements [ode\\_step< func\\_t, vec\\_t >](#).

Definition at line 160 of file `gsl_rkck.h`.

The documentation for this class was generated from the following file:

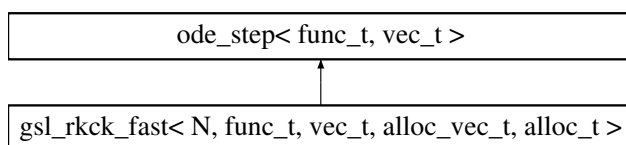
- `gsl_rkck.h`

## 46.149 `gsl_rkck_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference

Faster Cash-Karp embedded Runge-Kutta ODE stepper (GSL)

```
#include <gsl_rkck.h>
```

Inheritance diagram for `gsl_rkck_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >`:



### 46.149.1 Detailed Description

```
template<size_t N, class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_rkck_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >
```

This is a faster version of [gsl\\_rkck](#), which is a stepper for a fixed number of ODEs. It ignores the error values returned by the `derivs` argument. The argument `n` to `step()` should always be equal to the template parameter `N`, and the vector parameters to `step` must have space allocated for at least `N` elements. No error checking is performed to ensure that this is the case.

Based on [Cash90](#).

Definition at line 253 of file `gsl_rkck.h`.

### Public Member Functions

- virtual int [step](#) (double x, double h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Perform an integration step.*

### Protected Attributes

- alloc\_t [ao](#)  
*Memory allocator for objects of type `alloc_vec_t`.*

### Storage for the intermediate steps

- alloc\_vec\_t **k2**
- alloc\_vec\_t **k3**
- alloc\_vec\_t **k4**
- alloc\_vec\_t **k5**
- alloc\_vec\_t **k6**
- alloc\_vec\_t **ytmp**

## Storage for the coefficients

- double **ah** [5]
- double **b3** [2]
- double **b4** [3]
- double **b5** [4]
- double **b6** [5]
- double **ec** [7]
- double **b21**
- double **c1**
- double **c3**
- double **c4**
- double **c6**

## 46.149.2 Member Function Documentation

46.149.2.1 `template<size_t N, class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>`  
`virtual int gsl_rkck_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >::step ( double x, double h, size_t n, vec_t & y, vec_t & dydx, vec_t &`  
`yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [inline, virtual]`

Given initial value of the n-dimensional function in `y` and the derivative in `dydx` (which must be computed beforehand) at the point `x`, take a step of size `h` giving the result in `yout`, the uncertainty in `yerr`, and the new derivative in `dydx_out` using function `derivs` to calculate derivatives. The parameters `yout` and `y` and the parameters `dydx_out` and `dydx` may refer to the same object.

## Note

The value of the parameter `n` must be equal to the template parameter `N`.

Implements [ode\\_step< func\\_t, vec\\_t >](#).

Definition at line 344 of file `gsl_rkck.h`.

The documentation for this class was generated from the following file:

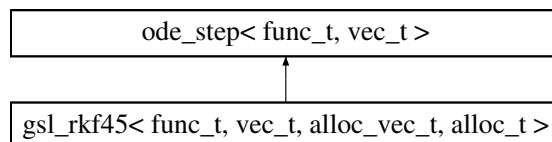
- `gsl_rkck.h`

## 46.150 gsl\_rkf45&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Runge-Kutta-Fehlberg embedded Runge-Kutta ODE stepper (GSL)

```
#include <gsl_rkf45.h>
```

Inheritance diagram for `gsl_rkf45< func_t, vec_t, alloc_vec_t, alloc_t >`:



## 46.150.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_rkf45< func_t,
vec_t, alloc_vec_t, alloc_t >
```

Based on [Hairer00](#) .

**Todo** Check this because it may not give exact dydt\_out.

Definition at line 60 of file gsl\_rkf45.h.

### Public Member Functions

- virtual int [step](#) (double x, double h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Perform an integration step.*

### Protected Attributes

- size\_t [ndim](#)  
*Size of allocated vectors.*
- alloc\_t [ao](#)  
*Memory allocator for objects of type alloc\_vec\_t.*

### Storage for the intermediate steps

- alloc\_vec\_t **k2**
- alloc\_vec\_t **k3**
- alloc\_vec\_t **k4**
- alloc\_vec\_t **k5**
- alloc\_vec\_t **k6**
- alloc\_vec\_t **ytmp**

### Storage for the coefficients

- double **ah** [5]
- double **b3** [2]
- double **b4** [3]
- double **b5** [4]
- double **b6** [5]
- double **c1**
- double **c3**
- double **c4**
- double **c5**
- double **c6**
- double **ec** [7]

## 46.150.2 Member Function Documentation

**46.150.2.1** `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int gsl_rkf45< func_t, vec_t, alloc_vec_t, alloc_t >::step ( double x, double h, size_t n, vec_t &y, vec_t &dydx, vec_t &yout, vec_t &yerr, vec_t &dydx_out, func_t &derivs ) [inline, virtual]`

Given initial value of the n-dimensional function in y and the derivative in dydx (which must be computed beforehand) at the point x, take a step of size h giving the result in yout, the uncertainty in yerr, and the new derivative in dydx\_out using function derivs to calculate derivatives. The parameters yout and y and the parameters dydx\_out and dydx may refer to the same object.

If derivs always returns zero, then this function will also return zero. If not, [step\(\)](#) will return the first non-zero value which was obtained in a call to derivs. The error handler is never called.

Implements [ode\\_step< func\\_t, vec\\_t >](#).

Definition at line 156 of file gsl\_rkf45.h.

The documentation for this class was generated from the following file:

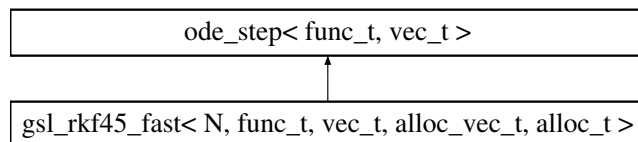
- [gsl\\_rkf45.h](#)

46.151 `gsl_rkf45_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >` Class Template Reference

Faster Runge-Kutta-Fehlberg embedded Runge-Kutta ODE stepper (GSL)

```
#include <gsl_rkf45.h>
```

Inheritance diagram for `gsl_rkf45_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >`:



## 46.151.1 Detailed Description

```
template<size_t N, class func_t = ode_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class gsl_rkf45-
_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >
```

This is a faster version of `gsl_rkf45`, which is a stepper for a fixed number of ODEs. It ignores the error values returned by the `derivs` argument. The argument `n` to `step()` should always be equal to the template parameter `N`, and the vector parameters to `step` must have space allocated for at least `N` elements. No error checking is performed to ensure that this is the case.

Based on [Hairer00](#).

Definition at line 256 of file `gsl_rkf45.h`.

## Public Member Functions

- virtual int `step` (double `x`, double `h`, size\_t `n`, vec\_t &`y`, vec\_t &`dydx`, vec\_t &`yout`, vec\_t &`yerr`, vec\_t &`dydx_out`, func\_t &`derivs`)  
*Perform an integration step.*

## Protected Attributes

- alloc\_t `ao`  
*Memory allocator for objects of type `alloc_vec_t`.*

## Storage for the intermediate steps

- alloc\_vec\_t `k2`
- alloc\_vec\_t `k3`
- alloc\_vec\_t `k4`
- alloc\_vec\_t `k5`
- alloc\_vec\_t `k6`
- alloc\_vec\_t `ytmp`

## Storage for the coefficients

- double `ah` [5]
- double `b3` [2]
- double `b4` [3]
- double `b5` [4]
- double `b6` [5]
- double `c1`
- double `c3`
- double `c4`
- double `c5`
- double `c6`
- double `ec` [7]

## 46.151.2 Member Function Documentation

46.151.2.1 `template<size_t N, class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>  
virtual int gsl_rkf45_fast< N, func_t, vec_t, alloc_vec_t, alloc_t >::step ( double x, double h, size_t n, vec_t & y, vec_t & dydx, vec_t & yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [inline, virtual]`

Given initial value of the n-dimensional function in `y` and the derivative in `dydx` (which must be computed beforehand) at the point `x`, take a step of size `h` giving the result in `yout`, the uncertainty in `yerr`, and the new derivative in `dydx_out` using function `derivs` to calculate derivatives. The parameters `yout` and `y` and the parameters `dydx_out` and `dydx` may refer to the same object.

## Note

The value of the parameter `n` should be equal to the template parameter `N`.

Implements `ode_step< func_t, vec_t >`.

Definition at line 352 of file `gsl_rkf45.h`.

The documentation for this class was generated from the following file:

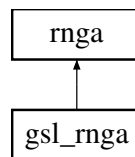
- `gsl_rkf45.h`

## 46.152 gsl\_rnga Class Reference

Random number generator (GSL)

```
#include <gsl_rnga.h>
```

Inheritance diagram for `gsl_rnga`:



## 46.152.1 Detailed Description

If `seed` is zero, or is not given, then the default seed specific to the particular random number generator is used. No virtual functions are used in this class or its parent, `rnga`. This should be as fast as the original GSL version.

An interesting application of this class to generate an arbitrary distribution through a Markov chain Monte Carlo method is in [Generate an arbitrary distribution](#).

Definition at line 45 of file `gsl_rnga.h`.

## Public Member Functions

- `gsl_rnga (const gsl_rng_type *gtype=gsl_rng_mt19937)`  
*Initialize the random number generator with type `gtype` and the default seed.*
- `gsl_rnga (unsigned long int seed, const gsl_rng_type *gtype=gsl_rng_mt19937)`  
*Initialize the random number generator with `seed`.*
- `const gsl_rng_type * get_type ()`  
*Return generator type.*
- `double random ()`  
*Return a random number in (0,1].*

- unsigned long int `get_max` ()  
Return the maximum integer for `random_int()`
- unsigned long int `random_int` (unsigned long int n=0)  
Return random integer in  $[0, \text{max} - 1]$ .
- void `set_seed` (unsigned long int s)  
Set the seed.
- void `clock_seed` ()  
Set the seed.

#### Protected Attributes

- `gsl_rng * gr`  
The GSL random number generator.
- `const gsl_rng_type * rng`  
The GSL random number generator type.

The documentation for this class was generated from the following file:

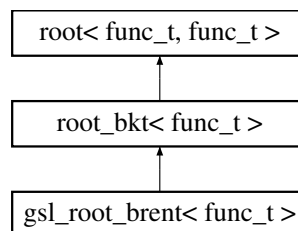
- `gsl_rnga.h`

## 46.153 `gsl_root_brent< func_t >` Class Template Reference

One-dimensional root-finding (GSL)

```
#include <gsl_root_brent.h>
```

Inheritance diagram for `gsl_root_brent< func_t >`:



### 46.153.1 Detailed Description

```
template<class func_t = funct>class gsl_root_brent< func_t >
```

This class finds the root of a user-specified function. If `test_form` is 0, then `solve_bkt()` stops when the size of the bracket is smaller than `root::tol_abs`. If `test_form` is 1, then the function stops when the residual is less than `root::tol_rel`. If `test_form` is 2, then both tests are applied.

An example demonstrating the usage of this class is given in `examples/ex_fptr.cpp` and the [Function object example](#).

**Idea for Future** There is some duplication in the variables `x_lower`, `x_upper`, `a`, and `b`, which could be removed. Some better variable names would also be helpful.

**Idea for Future** Create a meaningful enum list for `gsl_root_brent::test_form`.

Definition at line 85 of file `gsl_root_brent.h`.



## Public Member Functions

- virtual const char \* [type](#) ()  
*Return the type, "gsl\_root\_brent".*
- int [iterate](#) (func\_t &f)  
*Perform an iteration.*
- virtual int [solve\\_bkt](#) (double &x1, double x2, func\_t &f)  
*Solve *func* in region  $x_1 < x < x_2$  returning  $x_1$ .*
- double [get\\_root](#) ()  
*Get the most recent value of the root.*
- double [get\\_lower](#) ()  
*Get the lower limit.*
- double [get\\_upper](#) ()  
*Get the upper limit.*
- int [set](#) (func\_t &ff, double lower, double upper)  
*Set the information for the solver.*

## Data Fields

- int [test\\_form](#)  
*The type of convergence test applied: 0, 1, or 2 (default 0)*

## Protected Attributes

- double [root](#)  
*The present solution estimate.*
- double [x\\_lower](#)  
*The present lower limit.*
- double [x\\_upper](#)  
*The present upper limit.*

## Storage for solver state

- double **a**
- double **b**
- double **c**
- double **d**
- double **e**
- double **fa**
- double **fb**
- double **fc**

## 46.153.2 Member Function Documentation

46.153.2.1 `template<class func_t = func_t> int gsl_root_brent< func_t >::iterate ( func_t & f )` `[inline]`

This function currently always returns [gsl\\_success](#).

Definition at line 101 of file `gsl_root_brent.h`.

46.153.2.2 `template<class func_t = func_t> int gsl_root_brent< func_t >::set ( func_t & ff, double lower, double upper )` `[inline]`

This function currently always returns [gsl\\_success](#).

Definition at line 335 of file `gsl_root_brent.h`.

The documentation for this class was generated from the following file:

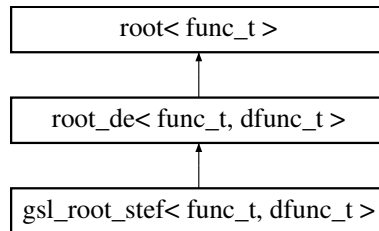
- `gsl_root_brent.h`

46.154 `gsl_root_stef< func_t, dfunc_t >` Class Template Reference

Steffenson equation solver (GSL)

```
#include <gsl_root_stef.h>
```

Inheritance diagram for `gsl_root_stef< func_t, dfunc_t >`:



## 46.154.1 Detailed Description

```
template<class func_t, class dfunc_t = func_t>class gsl_root_stef< func_t, dfunc_t >
```

This is Newton's method with an Aitken "delta-squared" acceleration of the iterates. This can improve the convergence on multiple roots where the ordinary Newton algorithm is slow.

Defining the next iteration with

$$x_{i+1} = x_i - f(x_i) / f'(x_i)$$

the accelerated value is

$$x_{\text{acc},i} = x_i - (x_{i+1} - x_i)^2 / (x_{i+2} - 2x_{i+1} + x_i)$$

We can only use the accelerated estimate after three iterations, and use the unaccelerated value until then.

This class finds a root of a function a derivative. If the derivative is not analytically specified, it is most likely preferable to use of the alternatives, `gsl_root_brent`, `cern_root`, or `cern_mroot_root`. The function `solve_de()` performs the solution automatically, and a lower-level GSL-like interface with `set()` and `iterate()` is also provided.

By default, this solver compares the present value of the root ( `root`) to the previous value ( `x`), and returns success if  $|\text{root} - x| < \text{tol}$ , where  $\text{tol} = \text{tol\_abs} + \text{tolf2} \text{ root}$ .

If `test_residual` is set to true, then the solver additionally requires that the absolute value of the function is less than `root::tol_rel`.

The original variable `x_2` has been removed as it was unused in the original GSL code.

**Idea for Future** There's some extra copying here which can probably be removed.

**Idea for Future** Compare directly to GSL.

**Idea for Future** This can probably be modified to shorten the step if the function goes out of bounds as in `gsl_mroot_hybrids`.

Definition at line 104 of file `gsl_root_stef.h`.

## Public Member Functions

- virtual const char \* `type` ()  
*Return the type, "gsl\_root\_stef".*
- int `iterate` ()  
*Perform an iteration.*
- virtual int `solve_de` (double &xx, func\_t &fun, dfunc\_t &dfunc)

Solve *func* using *x* as an initial guess using derivatives *df*.

- int [set](#) ([func\\_t](#) &*fun*, [dfunc\\_t](#) &*dfunc*, double *guess*)  
Set the information for the solver.

#### Data Fields

- double [root](#)  
The present solution estimate.
- double [tolf2](#)  
The relative tolerance for subsequent solutions (default  $10^{-12}$ )
- bool [test\\_residual](#)  
True if we should test the residual also (default false)

#### Protected Attributes

- double [f](#)  
Function value.
- double [df](#)  
Derivative value.
- double [x\\_1](#)  
Previous value of root.
- double [x](#)  
Root.
- int [count](#)  
Number of iterations.
- [func\\_t](#) \* [fp](#)  
The function to solve.
- [dfunc\\_t](#) \* [dfp](#)  
The derivative.

#### 46.154.2 Member Function Documentation

46.154.2.1 `template<class func_t, class dfunc_t = func_t> int gsl_root_stef< func_t, dfunc_t >::iterate ( ) [inline]`

After a successful iteration, [root](#) contains the most recent value of the root.

Definition at line 158 of file `gsl_root_stef.h`.

46.154.2.2 `template<class func_t, class dfunc_t = func_t> int gsl_root_stef< func_t, dfunc_t >::set ( func_t & fun, dfunc_t & dfunc, double guess ) [inline]`

Set the function, the derivative, the initial guess and the parameters.

Definition at line 277 of file `gsl_root_stef.h`.

The documentation for this class was generated from the following file:

- `gsl_root_stef.h`

#### 46.155 gsl\_series Class Reference

Series acceleration by Levin u-transform (GSL)

```
#include <gsl_series.h>
```

## 46.155.1 Detailed Description

Given an array of terms in a sum, this attempts to evaluate the entire sum with an estimate of the error.

**Idea for Future** Move the workspaces to classes?

Definition at line 64 of file `gsl_series.h`.

## Public Member Functions

- `gsl_series` (size\_t size=0)  
*size is the number of terms in the series*
- `template<class vec_t > double series_accel` (size\_t na, vec\_t &array, double &abserr\_trunc)  
*Return the accelerated sum of the series with a simple error estimate.*
- `template<class vec_t > double series_accel_err` (size\_t na, vec\_t &array, double &abserr)  
*Return the accelerated sum of the series with an accurate error estimate.*
- `void set_size` (size\_t new\_size)  
*Set the number of terms.*

## 46.155.2 Member Function Documentation

46.155.2.1 `template<class vec_t > double gsl_series::series_accel ( size_t na, vec_t & array, double & abserr_trunc )` `[inline]`

The input vector `x` should be an array with `n` values from `x[0]` to `x[n-1]`.

Definition at line 81 of file `gsl_series.h`.

46.155.2.2 `template<class vec_t > double gsl_series::series_accel_err ( size_t na, vec_t & array, double & abserr )` `[inline]`

The input vector `x` should be an array with `n` values from `x[0]` to `x[n-1]`.

Definition at line 204 of file `gsl_series.h`.

The documentation for this class was generated from the following file:

- `gsl_series.h`

## 46.156 gsl\_smooth Class Reference

Smooth a GSL vector using GSL bsplines.

```
#include <gsl_smooth.h>
```

## 46.156.1 Detailed Description

**Todo** Needs a bit more error checking and more documentation.

**Idea for Future** Generalize to generic vector types. (Does this require reworking the GSL linear fitting routines?) In the meantime, make a `ovector` interface.

**Idea for Future** Possibly create a new `gsl_bspline` class which replaces the GSL bspline workspace

**Idea for Future** Allow user to probe chi squared and the covariance?

Definition at line 53 of file `gsl_smooth.h`.

## Public Member Functions

- [gsl\\_smooth](#) (const [gsl\\_vector](#) \*ix)  
*Begin using x-values from vector i x.*
- void [set\\_ncoeff](#) (int incoeffs)  
*Set the number of coefficients.*
- void [set\\_order](#) (int order)  
*Set order.*
- void [set\\_pars](#) (int incoeffs, int order)  
*Set parameters.*
- void [set\\_x](#) (const [gsl\\_vector](#) \*ix)  
*Set the x-values.*
- int [smooth\\_data](#) (const [gsl\\_vector](#) \*y, const [gsl\\_vector](#) \*e, [gsl\\_vector](#) \*ys)  
*Smooth data in y with errors e returning result ys.*
- int [smooth\\_data](#) (const [gsl\\_vector](#) \*y, [gsl\\_vector](#) \*ys)  
*Smooth data in y returning result ys.*

## Protected Member Functions

- int [fit](#) (const [gsl\\_vector](#) \*y)  
*Construct un-weighted fit.*
- int [fit\\_errors](#) (const [gsl\\_vector](#) \*y, const [gsl\\_vector](#) \*e)  
*Construct weighted fit.*
- double [calc\\_for\\_x](#) (double xi)  
*calculate smoothed curve value for a certain xi*
- int [init](#) ()  
*Allocate memory and initialize splines.*
- void [init\\_pointers\\_and\\_defs](#) ()  
*Set default values and zero pointers.*
- int [free](#) ()  
*Free memory.*

## Protected Attributes

- size\_t [ncoeffs](#)  
*Number of free coefficients for spline.*
- size\_t [norder](#)  
*Order of spline to be used (4=cubic)*
- size\_t [nbreak](#)  
*internally calculated, number of "segment" to split the data into*
- bool [x\\_set](#)  
*True of the x values have been set.*
- [gsl\\_bspline\\_workspace](#) \* [bw](#)  
*Spline workspace.*
- [gsl\\_vector](#) \* [B](#)  
*Spline temporary vector.*
- [gsl\\_vector](#) \* [c](#)  
*Parameters of linear fit,  $y=X*c$ .*
- [gsl\\_multifit\\_linear\\_workspace](#) \* [mw](#)  
*Linear fit workspace.*
- [gsl\\_matrix](#) \* [X](#)  
*Workspace for spline fitting.*
- const [gsl\\_vector](#) \* [x](#)  
*Values of the independent variable.*
- [gsl\\_matrix](#) \* [cov](#)  
*Covariance matrix.*

## 46.156.2 Member Function Documentation

46.156.2.1 void `gsl_smooth::set_x` ( const `gsl_vector` \* *ix* ) [inline]

Definition at line 95 of file `gsl_smooth.h`.

46.156.2.2 int `gsl_smooth::init` ( ) [protected]

The documentation for this class was generated from the following file:

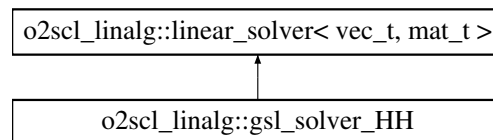
- `gsl_smooth.h`

## 46.157 o2scl\_linalg::gsl\_solver\_HH Class Reference

GSL Householder solver.

```
#include <linear_solver.h>
```

Inheritance diagram for `o2scl_linalg::gsl_solver_HH`:



## 46.157.1 Detailed Description

Definition at line 174 of file `linear_solver.h`.

## Public Member Functions

- virtual int `solve` (size\_t *n*, `o2scl::omatrix_base` &*A*, `o2scl::ovector_base` &*b*, `o2scl::ovector_base` &*x*)  
Solve square linear system  $Ax = b$  of size *n*.

The documentation for this class was generated from the following file:

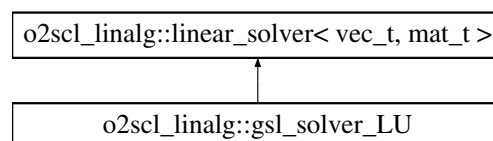
- `linear_solver.h`

## 46.158 o2scl\_linalg::gsl\_solver\_LU Class Reference

GSL solver by LU decomposition.

```
#include <linear_solver.h>
```

Inheritance diagram for `o2scl_linalg::gsl_solver_LU`:



## 46.158.1 Detailed Description

Definition at line 119 of file linear\_solver.h.

## Public Member Functions

- virtual int [solve](#) (size\_t n, [o2scl::omatrix\\_base](#) &A, [o2scl::ovector\\_base](#) &b, [o2scl::ovector\\_base](#) &x)  
*Solve square linear system  $Ax = b$  of size  $n$ .*

The documentation for this class was generated from the following file:

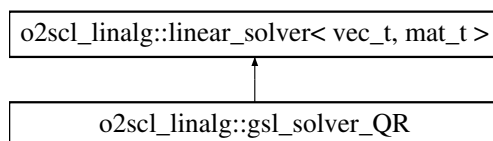
- linear\_solver.h

## 46.159 o2scl\_linalg::gsl\_solver\_QR Class Reference

GSL solver by QR decomposition.

```
#include <linear_solver.h>
```

Inheritance diagram for o2scl\_linalg::gsl\_solver\_QR:



## 46.159.1 Detailed Description

Definition at line 148 of file linear\_solver.h.

## Public Member Functions

- virtual int [solve](#) (size\_t n, [o2scl::omatrix\\_base](#) &A, [o2scl::ovector\\_base](#) &b, [o2scl::ovector\\_base](#) &x)  
*Solve square linear system  $Ax = b$  of size  $n$ .*

The documentation for this class was generated from the following file:

- linear\_solver.h

## 46.160 gsl\_vector\_norm Class Reference

Norm object for gsl vectors.

```
#include <ovector_tlate.h>
```

Inherited by [ovector\\_const\\_view\\_tlate< double, gsl\\_vector\\_norm, gsl\\_block >](#).

## 46.160.1 Detailed Description

This object is principally for use inside the ovector templates e.g.. [ovector\\_tlate](#) . For most applications, this object need not be instantiated directly by the end-user.

For an empty vector, this function returns zero and does not call the error handler.

Definition at line 64 of file ovector\_tlate.h.

#### Public Member Functions

- double [norm](#) () const  
*Compute the norm of a gsl\_vector.*

The documentation for this class was generated from the following file:

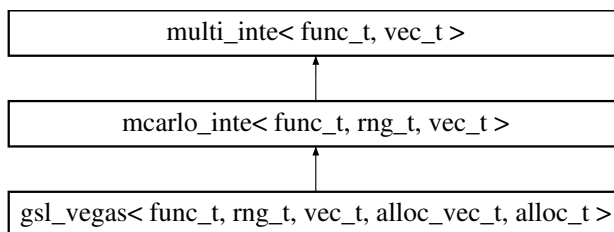
- [ovector\\_tlate.h](#)

## 46.161 gsl\_vegas< func\_t, rng\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Multidimensional integration using Vegas Monte Carlo (GSL)

```
#include <gsl_vegas.h>
```

Inheritance diagram for `gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`:



### 46.161.1 Detailed Description

```
template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_-
alloc>class gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >
```

The output options are a little different than the original GSL routine. The default setting of `mcarlo_inte::verbose` is 0, which turns off all output. A verbose value of 1 prints summary information about the weighted average and final result, while a value of 2 also displays the grid coordinates. A value of 3 prints information from the rebinning procedure for each iteration.

Some original documentation from GSL:

The input coordinates are `x[j]`, with upper and lower limits `xu[j]` and `xl[j]`. The integration length in the `j`-th direction is `delx[j]`. Each coordinate `x[j]` is rescaled to a variable `y[j]` in the range 0 to 1. The range is divided into bins with boundaries `xi[i][j]`, where `i=0` corresponds to `y=0` and `i=bins` to `y=1`. The grid is refined (ie, bins are adjusted) using `d[i][j]` which is some variation on the squared sum. A third parameter used in defining the real coordinate using random numbers is called `z`. It ranges from 0 to `bins`. Its integer part gives the lower index of the bin into which a call is to be placed, and the remainder gives the location inside the bin.

When stratified sampling is used the bins are grouped into boxes, and the algorithm allocates an equal number of function calls to each box.

The variable `alpha` controls how "stiff" the rebinning algorithm



is. `alpha = 0` means never change the grid. Alpha is typically set between 1 and 2.

**Todo** Mode = importance only doesn't give the same answer as GSL yet.

**Idea for Future** Prettify the verbose output

**Idea for Future** Allow the user to get information about the how the sampling was done, possibly by converting the bins and boxes into a structure or class.

**Idea for Future** Allow the user to change the maximum number of bins.

Based on [Lepage78](#) . The current version of the algorithm was described in the Cornell preprint CLNS-80/447 of March, 1980. The GSL code follows most closely the C version by D. R. Yennie, coded in 1984.

Definition at line 110 of file `gsl_vegas.h`.

### Public Member Functions

- virtual int [allocate](#) (size\_t ldim)  
*Allocate memory.*
- virtual int [free](#) ()  
*Free allocated memory.*
- virtual int [vegas\\_minteg\\_err](#) (int stage, func\_t &func, size\_t ndim, const vec\_t &xl, const vec\_t &xu, double &res, double &err)  
*Integrate function `func` from  $x=a$  to  $x=b$ .*
- virtual int [minteg\\_err](#) (func\_t &func, size\_t ndim, const vec\_t &a, const vec\_t &b, double &res, double &err)  
*Integrate function `func` from  $x=a$  to  $x=b$ .*
- virtual double [minteg](#) (func\_t &func, size\_t ndim, const vec\_t &a, const vec\_t &b)  
*Integrate function `func` over the hypercube from  $x_i = a_i$  to  $x_i = b_i$  for  $0 < i < ndim-1$ .*
- virtual const char \* [type](#) ()  
*Return string denoting type ("`gsl_vegas`")*

### Data Fields

- double [result](#)  
*Result from last iteration.*
- double [sigma](#)  
*Uncertainty from last iteration.*
- double [alpha](#)  
*The stiffness of the rebinning algorithm (default 1.5)*
- unsigned int [iterations](#)  
*Set the number of iterations (default 5)*
- double [chisq](#)  
*The chi-squared per degree of freedom for the weighted estimate of the integral.*
- std::ostream \* [outs](#)  
*The output stream to send output information (default `std::cout`)*

### Protected Member Functions

- virtual void [init\\_box\\_coord](#) (uvector\_int &boxt)  
*Initialize box coordinates.*
- int [change\\_box\\_coord](#) (uvector\_int &boxt)  
*Change box coordinates.*
- virtual void [init\\_grid](#) (const vec\_t &xl, const vec\_t &xu, size\_t ldim)

- Initialize grid.*
- virtual void [reset\\_grid\\_values](#) ()  
*Reset grid values.*
- void [accumulate\\_distribution](#) (uvector\_int &lbin, double y)  
*Add the most recently generated result to the distribution.*
- void [random\\_point](#) (vec\_t &lx, uvector\_int &lbin, double &bin\_vol, const uvector\_int &lbox, const vec\_t &xl, const vec\_t &xu)  
*Generate a random position in a given box.*
- virtual void [resize\\_grid](#) (unsigned int lbins)  
*Resize the grid.*
- virtual void [refine\\_grid](#) ()  
*Refine the grid.*
- virtual void [print\\_lim](#) (const vec\_t &xl, const vec\_t &xu, unsigned long ldim)  
*Print limits of integration.*
- virtual void [print\\_head](#) (unsigned long num\_dim, unsigned long calls, unsigned int lit\_num, unsigned int lbins, unsigned int lboxes)  
*Print header.*
- virtual void [print\\_res](#) (unsigned int itr, double res, double err, double cum\_res, double cum\_err, double chi\_sq)  
*Print results.*
- virtual void [print\\_dist](#) (unsigned long ldim)  
*Print distribution.*
- virtual void [print\\_grid](#) (unsigned long ldim)  
*Print grid.*

#### Protected Attributes

- size\_t [dim](#)  
*Number of dimensions.*
- unsigned int [bins](#)  
*Number of bins.*
- unsigned int [boxes](#)  
*Number of boxes.*
- uvector [xi](#)  
*Boundaries for each bin.*
- uvector [xin](#)  
*Storage for grid refinement.*
- uvector [delx](#)  
*The iteration length in each direction.*
- uvector [weight](#)  
*The weight for each bin.*
- double [vol](#)  
*The volume of the current bin.*
- uvector\_int [bin](#)  
*The bins for each direction.*
- uvector\_int [box](#)  
*The boxes for each direction.*
- uvector [d](#)  
*Distribution.*
- unsigned int [it\\_start](#)  
*The starting iteration number.*
- unsigned int [it\\_num](#)  
*The total number of iterations.*
- unsigned int [samples](#)  
*Number of samples for computing chi squared.*
- unsigned int [calls\\_per\\_box](#)  
*Number of function calls per box.*
- alloc\_t [ao](#)  
*Memory allocation object.*
- alloc\_vec\_t [x](#)  
*Point for function evaluation.*

Scratch variables preserved between calls to

[vegas\\_minteg\\_err\(\)](#)

- double **jac**
- double **wtd\_int\_sum**
- double **sum\_wgts**
- double **chi\_sum**

#### Static Protected Attributes

- static const size\_t **bins\_max** = 50  
*Maximum number of bins.*

Integration mode (default is mode\_importance)

- int **mode**
- static const int **mode\_importance** = 1
- static const int **mode\_importance\_only** = 0
- static const int **mode\_stratified** = -1

#### 46.161.2 Member Function Documentation

46.161.2.1 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::change_box_coord ( uvector_int & boxt ) [inline, protected]`

Steps through the box coordinates, e.g.

{0,0}, {0,1}, {0,2}, {0,3}, {1,0}, {1,1}, {1,2}, ...

This is among the member functions that is not virtual because it is part of the innermost loop.

Definition at line 222 of file `gsl_vegas.h`.

46.161.2.2 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> void gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::accumulate_distribution ( uvector_int & lbin, double y ) [inline, protected]`

This is among the member functions that is not virtual because it is part of the innermost loop.

Definition at line 274 of file `gsl_vegas.h`.

46.161.2.3 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> void gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::random_point ( vec_t & lx, uvector_int & lbin, double & bin_vol, const uvector_int & lbox, const vec_t & xl, const vec_t & xu ) [inline, protected]`

Use the random number generator `mcargo_inte::def_rng` to return a random position x in a given box. The value of bin gives the bin location of the random position (there may be several bins within a given box)

This is among the member functions that is not virtual because it is part of the innermost loop.

Definition at line 294 of file `gsl_vegas.h`.

46.161.2.4 `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::vegas_minteg_err ( int stage, func_t & func, size_t ndim, const vec_t & xl, const vec_t & xu, double & res, double & err ) [inline, virtual]`

Original documentation from GSL:

Normally, `stage = 0` which begins with a new uniform grid and empty weighted average. Calling `vegas` with `stage = 1` retains the grid from the previous run but discards the weighted average, so that one can "tune" the grid using a relatively small number of points and then do a large run with `stage = 1` on the optimized grid. Setting `stage = 2` keeps the grid and the weighted average from the previous run, but may increase (or decrease) the number of histogram bins in the grid depending on the number of calls available. Choosing `stage = 3` enters at the main loop, so that nothing is changed, and is equivalent to performing additional iterations in a previous call.

**Todo** Should `stage` be passed by reference?

There was an update between `gsl-1.12` and `1.15` which has not been implemented here yet.

Definition at line 618 of file `gsl_vegas.h`.

#### 46.161.3 Field Documentation

**46.161.3.1** `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::alpha`

This usual range is between 1 and 2.

Definition at line 133 of file `gsl_vegas.h`.

**46.161.3.2** `template<class func_t = multi_func_t<>, class rng_t = gsl_rnga, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >::chisq`

After an integration, this should be close to 1. If it is not, then this indicates that the values of the integral from different iterations are inconsistent, and the error may be underestimated. Further iterations of the algorithm may enable one to obtain more reliable results.

Definition at line 147 of file `gsl_vegas.h`.

The documentation for this class was generated from the following file:

- `gsl_vegas.h`

## 46.162 hdf\_file Class Reference

Store data in an HDF5 file.

```
#include <hdf_file.h>
```

#### 46.162.1 Detailed Description

The member functions which write or get data from an HDF file begin with either `get` or `set`. Where appropriate, the next character is either `c` for character, `d` for double, `f` for float, or `i` for int.

The get functions are:

- `getc()` - get a single character
- `getc_def()` - get a character or set to a default value
- `getc_arr()` - get an array
- `getc_arr_alloc()` - allocate memory with `new` and get an array

The set functions are:

- `setc()` - set a single character

- [setc\\_arr\(\)](#) - set an extensible array
- [setc\\_arr\\_fixed\(\)](#) - set a fixed array

The string I/O functions:

- [gets\(\)](#) - get a string
- [gets\\_def\(\)](#) - get a string or set to a default value
- [gets\\_arr\(\)](#) - Get an extensible string
- [gets\\_fixed\(\)](#) - get a fixed-length string
- [sets\(\)](#) - set a string
- [sets\\_fixed\(\)](#) - set a fixed-length string
- [sets\\_arr\(\)](#) - set an extensible array of strings

The vector I/O functions:

- [setd\\_vec\(\)](#) and [seti\\_vec\(\)](#) - set a vector
- [getd\\_vec\(\)](#) and [geti\\_vec\(\)](#) - get a vector
- [getd\\_vec\\_prealloc\(\)](#) and [geti\\_vec\\_prealloc\(\)](#) - get a pre-allocated vector

The matrix I/O functions:

- [setd\\_mat\(\)](#) and [seti\\_mat\(\)](#) - set a matrix
- [getd\\_mat\(\)](#) and [geti\\_mat\(\)](#) - get a matrix

By default, vectors and matrices are written to HDF files in a chunked format, so their length can be changed later as necessary. The chunk size is chosen in [def\\_chunk\(\)](#) to be the closest power of 10 to the current vector size.

All files not closed by the user are closed in the destructor, but the destructor does not automatically close groups.

#### Warning

This class is still in development. Because of this, hdf5 files generated by this class may not be easily read by future versions. Later versions of O<sub>2</sub>scl will have stronger guarantees on backwards compatibility.

**Todo** Error handling with HDF functions is a particular concern. Modify to throw O<sub>2</sub>scl exceptions when appropriate.

**Idea for Future** Automatically close groups, e.g. by storing `hid_t`'s in a stack?

Definition at line 94 of file `hdf_file.h`.

#### Public Member Functions

- int [getd\\_ten3](#) (std::string name, o2scl::tensor3 &t3)  
*Desc.*

#### Open and close files

- int [open](#) (std::string fname)  
*Open a file named fname.*
- int [close](#) ()  
*Close the file.*

## Manipulate ids

- `hid_t get_file_id ()`  
*Get the current file id.*
- `int set_current_id (hid_t cur)`  
*Set the current working id.*
- `hid_t get_current_id ()`  
*Retrieve the current working id.*

## Set functions

- `int setc (std::string name, char c)`  
*Set a character named name to value c.*
- `int setd (std::string name, double d)`  
*Set a double named name to value d.*
- `int setf (std::string name, float f)`  
*Set a float named name to value f.*
- `int seti (std::string name, int i)`  
*Set an integer named name to value i.*
- `int sets (std::string name, std::string s)`  
*Set a string named name to value s.*
- `int sets_fixed (std::string name, std::string s)`  
*Set a string named name to value s.*

## Group manipulation

- `hid_t open_group (hid_t init_id, std::string path)`  
*Open a group relative to the location specified in init\_id.*
- `hid_t open_group (std::string path)`  
*Open a group relative to the current location.*
- `int close_group (hid_t group)`  
*Close a previously created group.*

## Vector set functions

These functions automatically write all of the vector elements to the HDF file, if necessary extending the data that is already present.

- `int setd_vec (std::string name, const std::vector< double > &v)`  
*Set vector dataset named name with v.*
- `int setd_vec (std::string name, const o2scl::ovector_const_view &v)`  
*Set vector dataset named name with v.*
- `int setd_vec (std::string name, const o2scl::uvector_const_view &v)`  
*Set vector dataset named name with v.*
- `int seti_vec (std::string name, const std::vector< int > &v)`  
*Set vector dataset named name with v.*
- `int seti_vec (std::string name, const o2scl::ovector_int_const_view &v)`  
*Set vector dataset named name with v.*
- `int seti_vec (std::string name, const o2scl::uvector_int_const_view &v)`  
*Set vector dataset named name with v.*

## Vector get functions

These functions automatically free any previously allocated memory in v and then allocate the proper space required to read the information from the HDF file.

- `int getd_vec (std::string name, std::vector< double > &v)`  
*Get vector dataset and place data in v.*
- `int getd_vec (std::string name, o2scl::ovector &v)`  
*Get vector dataset and place data in v.*
- `int getd_vec (std::string name, o2scl::uvector &v)`  
*Get vector dataset and place data in v.*
- `int geti_vec (std::string name, std::vector< int > &v)`  
*Get vector dataset and place data in v.*
- `int geti_vec (std::string name, o2scl::ovector_int &v)`  
*Get vector dataset and place data in v.*
- `int geti_vec (std::string name, o2scl::uvector_int &v)`  
*Get vector dataset and place data in v.*

### Matrix set functions

These functions automatically write all of the vector elements to the HDF file, if necessary extending the data that is already present.

- int `setd_mat` (std::string name, const o2scl::omatrix\_const\_view &m)  
Set matrix dataset named *name* with *m*.
- int `setd_mat` (std::string name, const o2scl::umatrix\_const\_view &m)  
Set matrix dataset named *name* with *m*.
- int `seti_mat` (std::string name, const o2scl::omatrix\_int\_const\_view &m)  
Set matrix dataset named *name* with *m*.
- int `seti_mat` (std::string name, const o2scl::umatrix\_int\_const\_view &m)  
Set matrix dataset named *name* with *m*.

### Matrix get functions

These functions automatically free any previously allocated memory in *m* and then allocate the proper space required to read the information from the HDF file.

- int `getd_mat` (std::string name, o2scl::omatrix &m)  
Get matrix dataset and place data in *m*.
- int `getd_mat` (std::string name, o2scl::umatrix &m)  
Get matrix dataset and place data in *m*.
- int `geti_mat` (std::string name, o2scl::omatrix\_int &m)  
Get matrix dataset and place data in *m*.
- int `geti_mat` (std::string name, o2scl::umatrix\_int &m)  
Get matrix dataset and place data in *m*.

### Array set functions

- int `setc_arr` (std::string name, size\_t n, const char \*c)  
Set a character array named *name* of size *n* to value *c*.
- int `setd_arr` (std::string name, size\_t n, const double \*d)  
Set a double array named *name* of size *n* to value *d*.
- int `setf_arr` (std::string name, size\_t n, const float \*f)  
Set a float array named *name* of size *n* to value *f*.
- int `seti_arr` (std::string name, size\_t n, const int \*i)  
Set a integer array named *name* of size *n* to value *i*.
- int `sets_arr` (std::string name, std::vector< std::string > &s)  
Set a vector of strings named *name*.

### Fixed-length array set functions

If a dataset named *name* is already present, then the user-specified array must not be longer than the array already present in the HDF file.

- int `setc_arr_fixed` (std::string name, size\_t n, const char \*c)  
Set a character array named *name* of size *n* to value *c*.
- int `setd_arr_fixed` (std::string name, size\_t n, const double \*c)  
Set a double array named *name* of size *n* to value *d*.
- int `setf_arr_fixed` (std::string name, size\_t n, const float \*f)  
Set a float array named *name* of size *n* to value *f*.
- int `seti_arr_fixed` (std::string name, size\_t n, const int \*i)  
Set an integer array named *name* of size *n* to value *i*.

### Get functions

If the specified object is not found, the O<sub>2</sub>scl error handler will be called.

- int `getc` (std::string name, char &c)  
Get a character named *name*.
- int `getd` (std::string name, double &d)  
Get a double named *name*.
- int `getf` (std::string name, float &f)

- *Get a float named `name`.*  
• int `geti` (std::string name, int &i)  
*Get a integer named `name`.*
- int `gets` (std::string name, std::string &s)  
*Get a string named `name`.*
- int `gets_fixed` (std::string name, std::string &s)  
*Get a string named `name`.*
- int `gets_def_fixed` (std::string name, std::string def, std::string &s)  
*Get a string named `name`.*

#### Array get functions

All of these functions (except `gets_arr()`) assume that the pointer allocated beforehand, and matches the size of the array in the HDF file. If the specified object is not found, the `O2scl` error handler will be called.

- int `getc_arr` (std::string name, size\_t n, char \*c)  
*Get a character array named `name` of size `n`.*
- int `getd_arr` (std::string name, size\_t n, double \*d)  
*Get a double array named `name` of size `n`.*
- int `getf_arr` (std::string name, size\_t n, float \*f)  
*Get a float array named `name` of size `n`.*
- int `geti_arr` (std::string name, size\_t n, int \*i)  
*Get an integer array named `name` of size `n`.*
- int `gets_arr` (std::string name, std::vector< std::string > &s)  
*Get a string array named `name` and store it in `s`.*

#### Array get functions with memory allocation

These functions allocate memory with `new`, which should be freed by the user with `delete`.

- int `getc_arr_alloc` (std::string name, size\_t &n, char \*c)  
*Get a character array named `name` of size `n`.*
- int `getd_arr_alloc` (std::string name, size\_t &n, double \*d)  
*Get a double array named `name` of size `n`.*
- int `getf_arr_alloc` (std::string name, size\_t &n, float \*f)  
*Get a float array named `name` of size `n`.*
- int `geti_arr_alloc` (std::string name, size\_t &n, int \*i)  
*Get an integer array named `name` of size `n`.*

#### Get functions with default values

If the requested dataset is not found in the HDF file, the object is set to the specified default value and the error handler is not called.

- int `getc_def` (std::string name, char def, char &c)  
*Get a character named `name`.*
- int `getd_def` (std::string name, double def, double &d)  
*Get a double named `name`.*
- int `getf_def` (std::string name, float def, float &f)  
*Get a float named `name`.*
- int `geti_def` (std::string name, int def, int &i)  
*Get a integer named `name`.*
- int `gets_def` (std::string name, std::string def, std::string &s)  
*Get a string named `name`.*

#### Get functions with pre-allocated pointer

- int `getd_vec_prealloc` (std::string name, size\_t n, double \*d)  
*Get a double array `d` pre-allocated to have size `n`.*
- int `geti_vec_prealloc` (std::string name, size\_t n, int \*i)  
*Get an integer array `i` pre-allocated to have size `n`.*
- int `getd_mat_prealloc` (std::string name, size\_t n, size\_t m, double \*d)  
*Get a double matrix `d` pre-allocated to have size  $(n, m)$ .*
- int `geti_mat_prealloc` (std::string name, size\_t n, size\_t m, int \*i)  
*Get an integer matrix `i` pre-allocated to have size  $(n, m)$ .*



## Protected Member Functions

- virtual `hsize_t def_chunk (size_t n)`  
*Default chunk size.*

## Protected Attributes

- `hid_t file`  
*File ID.*
- `bool file_open`  
*True if a file has been opened.*
- `hid_t current`  
*Current file or group location.*

## 46.162.2 Member Function Documentation

46.162.2.1 `virtual hsize_t hdf_file::def_chunk ( size_t n ) [inline, protected, virtual]`

Choose the closest power of 10 which is greater than or equal to 10 and less than or equal to  $10^6$ .

Definition at line 114 of file `hdf_file.h`.

46.162.2.2 `int hdf_file::sets ( std::string name, std::string s )`

The string is stored in the HDF file as an extensible character array rather than a string.

46.162.2.3 `int hdf_file::sets_fixed ( std::string name, std::string s )`

This function stores `s` as a fixed-length string in the HDF file. If a dataset named `name` is already present, then `s` must not be longer than the string length already specified in the HDF file.

46.162.2.4 `hid_t hdf_file::open_group ( hid_t init_id, std::string path )`

## Note

In order to ensure that future objects are written to the newly-created group, the user must use `set_current_id()` using the newly-created group ID for the argument.

46.162.2.5 `hid_t hdf_file::open_group ( std::string path )`

## Note

In order to ensure that future objects are written to the newly-created group, the user must use `set_current_id()` using the newly-created group ID for the argument.

46.162.2.6 `int hdf_file::setd_vec ( std::string name, const o2scl::ovector_const_view & v )`

## Note

In the case that the stride of the vector `v` is not unity, this function requires copying the data twice: once from the vector to a pointer, and once from the pointer to the file. Keep this in mind when performing I/O with larger data sets.

46.162.2.7 `int hdf_file::seti_vec ( std::string name, const o2scl::ovector_int_const_view & v )`

## Note

In the case that the stride of the vector `v` is not unity, this function requires copying the data twice: once from the vector to a pointer, and once from the pointer to the file. Keep this in mind when performing I/O with larger data sets.

46.162.2.8 `int hdf_file::setd_mat ( std::string name, const o2scl::omatrix_const_view & m )`

**Note**

In the case that the trailing dimension (as reported by `omatrix_const_view_tlate::tda()`) of the matrix *m* is greater than the number of columns, this function requires copying the data twice: once from the matrix to a pointer, and once from the pointer to the file. Keep this in mind when performing I/O with larger data sets.

46.162.2.9 `int hdf_file::seti_mat ( std::string name, const o2scl::omatrix_int_const_view & m )`

**Note**

In the case that the trailing dimension (as reported by `omatrix_const_view_tlate::tda()`) of the matrix *m* is greater than the number of columns, this function requires copying the data twice: once from the matrix to a pointer, and once from the pointer to the file. Keep this in mind when performing I/O with larger data sets.

46.162.2.10 `int hdf_file::sets_arr ( std::string name, std::vector< std::string > & s )`

**Developer note:**

String vectors are reformatted as a single character array, in order to allow each string to have different length and to make each string extensible. The size of the vector *s* is stored as an integer named *nw*.

46.162.2.11 `int hdf_file::gets ( std::string name, std::string & s )`

**Note**

Strings are stored as character arrays and thus retrieving a string from a file requires loading the information from the file into a character array, and then copying it to the string. This will be slow for very long strings.

46.162.2.12 `int hdf_file::getc_arr ( std::string name, size_t n, char * c )`

**Note**

The pointer *c* must be allocated beforehand to hold *n* entries, and *n* must match the size of the array in the HDF file.

46.162.2.13 `int hdf_file::getd_arr ( std::string name, size_t n, double * d )`

**Note**

The pointer *d* must be allocated beforehand to hold *n* entries, and *n* must match the size of the array in the HDF file.

46.162.2.14 `int hdf_file::getf_arr ( std::string name, size_t n, float * f )`

**Note**

The pointer *f* must be allocated beforehand to hold *n* entries, and *n* must match the size of the array in the HDF file.

46.162.2.15 `int hdf_file::geti_arr ( std::string name, size_t n, int * i )`

**Note**

The pointer *i* must be allocated beforehand to hold *n* entries, and *n* must match the size of the array in the HDF file.

The documentation for this class was generated from the following file:

- `hdf_file.h`

## 46.163 hist Class Reference

A one-dimensional histogram class.

```
#include <hist.h>
```

### 46.163.1 Detailed Description

Experimental.

One may set the histogram bins using [set\\_bins\(\)](#) or one may manually set the limit of one bin using the reference returned by [get\\_bin\\_low\(\)](#), [get\\_bin\\_low\\_i\(\)](#), [get\\_bin\\_high\(\)](#), or [get\\_bin\\_high\\_i\(\)](#). Note that if one attempts to set the bins on a histogram where the bins have already been set, one must ensure that the new and old binnings have the same size. This requirement is designed to help prevent accidental data loss.

The upper edge of bin  $i$  is always equal to the lower edge of bin  $i+1$ .

By convention, all functions which take a bin index as an argument have an extra " $_{i}$ " suffix to distinguish them from functions which take a floating-point value to be binned as their argument.

Empty histograms have zero size.

The [set\\_bins\(\)](#) functions can only be used if (i) the current histogram is empty or (ii) the new number of bins is equal to the histogram size so that no reallocation is necessary.

To save space, representative vectors are not allocated until they are used.

---

#### Bin Representatives

One way to operate on a histogram as a function is to designate a particular value inside each bin which represents the coordinate associated with that bin. These "bin representative values" are automatically created and can be used by the function evaluation and interpolation functions [operator\(double\)](#), [interp\(\)](#), [deriv\(\)](#), [integ\(\)](#) for some particular interpolation type. By default, these representative values are taken to be the midpoint of each bin, but this option is configurable and the representative values may be set by the user for each individual bin.

---

**Todo** Check that the actions of [set\\_bins\(\)](#), [clear\(\)](#) and other functions perform the correct actions on the `user_rep` vector. I'm a bit concerned that [set\\_bins\\_auto\(\)](#) shouldn't call `user_rep.allocate()`.

**Todo** More documentation and testing.

**Idea for Future** Would be nice not to have to create a new `search_vec` object in [get\\_bin\\_index\(\)](#).

**Idea for Future** Consider adding the analogs of the GSL histogram sampling functions

**Idea for Future** Add a function which computes the bin sizes?

Definition at line 94 of file `hist.h`.

#### Public Member Functions

- [hist](#) (const [hist](#) &h)  
*Copy constructor.*
  - [hist](#) & [operator=](#) (const [hist](#) &h)  
*Copy constructor.*
  - `size_t` [size](#) () const  
*The histogram size.*
-

- double `get_max_wgt ()`  
*Get maximum weight.*
- size\_t `get_max_index ()`  
*Get the index of the maximum weight.*
- double `get_max_rep ()`  
*Get the representative for the bin with maximum weight.*

#### Initial bin setup

- int `set_bins (uniform_grid< double > g)`  
*Set bins from a `uniform_grid` object.*
- template<class vec\_t >  
int `set_bins (size_t n, const vec_t &v)`  
*Set the bins from a vector.*

#### Weight functions

- int `update (double x, double val=1.0)`  
*Increment bin for  $x$  by value  $val$ .*
- int `update_i (size_t i, double val=1.0)`  
*Increment bin with index  $i$  by value  $val$ .*
- const double & `get_wgt_i (size_t i) const`  
*Return contents of bin with index  $i$ .*
- double & `get_wgt_i (size_t i)`  
*Return contents of bin with index  $i$ .*
- const double & `get_wgt (double x) const`  
*Return contents of bin for  $x$ .*
- double & `get_wgt (double x)`  
*Return contents of bin for  $x$ .*
- int `set_wgt_i (size_t i, double val)`  
*Set contents of bin with index  $i$  to value  $val$ .*
- int `set_wgt (double x, double val)`  
*Set contents of bin for  $x$  to value  $val$ .*
- const `uvector` & `get_wgts () const`  
*Get a reference to the full  $y$  vector.*
- const double & `operator[] (size_t i) const`  
*Get a reference to the weight for the bin at index  $i$ .*
- double & `operator[] (size_t i)`  
*Get a reference to the weight for the bin at index  $i$ .*

#### Bin manipulation

- size\_t `get_bin_index (double x) const`  
*Get the index of the bin which holds  $x$ .*
- double & `get_bin_low_i (size_t i)`  
*Get the lower edge of bin of index  $i$ .*
- const double & `get_bin_low_i (size_t i) const`  
*Get the lower edge of bin of index  $i$ .*
- double & `get_bin_high_i (size_t i)`  
*Get the upper edge of bin of index  $i$ .*
- const double & `get_bin_high_i (size_t i) const`  
*Get the upper edge of bin of index  $i$ .*
- double & `get_bin_low (double x)`  
*Get the lower edge of bin of index  $i$ .*
- const double & `get_bin_low (double x) const`  
*Get the lower edge of bin of index  $i$ .*
- double & `get_bin_high (double x)`  
*Get the upper edge of bin of index  $i$ .*
- const double & `get_bin_high (double x) const`  
*Get the upper edge of bin of index  $i$ .*
- const `uvector` & `get_bins () const`  
*Get a reference to the full vector of bin specifications.*

## Delete functions

- int `clear_wgts` ()  
*Clear the data, but leave the bins as is.*
- int `clear` ()  
*Clear the entire histogram.*

## Representative functions

- template<class vec\_t >  
int `set_reps` (size\_t n, const vec\_t &v)  
*Set the representative x-values for each bin.*
- int `set_rep_mode` (size\_t mode)  
*Set mode used to compute bin representatives.*
- size\_t `get_rep_mode` () const  
*Get mode used to compute bin representatives.*
- double & `get_rep_i` (size\_t i)  
*Return the representative of bin of index i.*
- double & `get_rep` (double x)  
*Return the representative of bin containing x.*
- const `uvector` & `get_reps` ()  
*Get a reference to the full representative vector.*
- const `uvector` & `get_user_reps` () const  
*Get a reference to the full data vector.*

## Evaluation and interpolation functions

- double `operator()` (double x)  
*Return the value of the function at x.*
- double `interp` (double x)  
*Return the value of the function at x.*
- double `deriv` (double x)  
*Return the derivative of the function at x.*
- double `deriv2` (double x)  
*Return the second derivative of the function at x.*
- double `integ` (double x, double y)  
*Return the integral of the function between x and y.*
- int `set_interp` (base\_interp\_mgr< `uvector_const_view` > &bi1, base\_interp\_mgr< `uvector_const_subvector` > &bi2)  
*Set the base interpolation objects.*

## Data Fields

- bool `extend_rhs`  
*If true, allow abscissa larger than largest bin limit to correspond to the highest bin (default false)*

## Static Public Attributes

Rep modes (default is \c rmode\_avg)

- static const size\_t `rmode_avg` = 0
- static const size\_t `rmode_user` = 1
- static const size\_t `rmode_low` = 2
- static const size\_t `rmode_high` = 3
- static const size\_t `rmode_gmean` = 4

## Protected Types

- typedef `o2scl_interp_vec` < `uvector_const_view` > `interp_t`  
*Interpolation typedef.*

## Protected Member Functions

- void `set_reps_auto` ()  
*Set the representative array according to current rmode.*
- void `allocate` (size\_t n)  
*Allocate vectors for a histogram of size n.*

## Protected Attributes

- `uvector ubin`  
*Bin locations (N+1)*
- `uvector uwgt`  
*Bin contents (N)*
- `uvector urep`  
*Bin representative values (N)*
- `uvector user_rep`  
*User-defined representative values (N)*
- size\_t `hsize`  
*Number of bins.*
- size\_t `rmode`  
*Representative mode.*
- `base_interp_mgr` < `uvector_const_view` > \* `bim1`  
*A pointer to the interpolation manager.*
- `base_interp_mgr` < `uvector_const_subvector` > \* `bim2`  
*A pointer to the subvector interpolation manager.*
- `def_interp_mgr` < `uvector_const_view`, `cspline_interp` > `dim1`  
*Default interpolation manager.*
- `def_interp_mgr` < `uvector_const_subvector`, `cspline_interp` > `dim2`  
*Default interpolation manager.*

## 46.163.2 Member Function Documentation

## 46.163.2.1 void hist::allocate ( size\_t n ) [protected]

This function also sets all the weights to zero.

## 46.163.2.2 int hist::set\_bins ( uniform\_grid&lt; double &gt; g )

## Note

If the size of the histogram `uniform_grid` is not equal to the current histogram size, this function requires the histogram be empty so it can reallocate the vectors for both the bins and the weights.

## 46.163.2.3 template&lt;class vec.t&gt; int hist::set\_bins ( size\_t n, const vec.t &amp; v ) [inline]

## Note

If n is not equal to the current histogram size, this function requires the histogram be empty so it can reallocate the vectors for both the bins and the weights.

Definition at line 179 of file hist.h.

The documentation for this class was generated from the following file:

- hist.h

## 46.164 hist\_2d Class Reference

A two-dimensional histogram class.

```
#include <hist_2d.h>
```

### 46.164.1 Detailed Description

Experimental.

**Idea for Future** Write a function to create a 1-d histogram from a 2-d histogram either by selecting one bin in one axis or by marginalizing over one direction.

Definition at line 45 of file hist\_2d.h.

### Public Member Functions

- **hist\_2d** (const [hist\\_2d](#) &h)
- **hist\_2d & operator=** (const [hist\\_2d](#) &h)
- int **setup\_interp** ([twod\\_intp](#) &ti, bool x\_first=true)  
*Set up a [twod\\_intp](#) object for interpolation.*

### Initial bin setup

- int **set\_bins** ([uniform\\_grid](#)< double > gx, [uniform\\_grid](#)< double > gy)
- template<class vec\_t >  
int **set\_bins** (size\_t nx, vec\_t &vx, size\_t ny, vec\_t &vy)  
*Set the bins from a vector.*

### Weight functions

- int **update\_i** (size\_t i, size\_t j, double val=1.0)  
*Increment bin for x by value val.*
- int **update** (double x, double y, double val=1.0)  
*Increment bin for x by value val.*
- const double & **get\_wgt\_i** (size\_t i, size\_t j) const  
*Return contents of bin with index i.*
- const double & **get\_wgt** (double x, double y) const  
*Return contents of bin for x.*
- double & **get\_wgt\_i** (size\_t i, size\_t j)  
*Return contents of bin with index i.*
- double & **get\_wgt** (double x, double y)  
*Return contents of bin for x.*
- int **set\_wgt\_i** (size\_t i, size\_t j, double val)  
*Set contents of bin with index i to value val.*
- int **set\_wgt** (double x, double y, double val)  
*Set contents of bin for x to value val.*
- const [omatrix](#) & **get\_wgts** () const  
*Get a const reference to the full data vector.*
- [omatrix](#) & **get\_wgts** ()  
*Get a reference to the full data vector.*

### Delete functions

- int **clear\_wgts** ()  
*Clear the data, but leave the bins as is.*
- int **clear** ()  
*Clear the entire histogram.*

## Bin manipulation

- void [get\\_bin\\_indices](#) (double x, double y, size\_t &i, size\_t &j) const  
*Get the index of the bin which holds x.*
- size\_t [get\\_x\\_bin\\_index](#) (double x) const  
*Get the index of the bin which holds x.*
- size\_t [get\\_y\\_bin\\_index](#) (double y) const  
*Get the index of the bin which holds y.*
- double & [get\\_x\\_low\\_i](#) (size\_t i)  
*Get the lower edge of bin of index i.*
- const double & [get\\_x\\_low\\_i](#) (size\_t i) const  
*Get the lower edge of bin of index i.*
- double & [get\\_x\\_high\\_i](#) (size\_t i)  
*Get the upper edge of bin of index i.*
- const double & [get\\_x\\_high\\_i](#) (size\_t i) const  
*Get the upper edge of bin of index i.*
- double & [get\\_y\\_low\\_j](#) (size\_t j)  
*Get the lower edge of bin of index j.*
- const double & [get\\_y\\_low\\_j](#) (size\_t j) const  
*Get the lower edge of bin of index j.*
- double & [get\\_y\\_high\\_j](#) (size\_t j)  
*Get the upper edge of bin of index j.*
- const double & [get\\_y\\_high\\_j](#) (size\_t j) const  
*Get the upper edge of bin of index j.*

## Rep functions

- template<class vec\_t >  
int [set\\_reps](#) (size\_t nx, vec\_t &vx, size\_t ny, vec\_t &vy)  
*Set the representative x-values for each bin.*
- template<class vec\_t >  
int [set\\_x\\_reps](#) (size\_t nx, vec\_t &vx)  
*Set the representative x-values for each bin.*
- template<class vec\_t >  
int [set\\_y\\_reps](#) (size\_t ny, vec\_t &vy)  
*Set the representative y-values for each bin.*
- int [set\\_rep\\_mode](#) (size\_t x\_mode, size\_t y\_mode)  
*Set mode used to compute bin reps.*
- size\_t [get\\_x\\_rep\\_mode](#) () const  
*Get mode used to compute bin reps.*
- size\_t [get\\_y\\_rep\\_mode](#) () const  
*Get mode used to compute bin reps.*
- const [ovector](#) & [get\\_x\\_bins](#) () const  
*Get a reference to the full vector of bin specifications.*
- const [ovector](#) & [get\\_y\\_bins](#) () const  
*Get a reference to the full vector of bin specifications.*
- size\_t [size\\_x](#) () const  
*Return the histogram size of the x coordinate.*
- size\_t [size\\_y](#) () const  
*Return the histogram size of the y coordinate.*
- const [ovector](#) & [get\\_user\\_reps\\_x](#) () const  
*Get a reference to the user-specified reps for x coordinates.*
- const [ovector](#) & [get\\_user\\_reps\\_y](#) () const  
*Get a reference to the user-specified reps for y coordinates.*
- double & [get\\_x\\_rep\\_i](#) (size\_t i)  
*Return the rep of bin of index i.*
- const double & [get\\_x\\_rep\\_i](#) (size\_t i) const  
*Return the rep of bin of index i.*
- double & [get\\_y\\_rep\\_j](#) (size\_t j)  
*Return the rep of bin of index j.*
- const double & [get\\_y\\_rep\\_j](#) (size\_t j) const  
*Return the rep of bin of index j.*



## Data Fields

- bool [extend\\_rhs](#)  
*If true, allow abscissa larger than largest bin limit to correspond to the highest bin (default false).*

## Static Public Attributes

Rep modes (default is `\c rmode_avg`)

- static const size\_t [rmode\\_avg](#) = 0
- static const size\_t [rmode\\_user](#) = 1
- static const size\_t [rmode\\_low](#) = 2
- static const size\_t [rmode\\_high](#) = 3
- static const size\_t [rmode\\_gmean](#) = 4

## Protected Member Functions

- void [allocate](#) (size\_t nx, size\_t ny)  
*Allocate for a histogram of size nx, ny.*
- void [set\\_reps\\_auto](#) ()  
*An internal function to automatically set [xrep](#) and [yrep](#).*

## Protected Attributes

- [ovector xa](#)  
*Bin locations (Nx+1)*
- [ovector ya](#)  
*Bin locations (Ny+1)*
- [omatrix wgt](#)  
*Values (Nx,Ny)*
- [ovector xrep](#)  
*"Central" values for x-axis (N)*
- [ovector yrep](#)  
*"Central" values for y-axis (N)*
- [ovector user\\_xrep](#)  
*User-defined central values for x-axis (N)*
- [ovector user\\_yrep](#)  
*User-defined central values for y-axis (N)*
- size\_t [hsize\\_x](#)  
*Number of x-bins.*
- size\_t [hsize\\_y](#)  
*Number of y-bins.*
- size\_t [xrmode](#)  
*Rep mode for x.*
- size\_t [ymode](#)  
*Rep mode for y.*
- [base\\_interp\\_mgr](#) < [ovector\\_const\\_view](#) > \* [bim1](#)  
*A pointer to the interpolation manager.*
- [base\\_interp\\_mgr](#) < [ovector\\_const\\_subvector](#) > \* [bim2](#)  
*A pointer to the subvector interpolation manager.*
- [def\\_interp\\_mgr](#) < [ovector\\_const\\_view](#), [cspline\\_interp](#) > [dim1](#)  
*Default interpolation manager.*
- [def\\_interp\\_mgr](#) < [ovector\\_const\\_subvector](#), [cspline\\_interp](#) > [dim2](#)  
*Default interpolation manager.*

## 46.164.2 Member Function Documentation

## 46.164.2.1 void hist\_2d::allocate ( size\_t nx, size\_t ny ) [protected]

This function also sets all the weights to zero.

The documentation for this class was generated from the following file:

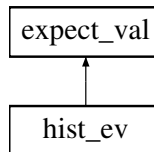
- hist\_2d.h

## 46.165 hist\_ev Class Reference

A set expectation values for histogram bins.

```
#include <hist_ev.h>
```

Inheritance diagram for hist\_ev:



## 46.165.1 Detailed Description

See [expect\\_val](#) for some general notes on this and related classes.

This class is experimental.

This class computes expectation values of bins in a histogram. It is most useful in cases where one does not know a priori how many measurements one is going to get for each bin. The class automatically arranges each bin into blocks, so that the standard deviation and error and the average can be computed even when not all bins have been filled with the same number of measurements.

## Note

This class always assumes that `n_per_block` is zero. See [expect\\_val](#) for more details.

**Todo** Test [set\\_grid\\_blocks\(\)](#) function.

**Todo** Create copy constructors as in the [scalar\\_ev](#) class.

Definition at line 58 of file `hist_ev.h`.

## Public Member Functions

- [hist\\_ev](#) ([uniform\\_grid](#)< double > g, size\_t n\_blocks)  
*Create a histogram expectation value.*
- void [reset](#) ()  
*Remove all currently stored data, but keep same block size.*
- void [set\\_grid\\_blocks](#) ([uniform\\_grid](#)< double > g, size\_t n\_blocks)  
*Set the histogram grid and the number of blocks.*
- virtual void [add](#) (double x, double val)  
*Add measurement of value val at location x.*
- virtual void [current\\_avg\\_stats](#) ([uvector](#) &reps, [uvector](#) &avg, [uvector](#) &std\_dev, [uvector](#) &avg\_err, [uvector\\_int](#) &m\_block, [uvector\\_int](#) &m\_per\_block)

*Report current average, standard deviation, and the error in the average.*

- virtual void `current_avg` (`uvector` &reps, `uvector` &avg, `uvector` &std\_dev, `uvector` &avg\_err)  
*Report current average, standard deviation, and the error in the average.*

#### Protected Attributes

- `umatrix last`  
*Last measurement for each block and each bin.*
- `umatrix vals`  
*Running average for each block and each bin.*
- `uvector_int iblock_bins`  
*The value of `iblock` for each bin.*
- `uvector_int i_bins`  
*The value of `i` for each bin.*
- `size_t hsize`  
*This should always be the same as the size as the histogram.*
- `hist h`  
*The associated histogram.*

#### 46.165.2 Member Function Documentation

46.165.2.1 virtual void `hist_ev::current_avg_stats` ( `uvector` &reps, `uvector` &avg, `uvector` &std\_dev, `uvector` &avg\_err, `uvector_int` &m\_block, `uvector_int` &m\_per\_block ) [virtual]

This function deallocates any space already allocated for the vector parameters and reallocates space as needed. Information previously stored in these vectors will be lost.

46.165.2.2 virtual void `hist_ev::current_avg` ( `uvector` &reps, `uvector` &avg, `uvector` &std\_dev, `uvector` &avg\_err ) [virtual]

This function deallocates any space already allocated for the vector parameters and reallocates space as needed. Information previously stored in these vectors will be lost.

#### 46.165.3 Field Documentation

46.165.3.1 `hist hist_ev::h` [protected]

This object is only currently used internally for binning. No data is added to it.

Definition at line 84 of file `hist_ev.h`.

The documentation for this class was generated from the following file:

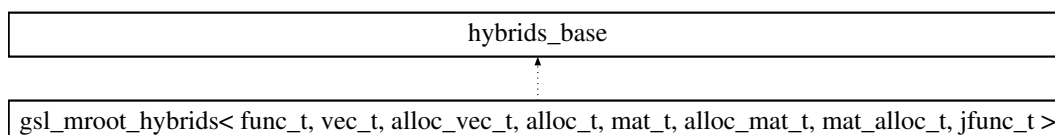
- `hist_ev.h`

## 46.166 hybrids\_base Class Reference

Base functions for `gsl_mroot_hybrids`.

```
#include <gsl_mroot_hybrids.h>
```

Inheritance diagram for `hybrids_base`:



## 46.166.1 Detailed Description

Definition at line 62 of file gsl\_mroot\_hybrids.h.

## Public Member Functions

- double [compute\\_actual\\_reduction](#) (double fnorm0, double fnorm1)  
*Compute the actual reduction.*
- double [compute\\_predicted\\_reduction](#) (double fnorm0, double fnorm1)  
*Compute the predicted reduction  $\phi|_p = |Q^T f + R \, dx|$ .*
- template<class vec2\_t >  
void [compute\\_Rg](#) (size\_t N, const [omatrix\\_base](#) &r2, const [ovector\\_base](#) &gradient2, vec2\_t &Rg)  
*Compute  $R \cdot g$  where  $g$  is the gradient.*
- template<class vec2\_t >  
void [compute\\_wv](#) (size\_t n, const [ovector\\_base](#) &qtf2, const [ovector\\_base](#) &rdx2, const vec2\_t &dx2, const [ovector\\_base](#) &diag2, double pnorm, [ovector\\_base](#) &w2, [ovector\\_base](#) &v2)  
*Compute  $w$  and  $v$ .*
- template<class vec2\_t >  
void [compute\\_rdx](#) (size\_t N, const [omatrix\\_base](#) &r2, const vec2\_t &dx2, [ovector\\_base](#) &rdx2)  
*Compute  $R \cdot dx$ .*
- template<class vec2\_t, class vec3\_t >  
double [scaled\\_enorm](#) (size\_t n, const vec2\_t &d, const vec3\_t &ff)  
*Compute the norm of the vector  $\vec{v}$  defined by  $v_i = d_i f f_i$ .*
- template<class vec2\_t >  
double [compute\\_delta](#) (size\_t n, [ovector\\_base](#) &diag2, vec2\_t &x2)  
*Compute delta.*
- template<class vec2\_t >  
double [enorm](#) (size\_t N, const vec2\_t &ff)  
*Compute the Euclidean norm of  $ff$ .*
- double [enorm\\_sum](#) (size\_t n, const [ovector\\_base](#) &a, const [ovector\\_base](#) &b)  
*Compute the Euclidean norm of the sum of  $a$  and  $b$ .*
- template<class vec2\_t >  
int [compute\\_trial\\_step](#) (size\_t N, vec2\_t &x1, vec2\_t &dx1, vec2\_t &xx\_trial)  
*Compute a trial step and put the result in  $xx\_trial$ .*
- template<class vec2\_t >  
int [compute\\_df](#) (size\_t n, const vec2\_t &ff\_trial, const vec2\_t &fl, [ovector\\_base](#) &dfl)  
*Compute the change in the function value.*
- template<class mat2\_t >  
void [compute\\_diag](#) (size\_t n, const mat2\_t &J2, [ovector\\_base](#) &diag2)  
*Compute  $diag$ , the norm of the columns of the Jacobian.*
- template<class vec2\_t, class vec3\_t, class vec4\_t >  
void [compute\\_qtf](#) (size\_t N, const vec2\_t &q2, const vec3\_t &f2, vec4\_t &qtf2)  
*Compute  $Q^T f$ .*
- template<class mat2\_t >  
void [update\\_diag](#) (size\_t n, const mat2\_t &J2, [ovector\\_base](#) &diag2)  
*Update  $diag$ .*
- template<class vec2\_t >  
void [scaled\\_addition](#) (size\_t N, double alpha, [ovector\\_base](#) &newton2, double beta, [ovector\\_base](#) &gradient2, vec2\_t &pp)  
*Form appropriate convex combination of the Gauss-Newton direction and the scaled gradient direction.*
- int [newton\\_direction](#) (const size\_t N, const [omatrix\\_base](#) &r2, const [ovector\\_base](#) &qtf2, [ovector\\_base](#) &p)  
*Compute the Gauss-Newton direction.*
- void [gradient\\_direction](#) (const size\_t M, const size\_t N, const [omatrix\\_base](#) &r2, const [ovector\\_base](#) &qtf2, const [ovector\\_base](#) &diag2, [ovector\\_base](#) &g)  
*Compute the gradient direction.*
- void [minimum\\_step](#) (const size\_t N, double gnorm, const [ovector\\_base](#) &diag2, [ovector\\_base](#) &g)  
*Compute the point at which the gradient is minimized.*
- template<class vec2\_t >  
int [dogleg](#) (size\_t n, const [omatrix\\_base](#) &r2, const [ovector\\_base](#) &qtf2, const [ovector\\_base](#) &diag2, double delta2, [ovector\\_base](#) &newton2, [ovector\\_base](#) &gradient2, vec2\_t &p)

*Take a dogleg step.*

#### 46.166.2 Member Function Documentation

46.166.2.1 `template<class vec2_t> double hybrids_base::enorm ( size_t N, const vec2_t & ff )` `[inline]`

**Idea for Future** Replace this with `dnrm2` from `cblas_base.h`

Definition at line 162 of file `gsl_mroot_hybrids.h`.

46.166.2.2 `template<class vec2_t> int hybrids_base::compute_trial_step ( size_t N, vec2_t & xl, vec2_t & dxl, vec2_t & xx_trial )` `[inline]`

**Idea for Future** Replace with `daxpy`.

Definition at line 187 of file `gsl_mroot_hybrids.h`.

46.166.2.3 `template<class vec2_t> int hybrids_base::compute_df ( size_t n, const vec2_t & ff_trial, const vec2_t & fl, ovector_base & dfl )` `[inline]`

**Idea for Future** Replace with `daxpy`?

Definition at line 200 of file `gsl_mroot_hybrids.h`.

46.166.2.4 `template<class vec2_t, class vec3_t, class vec4_t> void hybrids_base::compute_qtf ( size_t N, const vec2_t & q2, const vec3_t & f2, vec4_t & qtf2 )` `[inline]`

**Idea for Future** This is just right-multiplication, so we could use the `O2scl` `cblas` routines instead.

Definition at line 233 of file `gsl_mroot_hybrids.h`.

46.166.2.5 `template<class vec2_t> void hybrids_base::scaled_addition ( size_t N, double alpha, ovector_base & newton2, double beta, ovector_base & gradient2, vec2_t & pp )` `[inline]`

Using the Gauss-Newton direction given in `newton` (a vector of size `N`), and the gradient direction in `gradient` (also a vector of size `N`), this computes

$$pp = \alpha newton + \beta gradient$$

Definition at line 279 of file `gsl_mroot_hybrids.h`.

46.166.2.6 `template<class vec2_t> int hybrids_base::dogleg ( size_t n, const omatrix_base & r2, const ovector_base & qtf2, const ovector_base & diag2, double delta2, ovector_base & newton2, ovector_base & gradient2, vec2_t & p )` `[inline]`

Given the QR decomposition of an `n` by `n` matrix "A", a diagonal matrix `diag`, a vector `b`, and a positive number `delta`, this function determines the convex combination `x` of the Gauss-Newton and scaled gradient directions which minimizes  $Ax - b$  in the least squares sense, subject to the restriction that the Euclidean norm of  $dx$  is smaller than the value of `delta`.

Definition at line 344 of file `gsl_mroot_hybrids.h`.

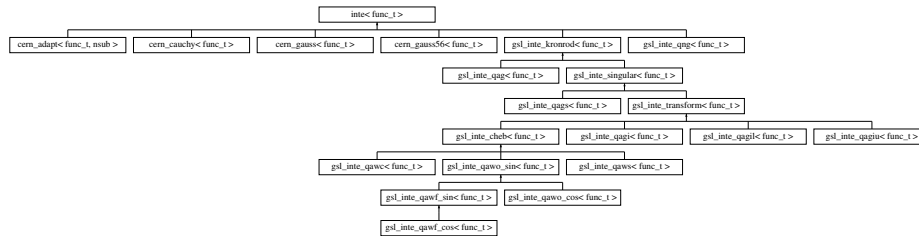
The documentation for this class was generated from the following file:

- `gsl_mroot_hybrids.h`

#### 46.167 `inte< func_t >` Class Template Reference

Base integration class [abstract base].

Inheritance diagram for `inte< func_t >`:



```
template<class func_t = funct>class inte< func_t >
```

Definition at line 41 of file inte.h.

- virtual double **integ** (func\_t &func, double a, double b)  
*Integrate function `func` from `a` to `b`.*
- virtual int **integ\_err** (func\_t &func, double a, double b, double &res, double &err)=0  
*Integrate function `func` from `a` to `b` and place the result in `res` and the error in `err`.*
- double **get\_error** ()  
*Return the numerically estimated error in the result from the last call to `integ()`*
- virtual const char \* **type** ()  
*Return string denoting type ("`inte`")*

- int `verbose`  
*Verbosity.*
- size\_t `last_iter`  
*The most recent number of iterations taken.*
- double `tol_rel`  
*The maximum relative uncertainty in the value of the integral (default  $10^{-8}$ )*
- double `tol_abs`  
*The maximum absolute uncertainty in the value of the integral (default  $10^{-8}$ )*
- bool `err_nonconv`  
*If true, call the error handler if the routine does not converge or reach the desired tolerance (default true)*
- int `last_conv`  
*Integer indicating convergence properties of the last call to `integ()` or `integ_errf()`.*

- double **interror**  
*The uncertainty for the last integration computation.*

## 46.167.2 Member Function Documentation

46.167.2.1 `template<class func_t = func_t> double inte< func_t >::get_error ( ) [inline]`

This will quietly return zero if no integrations have been performed or if the integrator does not estimate the error.

Definition at line 111 of file `inte.h`.

## 46.167.3 Field Documentation

46.167.3.1 `template<class func_t = func_t> bool inte< func_t >::err_nonconv`

If this is false, the function proceeds normally and may provide convergence information in [last\\_conv](#).

Definition at line 79 of file `inte.h`.

46.167.3.2 `template<class func_t = func_t> int inte< func_t >::last_conv`

This is zero if the last call to [integ\(\)](#) or [integ\\_err\(\)](#) converged successfully. This variable is particularly useful, in combination with setting [err\\_nonconv](#) to false, to test for non-convergence without calling the error handler.

Definition at line 89 of file `inte.h`.

The documentation for this class was generated from the following file:

- `inte.h`

46.168 `iterate_parms` Struct Reference

A structure to pass information to and from [iterate\\_func\(\)](#)

```
#include <hdf_io.h>
```

## 46.168.1 Detailed Description

Definition at line 103 of file `hdf_io.h`.

## Data Fields

- [hdf\\_file](#) \* **hf**
- `std::string` **type**
- `std::string` **group\_name**
- `bool` **found**
- `int` **verbose**

The documentation for this struct was generated from the following file:

- [hdf\\_io.h](#)

46.169 `ovector_const_view_tlate< data_t, vparent_t, block_t >::iterator` Class Reference

An iterator for ovector.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_const_view_tlate< data_t, vparent_t, block_t >::iterator`:



### Note

## Experimental.

Definition at line 223 of file ovector\_tlate.h.

## Public Member Functions

- `iterator` (const `const_iterator` &cit)  
*Copy constructor.*
- `const data_t operator* () const`  
*Dereference - return the corresponding vector element.*
- `data_t operator* ()`  
*Dereference - return the corresponding vector element.*

## Protected Member Functions

- **iterator** (data\_t \*p, size\_t s)  
*Internally create an iterator directly from a pointer.*

## Friends

- class `ovector_const_view_tlate< data_t, vparent_t, block_t >`  
Grant access to `ovector` classes for `begin()` and `end()` functions.
- class `ovector_base_tlate< data_t, vparent_t, block_t >`  
Grant access to `ovector` classes for `begin()` and `end()` functions.

The documentation for this class was generated from the following file:

- `ovector tlate.h`

### 46.170 jac\_funct< vec\_t, mat\_t > Class Template Reference

Base for a square Jacobian where J is computed at x given  $y=f(x)$  [abstract base].

```
#include <jacobian.h>
```

Inheritance diagram for jac\_funct< vec\_t, mat\_t >:





## 46.170.1 Detailed Description

```
template<class vec_t = ovector_base, class mat_t = omatrix_base>class jac_func_t< vec_t, mat_t >
```

Compute

$$J_{ij} = \frac{\partial f_i}{\partial x_j}$$

The `vec_t` objects in `operator()` could have been written to be `const`, but they are not `const` so that they can be used as temporary workspace. They are typically restored to their original values before `operator()` exits. The Jacobian is stored in the order  $J[i][j]$ , i.e. the rows have index  $i$  and the columns with index  $j$ .

Definition at line 52 of file `jacobian.h`.

## Public Member Functions

- virtual int `operator()` (size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j)=0  
*The operator()*

The documentation for this class was generated from the following file:

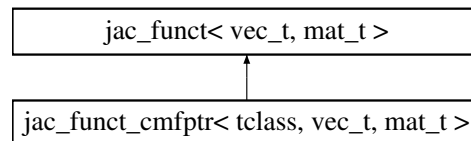
- `jacobian.h`

46.171 `jac_func_t_cmfp`< `tclass`, `vec_t`, `mat_t` > Class Template Reference

Const member function pointer to a Jacobian.

```
#include <jacobian.h>
```

Inheritance diagram for `jac_func_t_cmfp`< `tclass`, `vec_t`, `mat_t` >:



## 46.171.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base, class mat_t = omatrix_base>class jac_func_t_cmfp< tclass, vec_t, mat_t >
```

Definition at line 166 of file `jacobian.h`.

## Public Member Functions

- `jac_func_t_cmfp` (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j) const)  
*Specify the member function pointer.*
- virtual int `operator()` (size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j)  
*The operator()*

## Protected Attributes

- `int(tclass::* fptr)(size_t nv, vec_t &x, vec_t &y, mat_t &j) const`  
*Member function pointer.*
- `tclass * tptr`  
*Class pointer.*

The documentation for this class was generated from the following file:

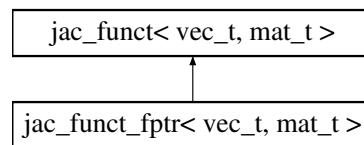
- `jacobian.h`

46.172 `jac_funct_fptr< vec_t, mat_t >` Class Template Reference

Function pointer to jacobian.

```
#include <jacobian.h>
```

Inheritance diagram for `jac_funct_fptr< vec_t, mat_t >`:



## 46.172.1 Detailed Description

```
template<class vec_t = ovector_base, class mat_t = omatrix_base>class jac_funct_fptr< vec_t, mat_t >
```

Definition at line 78 of file `jacobian.h`.

## Public Member Functions

- `jac_funct_fptr(int(*fp)(size_t nv, vec_t &x, vec_t &y, mat_t &j))`  
*Specify the function pointer.*
- `virtual int operator()(size_t nv, vec_t &x, vec_t &y, mat_t &j)`  
*The operator()*

The documentation for this class was generated from the following file:

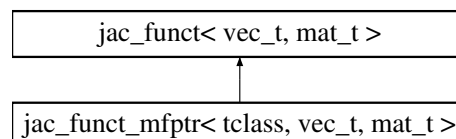
- `jacobian.h`

46.173 `jac_funct_mfptr< tclass, vec_t, mat_t >` Class Template Reference

Member function pointer to a Jacobian.

```
#include <jacobian.h>
```

Inheritance diagram for `jac_funct_mfptr< tclass, vec_t, mat_t >`:



## 46.173.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base, class mat_t = omatrix_base>class jac_funct_mfptr< tclass, vec_t, mat_t >
```

Definition at line 118 of file jacobian.h.

## Public Member Functions

- [jac\\_funct\\_mfptr](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j))  
*Specify the member function pointer.*
- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j)  
*The operator()*

## Protected Attributes

- int(tclass::\* [fptr](#) )(size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j)  
*Member function pointer.*
- tclass \* [tptr](#)  
*Class pointer.*

The documentation for this class was generated from the following file:

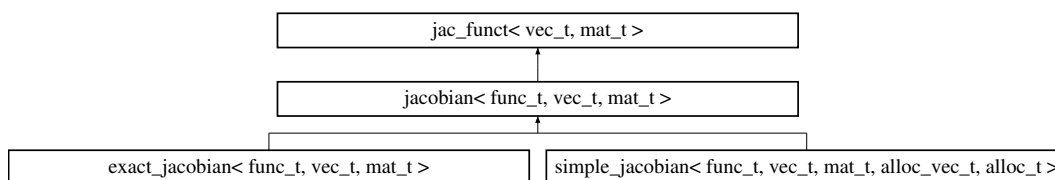
- jacobian.h

## 46.174 jacobian&lt; func\_t, vec\_t, mat\_t &gt; Class Template Reference

Base for providing a numerical jacobian [abstract base].

```
#include <jacobian.h>
```

Inheritance diagram for jacobian< func\_t, vec\_t, mat\_t >:



## 46.174.1 Detailed Description

```
template<class func_t = mm_funct<>, class vec_t = ovector_base, class mat_t = omatrix_base>class jacobian< func_t, vec_t, mat_t >
```

This provides a Jacobian which is numerically determined by differentiating a user-specified function (typically of the form of [mm\\_funct](#)).

Definition at line 218 of file jacobian.h.

## Public Member Functions

- virtual int [set\\_function](#) (func\_t &f)  
*Set the function to compute the Jacobian of.*
- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &y, mat\_t &j)=0  
*Evaluate the Jacobian  $j$  at point  $y(x)$*

## Protected Attributes

- `func_t * func`  
*A pointer to the user-specified function.*

## Private Member Functions

- `jacobian` (const `jacobian` &)
- `jacobian & operator=` (const `jacobian` &)

The documentation for this class was generated from the following file:

- `jacobian.h`

## 46.175 lanczos&lt; vec\_t, mat\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Lanczos diagonalization.

```
#include <lanczos_base.h>
```

## 46.175.1 Detailed Description

```
template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base, class alloc_vec_t = o2scl::ovector, class alloc_t = o2scl::ovector_-
alloc>class lanczos< vec_t, mat_t, alloc_vec_t, alloc_t >
```

This class approximates the largest eigenvalues of a symmetric matrix.

The vector and matrix types can be any type which provides access via `operator[]` or `operator()`, given a suitable vector allocation type. See [Vector types for template classes](#) in the User's guide for more details.

The tridiagonalization routine was rewritten from the EISPACK routines `imtql1.f` (but uses `gsl_hypot()` instead of `pythag.f`).

**Idea for Future** The function `eigen_tdiag()` automatically sorts the eigenvalues, which may not be necessary.

**Idea for Future** Do something better than the naive matrix-vector product. For example, use `dgemm()` and allow user to specify column or row-major.

**Idea for Future** Rework memory allocation to perform as needed.

Definition at line 54 of file `lanczos_base.h`.

## Public Member Functions

- int `eigenvalues` (size\_t size, mat\_t &mat, size\_t n\_iter, vec\_t &eigen, vec\_t &diag, vec\_t &off\_diag)  
*Approximate the largest eigenvalues of a symmetric matrix mat using the Lanczos method.*
- int `eigen_tdiag` (size\_t n, vec\_t &diag, vec\_t &off\_diag)  
*In-place diagonalization of a tridiagonal matrix.*

## Data Fields

- size\_t `td_iter`  
*Number of iterations for finding the eigenvalues of the tridiagonal matrix (default 30)*
- size\_t `td_lasteval`  
*The index for the last eigenvalue not determined if tridiagonalization fails.*

## Protected Member Functions

- void [product](#) (size\_t n, mat\_t &a, vec\_t &w, vec\_t &prod)  
*Naive matrix-vector product.*

## 46.175.2 Member Function Documentation

46.175.2.1 `template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base, class alloc_vec_t = o2scl::ovector, class alloc_t = o2scl::ovector_alloc> int lanczos< vec_t, mat_t, alloc_vec_t, alloc_t >::eigenvalues ( size_t size, mat_t & mat, size_t n_iter, vec_t & eigen, vec_t & diag, vec_t & off_diag ) [inline]`

Given a square matrix `mat` with size `size`, this function applies `n_iter` iterations of the Lanczos algorithm to produce `n_iter` approximate eigenvalues stored in `eigen`. As a by-product, this function also partially tridiagonalizes the matrix placing the result in `diag` and `off_diag`. Before calling this function, space must have already been allocated for `eigen`, `diag`, and `off_diag`. All three of these arrays must have at least enough space for `n_iter` elements.

Choosing `c n_iter = size` will produce all of the exact eigenvalues and the corresponding tridiagonal matrix, but this may be slower than diagonalizing the matrix directly.

Definition at line 90 of file `lanczos_base.h`.

46.175.2.2 `template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base, class alloc_vec_t = o2scl::ovector, class alloc_t = o2scl::ovector_alloc> int lanczos< vec_t, mat_t, alloc_vec_t, alloc_t >::eigen_tdiag ( size_t n, vec_t & diag, vec_t & off_diag ) [inline]`

On input, the vectors `diag` and `off_diag` should both be vectors of size `n`. The diagonal entries stored in `diag`, and the  $n - 1$  off-diagonal entries should be stored in `off_diag`, starting with `off_diag[1]`. The value in `off_diag[0]` is unused. The vector `off_diag` is destroyed by the computation.

This uses an implicit QL method from the EISPACK routine `imtql1`. The value of `ierr` from the original Fortran routine is stored in `td_lasteval`.

Definition at line 174 of file `lanczos_base.h`.

46.175.2.3 `template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base, class alloc_vec_t = o2scl::ovector, class alloc_t = o2scl::ovector_alloc> void lanczos< vec_t, mat_t, alloc_vec_t, alloc_t >::product ( size_t n, mat_t & a, vec_t & w, vec_t & prod ) [inline, protected]`

It is assumed that memory is already allocated for `prod`.

Definition at line 311 of file `lanczos_base.h`.

The documentation for this class was generated from the following file:

- `lanczos_base.h`

## 46.176 lib\_settings\_class Class Reference

A class to manage global library settings.

```
#include <lib_settings.h>
```

## 46.176.1 Detailed Description

A global object of this type is defined in `lib_settings.h` named `lib_settings`.

Definition at line 91 of file `lib_settings.h`.

### Public Member Functions

- `std::string get_data_dir ()`  
*Return the data directory.*
- `int set_data_dir (std::string dir)`  
*Set the data directory.*
- `std::string get_tmp_dir ()`  
*Return the temp file directory.*
- `int set_tmp_dir (std::string dir)`  
*Set the temp file directory.*
- `bool eos_installed ()`  
*Return true if the EOS library was installed.*
- `bool part_installed ()`  
*Return true if the particle library was installed.*
- `bool hdf_support ()`  
*Return true if O<sub>2</sub>scl was installed with HDF support.*
- `bool range_check ()`  
*Return true if range checking was turned on during installation (default true)*
- `std::string o2scl_version ()`  
*Return the library version.*

### Protected Attributes

- `std::string data_dir`  
*The present data directory.*
- `std::string tmp_dir`  
*The present temp file directory.*

The documentation for this class was generated from the following file:

- [lib\\_settings.h](#)

## 46.177 pinside::line Struct Reference

Internal line definition for [pinside](#).

```
#include <pinside.h>
```

### 46.177.1 Detailed Description

Definition at line 77 of file `pinside.h`.

### Data Fields

- `point p1`
- `point p2`

The documentation for this struct was generated from the following file:

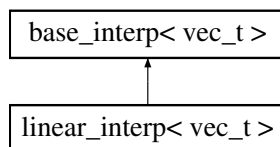
- `pinside.h`
-

46.178 `linear_interp< vec_t >` Class Template Reference

Linear interpolation (GSL)

```
#include <interp.h>
```

Inheritance diagram for `linear_interp< vec_t >`:



## 46.178.1 Detailed Description

```
template<class vec_t>class linear_interp< vec_t >
```

Linear interpolation requires no calls to `allocate()` or `free()` as there is no internal storage required.

Definition at line 159 of file `interp.h`.

## Public Member Functions

- virtual int `init` (const `vec_t` &x, const `vec_t` &y, size\_t size)  
*Initialize interpolation routine.*
- virtual int `interp` (const `vec_t` &x\_array, const `vec_t` &y\_array, size\_t size, double x, double &y)  
*Give the value of the function  $y(x = x_0)$ .*
- virtual int `deriv` (const `vec_t` &x\_array, const `vec_t` &y\_array, size\_t size, double x, double &dydx)  
*Give the value of the derivative  $y'(x = x_0)$ .*
- virtual int `deriv2` (const `vec_t` &x, const `vec_t` &y, size\_t size, double x0, double &d2ydx2)  
*Give the value of the second derivative  $y''(x = x_0)$  (always zero)*
- virtual int `integ` (const `vec_t` &x\_array, const `vec_t` &y\_array, size\_t size, double a, double b, double &result)  
*Give the value of the integral  $\int_a^b y(x) dx$ .*
- virtual const char \* `type` ()  
*Return the type, "linear\_interp".*

## Private Member Functions

- `linear_interp` (const `linear_interp< vec_t >` &)
- `linear_interp< vec_t >` & `operator=` (const `linear_interp< vec_t >` &)

The documentation for this class was generated from the following file:

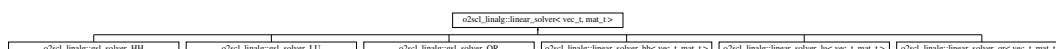
- `interp.h`

46.179 `o2scl::linalg::linear_solver< vec_t, mat_t >` Class Template Reference

A generic solver for the linear system  $Ax = b$  [abstract base].

```
#include <linear_solver.h>
```

Inheritance diagram for `o2scl::linalg::linear_solver< vec_t, mat_t >`:



## 46.179.1 Detailed Description

```
template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base>class o2scl_linalg::linear_solver< vec_t, mat_t >
```

A generic solver for dense linear systems.

Those writing production level code should consider calling LAPACK directly using O<sub>2</sub>scl objects as described in the [Linear Algebra](#) section of the User's Guide.

**Idea for Future** The test code uses a Hilbert matrix, which is known to be ill-conditioned, especially for the larger sizes. This should probably be changed.

Definition at line 52 of file linear\_solver.h.

## Public Member Functions

- virtual int [solve](#) (size\_t n, mat\_t &a, vec\_t &b, vec\_t &x)=0  
*Solve square linear system  $Ax = b$  of size  $n$ .*

The documentation for this class was generated from the following file:

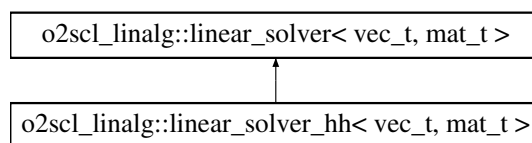
- linear\_solver.h

## 46.180 o2scl\_linalg::linear\_solver\_hh&lt; vec\_t, mat\_t &gt; Class Template Reference

Generic Householder linear solver.

```
#include <linear_solver.h>
```

Inheritance diagram for o2scl\_linalg::linear\_solver\_hh< vec\_t, mat\_t >:



## 46.180.1 Detailed Description

```
template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base>class o2scl_linalg::linear_solver_hh< vec_t, mat_t >
```

Definition at line 102 of file linear\_solver.h.

## Public Member Functions

- virtual int [solve](#) (size\_t n, mat\_t &A, vec\_t &b, vec\_t &x)  
*Solve square linear system  $Ax = b$  of size  $n$ .*

The documentation for this class was generated from the following file:

- linear\_solver.h

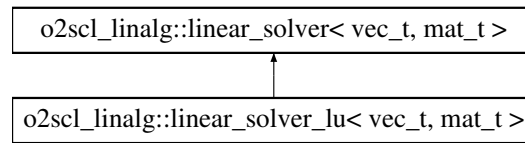


## 46.181 o2scl\_linalg::linear\_solver\_lu< vec\_t, mat\_t > Class Template Reference

Generic linear solver using LU decomposition.

```
#include <linear_solver.h>
```

Inheritance diagram for o2scl\_linalg::linear\_solver\_lu< vec\_t, mat\_t >:



### 46.181.1 Detailed Description

```
template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base>class o2scl_linalg::linear_solver_lu< vec_t, mat_t >
```

Definition at line 64 of file linear\_solver.h.

#### Public Member Functions

- virtual int [solve](#) (size\_t n, mat\_t &A, vec\_t &b, vec\_t &x)  
*Solve square linear system  $Ax = b$  of size  $n$ .*

The documentation for this class was generated from the following file:

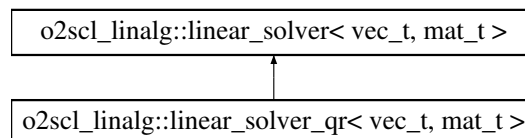
- linear\_solver.h

## 46.182 o2scl\_linalg::linear\_solver\_qr< vec\_t, mat\_t > Class Template Reference

Generic linear solver using QR decomposition.

```
#include <linear_solver.h>
```

Inheritance diagram for o2scl\_linalg::linear\_solver\_qr< vec\_t, mat\_t >:



### 46.182.1 Detailed Description

```
template<class vec_t = o2scl::ovector_base, class mat_t = o2scl::omatrix_base>class o2scl_linalg::linear_solver_qr< vec_t, mat_t >
```

Definition at line 84 of file linear\_solver.h.

#### Public Member Functions

- virtual int [solve](#) (size\_t n, mat\_t &A, vec\_t &b, vec\_t &x)

*Solve square linear system  $Ax = b$  of size  $n$ .*

The documentation for this class was generated from the following file:

- `linear_solver.h`

## 46.183 `matrix_row< mat_t >` Class Template Reference

Create a vector-like class from a row of a matrix.

```
#include <vector.h>
```

### 46.183.1 Detailed Description

```
template<class mat_t>class matrix_row< mat_t >
```

**Idea for Future** Generalize to `operator(.)`

Definition at line 769 of file `vector.h`.

#### Public Member Functions

- `matrix_row` (`mat_t &m`, `size_t r`)  
*Create an object which represents row  $r$  of matrix  $m$ .*
- `double & operator[]` (`size_t c`)  
*Access element of column  $c$  from the specified row.*
- `const double & operator[]` (`size_t c`) `const`  
*Access element of column  $c$  from the specified row.*

#### Protected Attributes

- `size_t r2`  
*The row index.*
- `mat_t * m2`  
*The pointer to the matrix.*

The documentation for this class was generated from the following file:

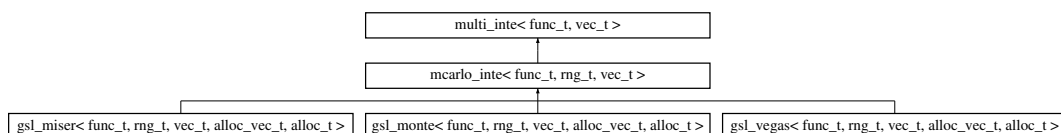
- `vector.h`

## 46.184 `mcarlo_inte< func_t, rng_t, vec_t >` Class Template Reference

Monte-Carlo integration [abstract base].

```
#include <mcarlo_inte.h>
```

Inheritance diagram for `mcarlo_inte< func_t, rng_t, vec_t >`:



## 46.184.1 Detailed Description

```
template<class func_t, class rng_t = gsl_rnga, class vec_t = ovector_base>class mcarlo_inte< func_t, rng_t, vec_t >
```

This class provides the generic Monte Carlo parameters and the random number generator. The default type for the random number generator is a [gsl\\_rnga](#) object.

Definition at line 42 of file mcarlo\_inte.h.

## Public Member Functions

- virtual const char \* [type](#) ()  
Return string denoting type ("mcarlo\_inte")

## Data Fields

- unsigned long [n\\_points](#)  
Number of integration points (default 1000)
- rng\_t [def\\_rng](#)  
The random number generator.

The documentation for this class was generated from the following file:

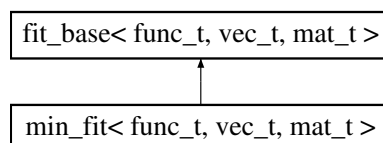
- mcarlo\_inte.h

## 46.185 min\_fit&lt; func\_t, vec\_t, mat\_t &gt; Class Template Reference

Non-linear least-squares fitting class with generic minimizer.

```
#include <min_fit.h>
```

Inheritance diagram for min\_fit< func\_t, vec\_t, mat\_t >:



## 46.185.1 Detailed Description

```
template<class func_t = fit_funct<>, class vec_t = ovector_base, class mat_t = omatrix_base>class min_fit< func_t, vec_t, mat_t >
```

This minimizes a generic fitting function using any [multi\\_min](#) object, and then uses the GSL routines to calculate the uncertainties in the parameters and the covariance matrix.

This can be useful for fitting problems which might be better handled by more complex minimizers than those that are used in [gsl\\_fit](#). For problems with many local minima near the global minimum, using a [sim\\_anneal](#) object with this class can sometimes produce better results than [gsl\\_fit](#).

Default template arguments

- func\_t - [fit\\_funct<>](#)
- vec\_t - [ovector\\_base](#)

- `alloc_vec_t` - [ovector](#)

Definition at line 57 of file `min_fit.h`.

## Data Structures

- struct [func\\_par](#)  
A structure for passing information to the GSL functions for the [min\\_fit](#) class.

## Public Member Functions

- virtual int [fit](#) (size\_t ndat, vec\_t &xdat, vec\_t &ydat, vec\_t &yerr, size\_t npar, vec\_t &par, mat\_t &covar, double &chi2, func\_t &fitfun)  
*Fit the data specified in (xdat,ydat) to the function `fitfun` with the parameters in `par`.*
- int [set\\_multi\\_min](#) ([multi\\_min](#)< [multi\\_func](#)< vec\_t > > &mm)  
*Set the [multi\\_min](#) object to use (default is `gsl_mmin_nmsimplex`)*
- virtual const char \* [type](#) ()  
*Return string denoting type ("min\_fit")*

## Data Fields

- [gsl\\_mmin\\_simp](#)< [multi\\_func](#) < vec\_t > > [def\\_multi\\_min](#)  
*The default minimizer.*

## Protected Member Functions

- double [min\\_func](#) (size\_t np, const vec\_t &xp, [func\\_par](#) \*&fp)  
*The function to minimize.*

## Static Protected Member Functions

- static int [func](#) (const [gsl\\_vector](#) \*x, void \*pa, [gsl\\_vector](#) \*f)  
*Evaluate the function.*
- static int [dfunc](#) (const [gsl\\_vector](#) \*x, void \*pa, [gsl\\_matrix](#) \*jac)  
*Evaluate the jacobian.*
- static int [fdfunc](#) (const [gsl\\_vector](#) \*x, void \*pa, [gsl\\_vector](#) \*f, [gsl\\_matrix](#) \*jac)  
*Evaluate the function and the jacobian.*

## Protected Attributes

- [multi\\_min](#)< [multi\\_func](#)< vec\_t > > \* [mmp](#)  
*The minimizer.*
- bool [min\\_set](#)  
*True if the minimizer has been set by the user.*

## 46.185.2 Member Function Documentation

46.185.2.1 `template<class func_t = fit_func<>, class vec_t = ovector_base, class mat_t = omatrix_base> virtual int min_fit< func_t, vec_t, mat_t >::fit ( size_t ndat, vec_t & xdat, vec_t & ydat, vec_t & yerr, size_t npar, vec_t & par, mat_t & covar, double & chi2, func_t & fitfun )`  
[inline, virtual]

The covariance matrix for the parameters is returned in `covar` and the value of  $\chi^2$  is returned in `chi2`.

Implements [fit\\_base< func\\_t, vec\\_t, mat\\_t >](#).

Definition at line 96 of file min\_fit.h.

The documentation for this class was generated from the following file:

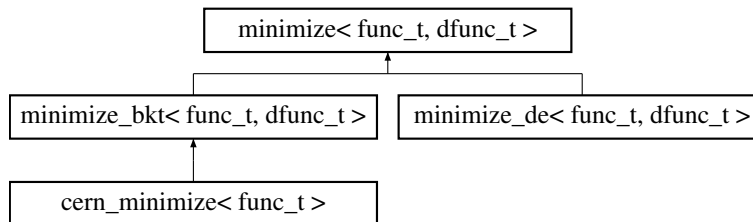
- min\_fit.h

## 46.186 minimize< func\_t, dfunc\_t > Class Template Reference

One-dimensional minimization [abstract base].

```
#include <minimize.h>
```

Inheritance diagram for minimize< func\_t, dfunc\_t >:



### 46.186.1 Detailed Description

```
template<class func_t = func_t, class dfunc_t = func_t>class minimize< func_t, dfunc_t >
```

**Idea for Future** Add a class for the quad\_golden algorithm from GSL.

Definition at line 44 of file minimize.h.

#### Public Member Functions

- virtual int [print\\_iter](#) (double x, double y, int iter, double value=0.0, double limit=0.0, std::string comment="")  
*Print out iteration information.*
- virtual int [min](#) (double &x, double &fmin, func\_t &func)=0  
*Calculate the minimum min of func w.r.t 'x'.*
- virtual int [min\\_bkt](#) (double &x2, double x1, double x3, double &fmin, func\_t &func)=0  
*Calculate the minimum min of func with x2 bracketed between x1 and x3.*
- virtual int [min\\_de](#) (double &x, double &fmin, func\_t &func, dfunc\_t &df)=0  
*Calculate the minimum min of func with derivative dfunc w.r.t 'x'.*
- virtual int [bracket](#) (double &ax, double &bx, double &cx, double &fa, double &fb, double &fc, func\_t &func)  
*Given interval (ax, bx), attempt to bracket a minimum for function func.*
- virtual const char \* [type](#) ()  
*Return string denoting type ("minimize")*

#### Data Fields

- int [verbose](#)  
*Output control.*
- int [ntrial](#)  
*Maximum number of iterations.*
- double [tol\\_rel](#)  
*The tolerance for the minimum function value.*

- double [tol\\_abs](#)  
*The tolerance for the location of the minimum.*
- int [last\\_ntrial](#)  
*The number of iterations for in the most recent minimization.*
- int [bracket\\_iter](#)  
*The number of iterations for automatically bracketing a minimum (default 20)*
- bool [err\\_nonconv](#)  
*If true, call the error handler if the routine does not "converge".*
- int [last\\_conv](#)  
*Zero if last call to [min\(\)](#), [min\\_bkt\(\)](#), or [min\\_de\(\)](#) converged.*

## 46.186.2 Member Function Documentation

46.186.2.1 `template<class func_t = funct, class dfunc_t = func_t> virtual int minimize< func_t, dfunc_t >::print_iter ( double x, double y, int iter, double value = 0.0, double limit = 0.0, std::string comment = " " ) [inline, virtual]`

Depending on the value of the variable [verbose](#), this prints out the iteration information. If `verbose=0`, then no information is printed, while if `verbose>1`, then after each iteration, the present values of `x` and `y` are output to `std::cout` along with the iteration number. If `verbose>=2` then each iteration waits for a character.

Definition at line 102 of file `minimize.h`.

46.186.2.2 `template<class func_t = funct, class dfunc_t = func_t> virtual int minimize< func_t, dfunc_t >::min ( double & x, double & fmin, func_t & func ) [pure virtual]`

If this is not overloaded, it attempts to bracket the minimum using [bracket\(\)](#) and then calls [min\\_bkt\(\)](#) with the newly bracketed minimum.

Implemented in [minimize\\_de< func\\_t, dfunc\\_t >](#), [minimize\\_bkt< func\\_t, dfunc\\_t >](#), and [minimize\\_bkt< func\\_t >](#).

46.186.2.3 `template<class func_t = funct, class dfunc_t = func_t> virtual int minimize< func_t, dfunc_t >::min_bkt ( double & x2, double x1, double x3, double & fmin, func_t & func ) [pure virtual]`

If this is not overloaded, it ignores the bracket and calls [min\(\)](#).

Implemented in [gsl\\_min\\_quad\\_golden< func\\_t >](#), [minimize\\_de< func\\_t, dfunc\\_t >](#), [gsl\\_min\\_brent< func\\_t >](#), [minimize\\_bkt< func\\_t, dfunc\\_t >](#), [minimize\\_bkt< func\\_t >](#), and [cern\\_minimize< func\\_t >](#).

46.186.2.4 `template<class func_t = funct, class dfunc_t = func_t> virtual int minimize< func_t, dfunc_t >::min_de ( double & x, double & fmin, func_t & func, dfunc_t & df ) [pure virtual]`

If this is not overloaded, it attempts to bracket the minimum using [bracket\(\)](#) and then calls [min\\_bkt\\_de\(\)](#) with the newly bracketed minimum.

Implemented in [minimize\\_de< func\\_t, dfunc\\_t >](#), [minimize\\_bkt< func\\_t, dfunc\\_t >](#), and [minimize\\_bkt< func\\_t >](#).

46.186.2.5 `template<class func_t = funct, class dfunc_t = func_t> virtual int minimize< func_t, dfunc_t >::bracket ( double & ax, double & bx, double & cx, double & fa, double & fb, double & fc, func_t & func ) [inline, virtual]`

Upon success, `fa=func(ax)`, `fb=func(bx)`, and `fc=func(cx)` with `fb<fa`, `fb<fc` and `ax<bx<cx`. The initial values of `cx`, `fa`, `fb`, and `fc` are all ignored.

The number of iterations is controlled by [bracket\\_iter](#).

### Note

This algorithm can fail if there's a minimum which has a much smaller size than  $bx - ax$ , or if the function has the same value at `ax`, `bx`, and the midpoint  $(ax+bx)/2$ .

**Idea for Future** Improve this algorithm with the golden ratio method in `gsl/min/bracketing.c?`

Definition at line 169 of file minimize.h.

#### 46.186.3 Field Documentation

46.186.3.1 `template<class func_t = func_t, class dfunc_t = func_t> int minimize< func_t, dfunc_t >::last_conv`

This is particularly useful if `err_nonconv` is false to test if the last call to `min()`, `min_bkt()`, or `min_de()` converged.

Definition at line 91 of file minimize.h.

The documentation for this class was generated from the following file:

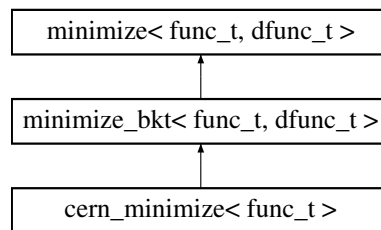
- [minimize.h](#)

### 46.187 minimize\_bkt< func\_t, dfunc\_t > Class Template Reference

One-dimensional bracketing minimization [abstract base].

```
#include <minimize.h>
```

Inheritance diagram for `minimize_bkt< func_t, dfunc_t >`:



#### 46.187.1 Detailed Description

```
template<class func_t, class dfunc_t = func_t>class minimize_bkt< func_t, dfunc_t >
```

Definition at line 241 of file minimize.h.

#### Public Member Functions

- virtual int [min](#) (double &x, double &fmin, func\_t &func)  
*Calculate the minimum min of func w.r.t 'x'.*
- virtual int [min\\_bkt](#) (double &x2, double x1, double x3, double &fmin, func\_t &func)=0  
*Calculate the minimum min of func with x2 bracketed between x1 and x3.*
- virtual int [min\\_de](#) (double &x, double &fmin, func\_t &func, dfunc\_t &df)  
*Calculate the minimum min of func with derivative dfunc w.r.t 'x'.*
- virtual const char \* [type](#) ()  
*Return string denoting type ("minimize\_bkt")*

#### Data Fields

- int [bracket\\_iter](#)  
*The number of iterations for automatically bracketing a minimum (default 20)*

## 46.187.2 Member Function Documentation

46.187.2.1 `template<class func_t, class dfunc_t = func_t> virtual int minimize_bkt< func_t, dfunc_t >::min ( double & x, double & fmin, func_t & func ) [inline, virtual]`

If this is not overloaded, it attempts to bracket the minimum using [bracket\(\)](#) and then calls [min\\_bkt\(\)](#) with the newly bracketed minimum.

Implements [minimize< func\\_t, dfunc\\_t >](#).

Definition at line 262 of file minimize.h.

46.187.2.2 `template<class func_t, class dfunc_t = func_t> virtual int minimize_bkt< func_t, dfunc_t >::min_bkt ( double & x2, double x1, double x3, double & fmin, func_t & func ) [pure virtual]`

If this is not overloaded, it ignores the bracket and calls [min\(\)](#).

Implements [minimize< func\\_t, dfunc\\_t >](#).

Implemented in [gsl\\_min\\_quad\\_golden< func\\_t >](#), [gsl\\_min\\_brent< func\\_t >](#), and [cern\\_minimize< func\\_t >](#).

46.187.2.3 `template<class func_t, class dfunc_t = func_t> virtual int minimize_bkt< func_t, dfunc_t >::min_de ( double & x, double & fmin, func_t & func, dfunc_t & df ) [inline, virtual]`

If this is not overloaded, it attempts to bracket the minimum using [bracket\(\)](#) and then calls [min\\_bkt\\_de\(\)](#) with the newly bracketed minimum.

Implements [minimize< func\\_t, dfunc\\_t >](#).

Definition at line 288 of file minimize.h.

The documentation for this class was generated from the following file:

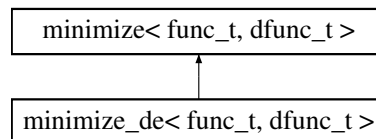
- [minimize.h](#)

## 46.188 minimize\_de&lt; func\_t, dfunc\_t &gt; Class Template Reference

One-dimensional minimization using derivatives [abstract base].

```
#include <minimize.h>
```

Inheritance diagram for minimize\_de< func\_t, dfunc\_t >:



## 46.188.1 Detailed Description

```
template<class func_t, class dfunc_t = func_t>class minimize_de< func_t, dfunc_t >
```

At the moment there are no minimizers of this type implemented in O<sub>2</sub>scl .

**Idea for Future** Create a version of [gsl\\_mmin\\_conf](#) which implements a minimizer with this interface.

Definition at line 314 of file minimize.h.



## Public Member Functions

- virtual int [min](#) (double &x, double &fmin, func\_t &func)=0  
*Calculate the minimum  $\min$  of  $func$  w.r.t 'x'.*
- virtual int [min\\_bkt](#) (double &x2, double x1, double x3, double &fmin, func\_t &func)=0  
*Calculate the minimum  $\min$  of  $func$  with  $x2$  bracketed between  $x1$  and  $x3$ .*
- virtual int [min\\_de](#) (double &x, double &fmin, func\_t &func, dfunc\_t &df)=0  
*Calculate the minimum  $\min$  of  $func$  with derivative  $dfunc$  w.r.t 'x'.*
- virtual const char \* [type](#) ()  
*Return string denoting type ("minimize\_de")*

## 46.188.2 Member Function Documentation

46.188.2.1 `template<class func_t, class dfunc_t = func_t> virtual int minimize_de< func_t, dfunc_t >::min ( double & x, double & fmin, func_t & func ) [pure virtual]`

If this is not overloaded, it attempts to bracket the minimum using [bracket\(\)](#) and then calls [min\\_bkt\(\)](#) with the newly bracketed minimum.

Implements [minimize< func\\_t, dfunc\\_t >](#).

46.188.2.2 `template<class func_t, class dfunc_t = func_t> virtual int minimize_de< func_t, dfunc_t >::min_bkt ( double & x2, double x1, double x3, double & fmin, func_t & func ) [pure virtual]`

If this is not overloaded, it ignores the bracket and calls [min\(\)](#).

Implements [minimize< func\\_t, dfunc\\_t >](#).

46.188.2.3 `template<class func_t, class dfunc_t = func_t> virtual int minimize_de< func_t, dfunc_t >::min_de ( double & x, double & fmin, func_t & func, dfunc_t & df ) [pure virtual]`

If this is not overloaded, it attempts to bracket the minimum using [bracket\(\)](#) and then calls [min\\_bkt\\_de\(\)](#) with the newly bracketed minimum.

Implements [minimize< func\\_t, dfunc\\_t >](#).

The documentation for this class was generated from the following file:

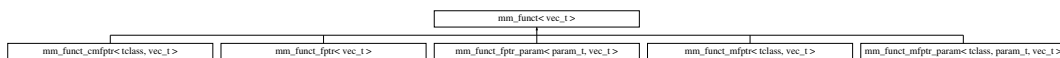
- [minimize.h](#)

## 46.189 mm\_func&lt; vec\_t &gt; Class Template Reference

Array of multi-dimensional functions [abstract base].

```
#include <mm_func.h>
```

Inheritance diagram for mm\_func< vec\_t >:



## 46.189.1 Detailed Description

```
template<class vec_t = ovector_base> class mm_func< vec_t >
```

This class generalizes  $nv$  functions of  $nv$  variables, i.e.  $y_j(x_0, x_1, \dots, x_{nv-1})$  for  $0 \leq j \leq nv - 1$ .

This class is one of a large number of function object classes in O<sub>2</sub>scl designed to provide a mechanism for the user to supply functions to solvers, minimizers, integrators, etc. See [Function Objects](#) for a general description.

Definition at line 44 of file mm\_func\_t.h.

#### Public Member Functions

- virtual int [operator\(\)](#) (size\_t nv, const vec\_t &x, vec\_t &y)=0  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

The documentation for this class was generated from the following file:

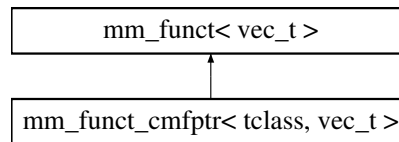
- mm\_func\_t.h

### 46.190 mm\_func\_t\_cmfp< tclass, vec\_t > Class Template Reference

Const member function pointer to an array of multi-dimensional functions.

```
#include <mm_func_t.h>
```

Inheritance diagram for mm\_func\_t\_cmfp< tclass, vec\_t >:



#### 46.190.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class mm_func_t_cmfp< tclass, vec_t >
```

Definition at line 297 of file mm\_func\_t.h.

#### Public Member Functions

- [mm\\_func\\_t\\_cmfp](#) ()  
*Empty constructor.*
- [mm\\_func\\_t\\_cmfp](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, vec\_t &y) const)  
*Specify the member function pointer.*
- int [set\\_function](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, vec\_t &y) const)  
*Specify the member function pointer.*
- virtual int [operator\(\)](#) (size\_t nv, const vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

#### Protected Attributes

- int(tclass::\* [fptr](#)) (size\_t nv, const vec\_t &x, vec\_t &y) const  
*The member function pointer.*
- tclass \* [tpr](#)  
*The class pointer.*

## Private Member Functions

- `mm_func_cmfp` (const `mm_func_cmfp` &)
- `mm_func_cmfp` & `operator=` (const `mm_func_cmfp` &)

The documentation for this class was generated from the following file:

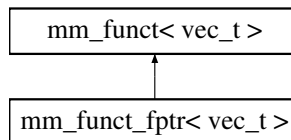
- `mm_func.h`

## 46.191 mm\_func\_ptr&lt; vec\_t &gt; Class Template Reference

Function pointer to array of multi-dimensional functions.

```
#include <mm_func.h>
```

Inheritance diagram for `mm_func_ptr< vec_t >`:



## 46.191.1 Detailed Description

```
template<class vec_t = ovector_base>class mm_func_ptr< vec_t >
```

Definition at line 69 of file `mm_func.h`.

## Public Member Functions

- `mm_func_ptr` (int(\*fp)(size\_t nv, const vec\_t &x, vec\_t &y))  
*Specify the function pointer.*
- int `set_function` (int(\*fp)(size\_t nv, const vec\_t &x, vec\_t &y))  
*Specify the function pointer.*
- virtual int `operator()` (size\_t nv, const vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- int(\* `fptr` )(size\_t nv, const vec\_t &x, vec\_t &y)  
*The function pointer to the user-supplied function.*

## Private Member Functions

- `mm_func_ptr` (const `mm_func_ptr` &)
- `mm_func_ptr` & `operator=` (const `mm_func_ptr` &)

The documentation for this class was generated from the following file:

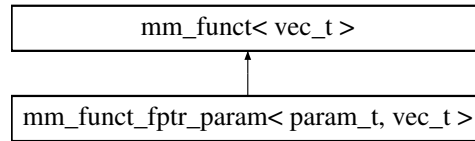
- `mm_func.h`

## 46.192 mm\_funcnt\_fptr\_param&lt; param\_t, vec\_t &gt; Class Template Reference

Function pointer to array of multi-dimensional functions.

```
#include <mm_funcnt.h>
```

Inheritance diagram for mm\_funcnt\_fptr\_param< param\_t, vec\_t >:



## 46.192.1 Detailed Description

```
template<class param_t, class vec_t = ovector_base>class mm_funcnt_fptr_param< param_t, vec_t >
```

Definition at line 118 of file mm\_funcnt.h.

## Public Member Functions

- [mm\\_funcnt\\_fptr\\_param](#) (int(\*fp)(size\_t nv, const vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the function pointer.*
- int [set\\_function](#) (int(\*fp)(size\_t nv, const vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the function pointer.*
- virtual int [operator\(\)](#) (size\_t nv, const vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- int(\* [fptr](#)) (size\_t nv, const vec\_t &x, vec\_t &y, param\_t &)  
*The function pointer to the user-supplied function.*
- param\_t \* [pp](#)  
*The parameter.*

## Private Member Functions

- [mm\\_funcnt\\_fptr\\_param](#) (const [mm\\_funcnt\\_fptr\\_param](#) &)
- [mm\\_funcnt\\_fptr\\_param](#) & [operator=](#) (const [mm\\_funcnt\\_fptr\\_param](#) &)

The documentation for this class was generated from the following file:

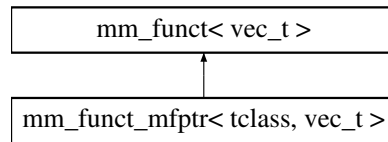
- mm\_funcnt.h

## 46.193 mm\_funcnt\_mfptr&lt; tclass, vec\_t &gt; Class Template Reference

Member function pointer to an array of multi-dimensional functions.

```
#include <mm_funcnt.h>
```

Inheritance diagram for mm\_funcnt\_mfptr< tclass, vec\_t >:



#### 46.193.1 Detailed Description

template<class tclass, class vec\_t = ovector\_base>class mm\_funcnt\_mfptr< tclass, vec\_t >

Definition at line 175 of file mm\_funcnt.h.

#### Public Member Functions

- [mm\\_funcnt\\_mfptr](#) ()  
*Empty constructor.*
- [mm\\_funcnt\\_mfptr](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, vec\_t &y))  
*Specify the member function pointer.*
- int [set\\_function](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, vec\_t &y))  
*Specify the member function pointer.*
- virtual int [operator](#)() (size\_t nv, const vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

#### Protected Attributes

- int(tclass::\* [fptr](#))(size\_t nv, const vec\_t &x, vec\_t &y)  
*The member function pointer.*
- tclass \* [tptr](#)  
*The class pointer.*

#### Private Member Functions

- [mm\\_funcnt\\_mfptr](#) (const [mm\\_funcnt\\_mfptr](#) &)
- [mm\\_funcnt\\_mfptr](#) & [operator=](#) (const [mm\\_funcnt\\_mfptr](#) &)

The documentation for this class was generated from the following file:

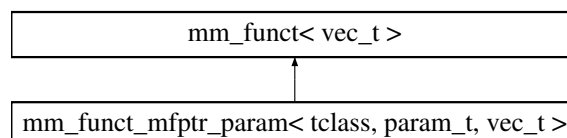
- mm\_funcnt.h

#### 46.194 mm\_funcnt\_mfptr\_param< tclass, param\_t, vec\_t > Class Template Reference

Member function pointer to an array of multi-dimensional functions.

```
#include <mm_funcnt.h>
```

Inheritance diagram for mm\_funcnt\_mfptr\_param< tclass, param\_t, vec\_t >:



## 46.194.1 Detailed Description

```
template<class tclass, class param_t, class vec_t = ovector_base>class mm_func_t_mfptr_param< tclass, param_t, vec_t >
```

Definition at line 233 of file mm\_func\_t.h.

## Public Member Functions

- [mm\\_func\\_t\\_mfptr\\_param](#) ()  
*Empty constructor.*
- [mm\\_func\\_t\\_mfptr\\_param](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the member function pointer.*
- int [set\\_function](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, vec\_t &y, param\_t &), param\_t &pa)  
*Specify the member function pointer.*
- virtual int [operator](#)() (size\_t nv, const vec\_t &x, vec\_t &y)  
*Compute nv functions, y, of nv variables stored in x with parameter pa.*

## Protected Attributes

- int(tclass::\* [fptr](#)) (size\_t nv, const vec\_t &x, vec\_t &y, param\_t &pa)  
*The member function pointer.*
- tclass \* [tptr](#)  
*The class pointer.*
- param\_t \* [pp](#)  
*Parameter.*

## Private Member Functions

- [mm\\_func\\_t\\_mfptr\\_param](#) (const [mm\\_func\\_t\\_mfptr\\_param](#) &)
- [mm\\_func\\_t\\_mfptr\\_param](#) & [operator=](#) (const [mm\\_func\\_t\\_mfptr\\_param](#) &)

The documentation for this class was generated from the following file:

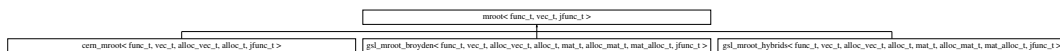
- mm\_func\_t.h

## 46.195 mroot&lt; func\_t, vec\_t, jfunc\_t &gt; Class Template Reference

Multidimensional root-finding [abstract base].

```
#include <mroot.h>
```

Inheritance diagram for mroot< func\_t, vec\_t, jfunc\_t >:



## 46.195.1 Detailed Description

```
template<class func_t, class vec_t = ovector_base, class jfunc_t = jac_func_t<vec_t,omatrix_base>>class mroot< func_t, vec_t, jfunc_t >
```

**The template parameters:** The template parameter `func_t` specifies the functions to solve and should be a class containing a definition

```
func_t::operator() (size_t nv, const vec_t &x, vec_t &y);
```

where  $y$  is the value of the functions at  $x$  with parameter  $pa$  and  $x$  and  $y$  are a array-like classes defining `operator[]` of size  $nv$ . If the Jacobian matrix is to be specified by the user, then the parameter `jfunc_t` specifies the jacobian and should contain the definition

```
jfunc_t::operator(size_t nv, vec_t &x, vec_t &y, mat_t &j);
```

where  $x$  is the independent variables,  $y$  is the array of function values, and  $j$  is the Jacobian matrix. This template parameter can be ignored if only the function `msolve()` will be used.

#### Warning

Many of the routines assume that the scale of the functions and their variables is of order unity. The solution routines may lose precision if this is not the case.

There is an example for the usage of the multidimensional solver classes given in `examples/ex_mroot.cpp`, see [Multi-dimensional solver](#).

**Idea for Future** Change `ntrial` to `size_t`?

Definition at line 65 of file `mroot.h`.

#### Public Member Functions

- virtual const char \* `type` ()  
*Return the type, "mroot".*
- virtual int `msolve` (size\_t n, vec\_t &x, func\_t &func)=0  
*Solve `func` using `x` as an initial guess, returning `x`.*
- virtual int `msolve_de` (size\_t n, vec\_t &x, func\_t &func, jfunc\_t &dfunc)  
*Solve `func` with derivatives `dfunc` using `x` as an initial guess, returning `x`.*
- template<class vec2\_t, class vec3\_t >  
int `print_iter` (size\_t n, const vec2\_t &x, const vec3\_t &y, int iter, double value=0.0, double limit=0.0, std::string comment="")  
*Print out iteration information.*

#### Data Fields

- double `tol_rel`  
*The maximum value of the functions for success (default 1.0e-8)*
- double `tol_abs`  
*The minimum allowable stepsize (default 1.0e-12)*
- int `verbose`  
*Output control (default 0)*
- int `ntrial`  
*Maximum number of iterations (default 100)*
- int `last_ntrial`  
*The number of iterations for in the most recent minimization.*
- bool `err_nonconv`  
*If true, call the error handler if `msolve()` or `msolve_de()` does not converge (default true)*
- int `last_conv`  
*Zero if last call to `msolve()` or `msolve_de()` converged.*

## 46.195.2 Member Function Documentation

46.195.2.1 `template<class func_t, class vec_t = ovector_base, class jfunc_t = jac_func<vec_t,omatrix_base>> virtual int mroot< func_t, vec_t, jfunc_t>::msolve_de ( size_t n, vec_t & x, func_t & func, jfunc_t & dfunc ) [inline, virtual]`

By default, this function just calls [msolve\(\)](#) and ignores the last argument.

Reimplemented in [gsl\\_mroot\\_hybrids< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t, mat\\_t, alloc\\_mat\\_t, mat\\_alloc\\_t, jfunc\\_t >](#).

Definition at line 119 of file mroot.h.

46.195.2.2 `template<class func_t, class vec_t = ovector_base, class jfunc_t = jac_func<vec_t,omatrix_base>> template<class vec2_t, class vec3_t> int mroot< func_t, vec_t, jfunc_t>::print_iter ( size_t n, const vec2_t & x, const vec3_t & y, int iter, double value = 0.0, double limit = 0.0, std::string comment = " " ) [inline]`

Depending on the value of the variable verbose, this prints out the iteration information. If verbose=0, then no information is printed, while if verbose>1, then after each iteration, the present values of x and y are output to std::cout along with the iteration number. If verbose>=2 then each iteration waits for a character.

This is implemented as a template class using a new vector type because sometimes the internal vector class is distinct from the user-specified vector class (e.g. in [gsl\\_mroot\\_hybrids](#)).

Definition at line 138 of file mroot.h.

## 46.195.3 Field Documentation

46.195.3.1 `template<class func_t, class vec_t = ovector_base, class jfunc_t = jac_func<vec_t,omatrix_base>> int mroot< func_t, vec_t, jfunc_t>::last_conv`

This is particularly useful if err\_nonconv is false to test if the last call to [msolve\(\)](#) or [msolve\\_de\(\)](#) converged.

Definition at line 105 of file mroot.h.

The documentation for this class was generated from the following file:

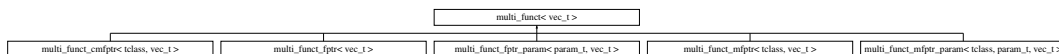
- mroot.h

## 46.196 multi\_func&lt; vec\_t &gt; Class Template Reference

Multi-dimensional function [abstract base].

`#include <multi_func.h>`

Inheritance diagram for multi\_func< vec\_t >:



## 46.196.1 Detailed Description

`template<class vec_t = ovector_base> class multi_func< vec_t >`

This class generalizes one function of several variables, i.e.  $y(x_0, x_1, \dots, x_{nv-1})$  where  $nv$  is the number of variables in the function  $y$ .

This class is one of a large number of function object classes in O2scl designed to provide a mechanism for the user to supply functions to solvers, minimizers, integrators, etc. See [Function Objects](#) for a general description.

Definition at line 47 of file multi\_func.h.



## Public Member Functions

- virtual double [operator\(\)](#) (size\_t nv, const vec\_t &x)=0  
*Compute a function  $y$  of  $nv$  variables stored in  $x$  with parameter  $pa$ .*

The documentation for this class was generated from the following file:

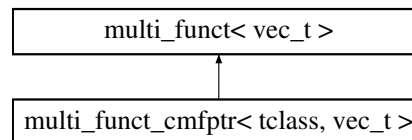
- multi\_func.h

## 46.197 multi\_func\_cmfp&lt; tclass, vec\_t &gt; Class Template Reference

Const member function pointer to a multi-dimensional function.

```
#include <multi_func.h>
```

Inheritance diagram for multi\_func\_cmfp< tclass, vec\_t >:



## 46.197.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class multi_func_cmfp< tclass, vec_t >
```

Definition at line 260 of file multi\_func.h.

## Public Member Functions

- [multi\\_func\\_cmfp](#) (tclass \*tp, double(tclass::\*fp)(size\_t nv, const vec\_t &x) const)  
*Specify the member function pointer.*
- virtual double [operator\(\)](#) (size\_t nv, const vec\_t &x)  
*Compute a function  $y$  of  $nv$  variables stored in  $x$  with parameter  $pa$ .*

## Protected Attributes

- double(tclass::\* [fptr](#) )(size\_t nv, const vec\_t &x) const  
*Store the function pointer.*
- tclass \* [tptr](#)  
*Store a pointer to the class instance.*

## Private Member Functions

- [multi\\_func\\_cmfp](#) (const [multi\\_func\\_cmfp](#) &)
- [multi\\_func\\_cmfp](#) & [operator=](#) (const [multi\\_func\\_cmfp](#) &)

The documentation for this class was generated from the following file:

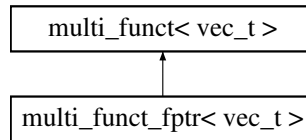
- multi\_func.h

## 46.198 multi\_funct\_fptr&lt; vec\_t &gt; Class Template Reference

Function pointer to a multi-dimensional function.

```
#include <multi_funct.h>
```

Inheritance diagram for multi\_funct\_fptr< vec\_t >:



## 46.198.1 Detailed Description

```
template<class vec_t = ovector_base>class multi_funct_fptr< vec_t >
```

Definition at line 74 of file multi\_funct.h.

## Public Member Functions

- [multi\\_funct\\_fptr](#) (double(\*fp)(size\_t nv, const vec\_t &x))  
*Specify the function pointer.*
- virtual double [operator\(\)](#) (size\_t nv, const vec\_t &x)  
*Compute a function  $y$  of  $nv$  variables stored in  $x$  with parameter  $pa$ .*

## Protected Attributes

- double(\* [fptr](#))(size\_t nv, const vec\_t &x)  
*Store the function pointer.*

## Private Member Functions

- [multi\\_funct\\_fptr](#) (const [multi\\_funct\\_fptr](#) &)
- [multi\\_funct\\_fptr](#) & [operator=](#) (const [multi\\_funct\\_fptr](#) &)

The documentation for this class was generated from the following file:

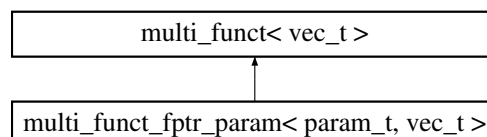
- multi\_funct.h

## 46.199 multi\_funct\_fptr\_param&lt; param\_t, vec\_t &gt; Class Template Reference

Function pointer to a multi-dimensional function.

```
#include <multi_funct.h>
```

Inheritance diagram for multi\_funct\_fptr\_param< param\_t, vec\_t >:



## 46.199.1 Detailed Description

```
template<class param_t, class vec_t = ovector_base>class multi_funct_fptr_param< param_t, vec_t >
```

Definition at line 117 of file multi\_funct.h.

## Public Member Functions

- [multi\\_funct\\_fptr\\_param](#) (double(\*fp)(size\_t nv, const vec\_t &x, param\_t &), param\_t &pa)  
*Specify the function pointer.*
- virtual double [operator\(\)](#) (size\_t nv, const vec\_t &x)  
*Compute a function  $y$  of  $nv$  variables stored in  $x$  with parameter  $pa$ .*

## Protected Attributes

- double(\* [fptr](#))(size\_t nv, const vec\_t &x, param\_t &)  
*Store the function pointer.*
- param\_t \* [pp](#)  
*Parameter.*

## Private Member Functions

- [multi\\_funct\\_fptr\\_param](#) (const [multi\\_funct\\_fptr\\_param](#) &)
- [multi\\_funct\\_fptr\\_param](#) & [operator=](#) (const [multi\\_funct\\_fptr\\_param](#) &)

The documentation for this class was generated from the following file:

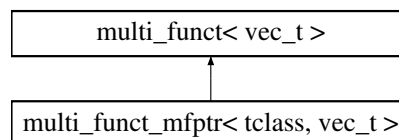
- multi\_funct.h

## 46.200 multi\_funct\_mfptr&lt; tclass, vec\_t &gt; Class Template Reference

Member function pointer to a multi-dimensional function.

```
#include <multi_funct.h>
```

Inheritance diagram for multi\_funct\_mfptr< tclass, vec\_t >:



## 46.200.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class multi_funct_mfptr< tclass, vec_t >
```

Definition at line 165 of file multi\_funct.h.

## Public Member Functions

- [multi\\_funct\\_mfptr](#) (tclass \*tp, double(tclass::\*fp)(size\_t nv, const vec\_t &x))  
*Specify the member function pointer.*
- virtual double [operator\(\)](#) (size\_t nv, const vec\_t &x)  
*Compute a function  $y$  of  $nv$  variables stored in  $x$  with parameter  $pa$ .*

## Protected Attributes

- double(tclass::\* [fptr](#)) (size\_t nv, const vec\_t &x)  
*Store the function pointer.*
- tclass \* [tptr](#)  
*Store a pointer to the class instance.*

## Private Member Functions

- [multi\\_funct\\_mfptr](#) (const [multi\\_funct\\_mfptr](#) &)
- [multi\\_funct\\_mfptr](#) & [operator=](#) (const [multi\\_funct\\_mfptr](#) &)

The documentation for this class was generated from the following file:

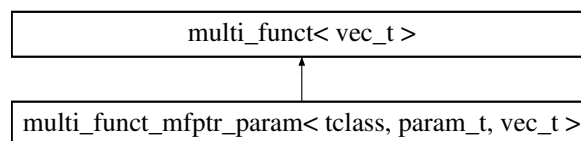
- multi\_funct.h

## 46.201 multi\_funct\_mfptr\_param&lt; tclass, param\_t, vec\_t &gt; Class Template Reference

Member function pointer to a multi-dimensional function.

```
#include <multi_funct.h>
```

Inheritance diagram for multi\_funct\_mfptr\_param< tclass, param\_t, vec\_t >:



## 46.201.1 Detailed Description

```
template<class tclass, class param_t, class vec_t = ovector_base>class multi_funct_mfptr_param< tclass, param_t, vec_t >
```

Definition at line 210 of file multi\_funct.h.

## Public Member Functions

- [multi\\_funct\\_mfptr\\_param](#) (tclass \*tp, double(tclass::\*fp)(size\_t nv, const vec\_t &x, param\_t &), param\_t &pa)  
*Specify the member function pointer.*
- virtual double [operator\(\)](#) (size\_t nv, const vec\_t &x)  
*Compute a function  $y$  of  $nv$  variables stored in  $x$  with parameter  $pa$ .*

## Protected Attributes

- double(tclass::\* [fptr](#))(size\_t nv, const vec\_t &x, param\_t &)  
*Store the function pointer.*
- param\_t \* [pp](#)  
*Parameter.*
- tclass \* [tptr](#)  
*Store a pointer to the class instance.*

## Private Member Functions

- [multi\\_func\\_t\\_mfptr\\_param](#) (const [multi\\_func\\_t\\_mfptr\\_param](#) &)
- [multi\\_func\\_t\\_mfptr\\_param](#) & [operator=](#) (const [multi\\_func\\_t\\_mfptr\\_param](#) &)

The documentation for this class was generated from the following file:

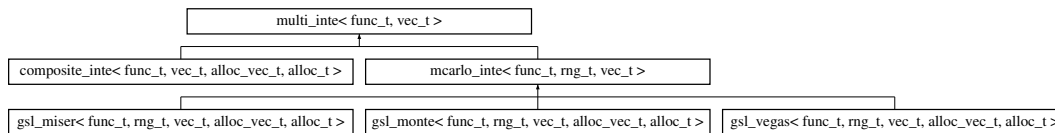
- [multi\\_func\\_t.h](#)

## 46.202 multi\_inte&lt; func\_t, vec\_t &gt; Class Template Reference

Multi-dimensional integration over a hypercube [abstract base].

```
#include <multi_inte.h>
```

Inheritance diagram for multi\_inte< func\_t, vec\_t >:



## 46.202.1 Detailed Description

```
template<class func_t, class vec_t = ovector_base>class multi_inte< func_t, vec_t >
```

Multi-dimensional integration over a region defined by constant limits. For more general regions of integration, use children of the class [gen\\_inte](#).

Definition at line 40 of file [multi\\_inte.h](#).

## Public Member Functions

- virtual double [minteg](#) (func\_t &func, size\_t ndim, const vec\_t &a, const vec\_t &b)  
*Integrate function `func` over the hypercube from  $x_i = a_i$  to  $x_i = b_i$  for  $0 < i < ndim-1$ .*
- virtual int [minteg\\_err](#) (func\_t &func, size\_t ndim, const vec\_t &a, const vec\_t &b, double &res, double &err)=0  
*Integrate function `func` over the hypercube from  $x_i = a_i$  to  $x_i = b_i$  for  $0 < i < ndim-1$ .*
- double [get\\_error](#) ()  
*Return the error in the result from the last call to [minteg\(\)](#) or [minteg\\_err\(\)](#)*
- const char \* [type](#) ()  
*Return string denoting type ("[multi\\_inte](#)")*

## Data Fields

- bool `err_nonconv`  
If true, call the error handler if the routine does not "converge".
- int `verbose`  
Verbosity.
- double `tol_rel`  
The maximum "uncertainty" in the value of the integral (default  $10^{-8}$ ).

## Protected Attributes

- double `interior`  
The uncertainty for the last integration computation.

## 46.202.2 Member Function Documentation

46.202.2.1 `template<class func_t, class vec_t = ovector_base> virtual double multi_inte< func_t, vec_t >::minteg ( func_t & func, size_t ndim, const vec_t & a, const vec_t & b ) [inline, virtual]`

Reimplemented in `gsl_vegas< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`, `gsl_miser< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`, and `gsl_monte< func_t, rng_t, vec_t, alloc_vec_t, alloc_t >`.

Definition at line 74 of file `multi_inte.h`.

46.202.2.2 `template<class func_t, class vec_t = ovector_base> double multi_inte< func_t, vec_t >::get_error ( ) [inline]`

This will quietly return zero if no integrations have been performed.

Definition at line 94 of file `multi_inte.h`.

The documentation for this class was generated from the following file:

- `multi_inte.h`

## 46.203 multi\_min&lt; func\_t, dfunc\_t, vec\_t &gt; Class Template Reference

Multidimensional minimization [abstract base].

```
#include <multi_min.h>
```

Inheritance diagram for `multi_min< func_t, dfunc_t, vec_t >`:



## 46.203.1 Detailed Description

```
template<class func_t, class dfunc_t = func_t, class vec_t = ovector_base> class multi_min< func_t, dfunc_t, vec_t >
```

**The template parameters:** The template parameter `func_t` specifies the function to minimize and should be a class containing a definition

```
func_t::operator()(size_t nv, const vec_t &x, double &f);
```

where `f` is the value of the function at `x`, where `x` is a array-like class defining `operator[]` of size `nv`. The parameter `dfunc_t` (if used) should provide the gradient with

```
func_t::operator()(size_t nv, vec_t &x, vec_t &g);
```

where  $g$  is the gradient of the function at  $x$ .

Verbose I/O is sent through `std::cout` and `std::cin` by default, but this can be modified using `set_verbose_stream()`.

Definition at line 463 of file `multi_min.h`.

### Public Member Functions

- int `set_verbose_stream` (std::ostream &out, std::istream &in)  
*Set streams for verbose I/O.*
- virtual int `mmin` (size\_t nvar, vec\_t &x, double &fmin, func\_t &func)=0  
*Calculate the minimum min of func w.r.t. the array x of size nvar.*
- virtual int `mmin_de` (size\_t nvar, vec\_t &x, double &fmin, func\_t &func, dfunc\_t &dfunc)  
*Calculate the minimum min of func w.r.t. the array x of size nvar with gradient dfunc.*
- template<class vec2\_t >  
int `print_iter` (size\_t nv, vec2\_t &x, double y, int iter, double value, double limit, std::string comment)  
*Print out iteration information.*
- const char \* `type` ()  
*Return string denoting type ("multi\_min")*

### Data Fields

- int `verbose`  
*Output control.*
- int `ntrial`  
*Maximum number of iterations.*
- double `tol_rel`  
*Function value tolerance.*
- double `tol_abs`  
*The independent variable tolerance.*
- int `last_ntrial`  
*The number of iterations for in the most recent minimization.*
- bool `err_nonconv`  
*If true, call the error handler if the routine does not "converge".*
- int `last_conv`  
*Zero if last call to `mmin()` or `mmin_de()` converged.*

### Protected Attributes

- std::ostream \* `outs`  
*Stream for verbose output.*
- std::istream \* `ins`  
*Stream for verbose input.*

### 46.203.2 Member Function Documentation

**46.203.2.1** template<class func\_t, class dfunc\_t = func\_t, class vec\_t = ovector\_base> template<class vec2\_t > int multi\_min< func\_t, dfunc\_t, vec\_t >::print\_iter ( size\_t nv, vec2\_t & x, double y, int iter, double value, double limit, std::string comment ) [inline]

Depending on the value of the variable `verbose`, this prints out the iteration information. If `verbose=0`, then no information is printed, while if `verbose>1`, then after each iteration, the present values of  $x$  and  $y$  are output to `std::cout` along with the iteration number. If `verbose>=2` then each iteration waits for a character.

Definition at line 551 of file `multi_min.h`.

## 46.203.3 Field Documentation

46.203.3.1 `template<class func_t, class dfunc_t = func_t, class vec_t = ovector_base> int multi_min< func_t, dfunc_t, vec_t >::last_conv`

This is particularly useful if `err_nonconv` is false to test if the last call to `mmin()` or `mmin_de()` converged.

Definition at line 516 of file `multi_min.h`.

The documentation for this class was generated from the following file:

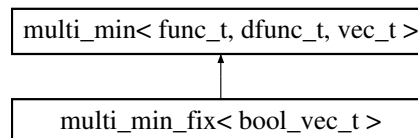
- `multi_min.h`

## 46.204 multi\_min\_fix&lt; bool\_vec\_t &gt; Class Template Reference

Multidimensional minimizer fixing some variables and varying others.

`#include <multi_min_fix.h>`

Inheritance diagram for `multi_min_fix< bool_vec_t >`:



## 46.204.1 Detailed Description

`template<class bool_vec_t> class multi_min_fix< bool_vec_t >`

See an example for the usage of this class in [Minimizer fixing variables](#) .

**Todo** Generalize to all vector types

Generalize to minimizers which require derivatives

At the moment, the user has to change `def_mmin::ntrial` instead of `multi_min_fix::ntrial`, which is a bit confusing. Fix this.

Definition at line 46 of file `multi_min_fix.h`.

## Public Member Functions

- `multi_min_fix ()`  
*Specify the member function pointer.*
- virtual int `mmin` (size\_t nvar, `ovector_base` &x, double &fmin, `multi_func_t`<> &func)  
*Calculate the minimum min of func w.r.t. the array x of size nvar.*
- virtual int `mmin_fix` (size\_t nvar, `ovector_base` &x, double &fmin, `bool_vec_t` &fix, `multi_func_t`<> &func)  
*Calculate the minimum of func while fixing some parameters as specified in fix.*
- int `set_mmin` (`multi_min`< `multi_func_t` mfp, `multi_min_fix` > > &min)  
*Change the base minimizer.*

## Data Fields

- `gsl_mmin_simp2` < `multi_func_t` mfp, `multi_min_fix` > > `def_mmin`  
*The default base minimizer.*



## Protected Member Functions

- virtual double [min\\_func](#) (size\_t nv, const [ovector\\_base](#) &x)  
*The new function to send to the minimizer.*

## Protected Attributes

- [multi\\_min](#)< [multi\\_func\\_mfptr](#) < [multi\\_min\\_fix](#) > > \* [mmp](#)  
*The minimizer.*
- [multi\\_func](#) \* [funcp](#)  
*The user-specified function.*
- size\_t [unv](#)  
*The user-specified number of variables.*
- size\_t [nv\\_new](#)  
*The new number of variables.*
- bool\_vec\_t \* [fixp](#)  
*Specify which parameters to fix.*
- [ovector\\_base](#) \* [xp](#)  
*The user-specified initial vector.*

## Private Member Functions

- [multi\\_min\\_fix](#) (const [multi\\_min\\_fix](#) &)
- [multi\\_min\\_fix](#) & [operator=](#) (const [multi\\_min\\_fix](#) &)

## 46.204.2 Member Function Documentation

46.204.2.1 `template<class bool_vec_t> virtual int multi\_min\_fix< bool_vec_t >::mmin_fix ( size_t nvar, ovector\_base & x, double & fmin, bool_vec_t & fix, multi\_func<> & func ) [inline, virtual]`

If all of entries `fix[0]`, `fix[1]`, ... `fix[nvar-1]` are true, then this function assumes all of the parameters are fixed and that there is no minimization to be performed. In this case, it will return 0 for success without calling the error handler.

Definition at line 107 of file `multi_min_fix.h`.

The documentation for this class was generated from the following file:

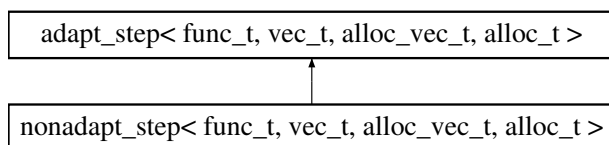
- `multi_min_fix.h`

## 46.205 nonadapt\_step&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

An non-adaptive stepper implementation of [adapt\\_step](#).

```
#include <nonadapt_step.h>
```

Inheritance diagram for `nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >`:



## 46.205.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class nonadapt_step<
func_t, vec_t, alloc_vec_t, alloc_t >
```

This class simply calls the specified ODE stepper without any attempt to modify the size of the step. It is primarily useful to allow for simple comparisons between adaptive and non-adaptive solution or to proceed with a solution in places where an adaptive stepper is failing.

To modify the ODE stepper which is used, use the function [adapt\\_step::set\\_step\(\)](#).

Definition at line 48 of file nonadapt\_step.h.

## Public Member Functions

- virtual int [astep](#) (double &x, double xlimit, double &h, size\_t n, vec\_t &y, vec\_t &dydx\_out, vec\_t &yerr, func\_t &derivs)  
*Make an adaptive integration step of the system derivs.*
- virtual int [astep\\_derivs](#) (double &x, double xlimit, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yerr, func\_t &derivs)  
*Make an adaptive integration step of the system derivs with derivatives.*
- virtual int [astep\\_full](#) (double x, double xlimit, double &x\_out, double &h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)  
*Make an adaptive integration step of the system derivs.*

## Protected Attributes

- size\_t [msize](#)  
*The allocated vector size.*
- alloc\_vec\_t [dydx\\_int](#)  
*Internal storage for dydx.*
- alloc\_t [ao](#)  
*Memory allocator for objects of type alloc\_vec\_t.*

## 46.205.2 Member Function Documentation

```
46.205.2.1 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::astep ( double & x, double xlimit, double & h, size_t n, vec_t & y, vec_t &
dydx_out, vec_t & yerr, func_t & derivs ) [inline, virtual]
```

This attempts to take a step of size h from the point x of an n-dimensional system derivs starting with y. On exit, x and y contain the new values at the end of the step, h contains the size of the step, dydx\_out contains the derivative at the end of the step, and yerr contains the estimated error at the end of the step.

If the base stepper returns a non-zero value, that value is passed on as the return value of [astep\(\)](#), though the input y may still have been modified by the base stepper.

Implements [adapt\\_step< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

Definition at line 99 of file nonadapt\_step.h.

```
46.205.2.2 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::astep_derivs ( double & x, double xlimit, double & h, size_t n, vec_t & y, vec_t
& dydx, vec_t & yerr, func_t & derivs ) [inline, virtual]
```

This attempts to take a step of size h from the point x of an n-dimensional system derivs starting with y and given the initial derivatives dydx. On exit, x, y and dydx contain the new values at the end of the step, h contains the size of the step, dydx contains the derivative at the end of the step, and yerr contains the estimated error at the end of the step.

If the base stepper returns a non-zero value, that value is passed on as the return value of `astep()`, though the inputs `y` and `dydx` may still have been modified by the base stepper.

Implements `adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >`.

Definition at line 135 of file `nonadapt_step.h`.

```
46.205.2.3  template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int
            nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::astep_full( double x, double xlimit, double &x_out, double &h, size_t n, vec_t
            &y, vec_t &dydx, vec_t &yout, vec_t &yerr, vec_t &dydx_out, func_t &derivs ) [inline, virtual]
```

This function performs an adaptive integration step with the  $n$ -dimensional system `derivs` and parameter `pa`. It Begins at `x` with initial stepsize `h`, ensuring that the step goes no farther than `xlimit`. At the end of the step, the size of the step taken is `h` and the new value of `x` is in `x_out`. Initially, the function values and derivatives should be specified in `y` and `dydx`. The function values, derivatives, and the error at the end of the step are given in `yout`, `yerr`, and `dydx_out`. Unlike in `ode_step` objects, the objects `y`, `yout`, `dydx`, and `dydx_out` must all be distinct.

If the base stepper returns a non-zero value, that value is passed on as the return value of `astep()`, though the output parameters may still have been modified by the base stepper.

Implements `adapt_step< func_t, vec_t, alloc_vec_t, alloc_t >`.

Definition at line 170 of file `nonadapt_step.h`.

#### 46.205.3 Field Documentation

```
46.205.3.1  template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> alloc_vec_t
            nonadapt_step< func_t, vec_t, alloc_vec_t, alloc_t >::dydx_int [protected]
```

Definition at line 65 of file `nonadapt_step.h`.

The documentation for this class was generated from the following file:

- `nonadapt_step.h`

## 46.206 o2\_int\_shared\_ptr< T > Class Template Reference

The internal shared pointer class used if no TR1 or Boost implementation is available.

```
#include <shared_ptr.h>
```

#### 46.206.1 Detailed Description

```
template<class T>class o2_int_shared_ptr< T >
```

See also `o2_shared_ptr`.

This class was based on the Aegis `shared_ptr` class from <http://aegis.sourceforge.net>, but is implemented in `O2scl` using a template struct rather than a define constant.

Definition at line 60 of file `shared_ptr.h`.

#### Public Member Functions

- `o2_int_shared_ptr()`  
*Create an empty shared\_ptr.*
- `template<class Y>`  
`o2_int_shared_ptr(Y *rhs)`

*Create a shared pointer.*

- `o2_int_shared_ptr` (const `o2_int_shared_ptr` &rhs)  
*Copy constructor.*
- `template<class Y >`  
`o2_int_shared_ptr` (const `o2_int_shared_ptr`< Y > &rhs)  
*Copy constructor for compatible pointer types.*
- `bool valid ()` const  
*Test if the shared\_ptr object is valid.*
- `void swap (o2_int_shared_ptr &rhs)`  
*Swap.*
- `void reset ()`  
*Drop the reference and set the pointer to zero.*
- `o2_int_shared_ptr & operator=` (const `o2_int_shared_ptr` &rhs)  
*Assignment operator.*
- `template<class Y >`  
`o2_int_shared_ptr & operator=` (const `o2_int_shared_ptr`< Y > &rhs)  
*Assignment operator for compatible pointer types.*
- `T & operator*` () const  
*Dereference operator.*
- `T * operator->` () const  
*Pointing at operator.*
- `T * get ()` const  
*Return a pointer to the object.*
- `operator bool ()` const  
*Return true if the pointer is not zero.*
- `bool operator!` () const  
*Logical not operator.*
- `bool operator==` (const `o2_int_shared_ptr` &rhs) const  
*Test equality.*
- `template<class U >`  
`bool operator==` (const `o2_int_shared_ptr`< U > &rhs) const  
*Test equality for compatible pointer types.*
- `bool operator!=` (`o2_int_shared_ptr` &rhs) const  
*Test inequality.*
- `template<class U >`  
`bool operator!=` (`o2_int_shared_ptr`< U > &rhs) const  
*Test inequality for compatible pointer types.*
- `bool operator<` (`o2_int_shared_ptr` &rhs) const  
*Less than operator.*
- `template<class U >`  
`bool operator<` (`o2_int_shared_ptr`< U > &rhs) const  
*Less than operator for compatible pointer types.*

#### Private Attributes

- `long * reference_count`  
*Reference count.*
- `T * subject`  
*Object being pointed to.*

#### Friends

- `class o2_int_shared_ptr`

## 46.206.2 Constructor &amp; Destructor Documentation

46.206.2.1 `template<class T> template<class Y> o2_int_shared_ptr< T >::o2_int_shared_ptr ( Y * rhs ) [inline, explicit]`

This constructor permits initialization from any compatible pointer where Y must be a complete type.

Definition at line 105 of file shared\_ptr.h.

## 46.206.3 Member Function Documentation

46.206.3.1 `template<class T> bool o2_int_shared_ptr< T >::valid ( ) const [inline]`

This method verifies that the internal state of the shared pointer object is valid.

Definition at line 163 of file shared\_ptr.h.

46.206.3.2 `template<class T> void o2_int_shared_ptr< T >::swap ( o2_int_shared_ptr< T > & rhs ) [inline]`

Swap the contents of two o2\_int\_shared\_ptr<T> objects. This method is more efficient than manually swapping shared\_ptr objects using a copy constructor or temporary.

Definition at line 174 of file shared\_ptr.h.

46.206.3.3 `template<class T> bool o2_int_shared_ptr< T >::operator! ( ) const [inline]`

Return true if and only if the pointer is zero.

Definition at line 282 of file shared\_ptr.h.

## 46.206.4 Field Documentation

46.206.4.1 `template<class T> long* o2_int_shared_ptr< T >::reference_count [private]`

Documentation from Aegis:

```
The reference_count instance variable is used to remember the
location of the reference count. By having the reference count
separate from the subject, we can cope with compatible pointers,
not just exact pointers.
```

```
This is not ideal because it allocates huge numbers of small
objects. Some heap implementations go slowly when faced with
many small allocations. Some heap implementations waste a lot of
memory when faced with many small allocations.
```

Definition at line 79 of file shared\_ptr.h.

46.206.4.2 `template<class T> T* o2_int_shared_ptr< T >::subject [private]`

Documentation from Aegis:

```
The subject instance variable is used to remember the location
of the object being reference counted. By having it separate
from the reference count, we can skip one indirection.
```

Definition at line 90 of file shared\_ptr.h.

The documentation for this class was generated from the following file:

- shared\_ptr.h

## 46.207 o2\_shared\_ptr< T > Struct Template Reference

A struct to provide the shared\_ptr type.

```
#include <shared_ptr.h>
```

### 46.207.1 Detailed Description

```
template<class T>struct o2_shared_ptr< T >
```

This object exists in order to provide the shared\_ptr template type used in O2scl . The full specification of a shared pointer in O2scl for an object of type T is thus

```
o2scl::o2_shared_ptr<T>::type
```

In a default O2scl installation, [type](#) (as given below) is a typedef of

```
std::tr1::shared_ptr<T>
```

If O2SCL\_NO\_TR1\_MEMORY is defined, then [type](#) is a typedef of [o2\\_int\\_shared\\_ptr](#), unless O2SCL\_HAVE\_BOOST is defined, in which case [type](#) is a typedef of

```
boost::shared_ptr<T>
```

See also the discussion at <http://www.gotw.ca/gotw/079.htm> . This struct won't be necessary when C++ allows template typedef's as part of the C++11 standard <http://en.wikipedia.org/wiki/C%2B%2B11> , but very few compilers have implemented this standard yet.

Definition at line 356 of file shared\_ptr.h.

### Public Types

- typedef std::tr1::shared\_ptr< T > [type](#)  
*The actual shared\_ptr type.*

The documentation for this struct was generated from the following file:

- shared\_ptr.h

## 46.208 o2scl\_interp< vec\_t > Class Template Reference

Interpolation class.

```
#include <interp.h>
```

### 46.208.1 Detailed Description

```
template<class vec_t = ovector_const_view>class o2scl_interp< vec_t >
```

Interpolation of [ovector](#) like objects is performed with the default template parameters, and [array\\_interp](#) is provided for simple interpolation on C-style arrays.

The type of interpolation to be performed can be specified using the [set\\_type\(\)](#) function or in the constructor. The default is cubic splines with natural boundary conditions.

Definition at line 1125 of file interp.h.

## Public Member Functions

- [o2scl\\_interp](#) ([base\\_interp\\_mgr](#)< [vec\\_t](#) > &it)  
*Create with base interpolation object [it](#).*
- [o2scl\\_interp](#) ()  
*Create an interpolator using the default cubic spline interpolation.*
- virtual double [interp](#) (const double x0, size\_t n, const [vec\\_t](#) &x, const [vec\\_t](#) &y)  
*Give the value of the function  $y(x = x_0)$ .*
- virtual double [deriv](#) (const double x0, size\_t n, const [vec\\_t](#) &x, const [vec\\_t](#) &y)  
*Give the value of the derivative  $y'(x = x_0)$ .*
- virtual double [deriv2](#) (const double x0, size\_t n, const [vec\\_t](#) &x, const [vec\\_t](#) &y)  
*Give the value of the second derivative  $y''(x = x_0)$ .*
- virtual double [integ](#) (const double x1, const double x2, size\_t n, const [vec\\_t](#) &x, const [vec\\_t](#) &y)  
*Give the value of the integral  $\int_a^b y(x) dx$ .*
- int [set\\_type](#) ([base\\_interp\\_mgr](#)< [vec\\_t](#) > &it)  
*Set base interpolation object.*

## Data Fields

- [def\\_interp\\_mgr](#)< [vec\\_t](#), [cspline\\_interp](#) > [dim1](#)  
*Default base interpolation object (cubic spline with natural boundary conditions)*

## Protected Attributes

- [base\\_interp](#)< [vec\\_t](#) > \* [itp](#)  
*Pointer to base interpolation object.*
- [base\\_interp\\_mgr](#)< [vec\\_t](#) > \* [bim1](#)  
*Pointer to base interpolation manager.*

## Private Member Functions

- [o2scl\\_interp](#) (const [o2scl\\_interp](#)< [vec\\_t](#) > &)
- [o2scl\\_interp](#)< [vec\\_t](#) > & **operator=** (const [o2scl\\_interp](#)< [vec\\_t](#) > &)

The documentation for this class was generated from the following file:

- [interp.h](#)

## 46.209 o2scl\_interp\_vec&lt; vec\_t &gt; Class Template Reference

Interpolation class for pre-specified vector.

```
#include <interp.h>
```

## 46.209.1 Detailed Description

```
template<class vec_t = ovector_const_view>class o2scl_interp_vec< vec_t >
```

This interpolation class is intended to be sufficiently general to handle any vector type. Interpolation of [ovector](#) like objects is performed with the default template parameters, and [array\\_interp\\_vec](#) is provided for simple interpolation on C-style arrays.

This class does not double check the vector to ensure that all of the intervals for the abscissa are all increasing or all decreasing.

The type of interpolation to be performed can be specified using the [set\\_type\(\)](#) function. The default is cubic splines with natural boundary conditions.

Definition at line 1293 of file [interp.h](#).

## Public Member Functions

- `o2scl_interp_vec` (`base_interp_mgr`< `vec_t` > &it, `size_t` n, const `vec_t` &x, const `vec_t` &y)  
*Create with base interpolation object it.*
- virtual double `interp` (const double x0)  
*Give the value of the function  $y(x=x_0)$ .*
- virtual double `deriv` (const double x0)  
*Give the value of the derivative  $y'(x=x_0)$ .*
- virtual double `deriv2` (const double x0)  
*Give the value of the second derivative  $y''(x=x_0)$ .*
- virtual double `integ` (const double x1, const double x2)  
*Give the value of the integral  $\int_a^b y(x) dx$ .*
- int `set_type` (`base_interp_mgr`< `vec_t` > &it)  
*Set base interpolation object.*

## Protected Attributes

- `base_interp`< `vec_t` > \* `itp`  
*Base interpolation object.*
- `base_interp_mgr`< `vec_t` > \* `bim`  
*The interpolation manager.*
- bool `inc`  
*True if the original array was increasing.*
- const `vec_t` \* `lx`  
*Pointer to the user-specified x vector.*
- const `vec_t` \* `ly`  
*Pointer to the user-specified y vector.*
- `size_t` `ln`  
*Size of user-specified vectors.*

## Private Member Functions

- `o2scl_interp_vec` (const `o2scl_interp_vec`< `vec_t` > &)
- `o2scl_interp_vec`< `vec_t` > & `operator=` (const `o2scl_interp_vec`< `vec_t` > &)

The documentation for this class was generated from the following file:

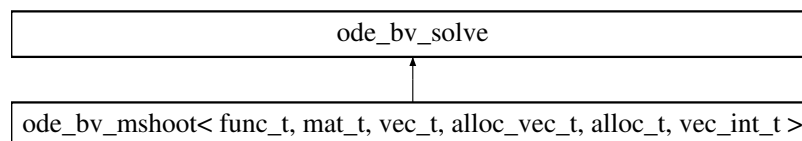
- `interp.h`

## 46.210 ode\_bv\_mshoot&lt; func\_t, mat\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t &gt; Class Template Reference

Solve boundary-value ODE problems by multishooting with a generic nonlinear solver.

```
#include <ode_bv_mshoot.h>
```

Inheritance diagram for `ode_bv_mshoot`< `func_t`, `mat_t`, `vec_t`, `alloc_vec_t`, `alloc_t`, `vec_int_t` >:





## 46.210.1 Detailed Description

```
template<class func_t = ode_func_t<>, class mat_t = omatrix_base, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc,
class vec_int_t = ovector_int_base>class ode_bv_mshoot< func_t, mat_t, vec_t, alloc_vec_t, alloc_t, vec_int_t >
```

This class is experimental.

Default template arguments

- func\_t - [ode\\_func\\_t](#)
- mat\_t - [omatrix\\_base](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)
- vec\_int\_t - [ovector\\_int\\_base](#)

**Idea for Future** Make a class which performs an iterative linear solver which uses sparse matrices like [ode\\_it\\_solve](#)?

Definition at line 52 of file ode\_bv\_mshoot.h.

## Public Member Functions

- int [solve\\_final\\_value](#) (double h, size\_t n, size\_t n\_bound, vec\_t &x\_bound, mat\_t &y\_bound, vec\_int\_t &index, func\_t &derivs)  
*Solve the boundary-value problem and store the solution.*
- template<class mat\_row\_t >  
int [solve\\_store](#) (double h, size\_t n, size\_t n\_bound, vec\_t &x\_bound, mat\_t &y\_bound, vec\_int\_t &index, size\_t &n\_sol, vec\_t &x\_sol, mat\_t &y\_sol, mat\_t &dydx\_sol, mat\_t &yerr\_sol, func\_t &derivs)  
*Solve the boundary-value problem and store the solution.*
- int [set\\_iv](#) ([ode\\_iv\\_solve](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > &ois)  
*Set initial value solver.*
- int [set\\_mroot](#) ([mroot](#)< [mm\\_func\\_t](#)<> > &root)  
*Set the equation solver.*

## Data Fields

- [ode\\_iv\\_solve](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > [def\\_ois](#)  
*The default initial value solver.*
- [gsl\\_mroot\\_hybrids](#)< [mm\\_func\\_t](#)<> > [def\\_mroot](#)  
*The default equation solver.*

## Protected Member Functions

- int [solve\\_fun](#) (size\_t nv, const vec\_t &tx, vec\_t &ty)  
*The shooting function to be solved by the multidimensional solver.*

## Protected Attributes

- `ode_iv_solve`< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > \* `ois`  
*The solver for the initial value problem.*
- `mroot`< `mm_func_t`<> > \* `mrootp`  
*The equation solver.*
- `vec_int_t` \* `l_index`  
*The index defining the boundary conditions.*
- `vec_t` \* `l_xbound`  
*Storage for the starting vector.*
- `mat_t` \* `l_ybound`  
*Storage for the ending vector.*
- `double` `l_h`  
*Storage for the stepsize.*
- `func_t` \* `l_derivs`  
*The functions to integrate.*
- `size_t` `l_n`  
*The number of functions.*
- `size_t` `l_nbound`  
*The number of boundaries.*
- `size_t` `l_lhs_unks`  
*The number of unknowns on the LHS.*
- `alloc_t` `ao`  
*Vector allocation object.*
- `size_t` `mem_size`  
*Size of recent allocation.*

## Temporary storage for \ref solve\_fun()

- `alloc_vec_t` `sy`
- `alloc_vec_t` `sy2`
- `alloc_vec_t` `syerr`
- `alloc_vec_t` `sdydx`
- `alloc_vec_t` `sdydx2`

The documentation for this class was generated from the following file:

- `ode_bv_mshoot.h`

## 46.211 ode\_bv\_multishoot&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t, mat\_t &gt; Class Template Reference

Multishooting.

```
#include <ode_bv_multishoot.h>
```

## 46.211.1 Detailed Description

```
template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class vec_int_t = ovector_int_base, class mat_t = omatrix> class ode_bv_multishoot< func_t, vec_t, alloc_vec_t, alloc_t, vec_int_t, mat_t >
```

This class is experimental.

**Todo** Improve documentation a little and create testing code

Definition at line 48 of file `ode_bv_multishoot.h`.

## Public Member Functions

- virtual int **solve** (vec\_t &mesh, int &n\_func, vec\_t &y\_start, func\_t &left\_b, func\_t &right\_b, func\_t &extra\_b, func\_t &derivs, vec\_t &x\_save, mat\_t &y\_save)
- int **set\_iv** (ode\_iv\_solve< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > &ois)
- int **set\_mroot** (mroot< mm\_funct<> > &root)

## Data Fields

- ode\_iv\_solve< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > **def\_ois**
- gsl\_mroot\_hybrids< mm\_funct<> > **def\_mroot**

## Protected Member Functions

- int **solve\_fun** (size\_t nv, const vec\_t &sx, vec\_t &sy)  
*Function to solve.*

## Protected Attributes

- ode\_iv\_solve< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > \* **ois**  
*The initial value solver.*
- gsl\_mroot\_hybrids< mm\_funct<> > \* **mrootp**  
*The equation solver.*
- vec\_t \* **l\_mesh**  
*Desc.*
- vec\_t \* **l\_y\_start**  
*Desc.*
- func\_t \* **l\_left\_b**  
*Desc.*
- func\_t \* **l\_right\_b**  
*Desc.*
- func\_t \* **l\_extra\_b**  
*Desc.*
- func\_t \* **l\_derivs**  
*Desc.*
- int \* **l\_n\_func**  
*Desc.*
- vec\_t \* **l\_x\_save**  
*Desc.*
- mat\_t \* **l\_y\_save**  
*Desc.*
- bool **save**  
*Desc.*

The documentation for this class was generated from the following file:

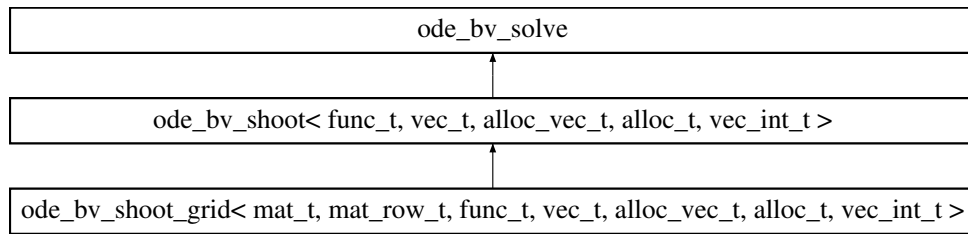
- ode\_bv\_multishoot.h

## 46.212 ode\_bv\_shoot&lt; func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t &gt; Class Template Reference

Solve boundary-value ODE problems by shooting from one boundary to the other.

```
#include <ode_bv_solve.h>
```

Inheritance diagram for ode\_bv\_shoot< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t >:



### 46.212.1 Detailed Description

template<class func\_t = ode\_func\_t<>, class vec\_t = ovector\_base, class alloc\_vec\_t = ovector, class alloc\_t = ovector\_alloc, class vec\_int\_t = ovector\_int\_base>class ode\_bv\_shoot< func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t >

This class is experimental.

Default template arguments

- func\_t - [ode\\_func\\_t](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)
- vec\_int\_t - [ovector\\_int\\_base](#)

Definition at line 82 of file ode\_bv\_solve.h.

### Public Member Functions

- void [allocate](#) (size\_t n)  
*Allocate internal storage.*
- int [solve\\_final\\_value](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, vec\_t &yend, vec\_int\_t &index, vec\_t &yerr, vec\_t &dydx\_end, func\_t &derivs)  
*Solve the boundary-value problem and store the solution.*
- template<class mat\_t, class mat\_row\_t>  
int [solve\\_store](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, vec\_t &yend, vec\_int\_t &index, size\_t &n\_sol, vec\_t &x\_sol, mat\_t &y\_sol, mat\_t &yerr\_sol, mat\_t &dydx\_sol, func\_t &derivs)  
*Solve the boundary-value problem and store the solution.*
- int [set\\_iv](#) ([ode\\_iv\\_solve](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > &ois)  
*Set initial value solver.*
- int [set\\_mroot](#) ([mroot](#)< [mm\\_func\\_t](#)<> > &root)  
*Set the equation solver.*

### Data Fields

- [ode\\_iv\\_solve](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > [def\\_ois](#)  
*The default initial value solver.*
- [gsl\\_mroot\\_hybrids](#)< [mm\\_func\\_t](#)<> > [def\\_mroot](#)  
*The default equation solver.*

### Protected Member Functions

- int [solve\\_fun](#) (size\_t nv, const vec\_t &tx, vec\_t &ty)  
*The shooting function to be solved by the multidimensional solver.*

## Protected Attributes

- `ode_iv_solve`< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > \* `ois`  
*The solver for the initial value problem.*
- `mroot`< `mm_func_t`<> > \* `mrootp`  
*The equation solver.*
- `vec_int_t` \* `l_index`  
*The index defining the boundary conditions.*
- `vec_t` \* `l_ystart`  
*Storage for the starting vector.*
- `vec_t` \* `l_yend`  
*Storage for the ending vector.*
- `vec_t` \* `l_yerr`  
*Storage for the starting vector.*
- `vec_t` \* `l_dydx_end`  
*Storage for the ending vector.*
- `double` `l_x0`  
*Storage for the starting point.*
- `double` `l_x1`  
*Storage for the ending abscissa.*
- `double` `l_h`  
*Storage for the stepsize.*
- `func_t` \* `l_derivs`  
*The functions to integrate.*
- `size_t` `l_n`  
*The number of functions.*
- `alloc_t` `ao`  
*Vector allocation object.*
- `size_t` `mem_size`  
*Size of recent allocation.*

## Temporary storage for \ref solve\_fun()

- `alloc_vec_t` `sy`
- `alloc_vec_t` `sy2`
- `alloc_vec_t` `syerr`
- `alloc_vec_t` `sdydx`

## 46.212.2 Member Function Documentation

46.212.2.1 `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc, class vec_int_t = ovector_int_base> int ode_bv_shoot< func_t, vec_t, alloc_vec_t, alloc_t, vec_int_t >::solve_final_value ( double x0, double x1, double h, size_t n, vec_t & ystart, vec_t & yend, vec_int_t & index, vec_t & yerr, vec_t & dydx_end, func_t & derivs ) [inline]`

Given the `n` initial values of the functions in `ystart`, this function integrates the ODEs specified in `derivs` over the interval from `x0` to `x1` with an initial stepsize of `h`. The final values of the function are given in `yend`, the derivatives in `dydx_end`, and the associated errors are given in `yerr`. The initial values of `yend` and `yerr` are ignored.

Definition at line 126 of file `ode_bv_solve.h`.

The documentation for this class was generated from the following file:

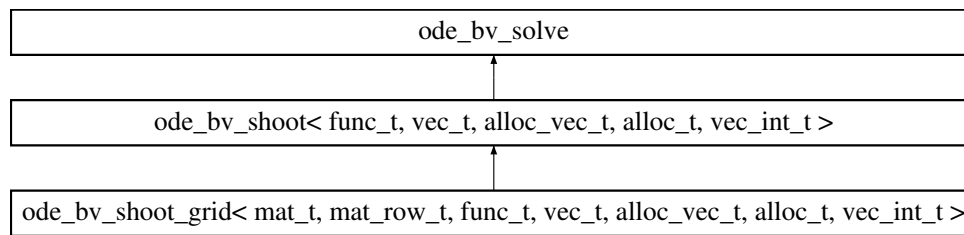
- `ode_bv_solve.h`

## 46.213 ode\_bv\_shoot\_grid&lt; mat\_t, mat\_row\_t, func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t &gt; Class Template Reference

Solve boundary-value ODE problems by shooting from one boundary to the other on a grid.

```
#include <ode_bv_solve.h>
```

Inheritance diagram for ode\_bv\_shoot\_grid< mat\_t, mat\_row\_t, func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t >:



#### 46.213.1 Detailed Description

template<class mat\_t = omatrix, class mat\_row\_t = omatrix\_row, class func\_t = ode\_func\_t<>, class vec\_t = ovector\_base, class alloc\_vec\_t = ovector, class alloc\_t = ovector\_alloc, class vec\_int\_t = ovector\_int\_base>class ode\_bv\_shoot\_grid< mat\_t, mat\_row\_t, func\_t, vec\_t, alloc\_vec\_t, alloc\_t, vec\_int\_t >

This class is experimental.

Default template arguments

- func\_t - [ode\\_func\\_t](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)
- vec\_int\_t - [ovector\\_int\\_base](#)

Definition at line 365 of file ode\_bv\_solve.h.

#### Public Member Functions

- int [solve\\_grid](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, vec\_t &yend, vec\_int\_t &index, size\_t nsol, vec\_t &xsol, mat\_t &ysol, mat\_t &err\_sol, mat\_t &dydx\_sol, func\_t &derivs)  
*Desc.*

#### Protected Member Functions

- int [solve\\_grid\\_fun](#) (size\_t nv, const vec\_t &tx, vec\_t &ty)  
*The shooting function to be solved by the multidimensional solver.*

#### Protected Attributes

- size\_t [l\\_nsol](#)  
*Desc.*
  - vec\_t \* [l\\_xsol](#)  
*Desc.*
  - mat\_t \* [l\\_ysol](#)  
*Desc.*
  - mat\_t \* [l\\_dydxsol](#)  
*Desc.*
  - mat\_t \* [l\\_errsol](#)  
*Desc.*
-

The documentation for this class was generated from the following file:

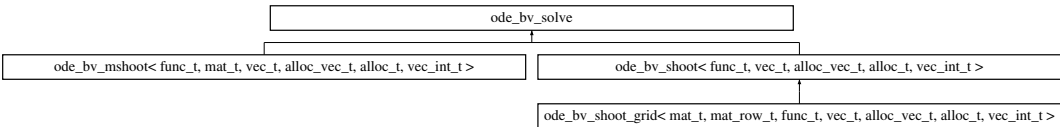
- ode\_bv\_solve.h

### 46.214 ode\_bv\_solve Class Reference

Base class for boundary-value ODE solvers.

```
#include <ode_bv_solve.h>
```

Inheritance diagram for ode\_bv\_solve:



#### 46.214.1 Detailed Description

This class is experimental.  
Definition at line 41 of file ode\_bv\_solve.h.

#### Data Fields

- int [verbose](#)  
Set output level.

#### Static Public Attributes

##### Values for index arrays

- static const int [unk](#) = 0  
Unknown on both the left and right boundaries.
- static const int [right](#) = 1  
Known on the right boundary.
- static const int [left](#) = 2  
Known on the left boundary.
- static const int [both](#) = 3  
Known on both the left and right boundaries.

The documentation for this class was generated from the following file:

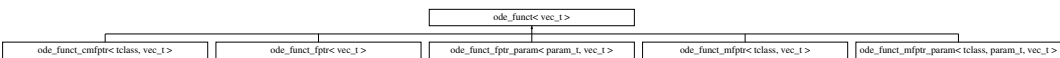
- ode\_bv\_solve.h

### 46.215 ode\_func< vec\_t > Class Template Reference

Ordinary differential equation function [abstract base].

```
#include <ode_func.h>
```

Inheritance diagram for ode\_func< vec\_t >:



## 46.215.1 Detailed Description

```
template<class vec_t = ovector_base>class ode_func< vec_t >
```

This base class provides the basic format for specifying ordinary differential equations to integrate with the O<sub>2</sub>scl ODE solvers. Select the appropriate child of this class according to the kind of functions which are to be given to the solver.

Definition at line 40 of file ode\_func.h.

## Public Member Functions

- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)=0  
*Compute the nv derivatives as a function of the nv functions specified in y at the point x.*

## Private Member Functions

- [ode\\_func](#) (const [ode\\_func](#) &)
- [ode\\_func](#) & [operator=](#) (const [ode\\_func](#) &)

The documentation for this class was generated from the following file:

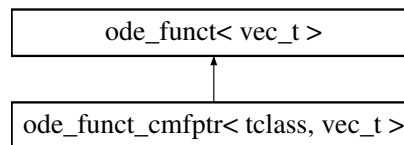
- ode\_func.h

## 46.216 ode\_func\_cmfp&lt; tclass, vec\_t &gt; Class Template Reference

Provide ODE functions in the form of const member function pointers.

```
#include <ode_func.h>
```

Inheritance diagram for ode\_func\_cmfp< tclass, vec\_t >:



## 46.216.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class ode_func_cmfp< tclass, vec_t >
```

Definition at line 256 of file ode\_func.h.

## Public Member Functions

- [ode\\_func\\_cmfp](#) (tclass \*tp, int(tclass::\*fp)(double x, size\_t nv, const vec\_t &y, vec\_t &dydx) const)  
*Create an object given a class and member function pointer.*
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)  
*Compute the nv derivatives as a function of the nv functions specified in y at the point x.*



## Protected Attributes

- `int(tclass::* fptr)(double x, size_t nv, const vec_t &y, vec_t &dydx) const`  
*The pointer to the member function.*
- `tclass * tptr`  
*The pointer to the class.*

## Private Member Functions

- `ode_funct_cmfp` (const `ode_funct_cmfp` &)
- `ode_funct_cmfp` & `operator=` (const `ode_funct_cmfp` &)

The documentation for this class was generated from the following file:

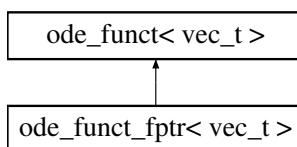
- `ode_funct.h`

## 46.217 ode\_funct\_fptr&lt; vec\_t &gt; Class Template Reference

Provide ODE functions in the form of function pointers.

```
#include <ode_funct.h>
```

Inheritance diagram for `ode_funct_fptr< vec_t >`:



## 46.217.1 Detailed Description

```
template<class vec_t = ovector_base>class ode_funct_fptr< vec_t >
```

Definition at line 68 of file `ode_funct.h`.

## Public Member Functions

- `ode_funct_fptr` (int(\*fp)(double, size\_t, const vec\_t &, vec\_t &))  
*Create an object given a function pointer.*
- virtual int `operator()` (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)  
*Compute the nv derivatives as a function of the nv functions specified in y at the point x.*

## Protected Attributes

- `int(* fptr)(double x, size_t nv, const vec_t &y, vec_t &dydx)`  
*The function pointer.*

## Private Member Functions

- `ode_funct_fptr` (const `ode_funct_fptr` &)
- `ode_funct_fptr` & `operator=` (const `ode_funct_fptr` &)

The documentation for this class was generated from the following file:

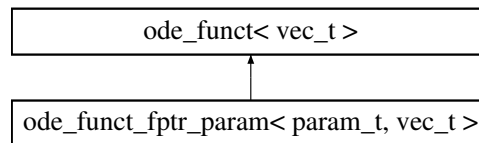
- ode\_funct.h

## 46.218 ode\_funct\_fptr\_param< param\_t, vec\_t > Class Template Reference

Provide ODE functions in the form of function pointers.

```
#include <ode_funct.h>
```

Inheritance diagram for ode\_funct\_fptr\_param< param\_t, vec\_t >:



### 46.218.1 Detailed Description

```
template<class param_t, class vec_t = ovector_base>class ode_funct_fptr_param< param_t, vec_t >
```

Definition at line 110 of file ode\_funct.h.

#### Public Member Functions

- [ode\\_funct\\_fptr\\_param](#) (int(\*fp)(double, size\_t, const vec\_t &, vec\_t &, param\_t &), param\_t &pa)  
*Create an object given a function pointer.*
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)  
*Compute the  $nv$  derivatives as a function of the  $nv$  functions specified in  $y$  at the point  $x$ .*

#### Protected Attributes

- int(\* [fptr](#))(double x, size\_t nv, const vec\_t &y, vec\_t &dydx, param\_t &)  
*The function pointer.*
- param\_t \* [pp](#)  
*The parameter.*

#### Private Member Functions

- [ode\\_funct\\_fptr\\_param](#) (const [ode\\_funct\\_fptr\\_param](#) &)
- [ode\\_funct\\_fptr\\_param](#) & [operator=](#) (const [ode\\_funct\\_fptr\\_param](#) &)

The documentation for this class was generated from the following file:

- ode\_funct.h

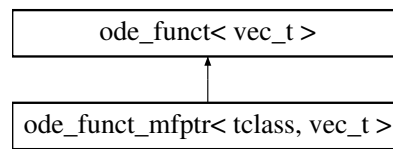
## 46.219 ode\_funct\_mfptr< tclass, vec\_t > Class Template Reference

Provide ODE functions in the form of member function pointers.

```
#include <ode_funct.h>
```

---

Inheritance diagram for ode\_funct\_mfptr< tclass, vec\_t >:



#### 46.219.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class ode_funct_mfptr< tclass, vec_t >
```

Definition at line 157 of file ode\_funct.h.

#### Public Member Functions

- [ode\\_funct\\_mfptr](#) (tclass \*tp, int(tclass::\*fp)(double x, size\_t nv, const vec\_t &y, vec\_t &dydx))  
*Create an object given a class and member function pointer.*
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)  
*Compute the `nv` derivatives as a function of the `nv` functions specified in `y` at the point `x`.*

#### Protected Attributes

- int(tclass::\* [fptr](#)) (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)  
*The pointer to the member function.*
- tclass \* [tptr](#)  
*The pointer to the class.*

#### Private Member Functions

- [ode\\_funct\\_mfptr](#) (const [ode\\_funct\\_mfptr](#) &)
- [ode\\_funct\\_mfptr](#) & [operator=](#) (const [ode\\_funct\\_mfptr](#) &)

The documentation for this class was generated from the following file:

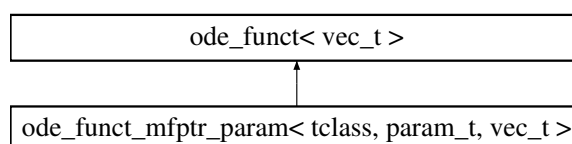
- ode\_funct.h

## 46.220 ode\_funct\_mfptr\_param< tclass, param\_t, vec\_t > Class Template Reference

Provide ODE functions in the form of member function pointers.

```
#include <ode_funct.h>
```

Inheritance diagram for ode\_funct\_mfptr\_param< tclass, param\_t, vec\_t >:



## 46.220.1 Detailed Description

```
template<class tclass, class param_t, class vec_t = ovector_base>class ode_func_mfptr_param< tclass, param_t, vec_t >
```

Definition at line 204 of file ode\_func.h.

## Public Member Functions

- [ode\\_func\\_mfptr\\_param](#) (tclass \*tp, int(tclass::\*fp)(double x, size\_t nv, const vec\_t &y, vec\_t &dydx, param\_t &), param\_t &pa)  
*Create an object given a class and member function pointer.*
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, vec\_t &dydx)  
*Compute the  $nv$  derivatives as a function of the  $nv$  functions specified in  $y$  at the point  $x$ .*

## Protected Attributes

- int(tclass::\* [fptr](#))(double x, size\_t nv, const vec\_t &y, vec\_t &dydx, param\_t &)  
*The pointer to the member function.*
- tclass \* [tptr](#)  
*The pointer to the class.*
- param\_t \* [pp](#)  
*The parameter.*

## Private Member Functions

- [ode\\_func\\_mfptr\\_param](#) (const [ode\\_func\\_mfptr\\_param](#) &)
- [ode\\_func\\_mfptr\\_param](#) & [operator=](#) (const [ode\\_func\\_mfptr\\_param](#) &)

The documentation for this class was generated from the following file:

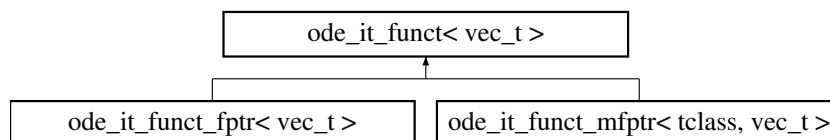
- ode\_func.h

## 46.221 ode\_it\_func&lt; vec\_t &gt; Class Template Reference

Function class for [ode\\_it\\_solve](#).

```
#include <ode_it_solve.h>
```

Inheritance diagram for ode\_it\_func< vec\_t >:



## 46.221.1 Detailed Description

```
template<class vec_t = ovector_base>class ode_it_func< vec_t >
```

Definition at line 42 of file ode\_it\_solve.h.

## Public Member Functions

- virtual double [operator\(\)](#) (size\_t ieq, double x, vec\_t &y)  
*Using  $x$  and  $y$ , return the value of function number  $ieq$ .*

The documentation for this class was generated from the following file:

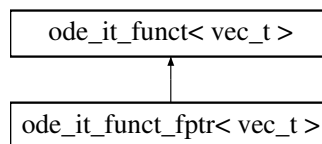
- ode\_it\_solve.h

## 46.222 ode\_it\_funct\_fptr&lt; vec\_t &gt; Class Template Reference

Function pointer for [ode\\_it\\_solve](#).

```
#include <ode_it_solve.h>
```

Inheritance diagram for ode\_it\_funct\_fptr< vec\_t >:



## 46.222.1 Detailed Description

```
template<class vec_t = ovector_base>class ode_it_funct_fptr< vec_t >
```

Definition at line 60 of file ode\_it\_solve.h.

## Public Member Functions

- [ode\\_it\\_funct\\_fptr](#) (double(\*fp)(size\_t, double, vec\_t &))  
*Create using a function pointer.*
- virtual double [operator\(\)](#) (size\_t ieq, double x, vec\_t &y)  
*Using  $x$  and  $y$ , return the value of function number  $ieq$ .*

## Protected Attributes

- double(\* [fptr](#))(size\_t ieq, double x, vec\_t &y)  
*The function pointer.*

The documentation for this class was generated from the following file:

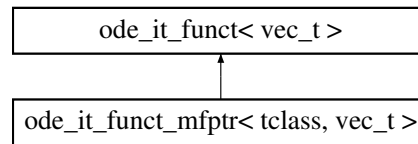
- ode\_it\_solve.h

## 46.223 ode\_it\_funct\_mfptr&lt; tclass, vec\_t &gt; Class Template Reference

Member function pointer for [ode\\_it\\_solve](#).

```
#include <ode_it_solve.h>
```

Inheritance diagram for ode\_it\_funct\_mfptr< tclass, vec\_t >:



#### 46.223.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class ode_it_func_t_mfptr< tclass, vec_t >
```

Definition at line 87 of file ode\_it\_solve.h.

#### Public Member Functions

- [ode\\_it\\_func\\_t\\_mfptr](#) (tclass \*tp, double(tclass::\*fp)(size\_t, double, vec\_t &))  
*Create using a class instance and member function.*
- virtual double [operator\(\)](#) (size\_t ieq, double x, vec\_t &y)  
*Using x and y, return the value of function number ieq.*

#### Protected Attributes

- tclass \* [tptr](#)  
*The class pointer.*
- double(tclass::\* [fptr](#))(size\_t ieq, double x, vec\_t &y)  
*The member function pointer.*

The documentation for this class was generated from the following file:

- ode\_it\_solve.h

## 46.224 ode\_it\_solve< func\_t, vec\_t, mat\_t, matrix\_row\_t, solver\_vec\_t, solver\_mat\_t > Class Template Reference

ODE solver using a generic linear solver to solve finite-difference equations.

```
#include <ode_it_solve.h>
```

#### 46.224.1 Detailed Description

```
template<class func_t = ode_it_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base, class matrix_row_t = omatrix_row, class solver_vec_t = ovector_base, class solver_mat_t = omatrix_base>class ode_it_solve< func_t, vec_t, mat_t, matrix_row_t, solver_vec_t, solver_mat_t >
```

#### Note

This class does not work with all matrix and vector types because using `operator[][]` would require it to be inefficient for use with sparse matrices.

**Idea for Future** Create a GSL-like `set()` and `iterate()` interface

**Idea for Future** Implement as a child of `ode_by_solve` ?

**Idea for Future** Max and average tolerance?

Definition at line 130 of file ode\_it\_solve.h.

## Public Member Functions

- int [set\\_solver](#) ([o2scl::linear\\_solver](#)< solver\_vec\_t, solver\_mat\_t > &ls)  
*Set the linear solver.*
- int [solve](#) (size\_t n\_grid, size\_t n\_eq, size\_t nb\_left, vec\_t &x, mat\_t &y, func\_t &derivs, func\_t &left, func\_t &right, solver\_mat\_t &mat, solver\_vec\_t &rhs, solver\_vec\_t &dy)  
*Solve derivs with boundary conditions left and right.*

## Data Fields

- bool **make\_mats**
- int [verbose](#)  
*Set level of output (default 0)*
- double **h**  
*Stepsize for finite differencing (default  $10^{-4}$ )*
- double [tol\\_rel](#)  
*Tolerance (default  $10^{-8}$ )*
- size\_t [niter](#)  
*Maximum number of iterations (default 30)*
- double [alpha](#)  
*Size of correction to apply (default 1.0)*
- [o2scl::linear\\_solver\\_hh](#) < solver\_vec\_t, solver\_mat\_t > [def\\_solver](#)  
*Default linear solver.*

## Protected Member Functions

- virtual double [fd\\_left](#) (size\_t ieq, size\_t ivar, double x, vec\_t &y)  
*Compute the derivatives of the LHS boundary conditions.*
- virtual double [fd\\_right](#) (size\_t ieq, size\_t ivar, double x, vec\_t &y)  
*Compute the derivatives of the RHS boundary conditions.*
- virtual double [fd\\_derivs](#) (size\_t ieq, size\_t ivar, double x, vec\_t &y)  
*Compute the finite-differenced part of the differential equations.*

## Protected Attributes

- [o2scl::linear\\_solver](#) < solver\_vec\_t, solver\_mat\_t > \* [solver](#)  
*Solver.*

## Storage for functions

- [ode\\_it\\_func\\_t](#)< vec\_t > \* **fl**
- [ode\\_it\\_func\\_t](#)< vec\_t > \* **fr**
- [ode\\_it\\_func\\_t](#)< vec\_t > \* **fd**

## 46.224.2 Member Function Documentation

**46.224.2.1** `template<class func_t = ode_it_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base, class matrix_row_t = omatrix_row, class solver_vec_t = ovector_base, class solver_mat_t = omatrix_base> int ode_it_solve< func_t, vec_t, mat_t, matrix_row_t, solver_vec_t, solver_mat_t >::solve ( size_t n_grid, size_t n_eq, size_t nb_left, vec_t &x, mat_t &y, func_t &derivs, func_t &left, func_t &right, solver_mat_t &mat, solver_vec_t &rhs, solver_vec_t &dy ) [inline]`

Given a grid of size `n_grid` and `n_eq` differential equations, solve them by relaxation. The grid is specified in `x`, which is a vector of size `n_grid`. The differential equations are given in `derivs`, the boundary conditions on the left hand side in `left`, and the boundary conditions on the right hand side in `right`. The number of boundary conditions on the left hand side is `nb_left`, and the number of boundary conditions on the right hand side should be `n_eq-nb_left`. The initial guess for the solution, a matrix of size `[n_grid][n_eq]` should be given in `y`. Upon success, `y` will contain an approximate solution of the differential

equations. The matrix `mat` is workspace of size `[n_grid*n_eq][n_grid*n_eq]`, and the vectors `rhs` and `y` are workspace of size `[n_grid*n_eq]`.

Definition at line 189 of file `ode_it_solve.h`.

```
46.224.2.2 template<class func_t = ode_it_func<>, class vec_t = ovector_base, class mat_t = omatrix_base, class matrix_row_t = omatrix_row, class
solver_vec_t = ovector_base, class solver_mat_t = omatrix_base> virtual double ode_it_solve< func_t, vec_t, mat_t, matrix_row_t,
solver_vec_t, solver_mat_t >::fd_left( size_t ieq, size_t ivar, double x, vec_t & y ) [inline, protected, virtual]
```

This function computes  $\partial f_{left,ieq}/\partial y_{ivar}$

Definition at line 356 of file `ode_it_solve.h`.

```
46.224.2.3 template<class func_t = ode_it_func<>, class vec_t = ovector_base, class mat_t = omatrix_base, class matrix_row_t = omatrix_row, class
solver_vec_t = ovector_base, class solver_mat_t = omatrix_base> virtual double ode_it_solve< func_t, vec_t, mat_t, matrix_row_t,
solver_vec_t, solver_mat_t >::fd_right( size_t ieq, size_t ivar, double x, vec_t & y ) [inline, protected, virtual]
```

This function computes  $\partial f_{right,ieq}/\partial y_{ivar}$

Definition at line 375 of file `ode_it_solve.h`.

```
46.224.2.4 template<class func_t = ode_it_func<>, class vec_t = ovector_base, class mat_t = omatrix_base, class matrix_row_t = omatrix_row, class
solver_vec_t = ovector_base, class solver_mat_t = omatrix_base> virtual double ode_it_solve< func_t, vec_t, mat_t, matrix_row_t,
solver_vec_t, solver_mat_t >::fd_derivs( size_t ieq, size_t ivar, double x, vec_t & y ) [inline, protected, virtual]
```

This function computes  $\partial f_{ieq}/\partial y_{ivar}$

Definition at line 395 of file `ode_it_solve.h`.

The documentation for this class was generated from the following file:

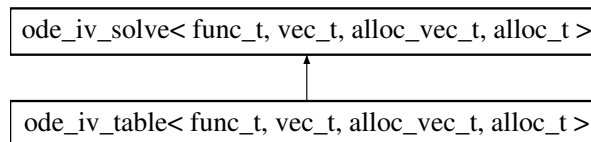
- `ode_it_solve.h`

## 46.225 ode\_iv\_solve< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Solve an initial-value ODE problems given an adaptive ODE stepper.

```
#include <ode_iv_solve.h>
```

Inheritance diagram for `ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >`:



### 46.225.1 Detailed Description

```
template<class func_t = ode_func<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>class ode_iv_solve<
func_t, vec_t, alloc_vec_t, alloc_t >
```

This class is experimental.

This class gives several functions which solve an initial value ODE problem. The functions [solve\\_final\\_value\(\)](#) give only the final value of the functions at the end of the ODE integration and are relatively fast.

The function [solve\\_store\(\)](#) stores the solution of the ODE over the full range into a set of vectors and matrices which are allocated



and specified by the user. This function is designed to give exactly the same results (though this cannot be guaranteed) as [solve\\_final\\_value\(\)](#) and additionally records some or all of the results from the adaptive steps which were taken.

The functions [solve\\_grid\(\)](#) works as in [solve\\_store\(\)](#) except that the solution is stored on a grid of points in the independent variable specified by the user, at the cost of taking extra steps to ensure that function values, derivatives, and errors are computed at each grid point.

All of these functions automatically evaluate the derivatives from the specified function at the initial point and user-specified initial derivatives are ignored. The total number of steps taken is limited by [ntrial](#) and [nsteps](#) stores the number of steps taken by the most recent solution. The variable [nsteps\\_out](#) is the maximum number of points in the interval for which verbose output will be given when [verbose](#) is greater than zero.

There is an example for the usage of this class in `examples/ex_ode.cpp` documented in the [Ordinary differential equations](#) section.

Default template arguments

- [func\\_t](#) - [ode\\_func\\_t](#)
- [vec\\_t](#) - [ovector\\_base](#)
- [alloc\\_vec\\_t](#) - [ovector](#)
- [alloc\\_t](#) - [ovector\\_alloc](#)

The default adaptive stepper is an object of type [gsl\\_astep](#).

**Idea for Future** The form of [solve\\_final\\_value\(\)](#) is very similar to that of [adapt\\_step::astep\\_full\(\)](#), but not quite the same. Maybe should probably be made to be consistent with each other?

Definition at line 84 of file `ode_iv_solve.h`.

## Public Member Functions

- virtual const char \* [type](#) ()  
*Return the type, "ode\_iv\_solve".*

## Main solver functions

- int [solve\\_final\\_value](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, vec\_t &yend, func\_t &derivs)  
*Solve the initial-value problem to get the final value.*
- int [solve\\_final\\_value](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, vec\_t &yend, vec\_t &yerr, func\_t &derivs)  
*Solve the initial-value problem to get the final value with errors.*
- int [solve\\_final\\_value](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, vec\_t &yend, vec\_t &yerr, vec\_t &dydx\_end, func\_t &derivs)  
*Solve the initial-value problem to get the final value, derivatives, and errors.*
- template<class mat\_t, class mat\_row\_t>  
int [solve\\_store](#) (double x0, double x1, double h, size\_t n, size\_t &n\_sol, vec\_t &x\_sol, mat\_t &y\_sol, mat\_t &yerr\_sol, mat\_t &dydx\_sol, func\_t &derivs, size\_t istart=0)  
*Solve the initial-value problem and store the associated output.*
- template<class mat\_t, class mat\_row\_t>  
int [solve\\_grid](#) (double h, size\_t n, size\_t nsol, vec\_t &xsol, mat\_t &ysol, mat\_t &err\_sol, mat\_t &dydx\_sol, func\_t &derivs)  
*Solve the initial-value problem from x0 to x1 over a grid storing derivatives and errors.*

## Data Fields

- int [verbose](#)  
*Set output level.*

- size\_t [nsteps\\_out](#)  
*Number of output points if [verbose](#) is greater than zero (default 10)*
- size\_t [ntrial](#)  
*Maximum number of applications of the adaptive stepper (default 1000)*
- size\_t [nsteps](#)  
*Number of adaptive steps employed.*

### Protected Member Functions

- virtual int [print\\_iter](#) (double x, size\_t nv, vec\_t &y)  
*Print out iteration information.*
- void [free](#) ()  
*Free allocated memory.*
- void [allocate](#) (size\_t n)  
*Allocate space for temporary vectors.*

### Protected Attributes

- alloc\_t [ao](#)  
*Memory allocator.*
- size\_t [mem\\_size](#)  
*Desc.*
- [adapt\\_step](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > \* [astp](#)  
*The adaptive stepper.*

### Desc

- alloc\_vec\_t [vtemp](#)
- alloc\_vec\_t [vtemp2](#)
- alloc\_vec\_t [vtemp3](#)
- alloc\_vec\_t [vtemp4](#)

### The adaptive stepper

- bool [exit\\_on\\_fail](#)  
*If true, stop the solution if the adaptive stepper fails (default true)*
- [gsl\\_astep](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > [gsl\\_astp](#)  
*The default adaptive stepper.*
- int [set\\_adapt\\_step](#) ([adapt\\_step](#)< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > &as)  
*Set the adaptive stepper to use.*

## 46.225.2 Member Function Documentation

**46.225.2.1** `template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int  
ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_final_value ( double x0, double x1, double h, size_t n, vec_t &ystart, vec_t  
&yend, func_t &derivs ) [inline]`

Given the `n` initial values of the functions in `ystart`, this function integrates the ODEs specified in `derivs` over the interval from `x0` to `x1` with an initial stepsize of `h`. The final values of the function are given in `yend` and the initial values of `yend` are ignored.

If [verbose](#) is greater than zero, The solution at less than or approximately equal to [nsteps\\_out](#) points will be written to `std::cout`. If [verbose](#) is greater than one, a character will be required after each selected point.

**Todo** Document if `yend` can be the same as `ystart`.

Definition at line 172 of file `ode_iv_solve.h`.

```
46.225.2.2 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int
ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_final_value ( double x0, double x1, double h, size_t n, vec_t & ystart, vec_t
& yend, vec_t & yerr, func_t & derivs ) [inline]
```

Given the  $n$  initial values of the functions in `ystart`, this function integrates the ODEs specified in `derivs` over the interval from  $x_0$  to  $x_1$  with an initial stepsize of  $h$ . The final values of the function are given in `yend` and the associated errors are given in `yerr`. The initial values of `yend` and `yerr` are ignored.

If `verbose` is greater than zero, The solution at less than or approximately equal to `nsteps_out` points will be written to `std::cout`. If `verbose` is greater than one, a character will be required after each selected point.

Definition at line 195 of file `ode_iv_solve.h`.

```
46.225.2.3 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int
ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_final_value ( double x0, double x1, double h, size_t n, vec_t & ystart, vec_t
& yend, vec_t & yerr, vec_t & dydx_end, func_t & derivs ) [inline]
```

Given the  $n$  initial values of the functions in `ystart`, this function integrates the ODEs specified in `derivs` over the interval from  $x_0$  to  $x_1$  with an initial stepsize of  $h$ . The final values of the function are given in `yend`, the derivatives in `dydx_end`, and the associated errors are given in `yerr`. The initial values of `yend` and `yerr` are ignored.

This function is designed to be relatively fast, avoiding extra copying of vectors back and forth.

If `verbose` is greater than zero, The solution at less than or approximately equal to `nsteps_out` points will be written to `std::cout`. If `verbose` is greater than one, a character will be required after each selected point.

This function computes `dydx_start` automatically and the values given by the user are ignored.

The solution fails if more than `ntrial` steps are required. This function will also fail if  $x_1 > x_0$  and  $h < 0$  or if  $x_1 < x_0$  but  $h > 0$ .

Definition at line 230 of file `ode_iv_solve.h`.

```
46.225.2.4 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>
template<class mat_t, class mat_row_t > int ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_store ( double x0, double x1,
double h, size_t n, size_t & n_sol, vec_t & x_sol, mat_t & y_sol, mat_t & yerr_sol, mat_t & dydx_sol, func_t & derivs, size_t istart = 0 )
[inline]
```

Initially, `x_sol` should be a vector of size `n_sol`, and `y_sol`, `dydx_sol`, and `yerr_sol` should be matrices with size `[n_sol][n]`. On exit, `n_sol` will be number of points store, less than or equal to the original value of `n_sol`. This function avoids performing extra calls to the adaptive stepper, and the table will be approximately evenly spaced.

This function is also designed to give the exactly the same results as `solve_final_value()`. This cannot be strictly guaranteed, but will likely hold in most applications.

This template function works with any matrix class `mat_t` which can be accessed using successive applications of operator[] and which has an associated class `mat_row_t` which returns a row of a matrix of type `mat_t` as an object with type `vec_t`.

If `verbose` is greater than zero, The solution at each internal point will be written to `std::cout`. If `verbose` is greater than one, a character will be required after each point.

**Idea for Future** It might be possible to remove some extra copying by removing the `yerr` and `dydx` vectors

Definition at line 425 of file `ode_iv_solve.h`.

```
46.225.2.5 template<class func_t = ode_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc>
template<class mat_t, class mat_row_t > int ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::solve_grid ( double h, size_t n,
size_t nsol, vec_t & x_sol, mat_t & y_sol, mat_t & err_sol, mat_t & dydx_sol, func_t & derivs ) [inline]
```

Initially, `x_sol` should be an array of size `nsol`, and `y_sol` should be a `omatrix` of size `[nsol][n]`. This function never takes a step larger than the grid size.

If `verbose` is greater than zero, The solution at each grid point will be written to `std::cout`. If `verbose` is greater than one, a

character will be required after each point.

**Idea for Future** Consider making a version of grid which gives the same answers as [solve\\_final\\_value\(\)](#). After each proposed step, it would go back and fill in the grid points if the proposed step was past the next grid point.

Definition at line 598 of file ode\_iv\_solve.h.

#### 46.225.3 Field Documentation

**46.225.3.1** `template<class func_t = ode_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> size_t ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::nsteps_out`

This is used in functions `solve_table()` and [solve\\_final\\_value\(\)](#) to control how often steps are output when verbose is greater than zero.

Definition at line 702 of file ode\_iv\_solve.h.

**46.225.3.2** `template<class func_t = ode_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> bool ode_iv_solve< func_t, vec_t, alloc_vec_t, alloc_t >::exit_on_fail`

If this is false, then failures in the adaptive stepper are ignored.

Definition at line 724 of file ode\_iv\_solve.h.

The documentation for this class was generated from the following file:

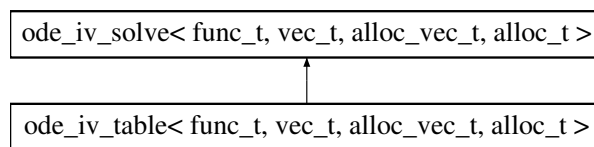
- ode\_iv\_solve.h

## 46.226 ode\_iv\_table< func\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Solve an initial-value ODE problem and store the result in a [table](#) object.

```
#include <ode_iv_table.h>
```

Inheritance diagram for `ode_iv_table< func_t, vec_t, alloc_vec_t, alloc_t >`:



#### 46.226.1 Detailed Description

```
template<class func_t = ode_funct<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> class ode_iv_table<
func_t, vec_t, alloc_vec_t, alloc_t >
```

This class is experimental.

Definition at line 43 of file ode\_iv\_table.h.

#### Public Member Functions

- `int solve_grid_table` (size\_t n, vec\_t &ystart, [table](#) &t, std::string x\_col, std::string y\_prefix, std::string dydx\_prefix, std::string yerr\_prefix, func\_t &derivs)

*Desc.*

- int [solve\\_store\\_table](#) (double x0, double x1, double h, size\_t n, vec\_t &ystart, size\_t &n\_sol, [table](#) &t, std::string x\_col, std::string y\_prefix, std::string dydx\_prefix, std::string yerr\_prefix, func\_t &derivs)

*Desc.*

The documentation for this class was generated from the following file:

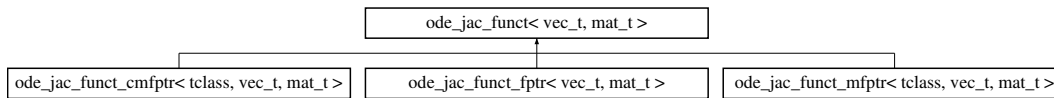
- ode\_iv\_table.h

## 46.227 ode\_jac\_funct< vec\_t, mat\_t > Class Template Reference

Ordinary differential equation Jacobian [abstract base].

```
#include <ode_jac_funct.h>
```

Inheritance diagram for ode\_jac\_funct< vec\_t, mat\_t >:



### 46.227.1 Detailed Description

```
template<class vec_t = ovector_base, class mat_t = omatrix_base>class ode_jac_funct< vec_t, mat_t >
```

This base class provides the basic format for specifying the Jacobian for ordinary differential equations to integrate with the O<sub>2</sub>scl ODE solvers. Select the appropriate child of this class according to the kind of functions which are to be given to the solver.

Definition at line 43 of file ode\_jac\_funct.h.

#### Public Member Functions

- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx)=0  
*Compute the derivatives  $dfdx$  and the Jacobian matrix  $dfdy$  given  $y$  at the point  $x$ .*

#### Private Member Functions

- [ode\\_jac\\_funct](#) (const [ode\\_jac\\_funct](#) &)
- [ode\\_jac\\_funct](#) & [operator=](#) (const [ode\\_jac\\_funct](#) &)

The documentation for this class was generated from the following file:

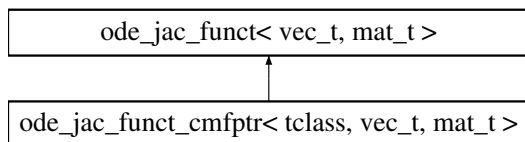
- ode\_jac\_funct.h

## 46.228 ode\_jac\_funct\_cmfp< tclass, vec\_t, mat\_t > Class Template Reference

Provide ODE Jacobian in the form of const member function pointers.

```
#include <ode_jac_funct.h>
```

Inheritance diagram for ode\_jac\_funct\_cmfp< tclass, vec\_t, mat\_t >:



#### 46.228.1 Detailed Description

template<class tclass, class vec\_t = ovector\_base, class mat\_t = omatrix\_base>class ode\_jac\_funct\_cmfptra< tclass, vec\_t, mat\_t >

Definition at line 177 of file ode\_jac\_funct.h.

#### Public Member Functions

- [ode\\_jac\\_funct\\_cmfptra](#) (tclass \*tp, int(tclass::\*fp)(double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx) const)  
Create an object given a class and member function pointer.
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx)  
Compute the derivatives  $dfdx$  and the Jacobian matrix  $dfdy$  given  $y$  at the point  $x$ .

#### Protected Attributes

- int(tclass::\* [fptr](#)) (double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx) const  
The pointer to the member function.
- tclass \* [tptr](#)  
The pointer to the class.

#### Private Member Functions

- [ode\\_jac\\_funct\\_cmfptra](#) (const [ode\\_jac\\_funct\\_cmfptra](#) &)
- [ode\\_jac\\_funct\\_cmfptra](#) & [operator=](#) (const [ode\\_jac\\_funct\\_cmfptra](#) &)

The documentation for this class was generated from the following file:

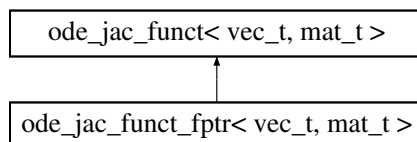
- ode\_jac\_funct.h

#### 46.229 ode\_jac\_funct\_fptr< vec\_t, mat\_t > Class Template Reference

Provide ODE Jacobian in the form of function pointers.

```
#include <ode_jac_funct.h>
```

Inheritance diagram for ode\_jac\_funct\_fptr< vec\_t, mat\_t >:



## 46.229.1 Detailed Description

```
template<class vec_t = ovector_base, class mat_t = omatrix_base>class ode_jac_funcn_fptr< vec_t, mat_t >
```

Definition at line 72 of file ode\_jac\_funcn.h.

## Public Member Functions

- [ode\\_jac\\_funcn\\_fptr](#) (int(\*fp)(double, size\_t, const vec\_t &, mat\_t &, vec\_t &))  
*Create an object given a function pointer.*
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx)  
*Compute the derivatives  $dfdx$  and the Jacobian matrix  $dfdy$  given  $y$  at the point  $x$ .*

## Protected Attributes

- int(\* [fptr](#)) (double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx)  
*The function pointer.*

## Private Member Functions

- [ode\\_jac\\_funcn\\_fptr](#) (const [ode\\_jac\\_funcn\\_fptr](#) &)
- [ode\\_jac\\_funcn\\_fptr](#) & [operator=](#) (const [ode\\_jac\\_funcn\\_fptr](#) &)

The documentation for this class was generated from the following file:

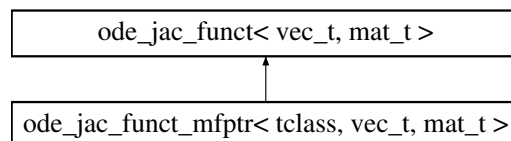
- ode\_jac\_funcn.h

## 46.230 ode\_jac\_funcn\_mfptr&lt; tclass, vec\_t, mat\_t &gt; Class Template Reference

Provide ODE Jacobian in the form of member function pointers.

```
#include <ode_jac_funcn.h>
```

Inheritance diagram for ode\_jac\_funcn\_mfptr< tclass, vec\_t, mat\_t >:



## 46.230.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base, class mat_t = omatrix_base>class ode_jac_funcn_mfptr< tclass, vec_t, mat_t >
```

Definition at line 122 of file ode\_jac\_funcn.h.

## Public Member Functions

- [ode\\_jac\\_funcn\\_mfptr](#) (tclass \*tp, int(tclass::\*fp)(double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx))  
*Create an object given a class and member function pointer.*
- virtual int [operator\(\)](#) (double x, size\_t nv, const vec\_t &y, mat\_t &dfdy, vec\_t &dfdx)  
*Compute the derivatives  $dfdx$  and the Jacobian matrix  $dfdy$  given  $y$  at the point  $x$ .*

## Protected Attributes

- `int(tclass::* fptr)(double x, size_t nv, const vec_t &y, mat_t &dfdy, vec_t &dfdx)`  
*The pointer to the member function.*
- `tclass * tptr`  
*The pointer to the class.*

## Private Member Functions

- `ode_jac_funcn_mfptr` (const `ode_jac_funcn_mfptr` &)
- `ode_jac_funcn_mfptr` & `operator=` (const `ode_jac_funcn_mfptr` &)

The documentation for this class was generated from the following file:

- `ode_jac_funcn.h`

## 46.231 ode\_step&lt; func\_t, vec\_t &gt; Class Template Reference

ODE stepper base [abstract base].

```
#include <ode_step.h>
```

Inheritance diagram for `ode_step< func_t, vec_t >`:



## 46.231.1 Detailed Description

```
template<class func_t = ode_funcn<>, class vec_t = ovector_base>class ode_step< func_t, vec_t >
```

Definition at line 37 of file `ode_step.h`.

## Public Member Functions

- virtual `int get_order()`  
*Return the order of the ODE stepper.*
- virtual `int step` (double x, double h, size\_t n, vec\_t &y, vec\_t &dydx, vec\_t &yout, vec\_t &yerr, vec\_t &dydx\_out, func\_t &derivs)=0  
*Perform an integration step.*

## Protected Attributes

- `int order`  
*The order of the ODE stepper.*

## 46.231.2 Member Function Documentation

```
46.231.2.1 template<class func_t = ode_funcn<>, class vec_t = ovector_base> virtual int ode_step< func_t, vec_t >::get_order ( )
[inline, virtual]
```

This is used, for example, by `gsl_astep` to adaptively adjust the stepsize.

Definition at line 62 of file `ode_step.h`.



46.231.2.2 `template<class func_t = ode_func_t<>, class vec_t = ovector_base> virtual int ode_step< func_t, vec_t >::step ( double x, double h, size_t n, vec_t & y, vec_t & dydx, vec_t & yout, vec_t & yerr, vec_t & dydx_out, func_t & derivs ) [pure virtual]`

Given initial value of the n-dimensional function in `y` and the derivative in `dydx` (which must generally be computed beforehand) at the point `x`, take a step of size `h` giving the result in `yout`, the uncertainty at  $x+h$  in `yerr`, and the new derivative at  $x+h$  in `dydx_out` using function `derivs` to calculate derivatives. Implementations which do not calculate `yerr` and/or `dydx_out` do not reference these variables so that a blank `vec_t` can be given. All of the current O2scl implementations allow `yout=y` and `dydx_out=dydx` if necessary

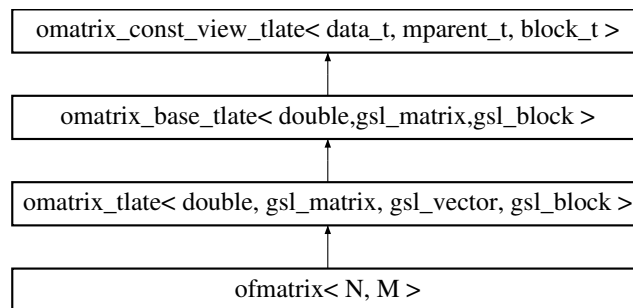
Implemented in [gsl\\_rk8pd\\_fast< N, func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#), [gsl\\_rkf45\\_fast< N, func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#), [gsl\\_rkck\\_fast< N, func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#), [gsl\\_rk8pd< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#), [gsl\\_rkck< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#), and [gsl\\_rkf45< func\\_t, vec\\_t, alloc\\_vec\\_t, alloc\\_t >](#).

The documentation for this class was generated from the following file:

- [ode\\_step.h](#)

## 46.232 ofmatrix< N, M > Class Template Reference

Inheritance diagram for `ofmatrix< N, M >`:



### 46.232.1 Detailed Description

`template<size_t N, size_t M>class ofmatrix< N, M >`

Definition at line 1334 of file `omatrix_tlate.h`.

The documentation for this class was generated from the following file:

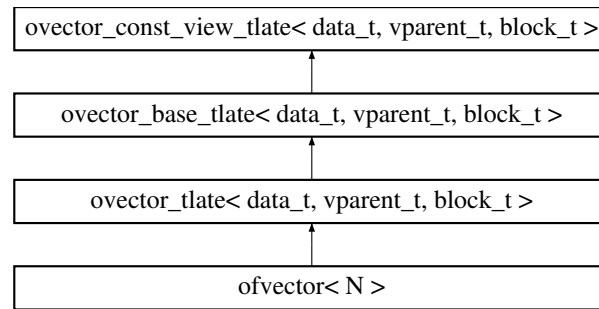
- [omatrix\\_tlate.h](#)

## 46.233 ofvector< N > Class Template Reference

A vector where the memory allocation is performed in the constructor.

`#include <ovector_tlate.h>`

Inheritance diagram for `ofvector< N >`:



#### 46.234.1 Detailed Description

```
template<size_t N = 0>class ofvector< N >
```

This can be useful, for example to easily make C-style arrays of [ovector](#) objects with a fixed size. For example,

```
ofvector<8> x[10];
```

would mean x is a 10-dimensional array of [ovector](#) object with initial length 8.

**Idea for Future** Consider making [allocate\(\)](#) and [free\(\)](#) functions private for this class?

Definition at line 1896 of file [ovector\\_tlate.h](#).

The documentation for this class was generated from the following file:

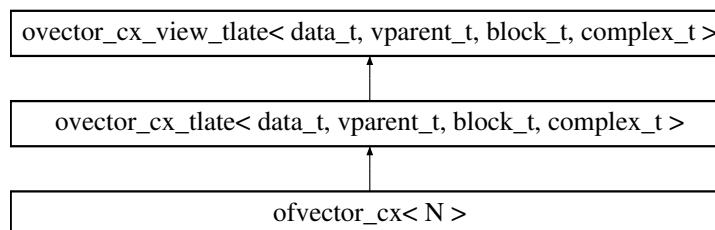
- [ovector\\_tlate.h](#)

## 46.234 ofvector\_cx< N > Class Template Reference

A complex vector where the memory allocation is performed in the constructor.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for [ofvector\\_cx< N >](#):



#### 46.234.1 Detailed Description

```
template<size_t N = 0>class ofvector_cx< N >
```

Definition at line 996 of file [ovector\\_cx\\_tlate.h](#).

The documentation for this class was generated from the following file:

- [ovector\\_cx\\_tlate.h](#)

## 46.235 `omatrix_alloc` Class Reference

A simple class to provide an `allocate()` function for `omatrix`.

```
#include <omatrix_tlate.h>
```

### 46.235.1 Detailed Description

Definition at line 1311 of file `omatrix_tlate.h`.

#### Public Member Functions

- void `allocate` (`omatrix` &o, size\_t i, size\_t j)  
*Allocate v for i elements.*
- void `free` (`omatrix` &o, size\_t i)  
*Free memory.*

The documentation for this class was generated from the following file:

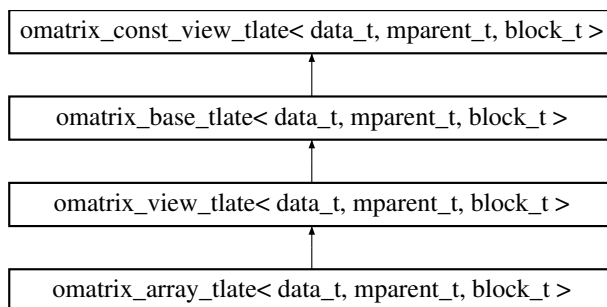
- [omatrix\\_tlate.h](#)

## 46.236 `omatrix_array_tlate< data_t, mparent_t, block_t >` Class Template Reference

Create a matrix from an array.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_array_tlate< data_t, mparent_t, block_t >`:



### 46.236.1 Detailed Description

```
template<class data_t, class mparent_t, class block_t>class omatrix_array_tlate< data_t, mparent_t, block_t >
```

Definition at line 1015 of file `omatrix_tlate.h`.

#### Public Member Functions

- `omatrix_array_tlate` (`data_t` \*dat, size\_t ltda, size\_t sz1, size\_t sz2)  
*Create a vector from dat with size n.*

The documentation for this class was generated from the following file:

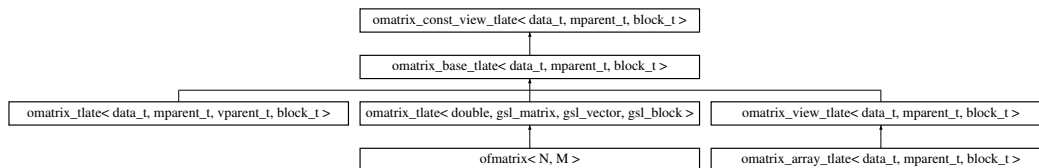
- [omatrix\\_tlate.h](#)

## 46.237 `omatrix_base_tlate< data_t, mparent_t, block_t >` Class Template Reference

A base class for `omatrix` and `omatrix_view`.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_base_tlate< data_t, mparent_t, block_t >`:



### 46.237.1 Detailed Description

```
template<class data_t, class mparent_t, class block_t>class omatrix_base_tlate< data_t, mparent_t, block_t >
```

Definition at line 260 of file `omatrix_tlate.h`.

#### Public Member Functions

##### Copy constructors

- `omatrix_base_tlate` (const `omatrix_base_tlate` &*v*)  
*Shallow copy constructor - create a new view of the same matrix.*
- `omatrix_base_tlate` & `operator=` (const `omatrix_base_tlate` &*v*)  
*Shallow copy constructor - create a new view of the same matrix.*

##### Get and set methods

- `data_t * operator[]` (size\_t *i*)  
*Array-like indexing.*
- const `data_t * operator[]` (size\_t *i*) const  
*Array-like indexing.*
- `data_t & operator()` (size\_t *i*, size\_t *j*)  
*Array-like indexing.*
- const `data_t & operator()` (size\_t *i*, size\_t *j*) const  
*Array-like indexing.*
- `data_t * get_ptr` (size\_t *i*, size\_t *j*)  
*Get pointer (with optional range-checking)*
- int `set` (size\_t *i*, size\_t *j*, data\_t *val*)  
*Set (with optional range-checking)*
- int `set_all` (double *val*)  
*Set all of the value to be the value val.*

##### Other methods

- `mparent_t * get_gsl_matrix` ()  
*Return a gsl matrix.*

##### Arithmetic

- `omatrix_base_tlate< data_t, mparent_t, block_t > & operator+=` (const `omatrix_base_tlate< data_t, mparent_t, block_t >` &*x*)  
*operator+=*
- `omatrix_base_tlate< data_t, mparent_t, block_t > & operator-=` (const `omatrix_base_tlate< data_t, mparent_t, block_t >` &*x*)

- operator-=*
- `omatrix_base_tlate< data_t, mparent_t, block_t > & operator+= (const data_t &y)`  
*operator+=*
- `omatrix_base_tlate< data_t, mparent_t, block_t > & operator-= (const data_t &y)`  
*operator-=*
- `omatrix_base_tlate< data_t, mparent_t, block_t > & operator*= (const data_t &y)`  
*operator\*=*

**Protected Member Functions**

- `omatrix_base_tlate ()`  
*The default constructor.*

The documentation for this class was generated from the following file:

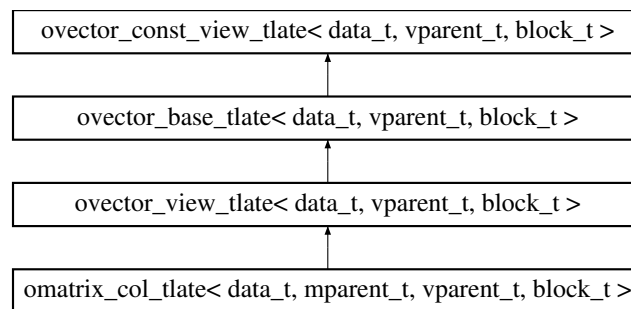
- `omatrix_tlate.h`

**46.238 `omatrix_col_tlate< data_t, mparent_t, vparent_t, block_t >` Class Template Reference**

Create a vector from a column of a matrix.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_col_tlate< data_t, mparent_t, vparent_t, block_t >`:

**46.238.1 Detailed Description**

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_col_tlate< data_t, mparent_t, vparent_t, block_t >
```

**Idea for Future** Also do a umatrix constructor since we can't do that with uvectors

Definition at line 1104 of file `omatrix_tlate.h`.

**Public Member Functions**

- `omatrix_col_tlate (omatrix_base_tlate< data_t, mparent_t, block_t > &m, size_t i)`  
*Create a vector from col i of matrix m.*

The documentation for this class was generated from the following file:

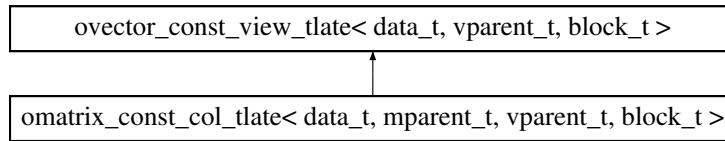
- `omatrix_tlate.h`

**46.239 `omatrix_const_col_tlate< data_t, mparent_t, vparent_t, block_t >` Class Template Reference**

Create a const vector from a column of a matrix.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_const_col_tlate< data_t, mparent_t, vparent_t, block_t >`:

**46.239.1 Detailed Description**

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_const_col_tlate< data_t, mparent_t, vparent_t, block_t >
```

Definition at line 1131 of file `omatrix_tlate.h`.

**Public Member Functions**

- [`omatrix\_const\_col\_tlate`](#) (const [`omatrix\_base\_tlate< data\_t, mparent\_t, block\_t >`](#) &m, size\_t i)  
*Create a vector from col i of matrix m.*

The documentation for this class was generated from the following file:

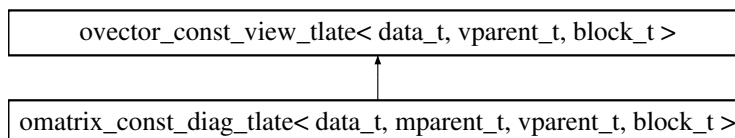
- [`omatrix\_tlate.h`](#)

**46.240 `omatrix_const_diag_tlate< data_t, mparent_t, vparent_t, block_t >` Class Template Reference**

Create a vector from the main diagonal.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_const_diag_tlate< data_t, mparent_t, vparent_t, block_t >`:

**46.240.1 Detailed Description**

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_const_diag_tlate< data_t, mparent_t, vparent_t, block_t >
```

Definition at line 1176 of file `omatrix_tlate.h`.

**Public Member Functions**

- [`omatrix\_const\_diag\_tlate`](#) (const [`omatrix\_view\_tlate< data\_t, mparent\_t, block\_t >`](#) &m)

Create a vector of the diagonal of matrix  $m$ .

The documentation for this class was generated from the following file:

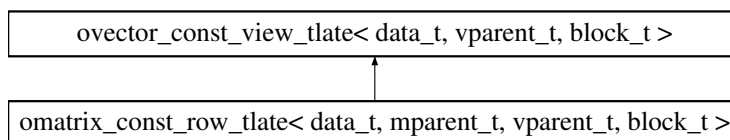
- [omatrix\\_tlate.h](#)

## 46.241 `omatrix_const_row_tlate< data_t, mparent_t, vparent_t, block_t >` Class Template Reference

Create a const vector from a row of a matrix.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_const_row_tlate< data_t, mparent_t, vparent_t, block_t >`:



### 46.241.1 Detailed Description

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_const_row_tlate< data_t, mparent_t, vparent_t, block_t >
```

Definition at line 1073 of file `omatrix_tlate.h`.

#### Public Member Functions

- [omatrix\\_const\\_row\\_tlate](#) (const [omatrix\\_base\\_tlate< data\\_t, mparent\\_t, block\\_t >](#) &m, size\_t i)  
Create a vector from row  $i$  of matrix  $m$ .

The documentation for this class was generated from the following file:

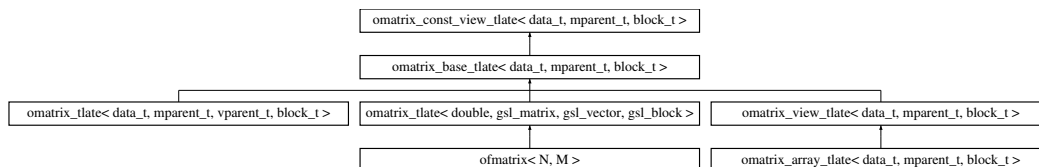
- [omatrix\\_tlate.h](#)

## 46.242 `omatrix_const_view_tlate< data_t, mparent_t, block_t >` Class Template Reference

A const matrix view of `omatrix` objects.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_const_view_tlate< data_t, mparent_t, block_t >`:



## 46.242.1 Detailed Description

```
template<class data_t, class mparent_t, class block_t>class omatrix_const_view_tlate< data_t, mparent_t, block_t >
```

Definition at line 55 of file `omatrix_tlate.h`.

## Public Member Functions

## Copy constructors

- `omatrix_const_view_tlate` (const `omatrix_const_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- `omatrix_const_view_tlate` & `operator=` (const `omatrix_const_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same matrix.*

## Get and set methods

- const `data_t` \* `operator[]` (size\_t i) const  
*Array-like indexing.*
- const `data_t` & `operator()` (size\_t i, size\_t j) const  
*Array-like indexing.*
- `data_t` `get` (size\_t i, size\_t j) const  
*Get (with optional range-checking)*
- `data_t` \* `get_ptr` (size\_t i, size\_t j)  
*Get pointer (with optional range-checking)*
- const `data_t` \* `get_const_ptr` (size\_t i, size\_t j) const  
*Get pointer (with optional range-checking)*
- size\_t `rows` () const  
*Method to return number of rows.*
- size\_t `cols` () const  
*Method to return number of columns.*
- size\_t `tda` () const  
*Method to return matrix tda.*

## Other methods

- bool `is_owner` () const  
*Return true if this object owns the data it refers to.*
- `data_t` `max` () const  
*The largest matrix element.*
- `data_t` `min` () const  
*The smallest matrix element.*
- const `mparent_t` \* `get_gsl_matrix_const` () const  
*Return a const gsl matrix.*

## Protected Member Functions

- `omatrix_const_view_tlate` ()  
*The default constructor.*

## 46.242.2 Member Function Documentation

```
46.242.2.1 template<class data_t, class mparent_t, class block_t> size_t omatrix_const_view_tlate< data_t, mparent_t, block_t >::rows ( )
const [inline]
```

If no memory has been allocated, this will quietly return zero.

Definition at line 179 of file `omatrix_tlate.h`.



```
46.242.2.2  template<class data_t, class mparent_t, class block_t> size_t omatrix_const_view_tlate< data_t, mparent_t, block_t >::cols ( )
            const [inline]
```

If no memory has been allocated, this will quietly return zero.

Definition at line 188 of file `omatrix_tlate.h`.

```
46.242.2.3  template<class data_t, class mparent_t, class block_t> size_t omatrix_const_view_tlate< data_t, mparent_t, block_t >::tda ( )
            const [inline]
```

If no memory has been allocated, this will quietly return zero.

Definition at line 197 of file `omatrix_tlate.h`.

```
46.242.2.4  template<class data_t, class mparent_t, class block_t> bool omatrix_const_view_tlate< data_t, mparent_t, block_t >::is_owner ( )
            const [inline]
```

This can be used to determine if an object is a "matrix\_view", or a "matrix". If `is_owner()` is true, then it is an `omatrix_tlate` object.

Definition at line 210 of file `omatrix_tlate.h`.

The documentation for this class was generated from the following file:

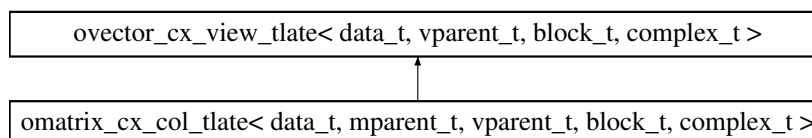
- [omatrix\\_tlate.h](#)

## 46.243 `omatrix_cx_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from a column of a matrix.

```
#include <omatrix_cx_tlate.h>
```

Inheritance diagram for `omatrix_cx_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`:



### 46.243.1 Detailed Description

```
template<class data_t, class mparent_t, class vparent_t, class block_t, class complex_t>class omatrix_cx_col_tlate< data_t, mparent_t, vparent_t,
block_t, complex_t >
```

Definition at line 659 of file `omatrix_cx_tlate.h`.

#### Public Member Functions

- `omatrix_cx_col_tlate` (`omatrix_cx_view_tlate< data_t, mparent_t, block_t, complex_t > &m`, `size_t i`)  
Create a vector from `col i` of matrix `m`.

The documentation for this class was generated from the following file:

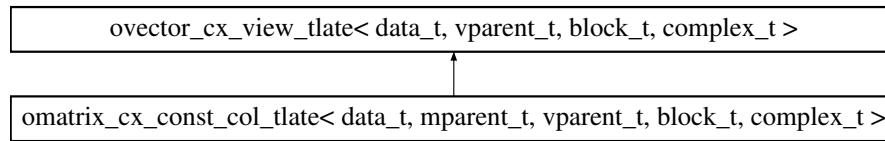
- [omatrix\\_cx\\_tlate.h](#)

**46.244 `omatrix_cx_const_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >` Class Template Reference**

Create a vector from a column of a matrix.

```
#include <omatrix_cx_tlate.h>
```

Inheritance diagram for `omatrix_cx_const_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`:

**46.244.1 Detailed Description**

```
template<class data_t, class mparent_t, class vparent_t, class block_t, class complex_t>class omatrix_cx_const_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >
```

Definition at line 679 of file `omatrix_cx_tlate.h`.

**Public Member Functions**

- [omatrix\\_cx\\_const\\_col\\_tlate](#) ([omatrix\\_cx\\_view\\_tlate< data\\_t, mparent\\_t, block\\_t, complex\\_t > &m](#), size\_t i)  
*Create a vector from col i of matrix m.*

The documentation for this class was generated from the following file:

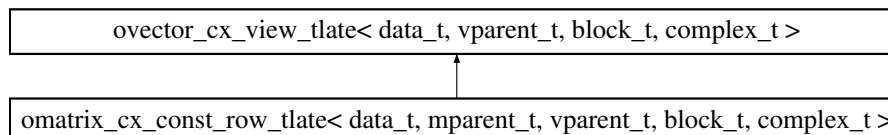
- [omatrix\\_cx\\_tlate.h](#)

**46.245 `omatrix_cx_const_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >` Class Template Reference**

Create a vector from a row of a matrix.

```
#include <omatrix_cx_tlate.h>
```

Inheritance diagram for `omatrix_cx_const_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`:

**46.245.1 Detailed Description**

```
template<class data_t, class mparent_t, class vparent_t, class block_t, class complex_t>class omatrix_cx_const_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >
```

Definition at line 639 of file `omatrix_cx_tlate.h`.

## Public Member Functions

- [`omatrix\_cx\_const\_row\_tlate`](#) (const [`omatrix\_cx\_view\_tlate< data\_t, mparent\_t, block\_t, complex\_t >`](#) &m, size\_t i)  
*Create a vector from row i of matrix m.*

The documentation for this class was generated from the following file:

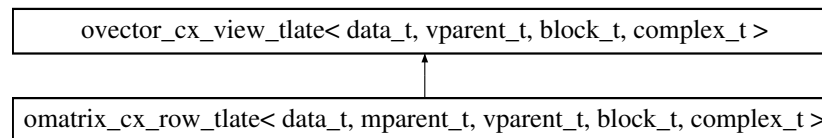
- [`omatrix\_cx\_tlate.h`](#)

46.246 `omatrix_cx_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from a row of a matrix.

```
#include <omatrix_cx_tlate.h>
```

Inheritance diagram for `omatrix_cx_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`:



## 46.246.1 Detailed Description

```
template<class data_t, class mparent_t, class vparent_t, class block_t, class complex_t>class omatrix_cx_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >
```

Definition at line 619 of file `omatrix_cx_tlate.h`.

## Public Member Functions

- [`omatrix\_cx\_row\_tlate`](#) ([`omatrix\_cx\_view\_tlate< data\_t, mparent\_t, block\_t, complex\_t >`](#) &m, size\_t i)  
*Create a vector from row i of matrix m.*

The documentation for this class was generated from the following file:

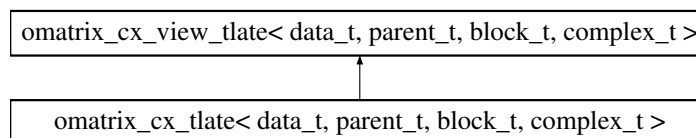
- [`omatrix\_cx\_tlate.h`](#)

46.247 `omatrix_cx_tlate< data_t, parent_t, block_t, complex_t >` Class Template Reference

A matrix of double-precision numbers.

```
#include <omatrix_cx_tlate.h>
```

Inheritance diagram for `omatrix_cx_tlate< data_t, parent_t, block_t, complex_t >`:



## 46.247.1 Detailed Description

```
template<class data_t, class parent_t, class block_t, class complex_t>class omatrix_cx_tlate< data_t, parent_t, block_t, complex_t >
```

Definition at line 389 of file `omatrix_cx_tlate.h`.

## Public Member Functions

## Standard constructor

- `omatrix_cx_tlate` (`size_t r=0`, `size_t c=0`)  
*Create an omatrix of size  $n$  with owner as 'true'.*

## Copy constructors

- `omatrix_cx_tlate` (`const omatrix_cx_tlate &v`)  
*Deep copy constructor; allocate new space and make a copy.*
- `omatrix_cx_tlate` (`const omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t > &v`)  
*Deep copy constructor; allocate new space and make a copy.*

## Memory allocation

- `int allocate` (`size_t nrows`, `size_t ncols`)  
*Allocate memory for size  $n$  after freeing any memory presently in use.*
- `int free` ()  
*Free the memory.*

## Other methods

- `omatrix_cx_tlate< data_t, parent_t, block_t, complex_t > transpose` ()  
*Compute the transpose.*
- `omatrix_cx_tlate< data_t, parent_t, block_t, complex_t > htranspose` ()  
*Compute the conjugate transpose.*

## 46.247.2 Member Function Documentation

```
46.247.2.1 template<class data_t, class parent_t, class block_t, class complex_t> int omatrix_cx_tlate< data_t, parent_t, block_t, complex_t
>::free ( ) [inline]
```

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 573 of file `omatrix_cx_tlate.h`.

The documentation for this class was generated from the following file:

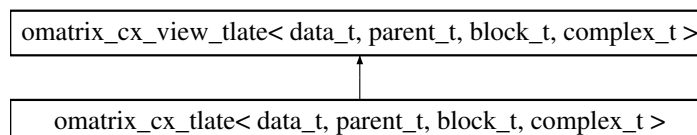
- [omatrix\\_cx\\_tlate.h](#)

46.248 `omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t >` Class Template Reference

A matrix view of double-precision numbers.

```
#include <omatrix_cx_tlate.h>
```

Inheritance diagram for `omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t >`:



## 46.248.1 Detailed Description

```
template<class data_t, class parent_t, class block_t, class complex_t>class omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t >
```

Definition at line 48 of file `omatrix_cx_tlate.h`.

## Public Member Functions

## Copy constructors

- `omatrix_cx_view_tlate` (const `omatrix_cx_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- `omatrix_cx_view_tlate` & `operator=` (const `omatrix_cx_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same matrix.*

## Get and set methods

- `complex_t * operator[]` (size\_t i)  
*Array-like indexing.*
- const `complex_t * operator[]` (size\_t i) const  
*Array-like indexing.*
- `complex_t & operator()` (size\_t i, size\_t j)  
*Array-like indexing.*
- const `complex_t & operator()` (size\_t i, size\_t j) const  
*Array-like indexing.*
- `complex_t get` (size\_t i, size\_t j) const  
*Get (with optional range-checking)*
- `std::complex< data_t > get_stl` (size\_t i, size\_t j) const  
*Get STL-like complex number (with optional range-checking)*
- `data_t real` (size\_t i, size\_t j) const  
*Get real part (with optional range-checking)*
- `data_t imag` (size\_t i, size\_t j) const  
*Get imaginary part (with optional range-checking)*
- `complex_t * get_ptr` (size\_t i, size\_t j)  
*Get pointer (with optional range-checking)*
- const `complex_t * get_const_ptr` (size\_t i, size\_t j) const  
*Get pointer (with optional range-checking)*
- int `set` (size\_t i, size\_t j, complex\_t &val)  
*Set (with optional range-checking)*
- int `set` (size\_t i, size\_t j, data\_t vr, data\_t vi)  
*Set (with optional range-checking)*
- int `set_real` (size\_t i, size\_t j, data\_t vr)  
*Set (with optional range-checking)*
- int `set_imag` (size\_t i, size\_t j, data\_t vi)  
*Set (with optional range-checking)*
- int `set_all` (complex\_t &val)  
*Set all.*
- size\_t `rows` () const  
*Method to return number of rows.*
- size\_t `cols` () const  
*Method to return number of columns.*
- size\_t `tda` () const  
*Method to return matrix tda.*

## Other methods

- bool `is_owner` () const  
*Return true if this object owns the data it refers to.*

## 46.248.2 Member Function Documentation

46.248.2.1 `template<class data_t, class parent_t, class block_t, class complex_t> size_t omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t>::rows ( ) const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 340 of file omatrix\_cx\_tlate.h.

46.248.2.2 `template<class data_t, class parent_t, class block_t, class complex_t> size_t omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t>::cols ( ) const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 349 of file omatrix\_cx\_tlate.h.

46.248.2.3 `template<class data_t, class parent_t, class block_t, class complex_t> size_t omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t>::tda ( ) const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 358 of file omatrix\_cx\_tlate.h.

The documentation for this class was generated from the following file:

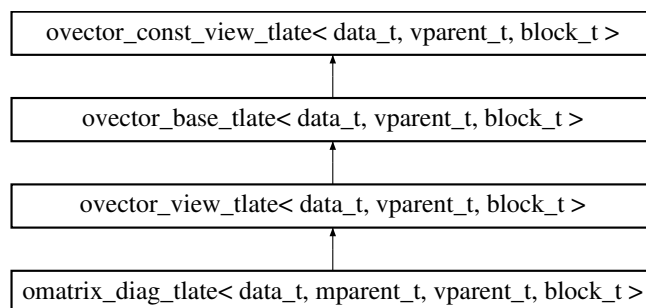
- [omatrix\\_cx\\_tlate.h](#)

## 46.249 omatrix\_diag\_tlate&lt; data\_t, mparent\_t, vparent\_t, block\_t &gt; Class Template Reference

Create a vector from the main diagonal.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for omatrix\_diag\_tlate< data\_t, mparent\_t, vparent\_t, block\_t >:



## 46.249.1 Detailed Description

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_diag_tlate< data_t, mparent_t, vparent_t, block_t >
```

Definition at line 1158 of file omatrix\_tlate.h.

## Public Member Functions

- [omatrix\\_diag\\_tlate](#) ([omatrix\\_view\\_tlate](#)< data\_t, mparent\_t, block\_t > &m)  
*Create a vector of the diagonal of matrix m.*

The documentation for this class was generated from the following file:

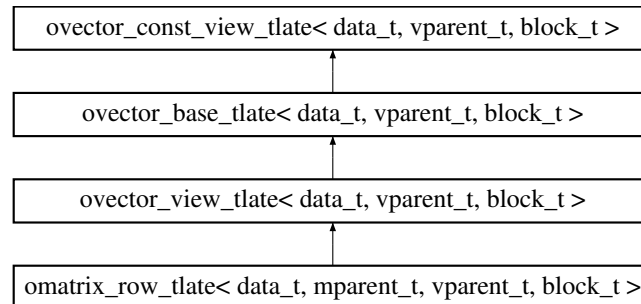
- [omatrix\\_tlate.h](#)

## 46.250 `omatrix_row_tlate< data_t, mparent_t, vparent_t, block_t >` Class Template Reference

Create a vector from a row of a matrix.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_row_tlate< data_t, mparent_t, vparent_t, block_t >`:



### 46.250.1 Detailed Description

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_row_tlate< data_t, mparent_t, vparent_t, block_t >
```

Definition at line 1045 of file `omatrix_tlate.h`.

#### Public Member Functions

- [omatrix\\_row\\_tlate](#) ([omatrix\\_base\\_tlate](#)< data\_t, mparent\_t, block\_t > &m, size\_t i)  
*Create a vector from row i of matrix m.*

The documentation for this class was generated from the following file:

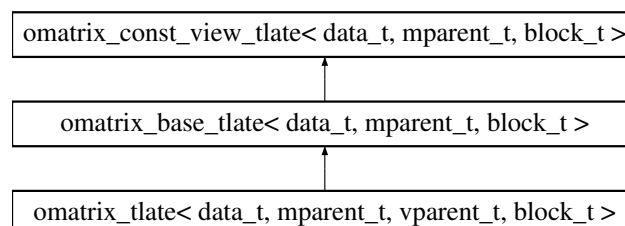
- [omatrix\\_tlate.h](#)

## 46.251 `omatrix_tlate< data_t, mparent_t, vparent_t, block_t >` Class Template Reference

A matrix of double-precision numbers.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_tlate< data_t, mparent_t, vparent_t, block_t >`:



## 46.251.1 Detailed Description

```
template<class data_t, class mparent_t, class vparent_t, class block_t>class omatrix_tlate< data_t, mparent_t, vparent_t, block_t >
```

The basic matrix classes are built upon this template. A matrix of double-precision numbers is an object of type `omatrix`, which is just a `typedef` defined using this class template. See [Arrays, Vectors, Matrices and Tensors](#) in the User's Guide for more information.

Definition at line 665 of file `omatrix_tlate.h`.

## Public Member Functions

## Standard constructor

- `omatrix_tlate` (size\_t r=0, size\_t c=0)  
*Create an omatrix of size n with owner as true.*

## Copy constructors

- `omatrix_tlate` (const `omatrix_tlate` &v)  
*Deep copy constructor; allocate new space and make a copy.*
- `omatrix_tlate` (const `omatrix_const_view_tlate`< data\_t, mparent\_t, block\_t > &v)  
*Deep copy constructor; allocate new space and make a copy.*
- `omatrix_tlate` & `operator=` (const `omatrix_tlate` &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `omatrix_tlate` & `operator=` (const `omatrix_const_view_tlate`< data\_t, mparent\_t, block\_t > &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `omatrix_tlate` (size\_t n, `ovector_base_tlate`< data\_t, vparent\_t, block\_t > ova[])  
*Deep copy from an array of ovector.*
- `omatrix_tlate` (size\_t n, `uvector_base_tlate`< data\_t > uva[])  
*Deep copy from an array of uvector.*
- `omatrix_tlate` (size\_t n, size\_t n2, data\_t \*\*csa)  
*Deep copy from a C-style 2-d array.*

## Memory allocation

- int `allocate` (size\_t nrows, size\_t ncols)  
*Allocate memory after freeing any memory presently in use.*
- int `free` ()  
*Free the memory.*

## Other methods

- `omatrix_tlate`< data\_t, mparent\_t, vparent\_t, block\_t > `transpose` ()  
*Compute the transpose (even if matrix is not square)*

## 46.251.2 Member Function Documentation

46.251.2.1 `template<class data_t, class mparent_t, class vparent_t, class block_t> int omatrix_tlate< data_t, mparent_t, vparent_t, block_t >::free ( ) [inline]`

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 975 of file `omatrix_tlate.h`.

The documentation for this class was generated from the following file:

- `omatrix_tlate.h`

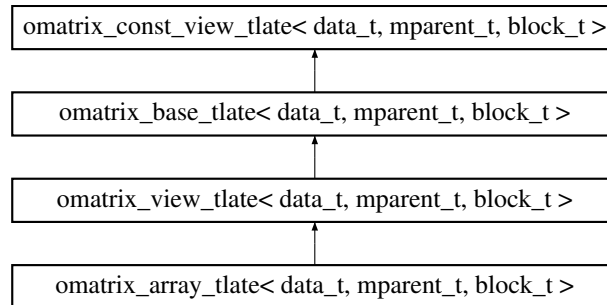


46.252 `omatrix_view_tlate< data_t, mparent_t, block_t >` Class Template Reference

A matrix view of double-precision numbers.

```
#include <omatrix_tlate.h>
```

Inheritance diagram for `omatrix_view_tlate< data_t, mparent_t, block_t >`:



## 46.252.1 Detailed Description

```
template<class data_t, class mparent_t, class block_t>class omatrix_view_tlate< data_t, mparent_t, block_t >
```

This is a matrix view, which views a matrix stored somewhere else. For a full matrix template class with its own memory, see [omatrix\\_tlate](#). The basic matrix classes are built upon these templates. A matrix of double-precision numbers is an object of type [omatrix](#). See [Arrays, Vectors, Matrices and Tensors](#) in the User's Guide for more information.

Definition at line 506 of file `omatrix_tlate.h`.

## Public Member Functions

## Copy constructors

- [omatrix\\_view\\_tlate](#) (const [omatrix\\_view\\_tlate](#) &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- [omatrix\\_view\\_tlate](#) & operator= (const [omatrix\\_view\\_tlate](#) &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- [omatrix\\_view\\_tlate](#) ([omatrix\\_base\\_tlate](#)< data\_t, mparent\_t, block\_t > &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- [omatrix\\_view\\_tlate](#) & operator= ([omatrix\\_base\\_tlate](#)< data\_t, mparent\_t, block\_t > &v)  
*Shallow copy constructor - create a new view of the same matrix.*

## Get and set methods

- data\_t \* [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*
- data\_t & [operator\(\)](#) (size\_t i, size\_t j) const  
*Array-like indexing.*
- data\_t \* [get\\_ptr](#) (size\_t i, size\_t j) const  
*Get pointer (with optional range-checking)*
- int [set](#) (size\_t i, size\_t j, data\_t val) const  
*Set (with optional range-checking)*
- int [set\\_all](#) (double val) const  
*Set all of the value to be the value val.*

## Protected Member Functions

- [omatrix\\_view\\_tlate](#) ()

*The default constructor.*

The documentation for this class was generated from the following file:

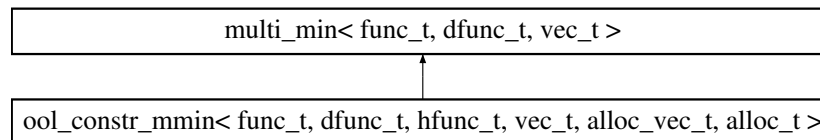
- [omatrix\\_tlate.h](#)

## 46.253 ool\_constr\_mmin< func\_t, dfunc\_t, hfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Constrained multidimensional minimization (OOL) [abstract base].

```
#include <ool_constr_mmin.h>
```

Inheritance diagram for ool\_constr\_mmin< func\_t, dfunc\_t, hfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



### 46.253.1 Detailed Description

```
template<class func_t, class dfunc_t = func_t, class hfunc_t = func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_-
alloc>class ool_constr_mmin< func_t, dfunc_t, hfunc_t, vec_t, alloc_vec_t, alloc_t >
```

**Idea for Future** Implement automatic computations of gradient and Hessian

**Idea for Future** Construct a more difficult example for the "examples" directory

**Idea for Future** Finish `mmin()` interface

**Idea for Future** Implement a direct computation of the hessian as the jacobian of the gradient

Definition at line 187 of file ool\_constr\_mmin.h.

#### Public Member Functions

- virtual int `allocate` (const size\_t n)  
*Allocate memory.*
- virtual int `free` ()  
*Free previously allocated memory.*
- virtual int `restart` ()  
*Restart the minimizer.*
- virtual int `set` (func\_t &fn, dfunc\_t &dfn, vec\_t &init)  
*Set the function, the gradient, and the initial guess.*
- virtual int `set_hess` (func\_t &fn, dfunc\_t &dfn, hfunc\_t &hfn, vec\_t &init)  
*Set the function, the gradient, the Hessian product, and the initial guess.*
- virtual int `set_constraints` (size\_t nc, vec\_t &lower, vec\_t &upper)  
*Set the constraints.*
- virtual int `iterate` ()=0  
*Perform an iteration.*
- virtual int `is_optimal` ()=0  
*See if we're finished.*
- virtual int `mmin` (size\_t nvar, vec\_t &xx, double &fmin, func\_t &ff)

*Calculate the minimum  $\min$  of  $\text{func}$  w.r.t. the array  $x$  of size  $nvar$ .*

- virtual int [mmin\\_hess](#) (size\_t nvar, vec\_t &xx, double &fmin, func\_t &ff, dfunc\_t &df, hfunc\_t &hf)  
*Calculate the minimum  $\min$  of  $\text{ff}$  w.r.t. the array  $x$  of size  $nvar$  with gradient  $\text{df}$  and hessian vector product  $\text{hf}$ .*
- virtual int [mmin\\_de](#) (size\_t nvar, vec\_t &xx, double &fmin, func\_t &ff, dfunc\_t &df)  
*Calculate the minimum  $\min$  of  $\text{func}$  w.r.t. the array  $x$  of size  $nvar$  with gradient  $\text{dfunc}$ .*
- const char \* [type](#) ()  
*Return string denoting type ("ool\_constr\_mmin")*

### Protected Member Functions

- void [shrink](#) (const size\_t nind, gsl\_vector\_uint \*Ind, const vec\_t &V)  
*Shrink vector  $V$  from the full to the reduced space.*
- void [expand](#) (const size\_t nind, gsl\_vector\_uint \*Ind, const vec\_t &V)  
*Expand vector  $V$  from the reduced to the full space.*
- double [calc\\_f](#) (const size\_t nind, gsl\_vector\_uint \*Ind, vec\_t &X, vec\_t &Xc)  
*Evaluate the objective function from the reduced space.*
- int [calc\\_g](#) (const size\_t nind, gsl\_vector\_uint \*Ind, vec\_t &X, vec\_t &Xc, vec\_t &G)  
*Compute gradient in the reduced space.*
- int [calc\\_Hv](#) (const size\_t nind, gsl\_vector\_uint \*Ind, vec\_t &X, vec\_t &Xc, vec\_t &V, vec\_t &Hv)  
*Evaluate a hessian times a vector from the reduced space.*

### Protected Attributes

- double [f](#)  
*The current function value.*
- double [size](#)  
*Desc.*
- alloc\_t [ao](#)  
*Memory allocation object.*
- alloc\_vec\_t [x](#)  
*The current minimum vector.*
- alloc\_vec\_t [gradient](#)  
*The current gradient vector.*
- alloc\_vec\_t [dx](#)  
*Desc.*
- size\_t [fcount](#)  
*Number of function evaluations.*
- size\_t [gcount](#)  
*Number of gradient evaluations.*
- size\_t [hcount](#)  
*Number of Hessian evaluations.*
- size\_t [dim](#)  
*Number of parameters.*
- size\_t [nconstr](#)  
*Number of constraints.*
- func\_t \* [func](#)  
*User-supplied function.*
- dfunc\_t \* [dfunc](#)  
*Gradient function.*
- hfunc\_t \* [hfunc](#)  
*Hessian function.*
- alloc\_vec\_t [L](#)  
*Lower bound constraints.*
- alloc\_vec\_t [U](#)  
*Upper bound constraints.*
- bool [requires\\_hess](#)  
*If true, the algorithm requires the hessian vector product.*

## 46.253.2 Member Function Documentation

46.253.2.1 `template<class func_t, class dfunc_t = func_t, class hfunc_t = func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> int ool_constr_mmin< func_t, dfunc_t, hfunc_t, vec_t, alloc_vec_t, alloc_t >::calc_Hv ( const size_t nind, gsl_vector_uint * Ind, vec_t & X, vec_t & Xc, vec_t & V, vec_t & Hv ) [inline, protected]`

Expand to full space

Definition at line 326 of file ool\_constr\_mmin.h.

46.253.2.2 `template<class func_t, class dfunc_t = func_t, class hfunc_t = func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> virtual int ool_constr_mmin< func_t, dfunc_t, hfunc_t, vec_t, alloc_vec_t, alloc_t >::mmin ( size_t nvar, vec_t & xx, double & fmin, func_t & ff ) [inline, virtual]`

## Note

This is unimplemented.

Implements [multi\\_min< func\\_t, dfunc\\_t, vec\\_t >](#).

Definition at line 476 of file ool\_constr\_mmin.h.

The documentation for this class was generated from the following file:

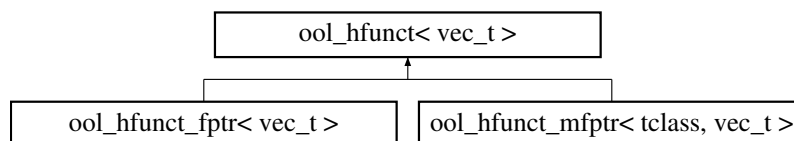
- ool\_constr\_mmin.h

## 46.254 ool\_hfunct&lt; vec\_t &gt; Class Template Reference

Hessian product function for [ool\\_constr\\_mmin](#) [abstract base].

```
#include <ool_constr_mmin.h>
```

Inheritance diagram for ool\_hfunct< vec\_t >:



## 46.254.1 Detailed Description

```
template<class vec_t = ovector_base>class ool_hfunct< vec_t >
```

Definition at line 60 of file ool\_constr\_mmin.h.

## Public Member Functions

- virtual int [operator\(\)](#) (size\_t nv, const vec\_t &x, const vec\_t &v, vec\_t &hv)=0  
*Evaluate  $H(x) \cdot v$ .*

The documentation for this class was generated from the following file:

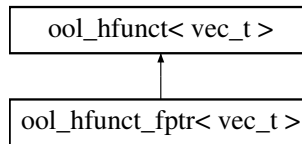
- ool\_constr\_mmin.h

## 46.255 ool\_hfunct\_fptr&lt; vec\_t &gt; Class Template Reference

A hessian product supplied by a function pointer.

```
#include <ool_constr_mmin.h>
```

Inheritance diagram for ool\_hfunct\_fptr< vec\_t >:



## 46.255.1 Detailed Description

```
template<class vec_t = ovector_base>class ool_hfunct_fptr< vec_t >
```

Definition at line 87 of file ool\_constr\_mmin.h.

## Public Member Functions

- `ool_hfunct_fptr` (`int(*fp)(size_t nv, const vec_t &x, const vec_t &v, vec_t &hv)`)  
*Specify the function pointer.*
- virtual `int operator()` (`size_t nv, const vec_t &x, const vec_t &v, vec_t &hv`)  
*Evaluate  $H(x) \cdot v$ .*

## Protected Attributes

- `int(* fptr)` (`size_t nv, const vec_t &x, const vec_t &v, vec_t &hv`)  
*Store the function pointer.*

## Private Member Functions

- `ool_hfunct_fptr` (`const ool_hfunct_fptr &`)
- `ool_hfunct_fptr & operator=` (`const ool_hfunct_fptr &`)

The documentation for this class was generated from the following file:

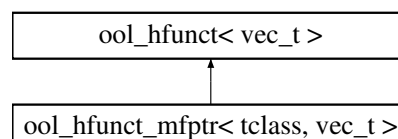
- ool\_constr\_mmin.h

## 46.256 ool\_hfunct\_mfptr&lt; tclass, vec\_t &gt; Class Template Reference

A hessian product supplied by a member function pointer.

```
#include <ool_constr_mmin.h>
```

Inheritance diagram for ool\_hfunct\_mfptr< tclass, vec\_t >:



## 46.256.1 Detailed Description

```
template<class tclass, class vec_t = ovector_base>class ool_hfunct_mfptr< tclass, vec_t >
```

Definition at line 132 of file ool\_constr\_mmin.h.

## Public Member Functions

- [ool\\_hfunct\\_mfptr](#) (tclass \*tp, int(tclass::\*fp)(size\_t nv, const vec\_t &x, const vec\_t &v, vec\_t &hv))  
*Specify the class instance and member function pointer.*
- virtual int [operator\(\)](#) (size\_t nv, const vec\_t &x, const vec\_t &v, vec\_t &hv)  
*Evaluate  $H(x) \cdot v$ .*

## Protected Attributes

- int(tclass::\* [fptr](#) )(size\_t nv, const vec\_t &x, const vec\_t &v, vec\_t &hv)  
*Store the function pointer.*
- tclass \* [tptr](#)  
*Store a pointer to the class instance.*

## Private Member Functions

- [ool\\_hfunct\\_mfptr](#) (const [ool\\_hfunct\\_mfptr](#) &)
- [ool\\_hfunct\\_mfptr](#) & [operator=](#) (const [ool\\_hfunct\\_mfptr](#) &)

The documentation for this class was generated from the following file:

- ool\_constr\_mmin.h

## 46.257 ool\_mmin\_gencan&lt; param\_t, func\_t, dfunc\_t, hfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Constrained minimization by the "GENCAN" method (OOL)

```
#include <ool_mmin_gencan.h>
```

## 46.257.1 Detailed Description

```
template<class param_t, class func_t, class dfunc_t = func_t, class hfunc_t = func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t  
= ovector_alloc>class ool_mmin_gencan< param_t, func_t, dfunc_t, hfunc_t, vec_t, alloc_vec_t, alloc_t >
```

## Note

Not working yet

Definition at line 68 of file ool\_mmin\_gencan.h.

## Public Member Functions

- virtual int [alloc](#) (const size\_t n)  
*Allocate memory.*
  - virtual int [free](#) ()  
*Free previously allocated memory.*
  - virtual int [set](#) (func\_t &fn, dfunc\_t &dfn, hfunc\_t &hfn, vec\_t &init, param\_t &par)
-

*Set the function, the initial guess, and the parameters.*

- virtual int [restart](#) ()  
*Restart the minimizer.*
- virtual int [iterate](#) ()  
*Perform an iteration.*
- virtual int [is\\_optimal](#) ()  
*See if we're finished.*
- const char \* [type](#) ()  
*Return string denoting type ("ool\_mmin\_gencan")*

## Data Fields

- double [epsgpen](#)  
*Tolerance on Euclidean norm of projected gradient (default 1.0e-5)*
- double [epsgpsn](#)  
*Tolerance on infinite norm of projected gradient (default 1.0e-5)*
- double [fmin](#)  
*Minimum function value (default  $10^{-99}$ )*
- double [udelta0](#)  
*Trust-region radius (default -1.0)*
- double [ucgmia](#)  
*Maximum iterations per variable (default -1.0)*
- double [ucgmib](#)  
*Extra maximum iterations (default -1.0)*
- int [cg\\_scre](#)  
*Conjugate gradient condition type (default 1)*
- double [cg\\_gpnf](#)  
*Projected gradient norm (default 1.0e-5)*
- double [cg\\_epsilon](#)  
*Desc (default 1.0e-1)*
- double [cg\\_epsf](#)  
*Desc (default 1.0e-5)*
- double [cg\\_epsnqmp](#)  
*Stopping fractional tolerance for conjugate gradient (default 1.0e-4)*
- int [cg\\_maxitnqmp](#)  
*Maximum iterations for conjugate gradient (default 5)*
- int [nearlyq](#)  
*Set to 1 if the function is nearly quadratic (default 0)*
- double [nint](#)  
*Interpolation constant (default 2.0)*
- double [next](#)  
*Extrapolation constant (default 2.0)*
- int [mininterp](#)  
*Minimum interpolation size (default 4)*
- int [maxextrap](#)  
*Maximum extrapolations in truncated Newton direction (default 100)*
- int [trtype](#)  
*Type of trust region (default 0)*
- double [eta](#)  
*Threshold for abandoning current face (default 0.9)*
- double [delmin](#)  
*Minimum trust region for truncated Newton direction (default 0.1)*
- double [lspgmi](#)  
*Minimum spectral steplength (default 1.0e-10)*
- double [lspgma](#)  
*Maximum spectral steplength (default 1.0e10)*
- double [theta](#)  
*Constant for the angle condition (default 1.0e-6)*
- double [gamma](#)  
*Constant for Armijo condition (default 1.0e-4)*

- double [beta](#)  
*Constant for beta condition (default 0.5)*
- double [sigma1](#)  
*Lower bound to the step length reduction (default 0.1)*
- double [sigma2](#)  
*Upper bound to the step length reduction (default 0.9)*
- double [epsrel](#)  
*Relative small number (default 1.0e-7)*
- double [epsabs](#)  
*Absolute small number (default 1.0e-10)*
- double [infrel](#)  
*Relative infinite number (default 1.0e20)*
- double [infabs](#)  
*Absolute infinite number (default 1.0e99)*

#### Protected Attributes

- double [cg\\_src](#)  
*Desc (default 1.0)*
- alloc\_vec\_t [S](#)  
*Temporary vector.*
- alloc\_vec\_t [Y](#)  
*Temporary vector.*
- alloc\_vec\_t [D](#)  
*Temporary vector.*
- alloc\_vec\_t [cg\\_W](#)  
*Temporary vector.*
- alloc\_vec\_t [cg\\_R](#)  
*Temporary vector.*
- alloc\_vec\_t [cg\\_D](#)  
*Temporary vector.*
- alloc\_vec\_t [cg\\_Sprev](#)  
*Temporary vector.*
- alloc\_vec\_t [Xtrial](#)  
*Temporary vector.*
- alloc\_vec\_t [tnls\\_Xtemp](#)  
*Temporary vector.*
- alloc\_vec\_t [near\\_l](#)  
*Temporary vector.*
- alloc\_vec\_t [near\\_u](#)  
*Temporary vector.*
- int \* [Ind](#)  
*Desc.*

#### 46.257.2 Field Documentation

46.257.2.1 `template<class param_t , class func_t , class dfunc_t = func_t, class hfunc_t = func_t, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double ool_mmin_gencan< param_t, func_t, dfunc_t, hfunc_t, vec_t, alloc_vec_t, alloc_t >::fmin`

If the function value is below this value, then the algorithm assumes that the function is not bounded and exits.

Definition at line 705 of file ool\_mmin\_gencan.h.

The documentation for this class was generated from the following file:

- ool\_mmin\_gencan.h
-

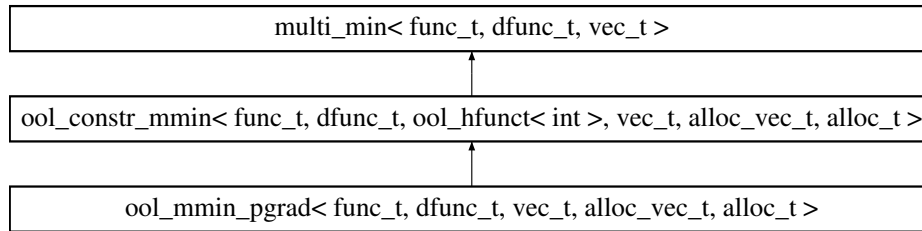


## 46.258 ool\_mmin\_pgrad&lt; func\_t, dfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Constrained minimization by the projected gradient method (OOL)

```
#include <ool_mmin_pgrad.h>
```

Inheritance diagram for ool\_mmin\_pgrad< func\_t, dfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



## 46.258.1 Detailed Description

```
template<class func_t = multi_func_t<>, class dfunc_t = grad_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector-
_alloc>class ool_mmin_pgrad< func_t, dfunc_t, vec_t, alloc_vec_t, alloc_t >
```

This is the simple extension of the steepest descent algorithm to constrained minimization. Each step a line search is performed along the projected gradient direction subject to the specified constraints.

This algorithm is likely not ideal for most problems and is provided mostly for demonstration and educational purposes. Based on implementation of Kelley99 in OOL.

Default template arguments

- func\_t - [multi\\_func\\_t<>](#)
- dfunc\_t - [grad\\_func\\_t<>](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)

**Idea for Future** Replace the explicit norm computation below with the more accurate dnm2 from linalg

**Idea for Future** Replace the generic variable 'tol' with 'tolf' or 'tolx' from [multi\\_min](#).

Definition at line 85 of file ool\_mmin\_pgrad.h.

## Public Member Functions

- virtual int [allocate](#) (const size\_t n)  
*Allocate memory.*
- virtual int [free](#) ()  
*Free previously allocated memory.*
- virtual int [set](#) (func\_t &fn, dfunc\_t &dfn, vec\_t &init)  
*Set the function, the initial guess, and the parameters.*
- virtual int [restart](#) ()  
*Restart the minimizer.*
- virtual int [iterate](#) ()

*Perform an iteration.*

- virtual int [is\\_optimal](#) ()

*See if we're finished.*

- const char \* [type](#) ()

*Return string denoting type ("ool\_mmin\_pgrad")*

#### Data Fields

- double [fmin](#)  
*Minimum function value (default  $10^{-99}$ )*
- double [tol](#)  
*Tolerance on infinite norm.*
- double [alpha](#)  
*Constant for the sufficient decrease condition (default  $10^{-4}$ )*
- double [sigma1](#)  
*Lower bound to the step length reduction.*
- double [sigma2](#)  
*Upper bound to the step length reduction.*

#### Protected Types

- typedef [ool\\_hfunct](#)< int > [hfunc\\_t](#)  
*A convenient typedef for the unused Hessian product type.*

#### Protected Member Functions

- int [proj](#) (vec\_t &xt)  
*Project into feasible region.*
- int [line\\_search](#) ()  
*Line search.*

#### Protected Attributes

- alloc\_vec\_t [xx](#)  
*Temporary vector.*

#### 46.258.2 Field Documentation

46.258.2.1 `template<class func_t = multi_func<>, class dfunc_t = grad_func<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double ool_mmin_pgrad< func_t, dfunc_t, vec_t, alloc_vec_t, alloc_t >::fmin`

If the function value is below this value, then the algorithm assumes that the function is not bounded and exits.

Definition at line 174 of file ool\_mmin\_pgrad.h.

The documentation for this class was generated from the following file:

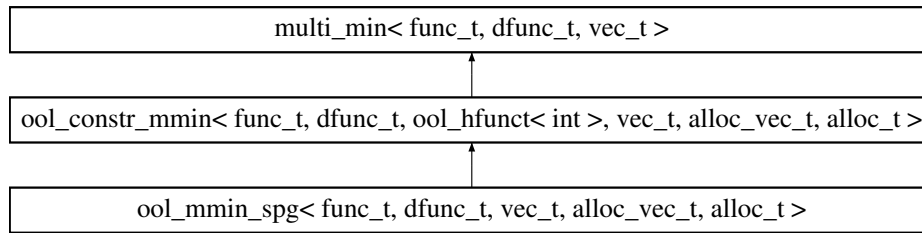
- ool\_mmin\_pgrad.h

#### 46.259 ool\_mmin\_spg< func\_t, dfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t > Class Template Reference

Constrained minimization by the spectral projected gradient method (OOL)

```
#include <ool_mmin_spg.h>
```

Inheritance diagram for ool\_mmin\_spg< func\_t, dfunc\_t, vec\_t, alloc\_vec\_t, alloc\_t >:



#### 46.259.1 Detailed Description

```
template<class func_t = multi_func<>, class dfunc_t = grad_func<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector-
_alloc>class ool_mmin_spg< func_t, dfunc_t, vec_t, alloc_vec_t, alloc_t >
```

This class applies a non-monotone line search strategy to the classical projected gradient method.

As in [Birgin00](#), this class applies a nonmonotone Armijo sufficient decrease condition for accepting trial points as an improvement over the classical spectral projected gradient method. This method may be competitive with large problems because it has low memory requirements.

Default template arguments

- func\_t - [multi\\_func<>](#)
- dfunc\_t - [grad\\_func<>](#)
- vec\_t - [ovector\\_base](#)
- alloc\_vec\_t - [ovector](#)
- alloc\_t - [ovector\\_alloc](#)

**Idea for Future** There is some memory allocation which isn't deallocated until the destructor, and should be handled a bit more elegantly.

Definition at line 84 of file ool\_mmin\_spg.h.

#### Public Member Functions

- virtual int [allocate](#) (const size\_t n)  
*Allocate memory.*
- virtual int [free](#) ()  
*Free previously allocated memory.*
- virtual int [set](#) (func\_t &fn, dfunc\_t &dfn, vec\_t &init)  
*Set the function, the initial guess, and the parameters.*
- virtual int [restart](#) ()  
*Restart the minimizer.*
- virtual int [iterate](#) ()  
*Perform an iteration.*
- virtual int [is\\_optimal](#) ()  
*See if we're finished.*
- const char \* [type](#) ()  
*Return string denoting type ("ool\_mmin\_spg")*

## Data Fields

- double [fmin](#)  
*Minimum function value (default  $10^{-99}$ )*
- double [tol](#)  
*Tolerance on infinite norm (default  $10^{-4}$ )*
- double [alphamin](#)  
*Lower bound to spectral step size (default  $10^{-30}$ )*
- double [alphamax](#)  
*Upper bound to spectral step size (default  $10^{30}$ )*
- double [gamma](#)  
*Sufficient decrease parameter (default  $10^{-4}$ )*
- double [sigma1](#)  
*Lower bound to the step length reduction (default 0.1)*
- double [sigma2](#)  
*Upper bound to the step length reduction (default 0.9)*
- size\_t [M](#)  
*Monotonicity parameter ( $M=1$  forces monotonicity) (default 10)*

## Protected Types

- typedef [ool\\_hfunct](#)< int > [hfunc\\_t](#)  
*A convenient typedef for the unused Hessian product type.*

## Protected Member Functions

- int [line\\_search](#) ()  
*Line search.*
- int [proj](#) (vec\_t &xt)  
*Project into feasible region.*

## Protected Attributes

- double [alpha](#)  
*Armijo parameter.*
- alloc\_vec\_t [xx](#)  
*Temporary vector.*
- alloc\_vec\_t [d](#)  
*Temporary vector.*
- alloc\_vec\_t [s](#)  
*Temporary vector.*
- alloc\_vec\_t [y](#)  
*Temporary vector.*
- alloc\_vec\_t [fvec](#)  
*Temporary vector.*
- size\_t [m](#)  
*Non-monotone parameter.*
- int [tail](#)  
*Desc.*

## 46.259.2 Field Documentation

46.259.2.1 `template<class func_t = multi_func_t<>, class dfunc_t = grad_func_t<>, class vec_t = ovector_base, class alloc_vec_t = ovector, class alloc_t = ovector_alloc> double ool_mmin_spg< func_t, dfunc_t, vec_t, alloc_vec_t, alloc_t >::fmin`

If the function value is below this value, then the algorithm assumes that the function is not bounded and exits.

Definition at line 237 of file ool\_mmin\_spg.h.

The documentation for this class was generated from the following file:

- ool\_mmin\_spg.h

## 46.260 other\_todos\_and\_bugs Class Reference

An empty class to add some items to the todo and bug lists.

### 46.260.1 Detailed Description

- Todo**
- Make sure an error message is printed to ensure users do 'make o2scl-test' and not 'make check'
  - Make sure cstdlib is included wherever exit() is used [5/22/11 - Most of these are taken care of now.]

- Idea for Future**
- Make sure we have a `uvector_cx_alloc`, `ovector_cx_const_reverse`, `ovector_cx_const_subvector_reverse`, `uvector-_reverse`, `uvector_const_reverse`, `uvector_subvector_reverse`, `uvector_const_subvector_reverse`, `omatrix_cx-_diag`, `blah_const_diag`, `umatrix_diag`, and `umatrix_cx_diag`
  - `ovector_cx_view::operator=(uvector_cx_view &)` is missing
  - `ovector_cx::operator=(uvector_cx_view &)` is missing
  - `uvector_c_view::operator+=(complex)` is missing
  - `uvector_c_view::operator-=(complex)` is missing
  - `uvector_c_view::operator*=(complex)` is missing

**Idea for Future** Currently, I believe the testing code requires the shared libraries and may not work if the static libraries only are installed. It would be nice to ensure the tests could be compiled in either case.

Definition at line 159 of file main.dox.

The documentation for this class was generated from the following file:

- main.dox

## 46.261 ovector\_alloc Class Reference

A simple class to provide an `allocate()` function for `ovector`.

```
#include <ovector_tlate.h>
```

### 46.261.1 Detailed Description

**Idea for Future** Could (or should?) the `allocate()` functions be adapted to return an integer error value?

Definition at line 1862 of file ovector\_tlate.h.

#### Public Member Functions

- void `allocate` (`ovector` &o, size\_t i)  
*Allocate v for i elements.*
- void `free` (`ovector` &o)  
*Free memory.*

The documentation for this class was generated from the following file:

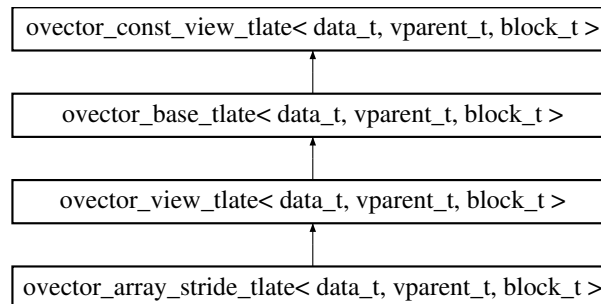
- [ovector\\_tlate.h](#)

## 46.262 `ovector_array_stride_tlate< data_t, vparent_t, block_t >` Class Template Reference

Create a vector from an array with a stride.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_array_stride_tlate< data_t, vparent_t, block_t >`:



### 46.262.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_array_stride_tlate< data_t, vparent_t, block_t >
```

Definition at line 1615 of file `ovector_tlate.h`.

#### Public Member Functions

- [ovector\\_array\\_stride\\_tlate](#) (size\_t n, data\_t \*dat, size\_t s)  
*Create a vector from dat with size n and stride s.*

The documentation for this class was generated from the following file:

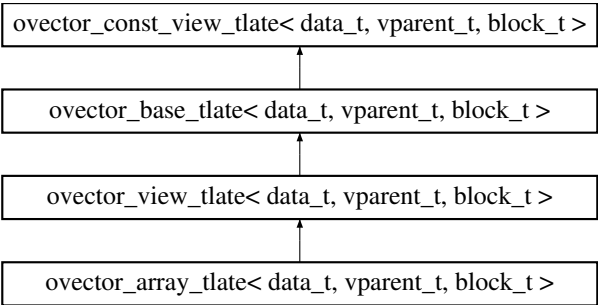
- [ovector\\_tlate.h](#)

## 46.263 `ovector_array_tlate< data_t, vparent_t, block_t >` Class Template Reference

Create a vector from an array.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_array_tlate< data_t, vparent_t, block_t >`:



46.263.1    Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_array_tlate< data_t, vparent_t, block_t >
```

Definition at line 1590 of file ovector\_tlate.h.

Public Member Functions

- [ovector\\_array\\_tlate](#) (size\_t n, data\_t \*dat)  
Create a vector from dat with size n.

The documentation for this class was generated from the following file:

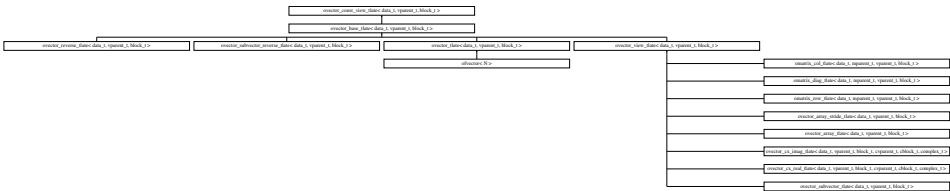
- [ovector\\_tlate.h](#)

46.264    ovector\_base\_tlate< data\_t, vparent\_t, block\_t > Class Template Reference

A base class for ovector and ovector\_view.

```
#include <ovector_tlate.h>
```

Inheritance diagram for ovector\_base\_tlate< data\_t, vparent\_t, block\_t >:



46.264.1    Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_base_tlate< data_t, vparent_t, block_t >
```

This class provides a base class for ovector and ovector\_view, mostly useful for creating function arguments which accept either ovector or ovector\_view.

Definition at line 640 of file ovector\_tlate.h.

## Public Types

- typedef `ovector_const_view_tlate< data_t, vparent_t, block_t >::const_iterator` `const_iterator`  
*Desc.*
- typedef `ovector_const_view_tlate< data_t, vparent_t, block_t >::iterator` `iterator`  
*Desc.*

## Public Member Functions

- `const_iterator begin ()` `const`  
*Desc.*
- `const_iterator end ()` `const`  
*Desc.*
- `iterator begin ()`  
*Desc.*
- `iterator end ()`  
*Desc.*

## Copy constructors

- `ovector_base_tlate (ovector_base_tlate &v)`  
*Shallow copy constructor - create a new view of the same vector.*
- `ovector_base_tlate & operator= (ovector_base_tlate &v)`  
*Shallow copy constructor - create a new view of the same vector.*

## Get and set methods

- `const data_t & operator[] (size_t i)` `const`  
*Array-like indexing.*
- `const data_t & operator() (size_t i)` `const`  
*Array-like indexing with operator()*
- `data_t & operator[] (size_t i)`  
*Array-like indexing.*
- `data_t & operator() (size_t i)`  
*Array-like indexing with operator()*
- `data_t * get_ptr (size_t i)`  
*Get pointer (with optional range-checking)*
- `int set (size_t i, data_t val)`  
*Set (with optional range-checking)*
- `int set_all (data_t val)`  
*Set all of the value to be the value val.*

## Arithmetic

- `ovector_base_tlate< data_t, vparent_t, block_t > & operator+= (const ovector_base_tlate< data_t, vparent_t, block_t > &x)`  
*operator+=*
- `ovector_base_tlate< data_t, vparent_t, block_t > & operator-= (const ovector_base_tlate< data_t, vparent_t, block_t > &x)`  
*operator-=*
- `ovector_base_tlate< data_t, vparent_t, block_t > & operator+= (const data_t &x)`  
*operator+=*
- `ovector_base_tlate< data_t, vparent_t, block_t > & operator-= (const data_t &x)`  
*operator-=*
- `ovector_base_tlate< data_t, vparent_t, block_t > & operator*= (const data_t &y)`  
*operator\*=*

## Other methods

- `vparent_t * get_gsl_vector ()`  
*Return a gsl vector.*
- `const vparent_t * get_gsl_vector_const ()` `const`  
*Return a const gsl vector.*



## Protected Member Functions

- [ovector\\_base\\_tlate\(\)](#)  
*Empty constructor for use by children.*

## 46.264.2 Constructor &amp; Destructor Documentation

46.264.2.1 `template<class data_t, class vparent_t, class block_t> ovector_base_tlate< data_t, vparent_t, block_t >::ovector_base_tlate ( )`  
[inline, protected]

Definition at line 898 of file ovector\_tlate.h.

## 46.264.3 Member Function Documentation

46.264.3.1 `template<class data_t, class vparent_t, class block_t> int ovector_base_tlate< data_t, vparent_t, block_t >::set_all ( data_t val )`  
[inline]

If the vector is empty, this function does not perform any assignment and does not call the error handler.

Definition at line 801 of file ovector\_tlate.h.

46.264.3.2 `template<class data_t, class vparent_t, class block_t> ovector_base_tlate<data_t,vparent_t,block_t>& ovector_base_tlate< data_t, vparent_t, block_t >::operator+=( const ovector_base_tlate< data_t, vparent_t, block_t > & x )` [inline]

This operator only operates on elements which are present in both vectors, i.e. elements which are present in one vector but missing in the other will be ignored. If one of the two vectors is empty, this function does nothing and does not call the error handler.

Definition at line 820 of file ovector\_tlate.h.

46.264.3.3 `template<class data_t, class vparent_t, class block_t> ovector_base_tlate<data_t,vparent_t,block_t>& ovector_base_tlate< data_t, vparent_t, block_t >::operator-=( const ovector_base_tlate< data_t, vparent_t, block_t > & x )` [inline]

This operator only operates on elements which are present in both vectors, i.e. elements which are present in one vector but missing in the other will be ignored. If one of the two vectors is empty, this function does nothing and does not call the error handler.

Definition at line 837 of file ovector\_tlate.h.

46.264.3.4 `template<class data_t, class vparent_t, class block_t> ovector_base_tlate<data_t,vparent_t,block_t>& ovector_base_tlate< data_t, vparent_t, block_t >::operator+=( const data_t & x )` [inline]

If the vector is empty, this function does not perform any modifications and does not call the error handler.

Definition at line 850 of file ovector\_tlate.h.

46.264.3.5 `template<class data_t, class vparent_t, class block_t> ovector_base_tlate<data_t,vparent_t,block_t>& ovector_base_tlate< data_t, vparent_t, block_t >::operator-=( const data_t & x )` [inline]

If the vector is empty, this function does not perform any modifications and does not call the error handler.

Definition at line 860 of file ovector\_tlate.h.

46.264.3.6 `template<class data_t, class vparent_t, class block_t> ovector_base_tlate<data_t,vparent_t,block_t>& ovector_base_tlate< data_t, vparent_t, block_t >::operator*=( const data_t & y )` [inline]

If the vector is empty, this function does not perform any modifications and does not call the error handler.

Definition at line 871 of file ovector\_tlate.h.

The documentation for this class was generated from the following file:

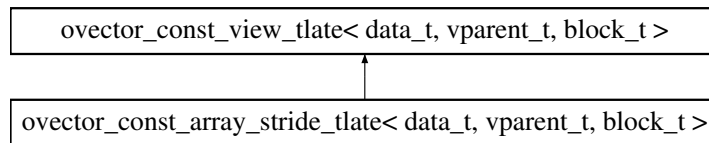
- [ovector\\_tlate.h](#)

## 46.265 `ovector_const_array_stride_tlate< data_t, vparent_t, block_t >` Class Template Reference

Create a const vector from an array with a stride.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_const_array_stride_tlate< data_t, vparent_t, block_t >`:



### 46.265.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_array_stride_tlate< data_t, vparent_t, block_t >
```

The constructor will fail if the size argument `n` is zero, the stride `s` is zero, or if the pointer `dat` is 0.

Definition at line 1716 of file `ovector_tlate.h`.

#### Public Member Functions

- [ovector\\_const\\_array\\_stride\\_tlate](#) (size\_t `n`, const data\_t \*`dat`, size\_t `s`)  
Create a vector from `dat` with size `n`.

The documentation for this class was generated from the following file:

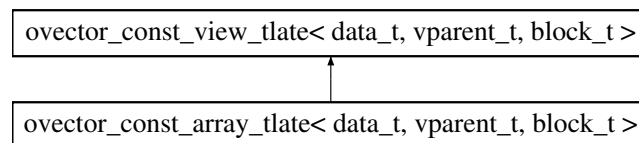
- [ovector\\_tlate.h](#)

## 46.266 `ovector_const_array_tlate< data_t, vparent_t, block_t >` Class Template Reference

Create a const vector from an array.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_const_array_tlate< data_t, vparent_t, block_t >`:



### 46.266.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_array_tlate< data_t, vparent_t, block_t >
```

The constructor will fail if the size argument `n` is zero or if the pointer `dat` is 0.

Definition at line 1680 of file `ovector_tlate.h`.

## Public Member Functions

- [`ovector\_const\_array\_tlate`](#) (`size_t n`, `const data_t *dat`)  
*Create a vector from `dat` with size `n`.*

The documentation for this class was generated from the following file:

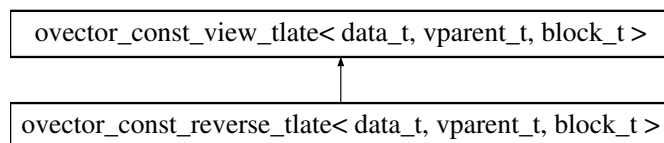
- [`ovector\_tlate.h`](#)

46.267 `ovector_const_reverse_tlate< data_t, vparent_t, block_t >` Class Template Reference

Reversed view of a vector.

```
#include <ovector_rev_tlate.h>
```

Inheritance diagram for `ovector_const_reverse_tlate< data_t, vparent_t, block_t >`:



## 46.267.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_reverse_tlate< data_t, vparent_t, block_t >
```

## Warning

At present, reversing a reversed vector does not give the original ordering.

**Idea for Future** I think that maybe in order to ensure that this isn't created from an already reversed vector, this class has to be separated from the hierarchy altogether. However, I think this might break the smart interpolation stuff.

Definition at line 229 of file `ovector_rev_tlate.h`.

## Public Member Functions

- [`ovector\_const\_reverse\_tlate`](#) (`const ovector_const_view_tlate< data_t, vparent_t, block_t > &v`)  
*Create a vector from `dat` with size `n` and stride `s`.*

## Get and set methods

- `const data_t & operator[]` (`size_t i`) `const`  
*Array-like indexing.*
- `const data_t & operator()` (`size_t i`) `const`  
*Array-like indexing.*
- `data_t get` (`size_t i`) `const`  
*Get (with optional range-checking)*
- `const data_t * get_const_ptr` (`size_t i`) `const`  
*Get pointer (with optional range-checking)*

The documentation for this class was generated from the following file:

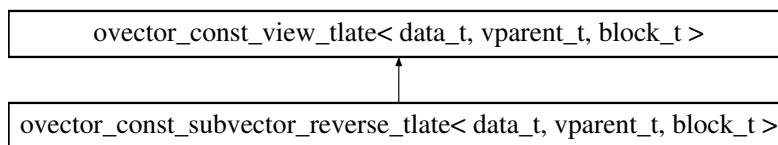
- [`ovector\_rev\_tlate.h`](#)

46.268 `ovector_const_subvector_reverse_tlate< data_t, vparent_t, block_t >` Class Template Reference

Reversed view of a const subvector.

```
#include <ovector_rev_tlate.h>
```

Inheritance diagram for `ovector_const_subvector_reverse_tlate< data_t, vparent_t, block_t >`:



## 46.268.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_subvector_reverse_tlate< data_t, vparent_t, block_t >
```

## Warning

At present, reversing a reversed vector does not give the original ordering.

Definition at line 483 of file `ovector_rev_tlate.h`.

## Public Member Functions

- [ovector\\_const\\_subvector\\_reverse\\_tlate](#) (const [ovector\\_const\\_view\\_tlate< data\\_t, vparent\\_t, block\\_t >](#) &*v*, *size\_t* *offset*, *size\_t* *n*)  
Create a vector from *dat* with size *n* and stride *s*.

## Get and set methods

- const *data\_t* & [operator\[\]](#) (*size\_t* *i*) const  
Array-like indexing.
- const *data\_t* & [operator\(\)](#) (*size\_t* *i*) const  
Array-like indexing.
- *data\_t* [get](#) (*size\_t* *i*) const  
Get (with optional range-checking)
- const *data\_t* \* [get\\_const\\_ptr](#) (*size\_t* *i*) const  
Get pointer (with optional range-checking)

The documentation for this class was generated from the following file:

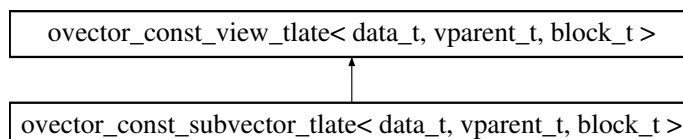
- [ovector\\_rev\\_tlate.h](#)

46.269 `ovector_const_subvector_tlate< data_t, vparent_t, block_t >` Class Template Reference

Create a const vector from a subvector of another vector.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_const_subvector_tlate< data_t, vparent_t, block_t >`:



## 46.269.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_subvector_tlate< data_t, vparent_t, block_t >
```

Definition at line 1747 of file `ovector_tlate.h`.

## Public Member Functions

- [`ovector\_const\_subvector\_tlate`](#) (const [`ovector\_const\_view\_tlate< data\_t, vparent\_t, block\_t >`](#) &orig, size\_t offset, size\_t n)  
*Create a vector from orig.*

The documentation for this class was generated from the following file:

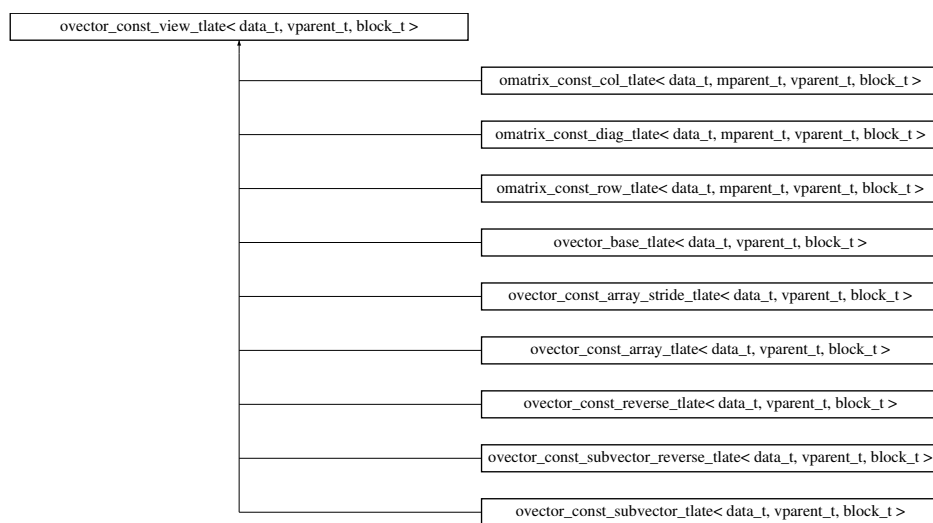
- [`ovector\_tlate.h`](#)

46.270 `ovector_const_view_tlate< data_t, vparent_t, block_t >` Class Template Reference

A const vector view with finite stride.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_const_view_tlate< data_t, vparent_t, block_t >`:



## 46.270.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_const_view_tlate< data_t, vparent_t, block_t >
```

Definition at line 109 of file `ovector_tlate.h`.

## Data Structures

- class [`const\_iterator`](#)  
*A const iterator for ovector.*
- class [`iterator`](#)  
*An iterator for ovector.*

## Public Member Functions

- `const_iterator begin () const`  
*An iterator for the beginning of the vector.*
- `const_iterator end () const`  
*An iterator for the end of the vector.*

## Copy constructors

- `ovector_const_view_tlate (const ovector_const_view_tlate &v)`  
*Shallow copy constructor - create a new view of the same vector.*
- `ovector_const_view_tlate & operator= (const ovector_const_view_tlate &v)`  
*Shallow copy constructor - create a new view of the same vector.*
- `ovector_const_view_tlate (const uvector_const_view_tlate< data_t > &v)`  
*Shallow copy constructor - view a unit-stride vector.*
- `ovector_const_view_tlate & operator= (const uvector_const_view_tlate< data_t > &v)`  
*Shallow copy constructor - view a unit-stride vector.*

## Get methods

- `const data_t & operator[] (size_t i) const`  
*Array-like indexing (with optional range-checking)*
- `const data_t & operator() (size_t i) const`  
*Array-like indexing (with optional range-checking)*
- `data_t get (size_t i) const`  
*Get (with optional range-checking)*
- `const data_t * get_const_ptr (size_t i) const`  
*Get pointer (with optional range-checking)*
- `size_t size () const`  
*Method to return vector size.*
- `size_t capacity () const`  
*Method to return capacity.*
- `size_t stride () const`  
*Method to return vector stride.*

## Other methods

- `bool is_owner () const`  
*Return true if this object owns the data it refers to.*
- `size_t lookup (const data_t x0) const`  
*Exhaustively look through the vector for a particular value and return the closest match.*
- `data_t max () const`  
*Find the maximum element.*
- `size_t max_index () const`  
*Find the location of the maximum element.*
- `data_t min () const`  
*Find the minimum element.*
- `size_t min_index () const`  
*Find the location of the minimum element.*

## Protected Member Functions

- `ovector_const_view_tlate ()`  
*Empty constructor provided for use by ovector\_view\_tlate(const ovector\_view\_tlate &v)*

## 46.270.2 Member Function Documentation

46.270.2.1 `template<class data_t, class vparent_t, class block_t> size_t ovector_const_view_tlate< data_t, vparent_t, block_t >::size ( )`  
`const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 383 of file ovector\_tlate.h.

46.270.2.2 `template<class data_t, class vparent_t, class block_t> size_t ovector_const_view_tlate< data_t, vparent_t, block_t >::capacity ( )`  
`const [inline]`

Analogous to `std::vector<>.capacity()`.

Definition at line 391 of file `ovector_tlate.h`.

46.270.2.3 `template<class data_t, class vparent_t, class block_t> size_t ovector_const_view_tlate< data_t, vparent_t, block_t >::stride ( )`  
`const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 401 of file `ovector_tlate.h`.

46.270.2.4 `template<class data_t, class vparent_t, class block_t> bool ovector_const_view_tlate< data_t, vparent_t, block_t >::is_owner ( )`  
`const [inline]`

This can be used to determine if an object is a "vector\_view", or a "vector". If `is_owner()` is true, then it is an `ovector_tlate` object.

If any O<sub>2</sub>sl class creates a `ovector_tlate` object in which `is_owner()` returns false, then it is a bug and should be reported.

Definition at line 418 of file `ovector_tlate.h`.

46.270.2.5 `template<class data_t, class vparent_t, class block_t> size_t ovector_const_view_tlate< data_t, vparent_t, block_t >::lookup (`  
`const data_t x0 ) const [inline]`

This can only fail if the vector is empty or if *all* of the entries in the vector are not finite. In these cases the function calls the error handler and returns 0.

If more than one entry is the same distance from `x0`, this function returns the entry with smallest index.

Definition at line 433 of file `ovector_tlate.h`.

46.270.2.6 `template<class data_t, class vparent_t, class block_t> data_t ovector_const_view_tlate< data_t, vparent_t, block_t >::max ( )`  
`const [inline]`

This can only fail if *all* of the entries in the array are not finite or if the vector is empty, in which case it calls the error handler and returns 0.

Definition at line 464 of file `ovector_tlate.h`.

46.270.2.7 `template<class data_t, class vparent_t, class block_t> size_t ovector_const_view_tlate< data_t, vparent_t, block_t >::max_index (`  
`) const [inline]`

This can only fail if *all* of the entries in the array are not finite or if the vector is empty, in which case it calls the error handler and returns 0.

Definition at line 498 of file `ovector_tlate.h`.

46.270.2.8 `template<class data_t, class vparent_t, class block_t> data_t ovector_const_view_tlate< data_t, vparent_t, block_t >::min ( )`  
`const [inline]`

This can only fail if *all* of the entries in the array are not finite or if the vector is empty, in which case it calls the error handler and returns 0.

Definition at line 544 of file `ovector_tlate.h`.

46.270.2.9 `template<class data_t, class vparent_t, class block_t> size_t ovector_const_view_tlate< data_t, vparent_t, block_t >::min_index (`  
`) const [inline]`

This can only fail if *all* of the entries in the array are not finite or if the vector is empty, in which case it calls the error handler and returns 0.

Definition at line 578 of file `ovector_tlate.h`.

The documentation for this class was generated from the following file:

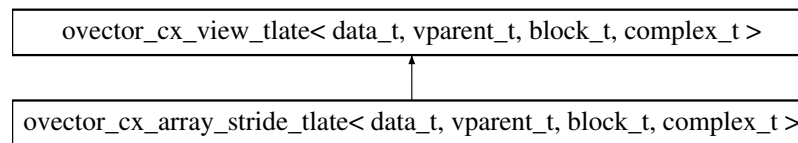
- [ovector\\_tlate.h](#)

## 46.271 `ovector_cx_array_stride_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from an array with a stride.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_array_stride_tlate< data_t, vparent_t, block_t, complex_t >`:



### 46.271.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_array_stride_tlate< data_t, vparent_t, block_t, complex_t >
```

Definition at line 740 of file `ovector_cx_tlate.h`.

#### Public Member Functions

- [ovector\\_cx\\_array\\_stride\\_tlate](#) (size\_t n, complex\_t \*dat, size\_t s)  
*Create a vector from dat with size n and stride s.*

The documentation for this class was generated from the following file:

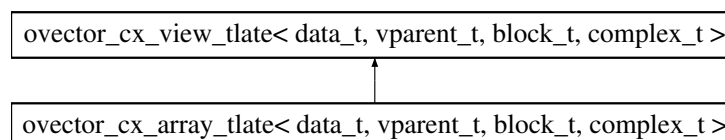
- [ovector\\_cx\\_tlate.h](#)

## 46.272 `ovector_cx_array_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from an array.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_array_tlate< data_t, vparent_t, block_t, complex_t >`:



### 46.272.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_array_tlate< data_t, vparent_t, block_t, complex_t >
```

Definition at line 720 of file `ovector_cx_tlate.h`.



## Public Member Functions

- [ovector\\_cx\\_array\\_tlate](#) (size\_t n, complex\_t \*dat)  
*Create a vector from dat with size n.*

The documentation for this class was generated from the following file:

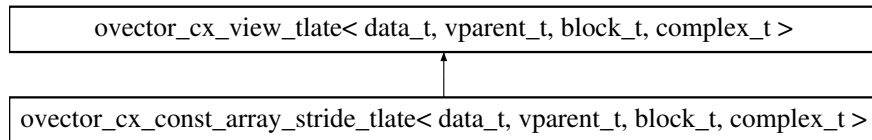
- [ovector\\_cx\\_tlate.h](#)

46.273 `ovector_cx_const_array_stride_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from an array\_stride.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_const_array_stride_tlate< data_t, vparent_t, block_t, complex_t >`:



## 46.273.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_const_array_stride_tlate< data_t, vparent_t, block_t, complex_t >
```

Definition at line 842 of file `ovector_cx_tlate.h`.

## Public Member Functions

- [ovector\\_cx\\_const\\_array\\_stride\\_tlate](#) (size\_t n, const complex\_t \*dat, size\_t s)  
*Create a vector from dat with size n.*

## Protected Member Functions

These are inaccessible to ensure the vector is `\c const`.

- `data_t & operator[]` (size\_t i)  
*Array-like indexing.*
- `data_t & operator()` (size\_t i)  
*Array-like indexing.*
- `data_t * get_ptr` (size\_t i)  
*Get pointer (with optional range-checking)*
- `int set` (size\_t i, data\_t val)
- `int set_all` (double val)
- `vparent_t * get_gsl_vector` ()
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t > & operator+=` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t > &x`)  
*operator+=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t > & operator-=` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t > &x`)  
*operator-=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t > & operator*=` (const `data_t &y`)

`operator*=`

The documentation for this class was generated from the following file:

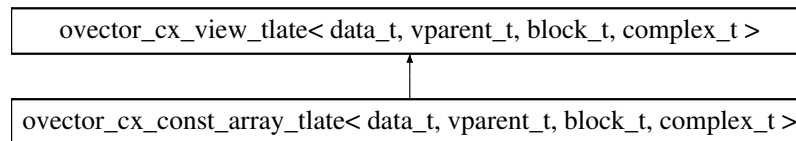
- [ovector\\_cx\\_tlate.h](#)

## 46.274 `ovector_cx_const_array_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from an array.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_const_array_tlate< data_t, vparent_t, block_t, complex_t >`:



### 46.274.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_const_array_tlate< data_t, vparent_t, block_t, complex_t >
```

Definition at line 790 of file `ovector_cx_tlate.h`.

#### Public Member Functions

- [ovector\\_cx\\_const\\_array\\_tlate](#) (size\_t n, const complex\_t \*dat)  
*Create a vector from dat with size n.*

#### Protected Member Functions

These are inaccessible to ensure the vector is `\c const`.

- data\_t & [operator\[\]](#) (size\_t i)  
*Array-like indexing.*
- data\_t & [operator\(\)](#) (size\_t i)  
*Array-like indexing.*
- data\_t \* [get\\_ptr](#) (size\_t i)  
*Get pointer (with optional range-checking)*
- int [set](#) (size\_t i, data\_t val)
- int [set\\_all](#) (double val)
- vparent\_t \* [get\\_gsl\\_vector](#) ()
- [ovector\\_cx\\_view\\_tlate< data\\_t, vparent\\_t, block\\_t, complex\\_t >](#) & [operator+=](#) (const [ovector\\_cx\\_view\\_tlate< data\\_t, vparent\\_t, block\\_t, complex\\_t >](#) &x)  
*operator+=*
- [ovector\\_cx\\_view\\_tlate< data\\_t, vparent\\_t, block\\_t, complex\\_t >](#) & [operator-=](#) (const [ovector\\_cx\\_view\\_tlate< data\\_t, vparent\\_t, block\\_t, complex\\_t >](#) &x)  
*operator-=*
- [ovector\\_cx\\_view\\_tlate< data\\_t, vparent\\_t, block\\_t, complex\\_t >](#) & [operator\\*=](#) (const data\_t &y)  
*operator\*=*

The documentation for this class was generated from the following file:

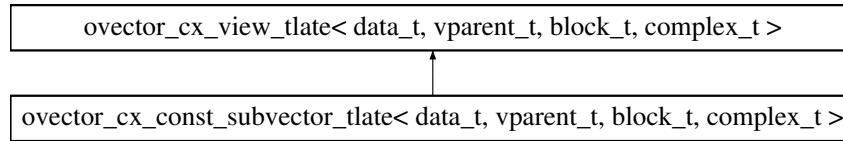
- [ovector\\_cx\\_tlate.h](#)

46.275 `ovector_cx_const_subvector_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from a subvector of another.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_const_subvector_tlate< data_t, vparent_t, block_t, complex_t >`:



## 46.275.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_const_subvector_tlate< data_t, vparent_t, block_t, complex_t
>
```

Definition at line 895 of file `ovector_cx_tlate.h`.

## Public Member Functions

- `ovector_cx_const_subvector_tlate` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` &orig, size\_t offset, size\_t n)  
*Create a vector from orig.*

## Protected Member Functions

These are inaccessible to ensure the vector is `\c const`.

- `data_t & operator[]` (size\_t i)  
*Array-like indexing.*
- `data_t & operator()` (size\_t i)  
*Array-like indexing.*
- `data_t * get_ptr` (size\_t i)  
*Get pointer (with optional range-checking)*
- `int set` (size\_t i, data\_t val)
- `int set_all` (double val)
- `vparent_t * get_gsl_vector` ()
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator+=` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` &x)  
*operator+=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator-=` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` &x)  
*operator-=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator*+=` (const data\_t &y)  
*operator\*+=*

The documentation for this class was generated from the following file:

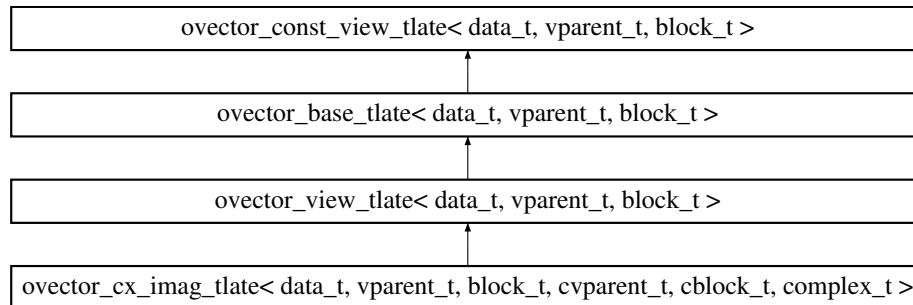
- `ovector_cx_tlate.h`

## 46.276 `ovector_cx_imag_tlate< data_t, vparent_t, block_t, cvparent_t, cblock_t, complex_t >` Class Template Reference

Create a imaginary vector from the imaginary parts of a complex vector.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_imag_tlate< data_t, vparent_t, block_t, cvparent_t, cblock_t, complex_t >`:



### 46.276.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class cvparent_t, class cblock_t, class complex_t>class ovector_cx_imag_tlate< data_t, vparent_t, block_t, cvparent_t, cblock_t, complex_t >
```

Definition at line 974 of file `ovector_cx_tlate.h`.

#### Public Member Functions

- [ovector\\_cx\\_imag\\_tlate](#) ([ovector\\_cx\\_view\\_tlate< data\\_t, cvparent\\_t, cblock\\_t, complex\\_t >](#) &x)  
*Create a imaginary vector from the imaginary parts of a complex vector.*

The documentation for this class was generated from the following file:

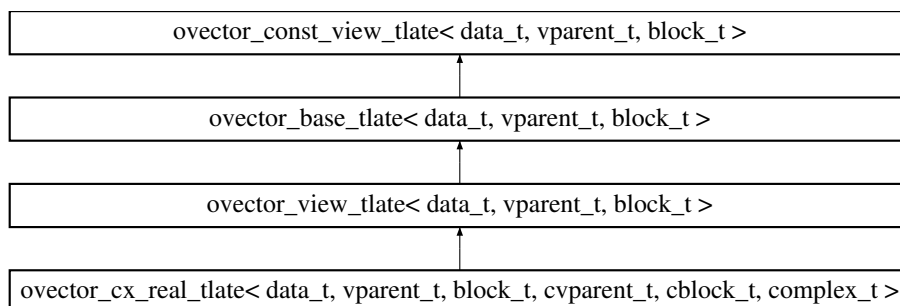
- [ovector\\_cx\\_tlate.h](#)

## 46.277 `ovector_cx_real_tlate< data_t, vparent_t, block_t, cvparent_t, cblock_t, complex_t >` Class Template Reference

Create a real vector from the real parts of a complex vector.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_real_tlate< data_t, vparent_t, block_t, cvparent_t, cblock_t, complex_t >`:



## 46.277.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class cvparent_t, class cblock_t, class complex_t>class ovector_cx_real_tlate< data_t, vparent_t, block_t, cvparent_t, cblock_t, complex_t >
```

Definition at line 952 of file `ovector_cx_tlate.h`.

## Public Member Functions

- [ovector\\_cx\\_real\\_tlate](#) ([ovector\\_cx\\_view\\_tlate](#)< data\_t, cvparent\_t, cblock\_t, complex\_t > &x)  
*Create a real vector from the real parts of a complex vector.*

The documentation for this class was generated from the following file:

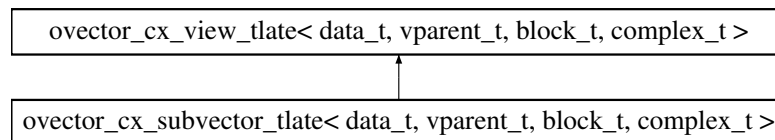
- [ovector\\_cx\\_tlate.h](#)

46.278 `ovector_cx_subvector_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

Create a vector from a subvector of another.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_subvector_tlate< data_t, vparent_t, block_t, complex_t >`:



## 46.278.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_subvector_tlate< data_t, vparent_t, block_t, complex_t >
```

Definition at line 761 of file `ovector_cx_tlate.h`.

## Public Member Functions

- [ovector\\_cx\\_subvector\\_tlate](#) ([ovector\\_cx\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t > &orig, size\_t offset, size\_t n)  
*Create a vector from orig.*

The documentation for this class was generated from the following file:

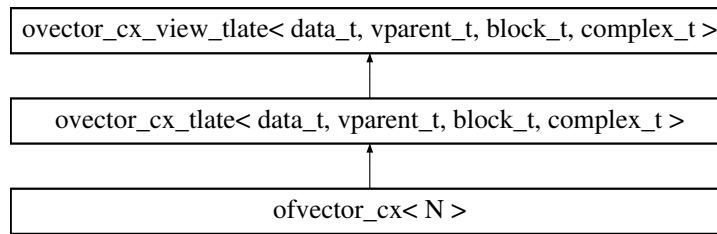
- [ovector\\_cx\\_tlate.h](#)

46.279 `ovector_cx_tlate< data_t, vparent_t, block_t, complex_t >` Class Template Reference

A vector of double-precision numbers.

```
#include <ovector_cx_tlate.h>
```

Inheritance diagram for `ovector_cx_tlate< data_t, vparent_t, block_t, complex_t >`:



#### 46.279.1 Detailed Description

template<class data\_t, class vparent\_t, class block\_t, class complex\_t>class ovector\_cx\_tlate< data\_t, vparent\_t, block\_t, complex\_t >

If the memory allocation fails, either in the constructor or in `allocate()`, then the error handler will be called, partially allocated memory will be freed, and the size will be reset to zero. You can test to see if the allocation succeeded using something like

```
const size_t n=10;
ovector_cx x(10);
if (x.size()==0) cout << "Failed." << endl;
```

**Todo** Add `subvector_stride`, `const_subvector_stride`

Definition at line 479 of file `ovector_cx_tlate.h`.

#### Public Member Functions

##### Standard constructor

- `ovector_cx_tlate` (size\_t n=0)  
Create an `ovector_cx` of size `n` with owner as 'true'.

##### Copy constructors

- `ovector_cx_tlate` (const `ovector_cx_tlate` &v)  
Deep copy constructor; allocate new space and make a copy.
- `ovector_cx_tlate` (const `ovector_cx_view_tlate`< data\_t, vparent\_t, block\_t, complex\_t > &v)  
Deep copy constructor; allocate new space and make a copy.
- `ovector_cx_tlate` & `operator=` (const `ovector_cx_tlate` &v)  
Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.
- `ovector_cx_tlate` & `operator=` (const `ovector_cx_view_tlate`< data\_t, vparent\_t, block\_t, complex\_t > &v)  
Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.

##### Memory allocation

- int `allocate` (size\_t nsize)  
Allocate memory for size `n` after freeing any memory presently in use.
- int `free` ()  
Free the memory.

##### Other methods

- vparent\_t \* `get_gsl_vector_complex` ()  
Return a `gsl vector_cx`.
- const vparent\_t \* `get_gsl_vector_complex_const` () const  
Return a `gsl vector_cx`.

46.279.2    Member Function Documentation

46.279.2.1    `template<class data_t, class vparent_t, class block_t, class complex_t> int ovector_cx_tlate< data_t, vparent_t, block_t, complex_t >::free ( )    [inline]`

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.  
Definition at line 690 of file `ovector_cx_tlate.h`.

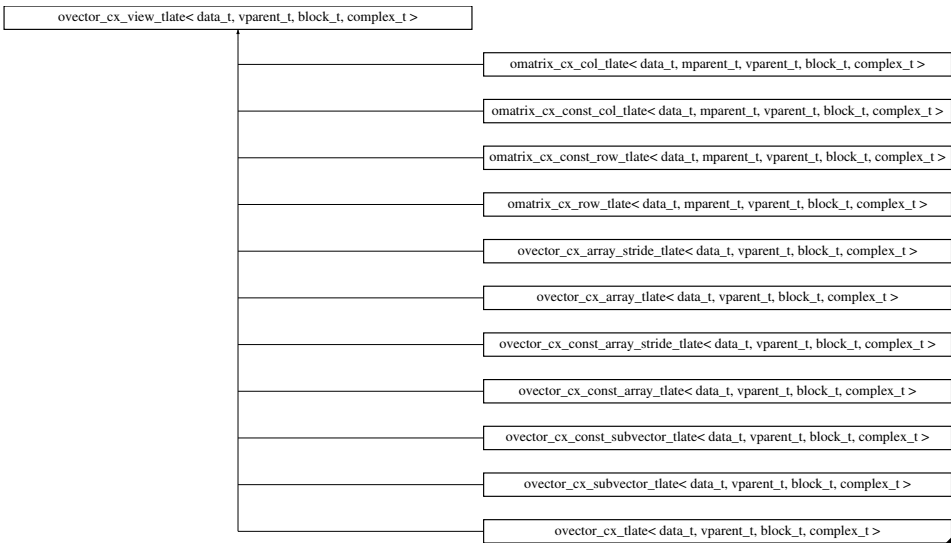
The documentation for this class was generated from the following file:

- [ovector\\_cx\\_tlate.h](#)

46.280    `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >`    Class Template Reference

A vector view of double-precision numbers.  
`#include <ovector_cx_tlate.h>`

Inheritance diagram for `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >`:



46.280.1    Detailed Description

`template<class data_t, class vparent_t, class block_t, class complex_t>class ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >`

Definition at line 51 of file `ovector_cx_tlate.h`.

Public Member Functions

- `int conjugate ( )`  
*Conjugate the vector.*
- `data_t norm ( ) const`  
*Complex norm  $v^\dagger v$ .*

Copy constructors

- `ovector_cx_view_tlate (const ovector_cx_view_tlate &v)`

*Shallow copy constructor - create a new view of the same vector.*

- `ovector_cx_view_tlate` & `operator=` (const `ovector_cx_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same vector.*

#### Get and set methods

- `complex_t` & `operator[]` (size\_t i)  
*Array-like indexing.*
- const `complex_t` & `operator[]` (size\_t i) const  
*Array-like indexing.*
- `complex_t` & `operator()` (size\_t i)  
*Array-like indexing.*
- const `complex_t` & `operator()` (size\_t i) const  
*Array-like indexing.*
- `complex_t` `get` (size\_t i) const  
*Get (with optional range-checking)*
- `data_t` `real` (size\_t i) const  
*Get real part (with optional range-checking)*
- `data_t` `imag` (size\_t i) const  
*Get imaginary part (with optional range-checking)*
- `std::complex< data_t >` `get_stl` (size\_t i) const  
*Get STL-like complex number (with optional range-checking)*
- `complex_t *` `get_ptr` (size\_t i)  
*Get pointer (with optional range-checking)*
- const `complex_t *` `get_const_ptr` (size\_t i) const  
*Get pointer (with optional range-checking)*
- int `set` (size\_t i, const `complex_t` &val)  
*Set (with optional range-checking)*
- int `set_stl` (size\_t i, const `std::complex< data_t >` &d)  
*Set (with optional range-checking)*
- int `set` (size\_t i, `data_t` vr, `data_t` vi)  
*Set (with optional range-checking)*
- int `set_all` (const `complex_t` &g)  
*Set all of the value to be the value val.*
- size\_t `size` () const  
*Method to return vector size.*
- size\_t `stride` () const  
*Method to return vector stride.*

#### Other methods

- bool `is_owner` () const  
*Return true if this object owns the data it refers to.*

#### Arithmetic

- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator+=` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` &x)  
*operator+=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator-=` (const `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` &x)  
*operator-=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator+=` (const `complex_t` &x)  
*operator+=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator-=` (const `complex_t` &x)  
*operator-=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator*=` (const `complex_t` &x)  
*operator\*=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator+=` (const `data_t` &x)  
*operator+=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator-=` (const `data_t` &x)  
*operator-=*
- `ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t >` & `operator*=` (const `data_t` &x)  
*operator\*=*



## Protected Member Functions

- [ovector\\_cx\\_view\\_tlate](#) ()  
*Empty constructor provided for use by ovector\_cx\_tlate(const ovector\_cx\_tlate &v) [protected].*

## 46.280.2 Member Function Documentation

46.280.2.1 `template<class data_t, class vparent_t, class block_t, class complex_t> size_t ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t>::size ( ) const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 303 of file ovector\_cx\_tlate.h.

46.280.2.2 `template<class data_t, class vparent_t, class block_t, class complex_t> size_t ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t>::stride ( ) const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 312 of file ovector\_cx\_tlate.h.

The documentation for this class was generated from the following file:

- [ovector\\_cx\\_tlate.h](#)

## 46.281 ovector\_int\_alloc Class Reference

A simple class to provide an [allocate](#) () function for [ovector\\_int](#).

```
#include <ovector_tlate.h>
```

## 46.281.1 Detailed Description

Definition at line 1873 of file ovector\_tlate.h.

## Public Member Functions

- void [allocate](#) ([ovector\\_int](#) &o, size\_t i)  
*Allocate v for i elements.*
- void [free](#) ([ovector\\_int](#) &o)  
*Free memory.*

The documentation for this class was generated from the following file:

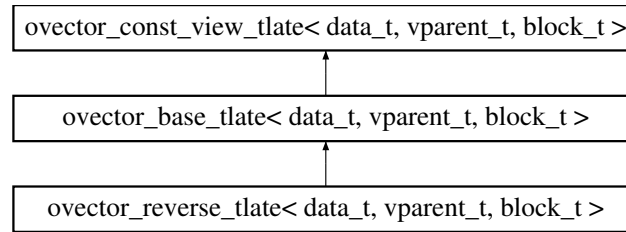
- [ovector\\_tlate.h](#)

## 46.282 ovector\_reverse\_tlate&lt; data\_t, vparent\_t, block\_t &gt; Class Template Reference

Reversed view of a vector.

```
#include <ovector_rev_tlate.h>
```

Inheritance diagram for ovector\_reverse\_tlate< data\_t, vparent\_t, block\_t >:



### 46.282.1 Detailed Description

`template<class data_t, class vparent_t, class block_t>class ovector_reverse_tlate< data_t, vparent_t, block_t >`

#### Note

Note that you can't reverse a reversed vector, and this is why this class does not have a constructor of the form `ovector_reverse(ovector_reverse &v)`.

Definition at line 55 of file `ovector_rev_tlate.h`.

#### Public Member Functions

- [ovector\\_reverse\\_tlate](#) ([ovector\\_tlate](#)< data\_t, vparent\_t, block\_t > &v)  
*Create a vector from dat with size n and stride s.*
- [ovector\\_reverse\\_tlate](#) ([ovector\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t > &v)  
*Create a vector from dat with size n and stride s.*

#### Get and set methods

- data\_t & [operator\[\]](#) (size\_t i)  
*Array-like indexing.*
- const data\_t & [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*
- data\_t & [operator\(\)](#) (size\_t i)  
*Array-like indexing.*
- const data\_t & [operator\(\)](#) (size\_t i) const  
*Array-like indexing.*
- data\_t [get](#) (size\_t i) const  
*Get (with optional range-checking)*
- data\_t \* [get\\_ptr](#) (size\_t i)  
*Get pointer (with optional range-checking)*
- const data\_t \* [get\\_const\\_ptr](#) (size\_t i) const  
*Get pointer (with optional range-checking)*
- int [set](#) (size\_t i, data\_t val)  
*Set (with optional range-checking)*
- int [set\\_all](#) (double val)  
*Set all of the value to be the value val.*

The documentation for this class was generated from the following file:

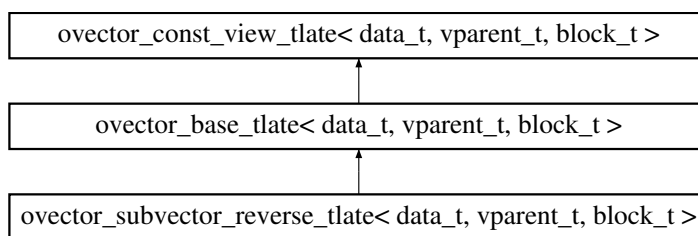
- [ovector\\_rev\\_tlate.h](#)

## 46.283 `ovector_subvector_reverse_tlate< data_t, vparent_t, block_t >` Class Template Reference

Reversed view of a subvector.

```
#include <ovector_rev_tlate.h>
```

Inheritance diagram for `ovector_subvector_reverse_tlate< data_t, vparent_t, block_t >`:



#### 46.283.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_subvector_reverse_tlate< data_t, vparent_t, block_t >
```

##### Warning

At present, reversing a reversed vector does not give the original ordering.

Definition at line 317 of file `ovector_rev_tlate.h`.

##### Public Member Functions

- [ovector\\_subvector\\_reverse\\_tlate](#) ([ovector\\_base\\_tlate](#)< data\_t, vparent\_t, block\_t > &v, size\_t offset, size\_t n)  
*Create a vector from dat with size n and stride s.*

##### Get and set methods

- data\_t & [operator\[\]](#) (size\_t i)  
*Array-like indexing.*
- const data\_t & [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*
- data\_t & [operator\(\)](#) (size\_t i)  
*Array-like indexing.*
- const data\_t & [operator\(\)](#) (size\_t i) const  
*Array-like indexing.*
- data\_t [get](#) (size\_t i) const  
*Get (with optional range-checking)*
- data\_t \* [get\\_ptr](#) (size\_t i)  
*Get pointer (with optional range-checking)*
- const data\_t \* [get\\_const\\_ptr](#) (size\_t i) const  
*Get pointer (with optional range-checking)*
- int [set](#) (size\_t i, data\_t val)  
*Set (with optional range-checking)*
- int [set\\_all](#) (double val)  
*Set all of the value to be the value val.*

The documentation for this class was generated from the following file:

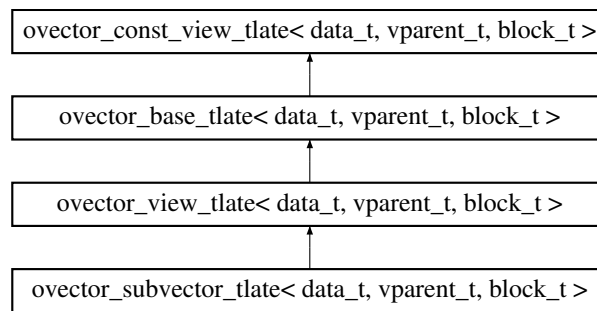
- [ovector\\_rev\\_tlate.h](#)

#### 46.284 `ovector_subvector_tlate< data_t, vparent_t, block_t >` Class Template Reference

Create a vector from a subvector of another.

```
#include <ovector_tlate.h>
```

Inheritance diagram for ovector\_subvector\_tlate< data\_t, vparent\_t, block\_t >:



#### 46.284.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_subvector_tlate< data_t, vparent_t, block_t >
```

The constructor will fail if the original vector is empty, or if the user requests a subvector which includes elements beyond the end of the original vector.

Definition at line 1645 of file ovector\_tlate.h.

#### Public Member Functions

- [ovector\\_subvector\\_tlate](#) ([ovector\\_base\\_tlate](#)< data\_t, vparent\_t, block\_t > &orig, size\_t offset, size\_t n)  
*Create a vector from orig.*

The documentation for this class was generated from the following file:

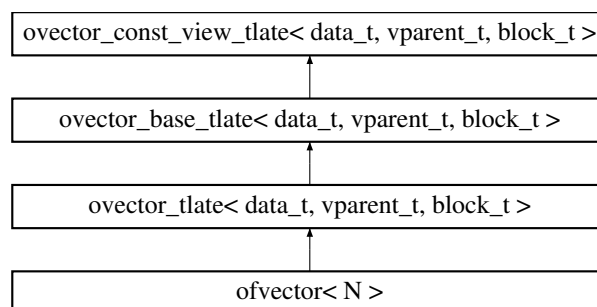
- [ovector\\_tlate.h](#)

## 46.285 ovector\_tlate< data\_t, vparent\_t, block\_t > Class Template Reference

A vector with finite stride.

```
#include <ovector_tlate.h>
```

Inheritance diagram for ovector\_tlate< data\_t, vparent\_t, block\_t >:



#### 46.285.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_tlate< data_t, vparent_t, block_t >
```

There are several global binary operators associated with objects of type `ovector_tlate`. They are documented in the "Functions" section of `ovector_tlate.h`.

### Design notes

At present, the owner variable can be used to distinguish between ovector and ovector\_views: for views, owner is always zero, but for normal ovector, owner is 1 (even for empty vectors).

The `reserve()`, `pop_back()`, and `push_back()` methods require the ability to have empty vectors which still have memory allocated for them, so the proper test for whether or not memory is allocated is to test whether or not 'block' is zero. This means we should never have a case where the block is non-zero (i.e. there is memory allocated there) but the size of the block is zero. This is the test used in the destructor and the `free()` method. The free method also sets block to zero accordingly.

Definition at line 1101 of file `ovector_tlate.h`.

### Public Member Functions

#### Standard constructor

- `ovector_tlate` (size\_t n=0)  
*Create an ovector of size n with owner as 'true'.*

#### Copy constructors

- `ovector_tlate` (const `ovector_tlate` &v)  
*Deep copy constructor.*
- `template<class alt_vec_t >`  
`ovector_tlate` (size\_t nv, alt\_vec\_t &v)  
*Deep copy constructor for generic vectors.*
- `ovector_tlate` (const `ovector_const_view_tlate`< data\_t, vparent\_t, block\_t > &v)  
*Deep copy constructor for other related vectors.*
- `ovector_tlate` & `operator=` (const `ovector_tlate` &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `ovector_tlate` & `operator=` (const `ovector_const_view_tlate`< data\_t, vparent\_t, block\_t > &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `ovector_tlate` & `operator=` (const `uvector_const_view_tlate`< data\_t > &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*

#### Memory allocation

- int `allocate` (size\_t nsize)  
*Allocate memory for size n after freeing any memory currently in use.*
- int `free` ()  
*Free the memory.*

#### Stack-like operations

- int `push_back` (data\_t val)  
*Add a value to the end of the vector.*
- int `reserve` (size\_t cap)  
*Reserve memory by increasing capacity.*
- data\_t `pop_back` ()  
*Return the last value and shrink the vector size by one.*

#### Other methods

- int `erase` (size\_t ix)  
*Remove element with index ix and decrease the vector size by one.*
- int `sort_unique` ()  
*Sort the vector and ensure all elements are unique by removing duplicates.*

## Protected Member Functions

- void `intl_sanity_check` (size\_t ix)  
*An internal sanity check to ensure correctness.*
- int `intl_allocate` (size\_t nsize)  
*An internal allocate function.*
- int `intl_free` ()  
*The internal free function.*
- template<class alt\_vec\_t >  
int `intl_init` (size\_t n, alt\_vec\_t &v)  
*An internal init() function.*
- template<class alt\_vec\_t >  
`ovector_tlate` & `intl_assign` (size\_t n, alt\_vec\_t &v)  
*An internal assignment function for `operator=()`*

## 46.285.2 Constructor &amp; Destructor Documentation

46.285.2.1 `template<class data_t, class vparent_t, class block_t> ovector_tlate< data_t, vparent_t, block_t >::ovector_tlate ( const ovector_tlate< data_t, vparent_t, block_t > & v )` [inline]

Definition at line 1257 of file `ovector_tlate.h`.

## 46.285.3 Member Function Documentation

46.285.3.1 `template<class data_t, class vparent_t, class block_t> int ovector_tlate< data_t, vparent_t, block_t >::intl_allocate ( size_t nsize )` [inline, protected]

## Note

This function does nothing if `nsize` is zero. Also, this does not free any already allocated memory first (unlike the user-interface version `allocate()`).

Definition at line 1129 of file `ovector_tlate.h`.

46.285.3.2 `template<class data_t, class vparent_t, class block_t> template<class alt_vec_t > int ovector_tlate< data_t, vparent_t, block_t >::intl_init ( size_t n, alt_vec_t & v )` [inline, protected]

This function calls `intl_allocate()` first, and then copies the data from the vector `v`.

Definition at line 1194 of file `ovector_tlate.h`.

46.285.3.3 `template<class data_t, class vparent_t, class block_t> int ovector_tlate< data_t, vparent_t, block_t >::allocate ( size_t nsize )` [inline]

Note that this automatically deallocates any previously allocated memory before attempting to allocate more. If this allocation fails (i.e. because we ran out of memory) then the original vector will still have been deallocated.

Definition at line 1360 of file `ovector_tlate.h`.

46.285.3.4 `template<class data_t, class vparent_t, class block_t> int ovector_tlate< data_t, vparent_t, block_t >::free ( )` [inline]

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 1373 of file `ovector_tlate.h`.

46.285.3.5 `template<class data_t, class vparent_t, class block_t> int ovector_tlate< data_t, vparent_t, block_t >::reserve ( size_t cap )` [inline]

Increase the maximum capacity of the vector so that calls to `push_back()` do not need to automatically increase the capacity.

If the argument `cap` is smaller than the present vector size given by `size()`, then this function does nothing and the error handler is not called.

Definition at line 1445 of file `ovector_tlate.h`.

The documentation for this class was generated from the following file:

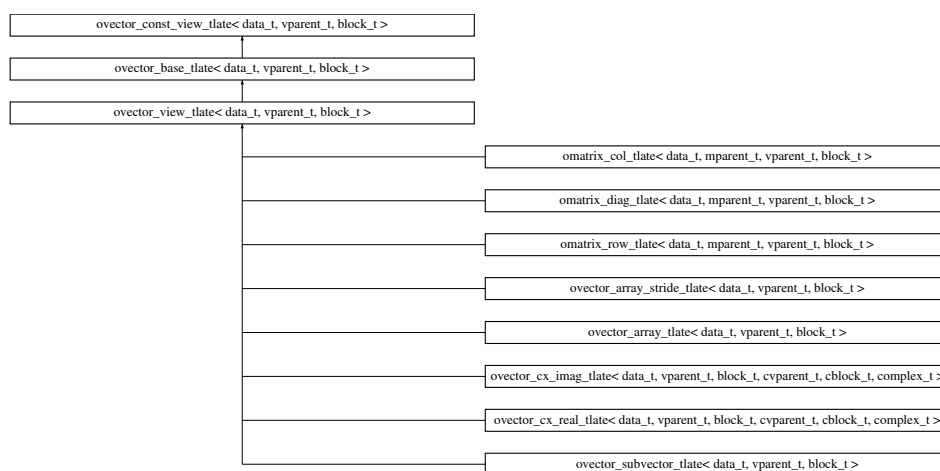
- [ovector\\_tlate.h](#)

## 46.286 `ovector_view_tlate< data_t, vparent_t, block_t >` Class Template Reference

A vector view with finite stride.

```
#include <ovector_tlate.h>
```

Inheritance diagram for `ovector_view_tlate< data_t, vparent_t, block_t >`:



### 46.286.1 Detailed Description

```
template<class data_t, class vparent_t, class block_t>class ovector_view_tlate< data_t, vparent_t, block_t >
```

Definition at line 905 of file `ovector_tlate.h`.

#### Public Member Functions

##### Copy constructors

- [ovector\\_view\\_tlate](#) (const [ovector\\_view\\_tlate](#) &v)  
*Shallow copy constructor - create a new view of the same vector.*
- [ovector\\_view\\_tlate](#) & [operator=](#) (const [ovector\\_view\\_tlate](#) &v)  
*Shallow copy constructor - create a new view of the same vector.*
- [ovector\\_view\\_tlate](#) ([ovector\\_base\\_tlate](#)< data\_t, vparent\_t, block\_t > &v)  
*Shallow copy constructor for non-views.*
- [ovector\\_view\\_tlate](#) & [operator=](#) ([ovector\\_base\\_tlate](#)< data\_t, vparent\_t, block\_t > &v)  
*Shallow copy constructor for non-views.*
- [ovector\\_view\\_tlate](#) ([uvector\\_base\\_tlate](#)< data\_t > &v)  
*Shallow copy constructor for unit-stride vectors.*
- [ovector\\_view\\_tlate](#) & [operator=](#) ([uvector\\_base\\_tlate](#)< data\_t > &v)  
*Shallow copy constructor for unit-stride vectors.*

## Get and set methods

- `data_t & operator[] (size_t i) const`  
*Array-like indexing.*
- `data_t & operator() (size_t i) const`  
*Array-like indexing with operator()*
- `data_t * get_ptr (size_t i) const`  
*Get pointer (with optional range-checking)*
- `int set (size_t i, data_t val) const`  
*Set (with optional range-checking)*
- `int set_all (double val) const`  
*Set all of the value to be the value val.*

## Protected Member Functions

- `ovector_view_tlate ()`  
*Empty constructor provided for use by `ovector_view_tlate(const ovector_view_tlate &v)`*

## 46.286.2 Member Function Documentation

46.286.2.1 `template<class data_t, class vparent_t, class block_t> int ovector_view_tlate< data_t, vparent_t, block_t >::set_all ( double val ) const [inline]`

If the vector is empty, this function does not perform any assignment and does not call the error handler.

Definition at line 1056 of file `ovector_tlate.h`.

The documentation for this class was generated from the following file:

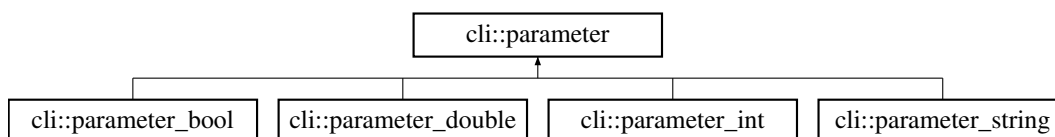
- `ovector_tlate.h`

## 46.287 cli::parameter Class Reference

Parameter for `cli`.

```
#include <cli.h>
```

Inheritance diagram for `cli::parameter`:



## 46.287.1 Detailed Description

Definition at line 235 of file `cli.h`.

## Public Member Functions

- `virtual int set (std::string s)=0`  
*Set from string.*
- `virtual std::string get ()=0`  
*Convert to string.*



### Data Fields

- std::string [help](#)  
*Help description.*

The documentation for this class was generated from the following file:

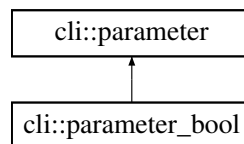
- cli.h

## 46.288 cli::parameter\_bool Class Reference

String parameter for [cli](#).

```
#include <cli.h>
```

Inheritance diagram for cli::parameter\_bool:



### 46.288.1 Detailed Description

Definition at line 276 of file cli.h.

### Public Member Functions

- virtual int [set](#) (std::string s)  
*Set from string.*
- virtual std::string [get](#) ()  
*Convert to string.*

### Data Fields

- bool \* [b](#)  
*Parameter.*

The documentation for this class was generated from the following file:

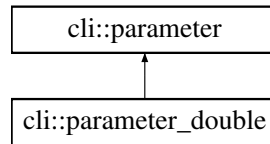
- cli.h

## 46.289 cli::parameter\_double Class Reference

Double parameter for [cli](#).

```
#include <cli.h>
```

Inheritance diagram for cli::parameter\_double:



#### 46.289.1 Detailed Description

Definition at line 299 of file cli.h.

##### Public Member Functions

- virtual int [set](#) (std::string s)  
*Set from string.*
- virtual std::string [get](#) ()  
*Convert to string.*

##### Data Fields

- double \* [d](#)  
*Parameter.*

The documentation for this class was generated from the following file:

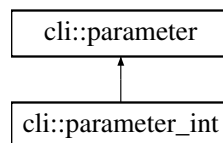
- cli.h

## 46.290 cli::parameter\_int Class Reference

Integer parameter for [cli](#).

```
#include <cli.h>
```

Inheritance diagram for cli::parameter\_int:



#### 46.290.1 Detailed Description

Definition at line 322 of file cli.h.

##### Public Member Functions

- virtual int [set](#) (std::string s)  
*Set from string.*
- virtual std::string [get](#) ()  
*Convert to string.*

### Data Fields

- int \* [i](#)  
*Parameter.*

The documentation for this class was generated from the following file:

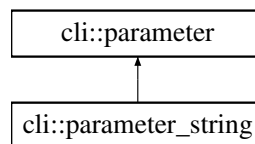
- cli.h

## 46.291 cli::parameter\_string Class Reference

String parameter for [cli](#).

```
#include <cli.h>
```

Inheritance diagram for cli::parameter\_string:



### 46.291.1 Detailed Description

Definition at line 253 of file cli.h.

### Public Member Functions

- virtual int [set](#) (std::string s)  
*Set from string.*
- virtual std::string [get](#) ()  
*Convert to string.*

### Data Fields

- std::string \* [str](#)  
*Parameter.*

The documentation for this class was generated from the following file:

- cli.h

## 46.292 permutation Class Reference

A class for representing permutations.

```
#include <permutation.h>
```

---

## 46.292.1 Detailed Description

A class for representing permutations. This permutation class is completely compatible with the GSL permutation object since it is derived from `gsl_permutation_struct` (and thus also `gsl_permutation`). For example, the last line in the code below is a trivial upcast, and permitted since `gsl_permutation` is a base type of this class.

```
permutation p(5);
p.init();
gsl_permutation *gp=&p;
```

See also the [Permutations](#) section of the User's guide.

Definition at line 84 of file `permutation.h`.

## Public Member Functions

- [permutation](#) (size\_t dim=0)  
*Create a permutation of size dim.*
- size\_t & [operator\[\]](#) (size\_t i)  
*Array-like indexing.*
- const size\_t & [operator\[\]](#) (size\_t i) const  
*Array-like indexing.*
- size\_t & [operator\(\)](#) (size\_t i)  
*Array-like indexing.*
- const size\_t & [operator\(\)](#) (size\_t i) const  
*Array-like indexing.*
- size\_t [get](#) (size\_t i) const  
*Get (with optional range-checking)*
- int [set](#) (size\_t i, size\_t val)  
*Set (with optional range-checking)*
- int [init](#) ()  
*Initialize permutation to the identity.*
- size\_t [size](#) () const  
*Return permutation size.*
- int [allocate](#) (size\_t dim)  
*Allocate memory for a permutation of size dim.*
- int [free](#) ()  
*Free the memory.*
- int [swap](#) (const size\_t i, const size\_t j)  
*Swap two elements of a permutation.*
- bool [valid](#) () const  
*Check to see that a permutation is valid.*
- int [reverse](#) ()  
*Reverse the permutation.*
- [permutation inverse](#) () const  
*Compute the inverse of a permutation.*
- template<class vec\_t >  
int [apply](#) (vec\_t &v) const  
*Apply the permutation to a vector.*
- template<class vec\_t >  
int [apply\\_inverse](#) (vec\_t &v) const  
*Apply the inverse permutation to a vector.*

## Copy constructors

- [permutation](#) (const [permutation](#) &v)
- [permutation & operator=](#) (const [permutation](#) &v)

## 46.292.2 Member Function Documentation

## 46.292.2.1 size\_t permutation::size ( ) const [inline]

If no memory has been allocated, this will quietly return zero.

Definition at line 234 of file permutation.h.

## 46.292.2.2 int permutation::free ( ) [inline]

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 255 of file permutation.h.

The documentation for this class was generated from the following file:

- [permutation.h](#)

## 46.293 pinside Class Reference

Test line intersection and point inside polygon.

```
#include <pinside.h>
```

## 46.293.1 Detailed Description

This is a fast and dirty implementation of the point inside polygon test from Jerome L. Lewis, SIGSCE Bulletin, 34 (2002) 81.

Note that an error in that article ("count-" should have been "count--") has been corrected here.

**Idea for Future** The [inside\(\)](#) functions actually copy the points twice. This can be made more efficient.

Definition at line 66 of file pinside.h.

## Data Structures

- struct [line](#)  
*Internal line definition for [pinside](#).*
- struct [point](#)  
*Internal point definition for [pinside](#).*

## Public Member Functions

- int [intersect](#) (double x1, double y1, double x2, double y2, double x3, double y3, double x4, double y4)  
*Determine if two line segments intersect.*
- int [inside](#) (double x, double y, const [o2scl::ovector\\_base](#) &xa, const [o2scl::ovector\\_base](#) &ya)  
*Determine if point (x,y) is inside a polygon.*
- template<class vec\_t >  
int [inside](#) (double x, double y, size\_t n, const vec\_t &xa, const vec\_t &ya)  
*Determine if point (x,y) is inside a polygon.*
- int [test](#) ([test\\_mgr](#) &t)  
*Perform some simple testing.*

## Protected Member Functions

- int [intersect](#) (line P, line Q)  
*Test if line segments P and Q intersect.*
- int [inside](#) (point t, point p[], int N)  
*Test if point t is inside polygon p of size N.*

## 46.293.2 Member Function Documentation

46.293.2.1 int [pinside::intersect](#) ( double x1, double y1, double x2, double y2, double x3, double y3, double x4, double y4 ) [inline]

The function returns 1 if the line segment determined by the endpoints  $(x_1, y_1)$  and  $(x_2, y_2)$  and the line segment determined by the endpoints  $(x_3, y_3)$  and  $(x_4, y_4)$  intersect, and 0 otherwise.

Definition at line 98 of file pinside.h.

46.293.2.2 int [pinside::inside](#) ( double x, double y, const o2scl::ovector\_base & xa, const o2scl::ovector\_base & ya )

This returns 1 if the point  $(x, y)$  is inside the polygon defined by xa and ya, and 0 otherwise.

Note that if the point  $(x, y)$  is exactly on the polygon, then the result of this function is not well-defined and it will return either 0 or 1.

46.293.2.3 template<class vec\_t> int [pinside::inside](#) ( double x, double y, size\_t n, const vec\_t & xa, const vec\_t & ya ) [inline]

This returns 1 if the point  $(x, y)$  is inside the polygon defined by xa and ya, and 0 otherwise.

The parameter n should be the number of polygon points specified in vectors xa and ya.

Note that if the point  $(x, y)$  is exactly on the polygon, then the result of this function is not well-defined and it will return either 0 or 1.

Definition at line 130 of file pinside.h.

The documentation for this class was generated from the following file:

- pinside.h

## 46.294 planar\_intp&lt; vec\_t, mat\_t &gt; Class Template Reference

Interpolate among two independent variables with planes.

```
#include <planar_intp.h>
```

## 46.294.1 Detailed Description

```
template<class vec_t, class mat_t> class planar_intp< vec_t, mat_t >
```

This class is experimental.

This is an analog of 1-d linear interpolation for two dimensions, which is particularly useful with the data points are not arranged in a specified order (i.e. on a grid). For a set of data  $x_i, y_i, f_{j,i}$ , the values of  $f_j$  are predicted given a value of x and y. In contrast to [twod\\_intp](#), the data need not be presented in a grid. This interpolation is performed by finding the plane that goes through three closest points in the data set. Distances are determined with

$$d_{ij} = \sqrt{\left(\frac{x_i - x_j}{\Delta x}\right)^2 + \left(\frac{y_i - y_j}{\Delta y}\right)^2}$$

where  $\Delta x = x_{\max} - x_{\min}$  and  $\Delta y = y_{\max} - y_{\min}$ .

This procedure will fail if the three closest points are co-linear, and `interp()` will then call the error handler.

There is no caching so the numeric values of the data may be freely changed between calls to `interp()`.

The vector and matrix types can be any types which have suitably defined functions `operator[]`.

For example, with 10 random points in the x-y plane with  $-1 < x < 1$  and  $-1 < y < 1$ , the planes are demarcated according to

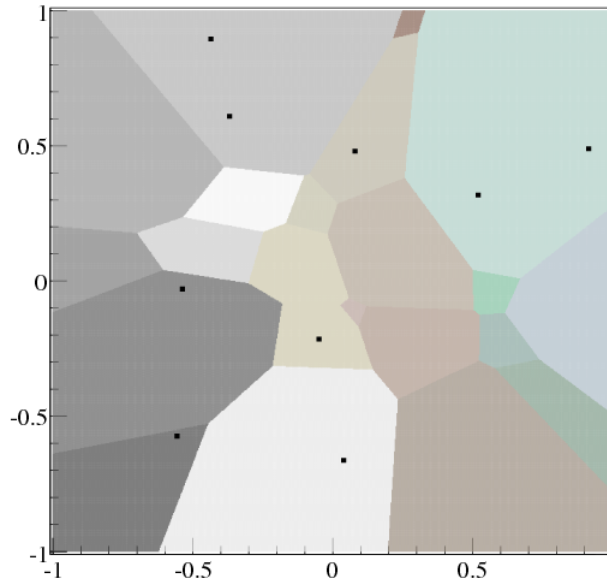


Figure 12: in\_planar\_intp.pdf

where each polygonal region represents the set of all points in the domain which will be mapped to the same plane to approximate the function.

**Idea for Future** Rewrite so that it never fails unless all the points in the data set lie on a line. This would probably demand sorting all of the points by distance from desired location. (11/1/11 - Maybe not. We might be able to get away with just storing an vector which records the index  $j$  of the point in the data set which is the nearest neighbor for each point  $i$  in the data set.)

**Idea for Future** Instead of comparing `den` with zero, add the option of comparing it with a small number.

**Idea for Future** Allow the user to specify the scales used for  $x$  and  $y$ , instead of computing max-min every time.

**Idea for Future** The generalization to more dimensions might be straight forward.

Definition at line 90 of file `planar_intp.h`.

#### Public Member Functions

- `int set_data` (`size_t n_points`, `vec_t &x`, `vec_t &y`, `size_t n_dat`, `mat_t &dat`)  
*Initialize the data for the planar interpolation.*
- `int interp` (`double x`, `double y`, `vec_t &ip`)  
*Perform the planar interpolation.*
- `int interp` (`double x`, `double y`, `vec_t &ip`, `size_t &i1`, `double &x1`, `double &y1`, `size_t &i2`, `double &x2`, `double &y2`, `size_t &i3`, `double &x3`, `double &y3`)  
*Planar interpolation returning the closest points.*

## Protected Member Functions

- `int swap (size_t &i1, double &c1, size_t &i2, double &c2)`  
*Swap points 1 and 2.*

## Protected Attributes

- `size_t np`  
*The number of points.*
- `size_t nd`  
*The number of functions.*
- `vec_t * ux`  
*The x-values.*
- `vec_t * uy`  
*The y-values.*
- `mat_t * udat`  
*The data.*
- `bool data_set`  
*True if the data has been specified.*

## 46.294.2 Member Function Documentation

46.294.2.1 `template<class vec_t, class mat_t> int planar_intp< vec_t, mat_t >::interp ( double x, double y, vec_t & ip ) [inline]`

It is assumed that `ip` is properly allocated beforehand.

Definition at line 118 of file `planar_intp.h`.

46.294.2.2 `template<class vec_t, class mat_t> int planar_intp< vec_t, mat_t >::interp ( double x, double y, vec_t & ip, size_t & i1, double & x1, double & y1, size_t & i2, double & x2, double & y2, size_t & i3, double & x3, double & y3 ) [inline]`

This function interpolates `x` and `y` into the data returning `ip`. It also returns the three closest `x`- and `y`-values used for computing the plane.

It is assumed that `ip` is properly allocated beforehand. Put in initial points

Sort initial points

Definition at line 132 of file `planar_intp.h`.

The documentation for this class was generated from the following file:

- `planar_intp.h`

46.295 `pinside::point` Struct Reference

Internal point definition for `pinside`.

```
#include <pinside.h>
```

## 46.295.1 Detailed Description

Definition at line 71 of file `pinside.h`.

## Data Fields

- `double x`



- double **y**

The documentation for this struct was generated from the following file:

- [pinside.h](#)

## 46.296 o2scl\_linalg::pointer\_2\_mem Class Reference

Allocation object for 2 C-style arrays of equal size.

```
#include <tridiag_base.h>
```

### 46.296.1 Detailed Description

This class is used in [solve\\_tridiag\\_nonsym\(\)](#).

Definition at line 58 of file [tridiag\\_base.h](#).

#### Public Member Functions

- void **allocate** (size\_t n)
- double \* **get\_pointer1** ()
- double \* **get\_pointer2** ()
- void **free** ()

#### Data Fields

- double \* **v1**
- double \* **v2**

The documentation for this class was generated from the following file:

- [tridiag\\_base.h](#)

## 46.297 pointer\_2d\_alloc< base\_t > Class Template Reference

A simple class to provide an [allocate\(\)](#) function for pointers.

```
#include <array.h>
```

### 46.297.1 Detailed Description

```
template<class base_t>class pointer_2d_alloc< base_t >
```

This class uses `new` and `delete` and may throw a C++ exception in the usual way. It contains a simple garbage collection mechanism to assist in exception safety.

This class is used in [columnify](#) and [cern\\_mroot](#).

**Idea for Future** There may be a slight issue here if the pointer allocation succeeds and the list insertion fails, and the user catches the exception thrown by the list insertion failure, then a memory leak will ensue. This might be partially ameliorated by counting allocations and insertions. This failure mechanism is rarely encountered in practice.

Definition at line 200 of file [array.h](#).

## Data Structures

- struct [pointer\\_comp](#)

## Public Member Functions

- void [allocate](#) (base\_t \*\*&v, size\_t i, size\_t j)  
*Allocate v for i elements.*
- void [free](#) (base\_t \*\*&v, size\_t i)  
*Free memory.*

## Protected Types

- typedef std::map< base\_t \*\*, size\_t, [pointer\\_comp](#) > ::iterator [iter](#)  
*Iterator type.*

## Protected Attributes

- std::map< base\_t \*\*, size\_t, [pointer\\_comp](#) > [list](#)  
*Store allocated pointers.*

The documentation for this class was generated from the following file:

- [array.h](#)

## 46.298 o2scl\_linalg::pointer\_4\_mem Class Reference

Allocation object for 4 C-style arrays of equal size.

```
#include <tridiag_base.h>
```

## 46.298.1 Detailed Description

This class is used in [solve\\_tridiag\\_sym\(\)](#) and [solve\\_cyc\\_tridiag\\_nonsym\(\)](#).

Definition at line 78 of file tridiag\_base.h.

## Public Member Functions

- void **allocate** (size\_t n)
- double \* **get\_pointer1** ()
- double \* **get\_pointer2** ()
- double \* **get\_pointer3** ()
- double \* **get\_pointer4** ()
- void **free** ()

## Data Fields

- double \* **v1**
  - double \* **v2**
  - double \* **v3**
  - double \* **v4**
-

The documentation for this class was generated from the following file:

- [tridiag\\_base.h](#)

## 46.299 o2scl\_linalg::pointer\_5\_mem Class Reference

Allocation object for 5 C-style arrays of equal size.

```
#include <tridiag_base.h>
```

### 46.299.1 Detailed Description

This class is used in [solve\\_cyc\\_tridiag\\_sym\(\)](#).

Definition at line 103 of file [tridiag\\_base.h](#).

#### Public Member Functions

- void **allocate** (size\_t n)
- double \* **get\_pointer1** ()
- double \* **get\_pointer2** ()
- double \* **get\_pointer3** ()
- double \* **get\_pointer4** ()
- double \* **get\_pointer5** ()
- void **free** ()

#### Data Fields

- double \* **v1**
- double \* **v2**
- double \* **v3**
- double \* **v4**
- double \* **v5**

The documentation for this class was generated from the following file:

- [tridiag\\_base.h](#)

## 46.300 pointer\_alloc< base\_t > Class Template Reference

A simple class to provide an [allocate\(\)](#) function for pointers.

```
#include <array.h>
```

### 46.300.1 Detailed Description

```
template<class base_t>class pointer_alloc< base_t >
```

This class uses `new` and `delete` and may throw a C++ exception in the usual way. It contains a simple garbage collection mechanism to assist in exception safety.

This class is used in [tensor\\_grid](#).

**Idea for Future** There may be a slight issue here if the pointer allocation succeeds and the list insertion fails, and the user catches the exception thrown by the list insertion failure, then a memory leak will ensue. This might be partially ameliorated by counting allocations and insertions. This failure mechanism is rarely encountered in practice.

Definition at line 145 of file `array.h`.

#### Public Member Functions

- void `allocate` (`base_t *&v`, `size_t i`)  
*Allocate  $v$  for  $i$  elements.*
- void `free` (`base_t *&v`)  
*Free memory.*

#### Protected Attributes

- `std::vector< base_t * >` `list`  
*Store allocated pointers.*

The documentation for this class was generated from the following file:

- `array.h`

## 46.301 `pointer_2d_alloc< base_t >::pointer_comp` Struct Reference

### 46.301.1 Detailed Description

```
template<class base_t>struct pointer_2d_alloc< base_t >::pointer_comp
```

Definition at line 204 of file `array.h`.

#### Public Member Functions

- bool `operator()` (`base_t **const &p1`, `base_t **const &p2`) const  
*Return  $p1 < p2$ .*

The documentation for this struct was generated from the following file:

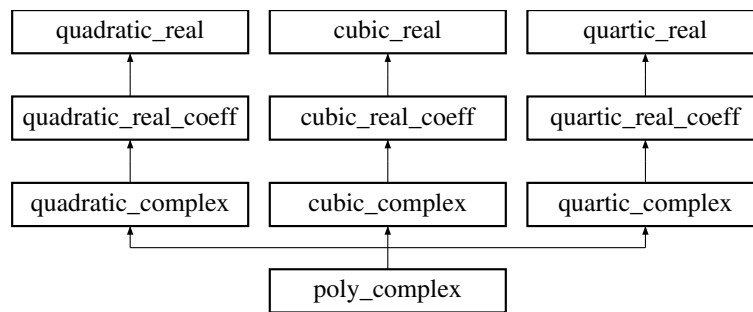
- `array.h`

## 46.302 `poly_complex` Class Reference

Solve a general polynomial with complex coefficients [abstract base].

```
#include <poly.h>
```

Inheritance diagram for `poly_complex`:



#### 46.302.1 Detailed Description

Definition at line 349 of file poly.h.

##### Public Member Functions

- virtual int [solve\\_c](#) (int n, const std::complex< double > co[], std::complex< double > ro[])=0  
*Solve the n-th order polynomial.*
- virtual int [polish\\_c](#) (int n, const std::complex< double > co[], std::complex< double > \*ro)=0  
*Polish the roots.*
- const char \* [type](#) ()  
*Return a string denoting the type ("poly\_complex")*

#### 46.302.2 Member Function Documentation

46.302.2.1 virtual int poly\_complex::solve\_c ( int n, const std::complex< double > co[], std::complex< double > ro[] ) [pure virtual]

The coefficients are stored in co[], with the leading coefficient as co[0] and the constant term as co[n]. The roots are returned in ro[0],...,ro[n-1].

The documentation for this class was generated from the following file:

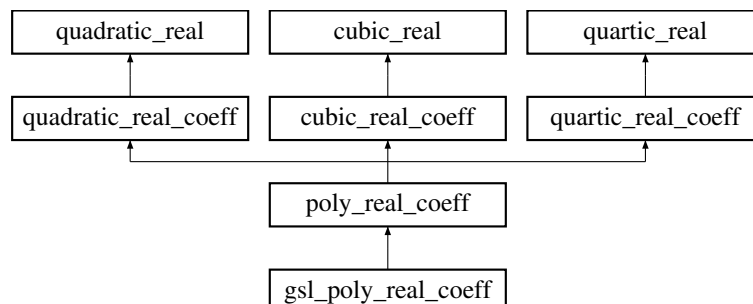
- [poly.h](#)

## 46.303 poly\_real\_coeff Class Reference

Solve a general polynomial with real coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for poly\_real\_coeff:



## 46.303.1 Detailed Description

Definition at line 326 of file poly.h.

## Public Member Functions

- virtual int [solve\\_rc](#) (int n, const double co[], std::complex< double > ro[])=0  
*Solve the n-th order polynomial.*
- const char \* [type](#) ()  
*Return a string denoting the type ("poly\_real\_coeff")*

## 46.303.2 Member Function Documentation

46.303.2.1 virtual int poly\_real\_coeff::solve\_rc ( int n, const double co[], std::complex< double > ro[] ) [pure virtual]

The coefficients are stored in co[], with the leading coefficient as co[0] and the constant term as co[n]. The roots are returned in ro[0],...,ro[n-1].

Implemented in [gsl\\_poly\\_real\\_coeff](#).

The documentation for this class was generated from the following file:

- [poly.h](#)

## 46.304 polylog Class Reference

Polylogarithms (approximate)  $Li_n(x)$ .

```
#include <polylog.h>
```

## 46.304.1 Detailed Description

This class is experimental.

This gives an approximation to the polylogarithm functions.

Only works at present for  $n = 0, 1, \dots, 6$ . Uses GSL library for  $n=2$ .

Uses linear interpolation for  $-1 < x < 0$  and a series expansion for  $x < -1$

## Idea for Future

- Give error estimate?
- Improve accuracy?
- Use more sophisticated interpolation?
- Add the series  $Li(n, x) = x + 2^{-n}x^2 + 3^{-n}x^3 + \dots$  for  $x \rightarrow 0$ ?
- Implement for positive arguments  $< 1.0$
- Make another polylog class which implements series acceleration?

For reference, there are exact relations

$$Li_2\left(\frac{1}{2}\right) = \frac{1}{12} \left[ \pi^2 - 6(\ln 2)^2 \right]$$

$$Li_3\left(\frac{1}{2}\right) = \frac{1}{24} \left[ 4(\ln 2)^3 - 2\pi^2 \ln 2 + 21\zeta(3) \right]$$

$$Li_{-1}(x) = \frac{x}{(1-x)^2}$$

$$\text{Li}_{-2}(x) = \frac{x(x+1)}{(1-x)^3}$$

Definition at line 78 of file polylog.h.

#### Public Member Functions

- double [li0](#) (double x)  
*0-th order polylogarithm* =  $x/(1-x)$
- double [li1](#) (double x)  
*1-st order polylogarithm* =  $-\ln(1-x)$
- double [li2](#) (double x)  
*2-nd order polylogarithm*
- double [li3](#) (double x)  
*3-rd order polylogarithm*
- double [li4](#) (double x)  
*4-th order polylogarithm*
- double [li5](#) (double x)  
*5-th order polylogarithm*
- double [li6](#) (double x)  
*6-th order polylogarithm*

The documentation for this class was generated from the following file:

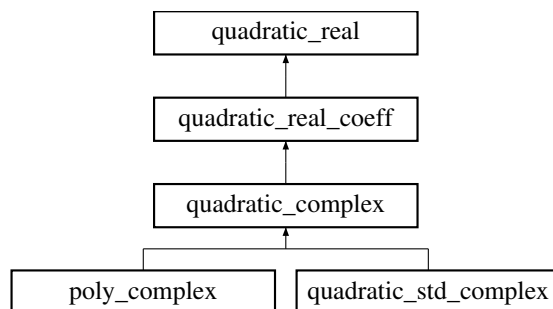
- polylog.h

## 46.305 quadratic\_complex Class Reference

Solve a quadratic polynomial with complex coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for quadratic\_complex:



### 46.305.1 Detailed Description

Definition at line 101 of file poly.h.

#### Public Member Functions

- virtual int [solve\\_r](#) (const double a2, const double b2, const double c2, double &x1, double &x2)  
*Solves the polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two solutions  $x = x_1$  and  $x = x_2$ .*
- virtual int [solve\\_rc](#) (const double a2, const double b2, const double c2, std::complex< double > &x1, std::complex< double > &x2)

- Solves the polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two complex solutions  $x = x_1$  and  $x = x_2$ .*
- virtual int [solve\\_c](#) (const std::complex< double > a2, const std::complex< double > b2, const std::complex< double > c2, std::complex< double > &x1, std::complex< double > &x2)=0  
*Solves the complex polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two complex solutions  $x = x_1$  and  $x = x_2$ .*
  - const char \* [type](#) ()  
*Return a string denoting the type ("quadratic\_complex")*

The documentation for this class was generated from the following file:

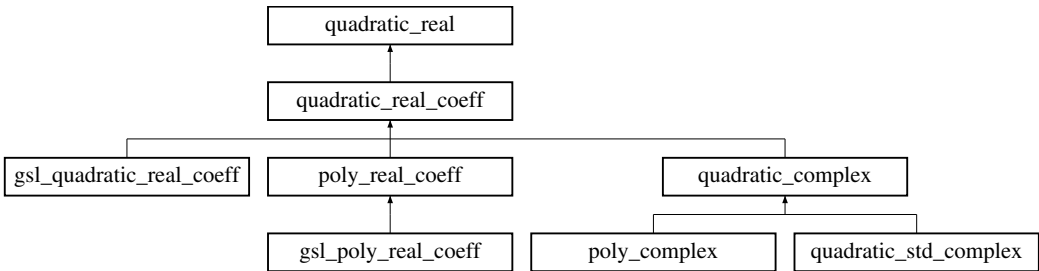
- [poly.h](#)

46.306   quadratic\_real Class Reference

Solve a quadratic polynomial with real coefficients and real roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for quadratic\_real:



46.306.1   Detailed Description

Definition at line 57 of file poly.h.

Public Member Functions

- virtual int [solve\\_r](#) (const double a2, const double b2, const double c2, double &x1, double &x2)=0  
*Solves the polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two solutions  $x = x_1$  and  $x = x_2$  .*
- const char \* [type](#) ()  
*Return a string denoting the type ("quadratic\_real")*

The documentation for this class was generated from the following file:

- [poly.h](#)

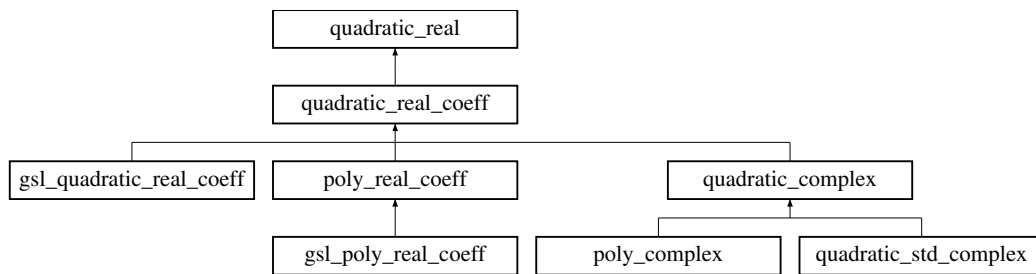
46.307   quadratic\_real\_coeff Class Reference

Solve a quadratic polynomial with real coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for quadratic\_real\_coeff:





#### 46.307.1 Detailed Description

Definition at line 75 of file poly.h.

#### Public Member Functions

- virtual int [solve\\_r](#) (const double a2, const double b2, const double c2, double &x1, double &x2)  
Solves the polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two solutions  $x = x_1$  and  $x = x_2$ .
- virtual int [solve\\_rc](#) (const double a2, const double b2, const double c2, std::complex< double > &x1, std::complex< double > &x2)=0  
Solves the polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two complex solutions  $x = x_1$  and  $x = x_2$ .
- const char \* [type](#) ()  
Return a string denoting the type ("quadratic\_real\_coeff")

The documentation for this class was generated from the following file:

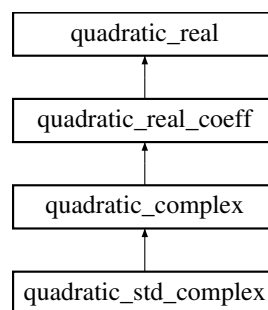
- [poly.h](#)

### 46.308 quadratic\_std\_complex Class Reference

Solve a quadratic with complex coefficients and complex roots.

```
#include <poly.h>
```

Inheritance diagram for quadratic\_std\_complex:



#### 46.308.1 Detailed Description

Definition at line 673 of file poly.h.

## Public Member Functions

- virtual int `solve_c` (const std::complex< double > a2, const std::complex< double > b2, const std::complex< double > c2, std::complex< double > &x1, std::complex< double > &x2)  
Solves the complex polynomial  $a_2x^2 + b_2x + c_2 = 0$  giving the two complex solutions  $x = x_1$  and  $x = x_2$ .
- const char \* `type` ()  
Return a string denoting the type ("quadratic\_std\_complex")

The documentation for this class was generated from the following file:

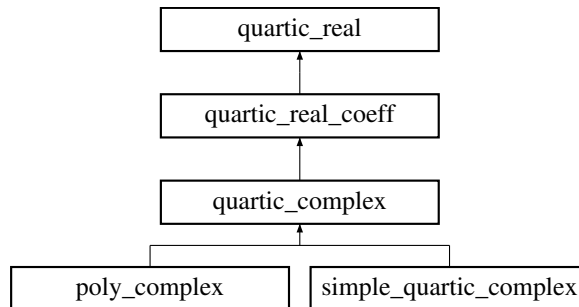
- [poly.h](#)

46.309 `quartic_complex` Class Reference

Solve a quartic polynomial with complex coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for `quartic_complex`:



## 46.309.1 Detailed Description

Definition at line 279 of file `poly.h`.

## Public Member Functions

- virtual int `solve_r` (const double a4, const double b4, const double c4, const double d4, const double e4, double &x1, double &x2, double &x3, double &x4)  
Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .
- virtual int `solve_rc` (const double a4, const double b4, const double c4, const double d4, const double e4, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3, std::complex< double > &x4)  
Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four complex solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .
- virtual int `solve_c` (const std::complex< double > a4, const std::complex< double > b4, const std::complex< double > c4, const std::complex< double > d4, const std::complex< double > e4, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3, std::complex< double > &x4)=0  
Solves the complex polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four complex solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .
- const char \* `type` ()  
Return a string denoting the type ("quartic\_complex")

The documentation for this class was generated from the following file:

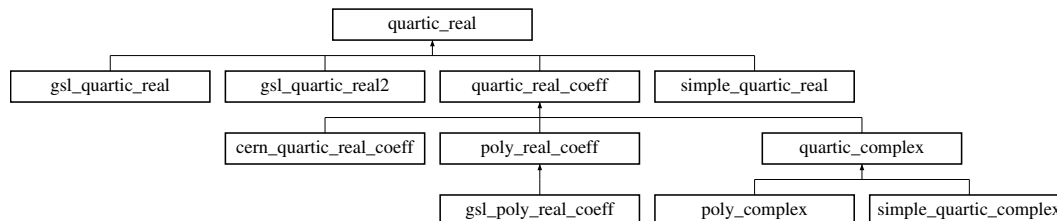
- [poly.h](#)

46.310 `quartic_real` Class Reference

Solve a quartic polynomial with real coefficients and real roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for `quartic_real`:



## 46.310.1 Detailed Description

Definition at line 223 of file `poly.h`.

## Public Member Functions

- virtual int `solve_r` (const double a4, const double b4, const double c4, const double d4, const double e4, double &x1, double &x2, double &x3, double &x4)=0  
Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .
- const char \* `type` ()  
Return a string denoting the type ("quartic\_real")

The documentation for this class was generated from the following file:

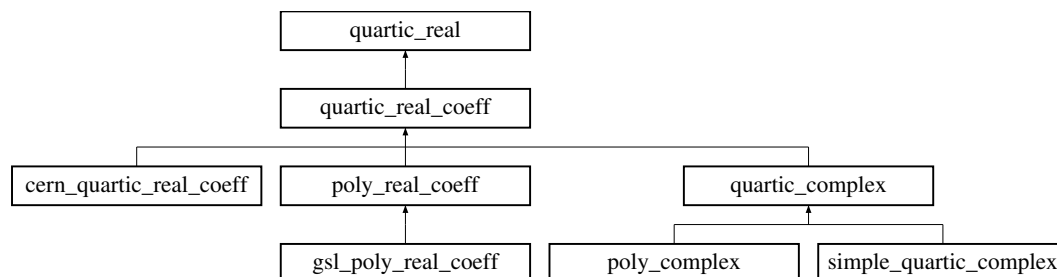
- `poly.h`

46.311 `quartic_real_coeff` Class Reference

Solve a quartic polynomial with real coefficients and complex roots [abstract base].

```
#include <poly.h>
```

Inheritance diagram for `quartic_real_coeff`:



## 46.311.1 Detailed Description

Definition at line 246 of file `poly.h`.

## Public Member Functions

- virtual int [solve\\_r](#) (const double a4, const double b4, const double c4, const double d4, const double e4, double &x1, double &x2, double &x3, double &x4)  
*Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .*
- virtual int [solve\\_rc](#) (const double a4, const double b4, const double c4, const double d4, const double e4, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3, std::complex< double > &x4)=0  
*Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four complex solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("quartic\_real\_coeff")*

The documentation for this class was generated from the following file:

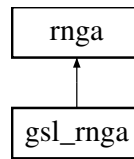
- [poly.h](#)

## 46.312 rnga Class Reference

Random number generator base.

```
#include <rnga.h>
```

Inheritance diagram for rnga:



## 46.312.1 Detailed Description

Using virtual functions is not recommended for random number generators, as speed is often an important issue. In order to facilitate the use of templates for routines which require random number generators, all descendants ought to provide the following functions:

- double random() - Provide a random number in [0.0,1.0)
- unsigned long int random\_int(unsigned long int n) - Provide a random integer in [0,n-1]
- unsigned long int get\_max() - Return the maximum integer for the random number generator. The argument to random\_int() should be less than the value returned by get\_max().

**Idea for Future** Consider some analog of the GSL function `gsl_rng_uniform_pos()`, i.e. as used in the GSL Monte Carlo classes.

Definition at line 52 of file `rnga.h`.

## Public Member Functions

- void [clock\\_seed](#) ()  
*Initialize the seed with a value taken from the computer clock.*
- unsigned long int [get\\_seed](#) ()  
*Get the seed.*
- void [set\\_seed](#) (unsigned long int s)  
*Set the seed.*

## Protected Member Functions

- **rnga** (const [rnga](#) &)
- **rnga & operator=** (const [rnga](#) &)

## Protected Attributes

- unsigned long int [seed](#)  
*The seed.*

## 46.312.2 Member Function Documentation

## 46.312.2.1 void rnga::clock\_seed ( )

This is a naive seed generator which uses `seed=time(0)` to generate a seed.

**Idea for Future** Figure out a better way of computing a random seed in a platform-independent way.

Reimplemented in [gsl\\_rnga](#).

The documentation for this class was generated from the following file:

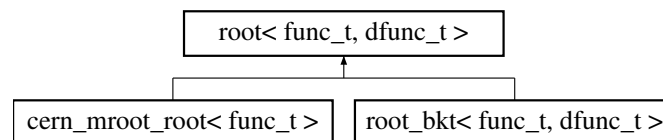
- [rnga.h](#)

## 46.313 root&lt; func\_t, dfunc\_t &gt; Class Template Reference

One-dimensional solver [abstract base].

```
#include <root.h>
```

Inheritance diagram for root< func\_t, dfunc\_t >:



## 46.313.1 Detailed Description

```
template<class func_t = funct, class dfunc_t = func_t>class root< func_t, dfunc_t >
```

**Idea for Future** Maybe consider allowing the user to specify the stream to which 'verbose' information is sent.

Definition at line 40 of file root.h.

## Public Member Functions

- virtual const char \* **type** ()  
*Return the type, "root".*
- virtual int **print\_iter** (double x, double y, int iter, double value=0.0, double limit=0.0, std::string comment="")  
*Print out iteration information.*
- virtual int **solve** (double &x, func\_t &func)=0

*Solve func using x as an initial guess.*

- virtual int [solve\\_bkt](#) (double &x1, double x2, func\_t &func)  
*Solve func in region  $x_1 < x < x_2$  returning  $x_1$ .*
- virtual int [solve\\_de](#) (double &x, func\_t &func, dfunc\_t &df)  
*Solve func using x as an initial guess using derivatives df.*

#### Data Fields

- double [tol\\_rel](#)  
*The maximum value of the functions for success (default  $10^{-8}$  )*
- double [tol\\_abs](#)  
*The minimum allowable stepsize (default  $10^{-12}$  )*
- int [verbose](#)  
*Output control (default 0)*
- int [ntrial](#)  
*Maximum number of iterations (default 100)*
- bool [err\\_nonconv](#)  
*If true, call the error handler if the routine does not "converge".*
- int [last\\_conv](#)  
*Zero if last call to [solve\(\)](#), [solve\\_bkt\(\)](#), or [solve\\_de\(\)](#) converged.*
- int [last\\_ntrial](#)  
*The number of iterations for in the most recent minimization.*

#### 46.313.2 Member Function Documentation

**46.313.2.1** `template<class func_t = funct, class dfunc_t = func_t> virtual int root< func_t, dfunc_t >::print_iter ( double x, double y, int iter, double value = 0.0, double limit = 0.0, std::string comment = "" ) [inline, virtual]`

Depending on the value of the variable verbose, this prints out the iteration information. If verbose=0, then no information is printed, while if verbose>1, then after each iteration, the present values of x and y are output to std::cout along with the iteration number. If verbose>=2 then each iteration waits for a character before continuing.

Definition at line 101 of file root.h.

#### 46.313.3 Field Documentation

**46.313.3.1** `template<class func_t = funct, class dfunc_t = func_t> int root< func_t, dfunc_t >::last_conv`

This is particularly useful if err\_nonconv is false to test if the last call to [solve\(\)](#), [solve\\_bkt\(\)](#), or [solve\\_de\(\)](#) converged.

Definition at line 82 of file root.h.

The documentation for this class was generated from the following file:

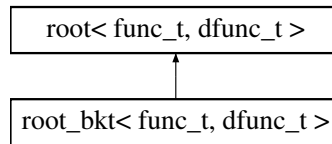
- root.h

### 46.314 root\_bkt< func\_t, dfunc\_t > Class Template Reference

One-dimensional bracketing solver [abstract base].

```
#include <root.h>
```

Inheritance diagram for root\_bkt< func\_t, dfunc\_t >:



#### 46.314.1 Detailed Description

```
template<class func_t = funct, class dfunc_t = func_t>class root_bkt< func_t, dfunc_t >
```

Definition at line 147 of file root.h.

##### Public Member Functions

- virtual const char \* [type](#) ()  
*Return the type, "root\_bkt".*
- virtual int [solve\\_bkt](#) (double &x1, double x2, func\_t &func)=0  
*Solve func in region  $x_1 < x < x_2$  returning  $x_1$ .*
- virtual int [solve](#) (double &x, func\_t &func)  
*Solve func using x as an initial guess.*
- virtual int [solve\\_de](#) (double &x, func\_t &func, dfunc\_t &df)  
*Solve func using x as an initial guess using derivatives df.*

##### Data Fields

- double [bracket\\_step](#)  
*The stepsize for automatic bracketing (default  $10^{-4}$ )*
- size\_t [bracket\\_iters](#)  
*The number of iterations in attempt to bracket root (default 10)*

#### 46.314.2 Field Documentation

46.314.2.1 `template<class func_t = funct, class dfunc_t = func_t> double root_bkt< func_t, dfunc_t >::bracket_step`

If this is exactly zero, it will be reset to  $10^{-4}$  by [solve\(\)](#).

Definition at line 165 of file root.h.

The documentation for this class was generated from the following file:

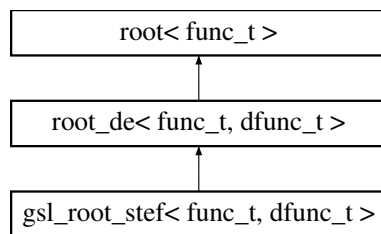
- root.h

#### 46.315 root\_de< func\_t, dfunc\_t > Class Template Reference

One-dimensional with solver with derivatives [abstract base].

```
#include <root.h>
```

Inheritance diagram for root\_de< func\_t, dfunc\_t >:



#### 46.315.1 Detailed Description

`template<class func_t = func_t, class dfunc_t = func_t>class root_de< func_t, dfunc_t >`

**Idea for Future** At the moment, the functions `solve()` and `solve_bkt()` are not implemented for derivative solvers.

Definition at line 259 of file root.h.

#### Public Member Functions

- virtual const char \* `type` ()  
*Return the type, "root\_de".*
- virtual int `solve_bkt` (double &x1, double x2, func\_t &func)  
*Solve func in region  $x_1 < x < x_2$  returning  $x_1$ .*
- virtual int `solve` (double &x, func\_t &func)  
*Solve func using x as an initial guess.*
- virtual int `solve_de` (double &x, func\_t &func, dfunc\_t &df)=0  
*Solve func using x as an initial guess using derivatives df.*

The documentation for this class was generated from the following file:

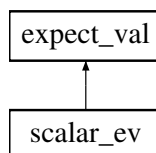
- root.h

## 46.316 scalar\_ev Class Reference

Scalar expectation value.

`#include <expect_val.h>`

Inheritance diagram for scalar\_ev:



#### 46.316.1 Detailed Description

See `expect_val` for some general notes on this and related classes.

This class is experimental.

---

#### Implementation notes

---



In the case where `nperblock` is zero, the vector `last` is used to store the most recent measurements, copying the results to `vals` only when `nblocks` measurements are stored in `last`. The variable `i` is only incremented when the vector `last` is full and the information is copied over to `vals`. This ensures that `vals` always contains averages with an equal number of measurements. The information in `last` is never used by `reblock_avg()`.

Definition at line 201 of file `expect_val.h`.

### Public Member Functions

- `scalar_ev ()`  
*Create with one unspecified block.*
- `scalar_ev (size_t n_blocks, size_t n_per_block)`  
*Create with `n_blocks` blocks and `n_per_block` points block.*
- `scalar_ev (const scalar_ev &ev)`  
*Copy constructor.*
- `scalar_ev & operator= (const scalar_ev &ev)`  
*Copy constructor.*
- virtual void `set_blocks (size_t n_blocks, size_t n_per_block)`  
*Reset for `n_blocks` blocks and `n_per_block` points block.*
- virtual void `free ()`  
*Free allocated data.*
- virtual void `reset ()`  
*Clear all the data.*
- virtual void `add (double val)`  
*Add measurement of value `val`.*

### Report statistics

- virtual void `current_avg_stats (double &avg, double &std_dev, double &avg_err, size_t &m_block, size_t &m_per_block) const`  
*Report current average, standard deviation, and the error in the average and include block information.*
- virtual void `current_avg (double &avg, double &std_dev, double &avg_err) const`  
*Report current average, standard deviation, and the error in the average.*
- virtual void `reblock_avg_stats (size_t new_blocks, double &avg, double &std_dev, double &avg_err, size_t &m_per_block) const`  
*Report average, standard deviation, and the error in the average assuming a new block size.*
- virtual void `reblock_avg (size_t new_blocks, double &avg, double &std_dev, double &avg_err) const`  
*Report average, standard deviation, and the error in the average assuming a new block size.*

### Direct manipulation of the stored data

- const `uvector & get_data () const`  
*Return the current data for all blocks.*
- const double & `operator[] (size_t i_block) const`  
*Return the current data for block with index `i_block`.*
- double & `operator[] (size_t i_block)`  
*Return the current data for block with index `i_block`.*
- template<class vec\_t >  
void `set_data (vec_t &v)`  
*Set the data for all blocks.*

### Protected Attributes

- `uvector vals`  
*The average for each block.*
- double `current`  
*The current rolling average.*
- `uvector last`  
*The most recent values for each block.*

## 46.316.2 Member Function Documentation

46.316.2.1 `virtual void scalar_ev::reblock_avg_stats ( size_t new_blocks, double & avg, double & std_dev, double & avg_err, size_t & m_per_block ) const` `[virtual]`

**Idea for Future** Use recurrence relation for averages here rather than dividing at the end.

## 46.316.3 Field Documentation

46.316.3.1 `uvector scalar_ev::vals` `[protected]`

This is a vector of length `nblocks`.

Definition at line 209 of file `expect_val.h`.

46.316.3.2 `uvector scalar_ev::last` `[protected]`

This is a vector of length `nblocks` used for when `n_per_block` is set to zero.

Definition at line 219 of file `expect_val.h`.

The documentation for this class was generated from the following file:

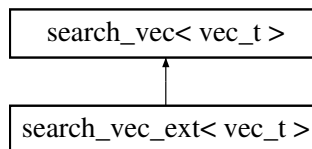
- `expect_val.h`

46.317 `search_vec< vec_t >` Class Template Reference

Searching class for monotonic data with caching.

```
#include <search_vec.h>
```

Inheritance diagram for `search_vec< vec_t >`:



## 46.317.1 Detailed Description

```
template<class vec_t>class search_vec< vec_t >
```

A searching class for monotonic vectors. A caching system similar to `gsl_interp_accel` is used.

To find the interval containing a value, use `find()`. If you happen to know in advance that the vector is increasing or decreasing, then you can use `find_inc()` or `find_dec()` instead. To ignore the caching and just use straight binary search, you can use the functions in `vector.h`.

Alternatively, if you just want to find the index with the element closest to a specified value, use `ordered_lookup()`. Note that `ordered_lookup()` is slightly different than `ovector_tlate::lookup()`, since the latter does not assume the data is monotonic.

The functions `find_inc()`, `find_dec()` and `find()` are designed to return the lower index of an interval containing the desired point, and as a result will never return the last index of a vector, e.g. for a vector of size `n` they always return a number between 0 and `n-2` inclusive. See `search_vec_ext` for an alternative.

## Note

The behavior of these functions is undefined if some of the user-specified data is not finite or not strictly monotonic. Two adjacent data points should not be equal. This class does not verify that the user-specified data has these properties.

This class does not store a copy of the data, but only a pointer to it. This means that one can safely modify the data after the constructor is called, so long as one does not make the vector smaller (as the cache might then point to a value outside the new vector) and so long as the new vector is still monotonic.

**Idea for Future** Consider a sanity check to ensure that the cache is never larger than the vector length.

Definition at line 77 of file search\_vec.h.

## Public Member Functions

- [search\\_vec](#) (size\_t nn, const vec\_t &x)  
*Create a searching object with vector x of size nn.*
- size\_t [find](#) (const double x0) const  
*Search an increasing or decreasing vector for the interval containing x0*
- size\_t [find\\_inc](#) (const double x0) const  
*Search an increasing vector for the interval containing x0*
- size\_t [find\\_dec](#) (const double x0) const  
*Search a decreasing vector for the interval containing x0*
- size\_t [ordered\\_lookup](#) (const double x0) const  
*Find the index of x0 in the ordered array x.*

## Protected Attributes

- size\_t [cache](#)  
*Storage for the most recent index.*
- const vec\_t \* [v](#)  
*The vector to be searched.*
- const size\_t [n](#)  
*The vector size.*

## 46.317.2 Member Function Documentation

46.317.2.1 `template<class vec_t> size_t search_vec< vec_t >::find ( const double x0 ) const` `[inline]`

This function is identical to [find\\_inc\(\)](#) if the data is increasing, and [find\\_dec\(\)](#) if the data is decreasing.

Reimplemented in [search\\_vec\\_ext< vec\\_t >](#).

Definition at line 116 of file search\_vec.h.

46.317.2.2 `template<class vec_t> size_t search_vec< vec_t >::find_inc ( const double x0 ) const` `[inline]`

This function is a cached version of [vector\\_bsearch\\_inc\(\)](#), analogous to `gsl_interp_accel_find()`, except that it does not internally record cache hits and misses.

Reimplemented in [search\\_vec\\_ext< vec\\_t >](#).

Definition at line 130 of file search\_vec.h.

46.317.2.3 `template<class vec_t> size_t search_vec< vec_t >::find_dec ( const double x0 ) const` `[inline]`

This function is a cached version of [vector\\_bsearch\\_dec\(\)](#). The operation of this function is undefined if the data is not strictly monotonic, i.e. if some of the data elements are equal.

Reimplemented in [search\\_vec\\_ext< vec\\_t >](#).

Definition at line 147 of file search\_vec.h.

**46.317.2.4** `template<class vec_t> size_t search_vec< vec_t >::ordered_lookup ( const double x0 ) const [inline]`

This returns the index *i* for which *x*[*i*] is as close as possible to *x0* if *x*[*i*] is either increasing or decreasing.

If you have a non-monotonic vector, you can use [vector\\_lookup\(\)](#) instead, or if you a non-monotonic [ovector](#) or [uvector](#) object, consider using [ovector\\_view\\_tlate::lookup\(\)](#) or [uvector\\_view\\_tlate::lookup\(\)](#) instead of this function.

Generally, if there are two adjacent entries with the same value, this function will return the entry with the smaller index. (This is the same as the convention in [ovector\\_view\\_tlate::lookup\(\)](#) and [uvector\\_view\\_tlate::lookup\(\)](#) ).

**Idea for Future** This function just uses the `find` functions and then adjusts the answer at the end if necessary. It might be possible to improve the speed by rewriting this from scratch.

Definition at line 178 of file search\_vec.h.

### 46.317.3 Field Documentation

**46.317.3.1** `template<class vec_t> size_t search_vec< vec_t >::cache [mutable, protected]`

#### Note

This is marked mutable to ensure const-correctness is straightforward.

Definition at line 88 of file search\_vec.h.

The documentation for this class was generated from the following file:

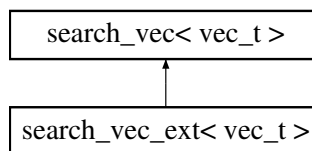
- search\_vec.h

## 46.318 search\_vec\_ext< vec\_t > Class Template Reference

An extended [search\\_vec](#) which is allowed to return the last element.

```
#include <search_vec.h>
```

Inheritance diagram for `search_vec_ext< vec_t >`:



### 46.318.1 Detailed Description

```
template<class vec_t>class search_vec_ext< vec_t >
```

Definition at line 217 of file search\_vec.h.

#### Public Member Functions

- [search\\_vec\\_ext](#) (size\_t nn, vec\_t &x)  
Create a searching object for vector *x* of size *nn*.

- `size_t find` (const double x0) const  
*Search an increasing or decreasing vector for the interval containing x0*
- `size_t find_inc` (const double x0) const  
*Search an increasing vector for the interval containing x0*
- `size_t find_dec` (const double x0) const  
*Search a decreasing vector for the interval containing x0*

#### 46.318.2 Constructor & Destructor Documentation

46.318.2.1 `template<class vec_t> search_vec_ext< vec_t >::search_vec_ext ( size_t nn, vec_t & x )` [inline]

**Idea for Future** This could be rewritten to allow vectors with only one element (5/2/11: It looks like this might have been done already?)

Create a searching object with vector `x` of size `nn`

Definition at line 230 of file `search_vec.h`.

The documentation for this class was generated from the following file:

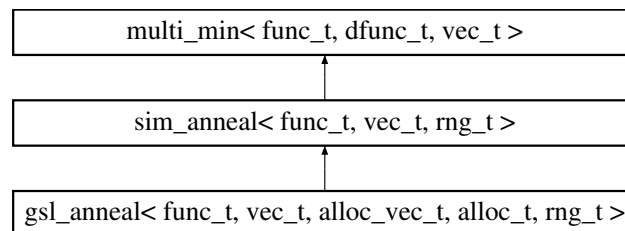
- `search_vec.h`

## 46.319 `sim_anneal< func_t, vec_t, rng_t >` Class Template Reference

Simulated annealing base.

```
#include <sim_anneal.h>
```

Inheritance diagram for `sim_anneal< func_t, vec_t, rng_t >`:



#### 46.319.1 Detailed Description

```
template<class func_t = multi_func_t, class vec_t = ovector_base, class rng_t = gsl_rng>class sim_anneal< func_t, vec_t, rng_t >
```

The seed of the generator is not fixed initially by calls to `mmin()`, so if successive calls should reproduce the same results, then the random seed should be set by the user before each call.

For the algorithms here, it is important that all of the inputs `x[i]` to the function are scaled similarly relative to the temperature. For example, if the inputs `x[i]` are all of order 1, one might consider a temperature schedule which begins with  $T = 1$ .

The number of iterations at each temperature is controlled by `multi_min::ntrial` which defaults to 100.

Definition at line 55 of file `sim_anneal.h`.

#### Public Member Functions

- virtual int `mmin` (size\_t nvar, vec\_t &x, double &fmin, func\_t &func)=0

*Calculate the minimum  $f_{min}$  of  $func$  w.r.t the array  $x$  of size  $nvar$ .*

- virtual int [print\\_iter](#) (size\_t nv, vec\_t &x, double y, int iter, double tptr, std::string comment)  
*Print out iteration information.*
- virtual const char \* [type](#) ()  
*Return string denoting type, "sim\_anneal".*

#### Data Fields

- rng\_t [def\\_rng](#)  
*The default random number generator.*

#### 46.319.2 Member Function Documentation

46.319.2.1 `template<class func_t = multi_func, class vec_t = ovector_base, class rng_t = gsl_rng> virtual int sim_anneal< func_t, vec_t, rng_t >::print_iter ( size_t nv, vec_t & x, double y, int iter, double tptr, std::string comment ) [inline, virtual]`

Depending on the value of the variable verbose, this prints out the iteration information. If verbose=0, then no information is printed, while if verbose>1, then after each iteration, the present values of x and y are output to std::cout along with the iteration number. If verbose>=2 then each iteration waits for a character.

Definition at line 87 of file sim\_anneal.h.

The documentation for this class was generated from the following file:

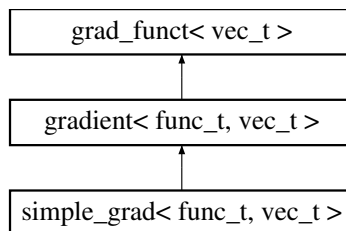
- sim\_anneal.h

#### 46.320 simple\_grad< func\_t, vec\_t > Class Template Reference

Simple automatic computation of gradient by finite differencing.

```
#include <multi_min.h>
```

Inheritance diagram for simple\_grad< func\_t, vec\_t >:



#### 46.320.1 Detailed Description

```
template<class func_t, class vec_t>class simple_grad< func_t, vec_t >
```

Definition at line 398 of file multi\_min.h.

#### Public Member Functions

- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &g)  
*Compute the gradient  $g$  at the point  $x$ .*

## Data Fields

- double [epsrel](#)  
*The relative stepsize for finite-differencing (default  $10^{-6}$ )*
- double [epsmin](#)  
*The minimum stepsize (default  $10^{-15}$ )*

The documentation for this class was generated from the following file:

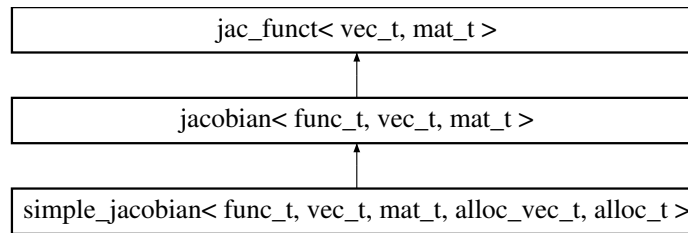
- multi\_min.h

## 46.321 simple\_jacobian&lt; func\_t, vec\_t, mat\_t, alloc\_vec\_t, alloc\_t &gt; Class Template Reference

Simple automatic Jacobian.

```
#include <jacobian.h>
```

Inheritance diagram for simple\_jacobian< func\_t, vec\_t, mat\_t, alloc\_vec\_t, alloc\_t >:



## 46.321.1 Detailed Description

```
template<class func_t = mm_func_t<>, class vec_t = ovector_base, class mat_t = omatrix_base, class alloc_vec_t = ovector, class alloc_t = ovector_-
alloc>class simple_jacobian< func_t, vec_t, mat_t, alloc_vec_t, alloc_t >
```

This class computes a numerical Jacobian by finite differencing. The stepsize is chosen to be  $h_j = \text{epsrel } x_j$  or  $h_j = \text{epsmin}$  if  $\text{epsrel } x_j < \text{epsmin}$ .

This is nearly equivalent to the GSL method for computing Jacobians as in `multiroots/fdjac.c`. To obtain the GSL behavior, set [epsrel](#) to `GSL_SQRT_DBL_EPSILON` and set [epsmin](#) to zero. The [gsl\\_mroot\\_hybrids](#) class sets [epsrel](#) to `GSL_SQRT_DBL_EPSILON` in its constructor, but does not set [epsmin](#) to zero.

This class does not separately check the vector and matrix sizes to ensure they are commensurate.

Definition at line 273 of file `jacobian.h`.

## Public Member Functions

- virtual int [operator\(\)](#) (size\_t nv, vec\_t &x, vec\_t &y, mat\_t &jac)  
*The operator()*

## Data Fields

- double [epsrel](#)  
*The relative stepsize for finite-differencing (default  $10^{-4}$ )*
- double [epsmin](#)  
*The minimum stepsize (default  $10^{-15}$ )*
- bool [err\\_nonconv](#)  
*If true, call the error handler if the routine does not "converge".*

## Protected Attributes

- `alloc_t ao`  
*For memory allocation.*
- `alloc_vec_t f`  
*Function values.*
- `alloc_vec_t xx`  
*Function arguments.*
- `size_t mem_size`  
*Size of allocated memory.*

The documentation for this class was generated from the following file:

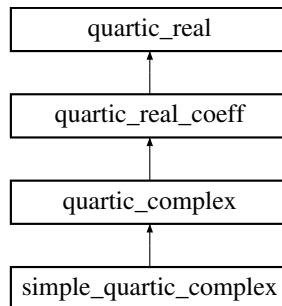
- `jacobian.h`

## 46.322 simple\_quartic\_complex Class Reference

Solve a quartic with complex coefficients and complex roots.

```
#include <poly.h>
```

Inheritance diagram for `simple_quartic_complex`:



## 46.322.1 Detailed Description

Definition at line 742 of file `poly.h`.

## Public Member Functions

- virtual int `solve_c` (const std::complex< double > a4, const std::complex< double > b4, const std::complex< double > c4, const std::complex< double > d4, const std::complex< double > e4, std::complex< double > &x1, std::complex< double > &x2, std::complex< double > &x3, std::complex< double > &x4)  
*Solves the complex polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four complex solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .*
- const char \* `type` ()  
*Return a string denoting the type ("simple\_quartic\_complex")*

The documentation for this class was generated from the following file:

- `poly.h`

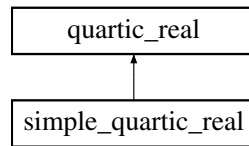


46.323 `simple_quartic_real` Class Reference

Solve a quartic with real coefficients and real roots.

```
#include <poly.h>
```

Inheritance diagram for `simple_quartic_real`:



## 46.323.1 Detailed Description

Definition at line 717 of file `poly.h`.

## Public Member Functions

- virtual int [solve\\_r](#) (const double a4, const double b4, const double c4, const double d4, const double e4, double &x1, double &x2, double &x3, double &x4)  
*Solves the polynomial  $a_4x^4 + b_4x^3 + c_4x^2 + d_4x + e_4 = 0$  giving the four solutions  $x = x_1$ ,  $x = x_2$ ,  $x = x_3$ , and  $x = x_4$ .*
- const char \* [type](#) ()  
*Return a string denoting the type ("simple\_quartic\_real")*

## Data Fields

- double [cube\\_root\\_tol](#)  
*A tolerance for determining the proper cube root (default  $10^{-6}$ )*

The documentation for this class was generated from the following file:

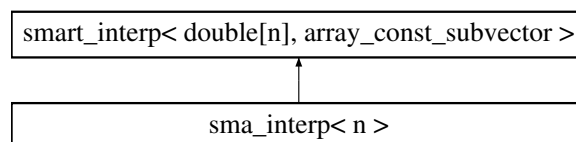
- [poly.h](#)

46.324 `sma_interp< n >` Class Template Reference

A specialization of [smart\\_interp](#) for C-style double arrays.

```
#include <smart_interp.h>
```

Inheritance diagram for `sma_interp< n >`:



## 46.324.1 Detailed Description

```
template<size_t n>class sma_interp< n >
```

Definition at line 807 of file `smart_interp.h`.

## Public Member Functions

- [sma\\_interp](#) (base\_interp\_mgr< double[n]> &it1, base\_interp\_mgr< array\_const\_subvector > &it3)  
*Create an interpolation object with user-specified interpolation types.*
- [sma\\_interp](#) ()  
*Create an interpolation object with the default interpolation types.*

The documentation for this class was generated from the following file:

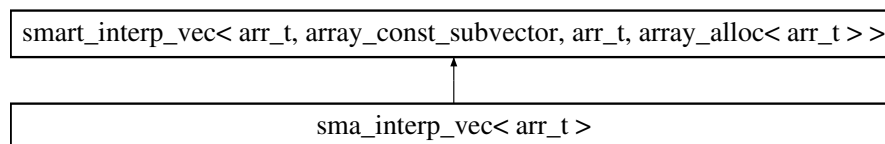
- [smart\\_interp.h](#)

## 46.325 sma\_interp\_vec&lt; arr\_t &gt; Class Template Reference

A specialization of [smart\\_interp\\_vec](#) for C-style double arrays.

```
#include <smart_interp.h>
```

Inheritance diagram for sma\_interp\_vec< arr\_t >:



## 46.325.1 Detailed Description

```
template<class arr_t>class sma_interp_vec< arr_t >
```

Definition at line 828 of file smart\_interp.h.

## Public Member Functions

- [sma\\_interp\\_vec](#) (base\_interp\_mgr< arr\_t > &it, base\_interp\_mgr< array\_const\_subvector > &it2, size\_t n, const arr\_t &x, const arr\_t &y)  
*Create an interpolation object with user-specified interpolation types.*
- [sma\\_interp\\_vec](#) (size\_t n, const arr\_t &x, const arr\_t &y)  
*Create an interpolation object with the default interpolation types.*

The documentation for this class was generated from the following file:

- [smart\\_interp.h](#)

## 46.326 smart\_interp&lt; vec\_t, svec\_t &gt; Class Template Reference

Smart interpolation class.

```
#include <smart_interp.h>
```

## 46.326.1 Detailed Description

```
template<class vec_t = ovector_const_view, class svec_t = ovector_const_subvector>class smart_interp< vec_t, svec_t >
```

This class can semi-intelligently handle arrays which are not-well formed outside the interpolation region. In particular, if an initial interpolation or derivative calculation fails, the arrays are searched for the largest neighborhood around the point  $x$  for which an interpolation or differentiation will likely produce a finite result.

Definition at line 51 of file `smart_interp.h`.

## Public Member Functions

- `smart_interp` (`base_interp_mgr< vec_t > &im1`, `base_interp_mgr< svec_t > &im3`)  
*Create a new interpolation object with the specified interpolation managers.*
- `smart_interp` ()  
*Create an interpolation object with the default cubic spline interpolation managers.*
- virtual double `interp` (const double  $x_0$ , size\_t  $n$ , const vec\_t & $x$ , const vec\_t & $y$ )  
*Give the value of the function  $y(x = x_0)$ .*
- virtual double `deriv` (const double  $x_0$ , size\_t  $n$ , const vec\_t & $x$ , const vec\_t & $y$ )  
*Give the value of the derivative  $y^{prime}(x = x_0)$ .*
- virtual double `deriv2` (const double  $x_0$ , size\_t  $n$ , const vec\_t & $x$ , const vec\_t & $y$ )  
*Give the value of the second derivative  $y^{prime2}(x = x_0)$ .*
- virtual double `integ` (const double  $a$ , const double  $b$ , size\_t  $n$ , const vec\_t & $x$ , const vec\_t & $y$ )  
*Give the value of the integral  $\int_a^b y(x) dx$ .*

## Data Fields

## Default interpolation managers

- `def_interp_mgr< vec_t, cspline_interp >` **dim1**
- `def_interp_mgr< svec_t, cspline_interp >` **dim3**

## Protected Member Functions

- size\_t `local_lookup` (size\_t  $n$ , const vec\_t & $x$ , double  $x_0$ )  
*A lookup function for generic vectors.*
- int `find_subset` (const double  $a$ , const double  $b$ , size\_t  $sz$ , const vec\_t & $x$ , const vec\_t & $y$ , size\_t & $nsz$ )  
*Try to find the largest monotonic and finite region around the desired location.*

## Protected Attributes

## Storage internally created subvectors

- bool `sxalloc`
- const svec\_t \* `sx`
- const svec\_t \* `sy`

## Pointers to interpolation objects

- `base_interp< vec_t > * rit1`
- `base_interp< svec_t > * rit3`

## Pointers to interpolation managers

- `base_interp_mgr< vec_t > * bim1`
- `base_interp_mgr< svec_t > * bim3`

## 46.326.2 Member Function Documentation

46.326.2.1 `template<class vec_t = ovector_const_view, class svec_t = ovector_const_subvector> virtual double smart_interp< vec_t, svec_t >::interp ( const double x0, size_t n, const vec_t & x, const vec_t & y ) [inline, virtual]`

**Todo** After calling `find_subset`, I think we might need to double check that `nn` is larger than the minimum interpolation size.

Definition at line 134 of file `smart_interp.h`.

46.326.2.2 `template<class vec_t = ovector_const_view, class svec_t = ovector_const_subvector> int smart_interp< vec_t, svec_t >::find_subset ( const double a, const double b, size_t sz, const vec_t & x, const vec_t & y, size_t & nsz ) [inline, protected]`

This function tries to find the largest monotonic region enclosing both `a` and `b` in the vector `x`. If it succeeds, it returns `gsl_success`, and if it fails, it returns `gsl_efaied`. It does not call the error handler.

**Todo** The error handling is a bit off here, as it can return a non-zero value even with there is no real "error". We should just make a new bool reference paramter.

Definition at line 409 of file `smart_interp.h`.

The documentation for this class was generated from the following file:

- [smart\\_interp.h](#)

46.327 `smart_interp_vec< vec_t, svec_t, alloc_vec_t, alloc_t >` Class Template Reference

Smart interpolation class with pre-specified vectors.

```
#include <smart_interp.h>
```

## 46.327.1 Detailed Description

```
template<class vec_t, class svec_t, class alloc_vec_t, class alloc_t>class smart_interp_vec< vec_t, svec_t, alloc_vec_t, alloc_t >
```

This class can semi-intelligently handle arrays which are not-well formed outside the interpolation region. In particular, if an initial interpolation or derivative calculation fails, the arrays are searched for the largest neighborhood around the point `x` for which an interpolation or differentiation will likely produce a finite result.

**Idea for Future** Properly implement handling of non-monotonic regions in the derivative functions as well as the interpolation function.

Definition at line 534 of file `smart_interp.h`.

## Public Member Functions

- `smart_interp_vec` (size\_t n, const vec\_t &x, const vec\_t &y)  
*Create with base interpolation objects `it` and `rit`.*
- `smart_interp_vec` (base\_interp\_mgr< vec\_t > &it1, base\_interp\_mgr< svec\_t > &it2, size\_t n, const vec\_t &x, const vec\_t &y)  
*Create with base interpolation objects `it` and `rit`.*
- virtual double `operator()` (const double x0)  
*Give the value of the function  $y(x = x_0)$ .*
- virtual double `interp` (const double x0)  
*Give the value of the function  $y(x = x_0)$ .*

- virtual double [deriv](#) (const double x0)  
*Give the value of the derivative  $y^{prime}(x = x_0)$ .*
- virtual double [deriv2](#) (const double x0)  
*Give the value of the second derivative  $y^{prime2}(x = x_0)$ .*
- virtual double [integ](#) (const double x1, const double x2)  
*Give the value of the integral  $\int_a^b y(x) dx$ .*

#### Data Fields

- [def\\_interp\\_mgr](#)< vec\_t, [cspline\\_interp](#) > [dim1](#)  
*Default interpolation manager.*
- [def\\_interp\\_mgr](#)< svec\_t, [cspline\\_interp](#) > [dim2](#)  
*Default interpolation manager.*

#### Protected Member Functions

- size\_t [local\\_lookup](#) (size\_t n, const vec\_t &x, double x0)  
*A lookup function for generic vectors.*
- int [find\\_inc\\_subset](#) (const double x0, size\_t sz, const vec\_t &x, const vec\_t &y, size\_t &nusz)  
*Try to find the largest monotonically increasing and finite region around the desired location.*

#### Protected Attributes

- bool [sxalloc](#)  
*If true, then [sx](#) and [sy](#) have been allocated.*
- svec\_t \* [sx](#)  
*Storage for internally created subvector.*
- svec\_t \* [sy](#)  
*Storage for internally created subvector.*
- [base\\_interp](#)< vec\_t > \* [rit1](#)  
*Pointer to base interpolation object.*
- [base\\_interp](#)< svec\_t > \* [rit2](#)  
*Pointer to base interpolation object.*
- [base\\_interp\\_mgr](#)< vec\_t > \* [bim1](#)  
*Pointer to base interpolation manager.*
- [base\\_interp\\_mgr](#)< svec\_t > \* [bim2](#)  
*Pointer to base interpolation manager.*
- alloc\_t [ao](#)  
*Memory allocator for objects of type `alloc_vec_t`.*
- bool [inc](#)  
*True if the user-specified  $x$  vector is increasing.*
- const vec\_t \* [lx](#)  
*Pointer to user-specified vector.*
- const vec\_t \* [ly](#)  
*Pointer to user-specified vector.*
- size\_t [ln](#)  
*Size of user-specified vector.*

#### 46.327.2 Member Function Documentation

46.327.2.1 `template<class vec_t, class svec_t, class alloc_vec_t, class alloc_t> int smart_interp_vec< vec_t, svec_t, alloc_vec_t, alloc_t >::find_inc_subset( const double x0, size_t sz, const vec_t &x, const vec_t &y, size_t &nusz ) [inline, protected]`

This function looks through the vector  $x$  near the element closest to  $x_0$  to find the largest possible monotonic region. If it succeeds, it returns [gsl\\_success](#), and if it fails, it returns [gsl\\_efault](#). It does not call the error handler.

**Todo** Variables `row` and `row` appear to be unused? (2/17/11)

Definition at line 761 of file `smart_interp.h`.

The documentation for this class was generated from the following file:

- [smart\\_interp.h](#)

## 46.328 `table::sortd_s` Struct Reference

A structure for sorting in [table](#) [protected].

```
#include <table.h>
```

### 46.328.1 Detailed Description

This struct is used internally by [table](#) to perform sorting and need not be instantiated by the casual end-user.

Definition at line 1052 of file `table.h`.

#### Data Fields

- double [val](#)  
*Value to sort.*
- int [indx](#)  
*Sorted index.*

The documentation for this struct was generated from the following file:

- `table.h`

## 46.329 `string_comp` Struct Reference

Simple string comparison.

```
#include <misc.h>
```

### 46.329.1 Detailed Description

This struct is used internally by `O2scl` for the STL routines which require a way to compare strings in the class [table](#) and in the I/O classes.

Definition at line 169 of file `misc.h`.

#### Public Member Functions

- bool [operator\(\)](#) (const std::string s1, const std::string s2) const  
*Return  $s1 < s2$ .*

The documentation for this struct was generated from the following file:

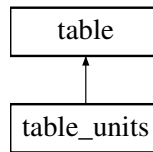
- [misc.h](#)
-

## 46.330 table Class Reference

Data table class.

```
#include <table.h>
```

Inheritance diagram for table:



### 46.330.1 Detailed Description

#### Summary

A class to contain and manipulate several equally-sized columns of data. The purpose of this class is to provide a structure which allows one to refer to the columns using a name represented by a string. Thus for a table object named `t` with 3 columns (named "colx", "coly" and "colz") and three rows, one could do the following:

```
// Set the 1st row of column "colx" to 1.0
t.set("colx",0,1.0);
// Set the 2nd row of column "colz" to 2.0
t.set("colz",1,2.0);
// Set the 3rd row of column "coly" to 4.0
t.set("coly",2,4.0);
// This will print out 2.0
cout << t.get("colz",1) << endl;
```

Note that the rows are numbered starting with 0 instead of starting with 1. To output all the rows of entire column, one can use

```
for(size_t i=0;i<t.get_nlines();i++) {
    cout << i << " " << t.get("colx",i) << endl;
}
```

To output all the columns of an entire row (in the following example it is the second row), labeled by their column name, one can use:

```
for(size_t i=0;i<t.get_ncolumns();i++) {
    cout << t.get_column_name(i) << " ";
}
cout << endl;
for(size_t i=0;i<t.get_ncolumns();i++) {
    cout << t.get(i,1) << " ";
}
cout << endl;
```

Methods are provided for interpolating columns, sorting columns, finding data points, and several other manipulations of the data.

#### Column size

The columns grow automatically (similar to the STL `<vector>`) in response to an attempt to call `set()` for a row that does not presently exist or in a call to `line_of_data()` when the table is already full. However, this forces memory rearrangements that are expensive,  $O(R \times C)$ . If the user has a good estimate of the number of rows beforehand, it is best to either specify this in the constructor, or in an explicit call to `inc_maxlines()`.

#### Lookup, differentiation, integration, and interpolation

Lookup, differentiation, integration, and interpolation are automatically implemented using splines from the class `smart_interp_vec`. A caching mechanism is implemented so that successive interpolations, derivative evaluations or integrations over the same two columns are fast.

## Sorting

The columns are automatically sorted by name for speed, the results can be accessed by `table::get_sorted_name(i)`. Individual columns can be sorted (`sort_column()`), or the entire table can be sorted by one column (`sort_table()`).

## Data representation

Each individual column is just an `ovector_base` object. The columns can be referred to in one of two ways:

- A numerical index from 0 to C-1 (where C is the number of columns). For example, data can be accessed through `table::get()` and `table::set(size_t c, size_t r, double val)`, or the overloaded `[]` operator, `table[c][r]`.
- A name of the column which is a string with no whitespace. For example, data can be accessed with `table::get(string cname, int r)` and `table::set(string cname, int r, double val)`.

The columns are organized in a both a `<map>` and a `<vector>` structure so that finding a column by its index, using either of

```
std::string table::get_column_name(size_t index);
ovector_base &table::get_column(int index);
```

takes only constant time, and finding a column by its name using either of

```
int lookup_column(std::string name, int &ix) const;
const ovector_base &get_column(std::string col) const;
```

is  $O(\log(C))$ . Insertion of a column (`new_column()`) is  $O(\log(C))$ , but deletion (`delete_column()`) is  $O(C)$ . Adding a row of data can be either  $O(1)$  or  $O(C)$ , but row insertion and deletion is slow, since the all of the rows must be shifted accordingly.

Because of the structure, this class is not suitable for the matrix manipulation. The classes `omatrix` and `umatrix` are better used for that purpose.

## Thread-safety

Generally, the member functions are thread-safe in the sense that one would expect: it is always permitted to have many threads accessing many distinct tables, but care must be taken if many threads are accessing only one table. Simple `get()` and `set()` functions are thread-safe (unless a `set()` function forces memory rearrangement), while insertion and deletion operations are not. Only the `const` version of the interpolation routines are thread-safe.

## I/O and command-line manipulation

When data from an object of type `table` is output to a file through a `hdf_output()` function (see `hdf_io.h`), the table can be manipulated on the command-line through the `acol` utility.

There is an example for the usage of this class given in `examples/ex_table.cpp`.

**Todo** Document or fix the fact that the table copy constructors do not copy the interpolation objects. Maybe `def_interp_mgr` objects can have their own copy constructors?

## Idea for Future

- Rewrite the `table::create_array()` and `table::insert_data()` functions for generic vector type
- Return the empty column in the operator[] functions as is done for the `get_column()` functions.
- A "delete rows" method to delete a range of several rows
- The present structure, `std::map<std::string, col, string_comp> atree` and `std::vector<aiter> alist`; could be replaced with `std::vector<col> list` and `std::map<std::string, int> tree` where the map just stores the index of the the column in the list.

Definition at line 191 of file `table.h`.

## Data Structures

- struct `col_s`  
*Column structure for `table` [protected].*
- struct `sortd_s`  
*A structure for sorting in `table` [protected].*



## Public Member Functions

- `table` (int cmaxlines=0)  
Create a new table with space for  $nlines \leq cmaxlines$ .
- `table` (const `table` &t)  
Copy constructor.
- `table` & `operator=` (const `table` &t)  
Copy constructor.
- virtual const char \* `type` ()  
Return the type, "table".

## Basic get and set methods

- int `set` (std::string col, size\_t row, double val)  
Set row `row` of column named `col` to value `val` -  $O(\log(C))$ .
- int `set` (size\_t icol, size\_t row, double val)  
Set row `row` of column number `icol` to value `val`.
- double `get` (std::string col, size\_t row) const  
Get value from row `row` of column named `col` -  $O(\log(C))$ .
- double `get` (size\_t icol, size\_t row) const  
Get value from row `row` of column number `icol` -  $O(1)$ .
- size\_t `get_ncolumns` () const  
Return the number of columns.
- size\_t `get_nlines` () const  
Return the number of lines.
- int `set_nlines` (size\_t il)  
Set the number of lines.
- int `set_nlines_auto` (size\_t il)  
Set the number of lines, increasing the size more aggressively.
- int `get_maxlines` ()  
Return the maximum number of lines.
- `ovector_base` & `get_column` (std::string col)  
Returns a reference to the column named `col` -  $O(\log(C))$
- const `ovector_base` & `get_column` (std::string col) const  
Returns a reference to the column named `col` -  $O(\log(C))$
- const `ovector_base` & `operator[]` (size\_t icol) const  
Returns the column of index `icol` -  $O(1)$  (const version)
- `ovector_base` & `operator[]` (size\_t icol)  
Returns the column of index `icol` -  $O(1)$ .
- const `ovector_base` & `operator[]` (std::string scol) const  
Returns the column named `scol` -  $O(\log(C))$  (const version)
- `ovector_base` & `operator[]` (std::string scol)  
Returns the column named `scol` -  $O(\log(C))$
- int `get_row` (std::string col, double val, `ovector` &row) const  
Returns a copy of the row with value `val` in column `col` -  $O(R*C)$
- int `get_row` (size\_t irow, `ovector` &row) const  
Returns a copy of row number `irow` -  $O(C)$

## Histogram-like functions

- int `hist_update` (std::string ix\_col, std::string scol, double ix, double inc=1.0)  
Update a histogram entry.
- double `hist_get` (std::string ix\_col, std::string scol, double ix)  
Get a histogram entry.
- int `hist_set` (std::string ix\_col, std::string scol, double ix, double value)  
Set a histogram entry.

## Column manipulation

- std::string `get_column_name` (size\_t col) const  
Returns the name of column `col` -  $O(1)$ .
- std::string `get_sorted_name` (size\_t col)  
Returns the name of column `col` in sorted order -  $O(1)$ .
- int `new_column` (std::string name)

- *Add a new column owned by the table -  $O(\log(C))$ .*  
 template<class vec\_t >  
 int **new\_column** (std::string name, size\_t sz, vec\_t &v)  
*Add a new column by copying data from another vector.*
- bool **is\_column** (std::string scol)  
*Return true if scol is a column in the current table .*
- int **lookup\_column** (std::string name, int &ix) const  
*Find the index for column named name -  $O(\log(C))$ .*
- int **copy\_column** (std::string src, std::string dest)  
*Make a new column named dest equal to src -  $O(\log(C)*R)$ .*
- double \* **create\_array** (std::string col) const  
*Create (using new) a generic array from column col.*
- int **init\_column** (std::string scol, double val)  
*Initialize all values of column named scol to val -  $O(\log(C)*R)$ .*
- const gsl\_vector \* **get\_gsl\_vector** (std::string name) const  
*Get a gsl\_vector from column name -  $O(\log(C))$ .*
- int **add\_col\_from\_table** (std::string loc\_index, table &source, std::string src\_index, std::string src\_col, std::string dest\_col="")  
*Insert a column from a separate table, interpolating it into a new column.*

#### Row manipulation and data input

- int **new\_row** (size\_t n)  
*Insert a row before row n.*
- int **copy\_row** (size\_t src, size\_t dest)  
*Copy the data in row src to row dest.*
- int **insert\_data** (size\_t n, size\_t nv, double \*v)  
*Insert a row of data before row n.*
- int **insert\_data** (size\_t n, size\_t nv, double \*\*v)  
*Insert a row of data before row n.*
- int **line\_of\_names** (std::string newheads)  
*Read a new set of names from newheads.*
- template<class vec\_t >  
 int **line\_of\_data** (size\_t nv, const vec\_t &v)  
*Read a line of data from an array.*

#### Lookup and search methods

- size\_t **ordered\_lookup** (std::string col, double val)  
*Look for a value in an ordered column.*
- size\_t **lookup** (std::string col, double val) const  
*Exhaustively search column col for the value val -  $O(\log(C)*R)$ .*
- double **lookup\_val** (std::string col, double val, std::string col2) const  
*Search column col for the value val and return value in col2.*
- size\_t **lookup** (int col, double val) const  
*Exhaustively search column col for the value val -  $O(\log(C)*R)$ .*
- size\_t **mlookup** (std::string col, double val, std::vector< double > &results, double threshold=0.0) const  
*Exhaustively search column col for many occurrences of val -  $O(\log(C)*R)$ .*

#### Interpolation, differentiation, and integration, max,

##### and min

- int **set\_interp** (base\_interp\_mgr< ovector\_const\_view > &bi1, base\_interp\_mgr< ovector\_const\_subvector > &bi2)  
*Set the base interpolation objects.*
- double **interp** (std::string sx, double x0, std::string sy)  
*Interpolate x0 from sx into sy.*
- double **interp\_const** (std::string sx, double x0, std::string sy) const  
*Interpolate x0 from sx into sy.*
- double **interp** (size\_t ix, double x0, size\_t iy)  
*Interpolate x0 from ix into iy.*
- double **interp\_const** (size\_t ix, double x0, size\_t iy) const  
*Interpolate x0 from ix into iy.*
- int **deriv** (std::string x, std::string y, std::string yp)  
*Make a new column yp which is the derivative  $y'(x)$  -  $O(\log(C)*R)$ .*

- double `deriv` (std::string sx, double x0, std::string sy)  
*The first derivative of the function sy(sx) at sx=x0.*
- double `deriv_const` (std::string sx, double x0, std::string sy) const  
*The first derivative of the function sy(sx) at sx=x0.*
- double `deriv` (size\_t ix, double x0, size\_t iy)  
*The first derivative of the function iy(ix) at ix=x0.*
- double `deriv_const` (size\_t ix, double x0, size\_t iy) const  
*The first derivative of the function iy(ix) at ix=x0.*
- int `deriv2` (std::string x, std::string y, std::string yp)  
*Make a new column yp which is  $y''(x) - O(\log(C)*R)$ .*
- double `deriv2` (std::string sx, double x0, std::string sy)  
*The second derivative of the function sy(sx) at sx=x0.*
- double `deriv2_const` (std::string sx, double x0, std::string sy) const  
*The second derivative of the function sy(sx) at sx=x0.*
- double `deriv2` (size\_t ix, double x0, size\_t iy)  
*The second derivative of the function iy(ix) at ix=x0.*
- double `deriv2_const` (size\_t ix, double x0, size\_t iy) const  
*The second derivative of the function iy(ix) at ix=x0.*
- double `integ` (std::string sx, double x1, double x2, std::string sy)  
*The integral of the function sy(sx) from sx=x1 to sx=x2.*
- double `integ_const` (std::string sx, double x1, double x2, std::string sy) const  
*The integral of the function sy(sx) from sx=x1 to sx=x2.*
- double `integ` (size\_t ix, double x1, double x2, size\_t iy)  
*The integral of the function iy(ix) from ix=x1 to ix=x2.*
- double `integ_const` (size\_t ix, double x1, double x2, size\_t iy) const  
*The integral of the function iy(ix) from ix=x1 to ix=x2.*
- int `integ` (std::string x, std::string y, std::string ynew)  
*The integral of the function iy(ix)*
- double `max` (std::string col) const  
*Return column maximum. Makes no assumptions about ordering -  $O(R)$ .*
- double `min` (std::string col) const  
*Return column minimum. Makes no assumptions about ordering -  $O(R)$ .*

#### Subtable method

- `table * subtable` (std::string list, size\_t top, size\_t bottom) const  
*Make a subtable.*

#### Add space

- int `inc_maxlines` (size\_t llines)  
*Manually increase the maximum number of lines.*

#### Delete methods

- virtual int `delete_column` (std::string scol)  
*Delete column named scol -  $O(C)$ .*
- int `delete_row` (std::string scol, double val)  
*Delete the row with the entry closest to the value val in column scol -  $O(R*C)$*
- int `delete_row` (size\_t irow)  
*Delete the row of index irow -  $O(R*C)$*

#### Clear methods

- void `zero_table` ()  
*Zero the data entries but keep the column names and nlines fixed.*
- void `clear_all` ()  
*Clear everything.*
- void `clear_table` ()  
*Clear the table and the column names (but leave constants)*
- void `clear_data` ()  
*Remove all of the data by setting the number of lines to zero.*
- void `clear_constants` ()  
*Clear all constants.*

## Sorting methods

- int [sort\\_table](#) (std::string scol)  
*Sort the entire table by the column `scol`.*
- int [sort\\_column](#) (std::string scol)  
*Individually sort the column `scol`.*

## Summary method

- virtual int [summary](#) (std::ostream \*out, int ncol=79) const  
*Output a summary of the information stored.*

## Constant manipulation

- virtual int [add\\_constant](#) (std::string name, double val)  
*Add a constant, or if the constant already exists, change its value.*
- virtual int [set\\_constant](#) (std::string name, double val, bool err\_on\_notfound=true)  
*Add a constant.*
- virtual double [get\\_constant](#) (std::string name) const  
*Get a constant.*
- virtual size\_t [get\\_nconsts](#) () const  
*Get the number of constants.*
- virtual int [get\\_constant](#) (size\_t ix, std::string &name, double &val) const  
*Get a constant by index.*
- virtual int [remove\\_constant](#) (std::string name)  
*Remove a constant.*

## Miscellaneous methods

- int [read\\_generic](#) (std::istream &fin, int verbose=0)  
*Clear the current table and read from a generic data file.*
- int [check\\_synchro](#) () const  
*Return 0 if the tree and list are properly synchronized.*
- bool [get\\_owner](#) (std::string name) const  
*Get ownership -  $O(\log(C))$ .*

## Data Fields

- [def\\_interp\\_mgr](#) < [ovector\\_const\\_view](#), [cspline\\_interp](#) > dim1  
*Default interpolation manager.*
- [def\\_interp\\_mgr](#) < [ovector\\_const\\_subvector](#), [cspline\\_interp](#) > dim2  
*Default interpolation manager.*
- bool [intp\\_set](#)  
*True if the interpolation type has been set.*

## Protected Types

- typedef struct [table::col\\_s](#) col  
*Column structure for [table](#) [protected].*
- typedef struct [table::sortd\\_s](#) sortd  
*A structure for sorting in [table](#) [protected].*

## Iterator types

- typedef std::map< std::string, [col](#), [string\\_comp](#) >::iterator **aiter**
- typedef std::map< std::string, [col](#), [string\\_comp](#) >::const\_iterator **aciter**
- typedef std::vector< aiter >::iterator **aviter**

## Protected Member Functions

- int [reset\\_list](#) ()  
*Set the elements of alist with the appropriate iterators from atree -  $O(C)$ .*
- int [make\\_fp\\_varname](#) (std::string &s)  
*Ensure a variable name does not match a function or contain non-alphanumeric characters.*
- int [make\\_unique\\_name](#) (std::string &col, std::vector< std::string > &cnames)  
*Make sure a name is unique.*

## Column manipulation methods

- aiter [get\\_iterator](#) (std::string lname)  
*Return the iterator for a column.*
- col \* [get\\_col\\_struct](#) (std::string lname)  
*Return the column structure for a column.*
- aiter [begin](#) ()  
*Return the beginning of the column tree.*
- aiter [end](#) ()  
*Return the end of the column tree.*

## Static Protected Member Functions

- static int [sortd\\_comp](#) (const void \*a, const void \*b)  
*The sorting function.*

## Protected Attributes

- std::map< std::string, double > [constants](#)  
*The list of constants.*
- [ovector empty\\_col](#)  
*An empty vector for [get\\_column\(\)](#)*

## Actual data

- size\_t [maxlines](#)  
*The size of allocated memory.*
- size\_t [nlines](#)  
*The size of presently used memory.*
- std::map< std::string, col, [string\\_comp](#) > [atree](#)  
*The tree of columns.*
- std::vector< aiter > [alist](#)  
*The list of tree iterators.*

## Interpolation

- [sm\\_interp\\_vec](#) \* [si](#)  
*The interpolation object.*
- [base\\_interp\\_mgr](#) < [ovector\\_const\\_view](#) > \* [bim1](#)  
*A pointer to the interpolation manager.*
- [base\\_interp\\_mgr](#) < [ovector\\_const\\_subvector](#) > \* [bim2](#)  
*A pointer to the subvector interpolation manager.*
- std::string [intp\\_colx](#)  
*The last x-column interpolated.*
- std::string [intp\\_coly](#)  
*The last y-column interpolated.*

## 46.330.2 Member Typedef Documentation

## 46.330.2.1 typedef struct table::col\_s table::col [protected]

This struct is used internally by [table](#) to organize the columns and need not be instantiated by the casual end-user.

#### 46.330.2.2 `typedef struct table::sortd_s table::sortd` `[protected]`

This struct is used internally by [table](#) to perform sorting and need not be instantiated by the casual end-user.

#### 46.330.3 Member Function Documentation

##### 46.330.3.1 `int table::set ( std::string col, size_t row, double val )`

This function adds the column `col` if it does not already exist and adds rows using [inc\\_maxlines\(\)](#) and [set\\_nlines\(\)](#) to create at least  $(row+1)$  rows if they do not already exist.

##### 46.330.3.2 `int table::set ( size_t icol, size_t row, double val )`

- $O(1)$ .

##### 46.330.3.3 `int table::set_nlines ( size_t il )`

This function is stingy about increasing the table memory space and will only increase it enough to fit `il` lines. Using it in succession to slowly increase the number of lines in the table is likely to be inefficient compared to [set\\_nlines\\_auto\(\)](#) in this case.

##### 46.330.3.4 `int table::set_nlines_auto ( size_t il )`

This function is like [set\\_nlines\(\)](#), but doubles the maximum column size if an increase in the maximum size is required instead of simply making enough room for the current number of lines. This function is used internally by [set\(\)](#) to ensure that the cost of setting lines in sequence is linear and not quadratic.

##### 46.330.3.5 `const ovector_base& table::operator[] ( size_t icol ) const` `[inline]`

This does not do any sort of bounds checking and is quite fast.

Note that several of the methods require reallocation of memory and references previously returned by this function will be incorrect.

Unlike [set\(\)](#), this function will not automatically result in an increase in the size of the table if the user attempts to set an element beyond the current column range.

Definition at line 291 of file `table.h`.

##### 46.330.3.6 `ovector_base& table::operator[] ( size_t icol )` `[inline]`

This does not do any sort of bounds checking and is quite fast.

Note that several of the methods require reallocation of memory and references previously returned by this function will be incorrect.

Unlike [set\(\)](#), this function will not automatically result in an increase in the size of the table if the user attempts to set an element beyond the current column range.

Definition at line 308 of file `table.h`.

##### 46.330.3.7 `const ovector_base& table::operator[] ( std::string scol ) const` `[inline]`

No error checking is performed.

Note that several of the methods require reallocation of memory and references previously returned by this function will be incorrect.

Unlike [set\(\)](#), this function will not automatically result in an increase in the size of the table if the user attempts to set an element beyond the current column range.

Definition at line 324 of file `table.h`.

46.330.3.8 `ovector_base& table::operator[] ( std::string scol ) [inline]`

No error checking is performed.

Note that several of the methods require reallocation of memory and references previously returned by this function will be incorrect.

Unlike `set()`, this function will not automatically result in an increase in the size of the table if the user attempts to set an element beyond the current column range.

Definition at line 341 of file `table.h`.

46.330.3.9 `int table::get_row ( std::string col, double val, ovector & row ) const`

This function searches the entire table for the row which has the entry in column `col` which is closest to the value `val`, and copies that row to the vector `row`.

If the `ovector` object `row` previously contains any data, it will be lost.

46.330.3.10 `int table::get_row ( size_t irow, ovector & row ) const`

This function returns a copy of row with index `irow`, where `irow` ranges from 0 to `get_nlines()` - 1, inclusive.

If the `ovector` object `row` previously contains any data, it will be lost.

46.330.3.11 `int table::hist_update ( std::string ix_col, std::string scol, double ix, double inc = 1.0 )`

Assuming that the histogram bins are given in column named `ix_col`, this updates the histogram found in column `scol` at index location `ix` by incrementing it by an amount given in `inc`.

46.330.3.12 `double table::hist_get ( std::string ix_col, std::string scol, double ix )`

Assuming that the histogram bins are given in column named `ix_col`, this returns the histogram entry found in column `scol` at index location `ix`.

46.330.3.13 `int table::hist_set ( std::string ix_col, std::string scol, double ix, double value )`

Assuming that the histogram bins are given in column named `ix_col`, this sets the histogram entry found in column `scol` at index location `ix` to the value given in `value`.

46.330.3.14 `int table::new_column ( std::string name )`

#### Note

This function does not set all the column entries to zero in the case that a new column is added to a table which already contains data.

46.330.3.15 `template<class vec_t> int table::new_column ( std::string name, size_t sz, vec_t & v ) [inline]`

This function copies `sz` elements of vector `v` into the table in a new column named `name`. If `sz` is larger than the current number of lines (as given, e.g. in `get_nlines()`), then only the first part of the vector `v` is copied, up to the current number of lines.

This function calls the error handler if `sz` is zero.

Definition at line 434 of file `table.h`.

46.330.3.16 `bool table::is_column ( std::string scol )`

This function does not call the error handler if the column is not found, but just silently returns false.

46.330.3.17 `int table::lookup_column ( std::string name, int & ix ) const`

If the column is not present, this does not call the error handler, but quietly sets `ix` to zero and returns `gsl_enotfound`.

46.330.3.18 `int table::init_column ( std::string scol, double val )`

Note that this does not initialize elements beyond `nlines` so that if the number of rows is increased afterwards, the new rows will have uninitialized values.

46.330.3.19 `int table::add_col_from_table ( std::string loc_index, table & source, std::string src_index, std::string src_col, std::string dest_col = "" )`

Given a pair of columns ( `src_index`, `src_col` ) in a separate table (`source`), this creates a new column in the present table named `src_col` which interpolates `loc_index` into `src_index`. The interpolation objects from the `source` table will be used. If there is already a column in the present table named `src_col`, then this will fail.

If there is an error in the interpolation for any particular row, then the value of `src_col` in that row will be set to zero.

46.330.3.20 `int table::new_row ( size_t n )`

Acceptable values for `n` are between 0 and `get_nlines()` inclusive, with the maximum value denoting the addition of a row after the last row presently in the table.

46.330.3.21 `int table::line_of_names ( std::string newheads )`

This function reads a set of white-space delimited column names from the string `newheads`, and creates a new column for each name which is specified.

For example

```
table t;
t.line_of_names("position velocity acceleration");
```

will create three new columns with the names "position", "velocity", and "acceleration".

46.330.3.22 `size_t table::ordered_lookup ( std::string col, double val )`

$O(\log(C) \cdot \log(R))$

This uses the function `search_vec::ordered_lookup()`, which offers caching and assumes the vector is monotonic. If you don't have monotonic data, you can still use the `table::lookup()` function, which is more general.

46.330.3.23 `double table::interp ( std::string sx, double x0, std::string sy )`

$O(\log(C) \cdot \log(R))$  but can be as bad as  $O(\log(C) \cdot R)$  if the relevant columns are not well ordered.

46.330.3.24 `double table::interp_const ( std::string sx, double x0, std::string sy ) const`

$O(\log(C) \cdot \log(R))$  but can be as bad as  $O(\log(C) \cdot R)$  if the relevant columns are not well ordered.

46.330.3.25 `double table::interp ( size_t ix, double x0, size_t iy )`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.26 `double table::interp_const ( size_t ix, double x0, size_t iy ) const`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.27 `double table::deriv ( std::string sx, double x0, std::string sy )`

$O(\log(C) \cdot \log(R))$  but can be as bad as  $O(\log(C) \cdot R)$  if the relevant columns are not well ordered.

46.330.3.28 `double table::deriv_const ( std::string sx, double x0, std::string sy ) const`

$O(\log(C) \cdot \log(R))$  but can be as bad as  $O(\log(C) \cdot R)$  if the relevant columns are not well ordered.



46.330.3.29 `double table::deriv ( size_t ix, double x0, size_t iy )`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.30 `double table::deriv_const ( size_t ix, double x0, size_t iy ) const`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.31 `double table::deriv2 ( std::string sx, double x0, std::string sy )`

$O(\log(C)*\log(R))$  but can be as bad as  $O(\log(C)*R)$  if the relevant columns are not well ordered.

46.330.3.32 `double table::deriv2_const ( std::string sx, double x0, std::string sy ) const`

$O(\log(C)*\log(R))$  but can be as bad as  $O(\log(C)*R)$  if the relevant columns are not well ordered.

46.330.3.33 `double table::deriv2 ( size_t ix, double x0, size_t iy )`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.34 `double table::deriv2_const ( size_t ix, double x0, size_t iy ) const`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.35 `double table::integ ( std::string sx, double x1, double x2, std::string sy )`

$O(\log(C)*\log(R))$  but can be as bad as  $O(\log(C)*R)$  if the relevant columns are not well ordered.

46.330.3.36 `double table::integ_const ( std::string sx, double x1, double x2, std::string sy ) const`

$O(\log(C)*\log(R))$  but can be as bad as  $O(\log(C)*R)$  if the relevant columns are not well ordered.

46.330.3.37 `double table::integ ( size_t ix, double x1, double x2, size_t iy )`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.38 `double table::integ_const ( size_t ix, double x1, double x2, size_t iy ) const`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.39 `int table::integ ( std::string x, std::string y, std::string ynew )`

$O(\log(R))$  but can be as bad as  $O(R)$  if the relevant columns are not well ordered.

46.330.3.40 `table* table::subtable ( std::string list, size_t top, size_t bottom ) const`

Uses the columns specified in `list` from the row `top` to the row of index `bottom` to generate a new table which is a copy of part of the original.

46.330.3.41 `virtual int table::delete_column ( std::string scol )` [virtual]

This is slow because the iterators in `alist` are mangled and we have to call `reset_list()` to get them back.

Reimplemented in `table_units`.

46.330.3.42 `void table::clear_data ( )` [inline]

This leaves the column names intact and does not remove the constants.

Definition at line 868 of file `table.h`.

46.330.3.43 `int table::sort_table ( std::string scol )`

#### Note

This function works by allocating space for an entirely new chunk of memory for the data in the table.

**Todo** Use `vector_sort()` rather than `qsort()`.

46.330.3.44 `int table::sort_column ( std::string scol )`

**Todo** Use `vector_sort()` rather than `qsort()`.

46.330.3.45 `virtual int table::summary ( std::ostream * out, int ncol = 79 ) const` `[virtual]`

Outputs the number of constants, the number of columns, a list of the column names, and the number of lines of data.

Reimplemented in `table_units`.

46.330.3.46 `int table::reset_list ( )` `[protected]`

Generally, the end-user shouldn't need this method. It is only used in `delete_column()` to rearrange the list when a column is deleted from the tree.

The documentation for this class was generated from the following file:

- `table.h`

## 46.331 table3d Class Reference

A data structure containing many slices of two-dimensional data points defined on a grid.

```
#include <table3d.h>
```

### 46.331.1 Detailed Description

**Idea for Future** Improve interpolation and derivative caching

**Idea for Future** Make a 'const' version of the interpolation functions

**Idea for Future** Should there be a `clear_grid()` function separate from `clear_data()` and `clear_table()`?

Definition at line 53 of file `table3d.h`.

#### Public Member Functions

- `table3d ()`  
*Create a new 3D table .*
- `bool is_size_set () const`
- `bool is_xy_set () const`
- `virtual const char * type ()`  
*Return the type, "table3d".*

## Initialization

- `template<class vec2_t>`  
`int set_xy (std::string x_name, size_t nx, const vec2_t &x, std::string y_name, size_t ny, const vec2_t &y)`  
*Initialize the x-y grid.*
- `int set_size (size_t nx, size_t ny)`  
*Initialize table size.*

## On-grid get and set methods

- `int set (size_t ix, size_t iy, std::string name, double val)`  
*Set element in slice name at location ix, iy to value val.*
- `int set (size_t ix, size_t iy, size_t z, double val)`  
*Set element in slice of index z at location ix, iy to value val.*
- `double & get (size_t ix, size_t iy, std::string name)`  
*Get element in slice name at location ix, iy*
- `const double & get (size_t ix, size_t iy, std::string name) const`  
*Get element in slice name at location ix, iy (const version)*
- `double & get (size_t ix, size_t iy, size_t z)`  
*Get element in slice of index z at location ix, iy*
- `const double & get (size_t ix, size_t iy, size_t z) const`  
*Get element in slice of index z at location ix, iy (const version)*

## Off-grid get and set methods

These methods return the value of a slice on the grid point nearest to a user-specified location. For interpolation into a point off the grid, use `table3d::interp()`.

- `int set_val (double x, double y, std::string name, double val)`  
*Set element in slice name at the nearest location to x, y to value val.*
- `int set_val (double x, double y, size_t z, double val)`  
*Set element in slice of index z at the nearest location to x, y to value val.*
- `double & get_val (double x, double y, std::string name)`  
*Get element in slice name at location closest to x, y*
- `const double & get_val (double x, double y, std::string name) const`  
*Get element in slice name at location closest to x, y*
- `double & get_val (double x, double y, size_t z)`  
*Get element in slice of index z at location closest to x, y*
- `const double & get_val (double x, double y, size_t z) const`  
*Get element in slice of index z at location closest to x, y*
- `template<class vec_t>`  
`int set_slices (double x, double y, size_t nv, vec_t &vals)`  
*Set elements in the first nv slices at the nearest location to x, y to value val.*
- `template<class vec_t>`  
`int get_slices (double x, double y, size_t nv, vec_t &v)`  
*Get the data for every slice at the nearest location to x, y*

## Off-grid get and set methods returning nearest point

- `int set_val_ret (double &x, double &y, std::string name, double val)`  
*Set element in slice name at the nearest location to x, y to value val.*
- `int set_val_ret (double &x, double &y, size_t z, double val)`  
*Set element in slice of index z at the nearest location to x, y to value val.*
- `double & get_val_ret (double &x, double &y, std::string name)`  
*Get element in slice name at location closest to x, y, and also return the corresponding values of x and y.*
- `const double & get_val_ret (double &x, double &y, std::string name) const`  
*Get element in slice name at location closest to x, y, and also return the corresponding values of x and y.*
- `double & get_val_ret (double &x, double &y, size_t z)`  
*Get element in slice of index z at location closest to x, y, and also return the corresponding values of x and y.*
- `const double & get_val_ret (double &x, double &y, size_t z) const`  
*Get element in slice of index z at location closest to x, y, and also return the corresponding values of x and y.*
- `template<class vec_t>`  
`int set_slices_ret (double &x, double &y, size_t nv, vec_t &vals)`  
*Set elements in the first nv slices at the nearest location to x, y to values vals.*
- `template<class vec_t>`  
`int get_slices_ret (double &x, double &y, size_t nv, vec_t &vals)`  
*Get elements in the first nv slices at the nearest location to x, y to value val.*

## Grid information get and set methods

- int `set_grid_x` (size\_t ix, double val)  
*Set x grid point at index ix.*
- int `set_grid_y` (size\_t iy, double val)  
*Set y grid point at index iy.*
- double `get_grid_x` (size\_t ix)  
*Get x grid point at index ix.*
- double `get_grid_y` (size\_t iy)  
*Get y grid point at index iy.*
- std::string `get_x_name` () const  
*Get the name of the x grid variable.*
- std::string `get_y_name` () const  
*Get the name of the y grid variable.*
- int `set_x_name` (std::string name)  
*Set the name of the x grid variable.*
- int `set_y_name` (std::string name)  
*Set the name of the y grid variable.*
- const `ovector` & `get_x_data` () const  
*Get a const reference to the full x grid.*
- const `ovector` & `get_y_data` () const  
*Get a const reference to the full y grid.*

## Size get methods

- int `get_size` (size\_t &nx, size\_t &ny) const  
*Get the size of the slices.*
- int `get_nx` () const  
*Get the x size.*
- int `get_ny` () const  
*Get the y size.*
- int `get_nslices` () const  
*Get the number of slices.*

## Slice manipulation

- int `line_of_names` (std::string names)  
*Create a set of new slices specified in the string names.*
- std::string `get_slice_name` (size\_t z) const  
*Returns the name of slice with index z.*
- int `new_slice` (std::string name)  
*Add a new slice.*
- int `set_slice_all` (std::string name, double val)  
*Set all of the values in slice name to val.*
- int `lookup_slice` (std::string name, size\_t &ix) const  
*Find the index for column named name.*
- bool `is_slice` (std::string name, int &ix)  
*Return true if slice is already present.*
- int `rename_slice` (std::string olds, std::string news)  
*Rename slice named olds to news.*
- int `copy_slice` (std::string src, std::string dest)  
*Make a new slice named dest which is a copy of the slice with name given in src.*
- int `init_slice` (std::string scol, double val)  
*Initialize all values of slice named scol to val.*
- const `omatrix` & `get_slice` (std::string scol) const  
*Return a constant reference to a slice.*
- const `omatrix` & `get_slice` (size\_t iz) const  
*Return a constant reference to a slice.*
- `omatrix` & `get_slice` (std::string scol)  
*Return a constant reference to a slice.*
- `omatrix` & `get_slice` (size\_t iz)  
*Return a constant reference to a slice.*
- const std::vector< `omatrix` > & `get_data` ()  
*Return a constant reference to all the slice data.*

## Lookup and search methods

- int `lookup_x` (double val, size\_t &ix) const  
*Look for a value in the x grid.*
- int `lookup_y` (double val, size\_t &iy) const  
*Look for a value in the y grid.*
- int `lookup` (double val, std::string slice, size\_t &ix, size\_t &iy) const  
*Look for a value in a specified slice.*

## Interpolation, differentiation, and integration

- int `set_interp` (base\_interp\_mgr< ovector\_const\_view > &b1, base\_interp\_mgr< ovector\_const\_subvector > &b2)  
*Specify the base interpolation objects to use.*
- double `interp` (double x, double y, std::string name)  
*Interpolate x and y in slice named name.*
- double `deriv_x` (double x, double y, std::string name)  
*Interpolate the derivative of the data with respect to the x grid at point x and y in slice named name.*
- double `deriv_y` (double x, double y, std::string name)  
*Interpolate the derivative of the data with respect to the y grid at point x and y in slice named name.*
- double `deriv_xy` (double x, double y, std::string name)  
*Interpolate the mixed second derivative of the data at point x and y in slice named name.*
- double `integ_x` (double x1, double x2, double y, std::string name)  
*Interpolate the integral of the data respect to the x grid.*
- double `integ_y` (double x, double y1, double y2, std::string name)  
*Interpolate the integral of the data respect to the y grid.*
- template<class vec\_t >  
int `interp_slices` (double x, double y, size\_t nv, vec\_t &v)  
*Fill a vector of interpolated values from each slice at the point x, y*

## Extract 2-dimensional tables

- int `extract_x` (double x, table &t)  
*Extract a table at a fixed x grid point.*
- int `extract_y` (double y, table &t)  
*Extract a table at a fixed y grid point.*

## Clear methods

- int `zero_table` ()  
*Zero the data entries but keep the slice names and grid.*
- void `clear_table` ()  
*Clear the table and the slice names.*
- void `clear_data` ()  
*Remove all of the data by setting the number of lines to zero.*

## Summary method

- int `summary` (std::ostream \*out, int ncol=79) const  
*Output a summary of the information stored.*

## Histogram-like functions

- int `hist_update` (double ix, double iy, std::string scol, double inc=1.0)  
*Update a histogram entry.*
- double `hist_get` (double ix, double iy, std::string scol) const  
*Get a histogram entry.*
- int `hist_set` (double ix, double iy, std::string scol, double value)  
*Set a histogram entry.*

## Manipulating constants

- virtual int `add_constant` (std::string name, double val)  
*Add a constant.*
- virtual int `remove_constant` (std::string name)  
*Remove a constant.*

- virtual int [set\\_constant](#) (std::string name, double val)  
*Add a constant.*
- virtual double [get\\_constant](#) (std::string name)  
*Get a constant.*
- virtual int [get\\_constant](#) (size\_t ix, std::string &name, double &val) const  
*Get a constant by index.*
- virtual size\_t [get\\_nconsts](#) () const  
*Get the number of constants.*

## Data Fields

### Default interpolation objects

- [def\\_interp\\_mgr](#) < [ovector\\_const\\_view](#), [cspline\\_interp](#) > **dim1**
- [def\\_interp\\_mgr](#) < [ovector\\_const\\_subvector](#), [cspline\\_interp](#) > **dim2**

## Protected Types

### Iterator types

- typedef std::map< std::string, size\_t, [string\\_comp](#) > ::iterator **map\_iter**
- typedef std::map< std::string, size\_t, [string\\_comp](#) > ::const\_iterator **map\_const\_iter**

## Protected Member Functions

### Tree iterator boundaries

- [map\\_iter](#) [begin](#) ()  
*Return the beginning of the slice tree.*
- [map\\_iter](#) [end](#) ()  
*Return the end of the slice tree.*
- [map\\_const\\_iter](#) [const\\_begin](#) () const  
*Return the beginning of the slice tree.*
- [map\\_const\\_iter](#) [const\\_end](#) () const  
*Return the end of the slice tree.*

## Protected Attributes

### Interpolation data

- [base\\_interp\\_mgr](#) < [ovector\\_const\\_view](#) > \* [bimp1](#)  
*The base interpolation object.*
- [base\\_interp\\_mgr](#) < [ovector\\_const\\_subvector](#) > \* [bimp2](#)  
*The subvector base interpolation object.*
- [sm\\_interp\\_vec](#) \*\* [si](#)  
*The array of sm\_interp\_vec pointers.*
- [omatrix\\_col](#) \*\* [aci](#)  
*Matrices for interpolation.*

### Data storage

- std::map< std::string, double > [constants](#)  
*The list of constants.*
- size\_t [numx](#)  
*The size of the x grid.*
- size\_t [numy](#)  
*The size of the y grid.*
- std::map< std::string, size\_t, [string\\_comp](#) > [tree](#)  
*A tree connecting column names to list indexes.*

- `std::string xname`  
*The name for the x grid.*
- `std::string yname`  
*The name for the y grid.*
- `std::vector< omatrix > list`  
*The pointers to the matrices.*
- `ovector xval`  
*The x grid.*
- `ovector yval`  
*The y grid.*
- `bool xy_set`  
*True if the grid has been set.*
- `bool size_set`  
*True if the size of the grid has been set.*
- `bool has_slice`  
*True if the table has at least one slice.*

#### 46.331.2 Member Function Documentation

**46.331.2.1** `template<class vec2_t> int table3d::set_xy ( std::string x_name, size_t nx, const vec2_t & x, std::string y_name, size_t ny, const vec2_t & y ) [inline]`

This function will not allow you to redefine the grid when there is data in the table if a grid of a different size was already set from a previous call to either `set_xy()` or `set_size()`. However, you may freely redefine the grid after a call to `clear_data()` or `clear_table()`. You may change individual grid points at any time with `set_grid_x()` and `set_grid_y()`.

Definition at line 76 of file `table3d.h`.

**46.331.2.2** `int table3d::set_size ( size_t nx, size_t ny )`

This function will not allow you to resize the table if it already has data or if the size has already been set with the `set_xy()` function, unless you clear the data with `clear_data()` or the table with `clear_table()` first.

**46.331.2.3** `int table3d::rename_slice ( std::string olds, std::string news )`

This is slow since we have to delete the column and re-insert it. This process in turn mangles all of the iterators in the list.

**46.331.2.4** `const std::vector<omatrix>& table3d::get_data ( )`

**46.331.2.5** `int table3d::extract_x ( double x, table & t )`

##### Note

All of the information previously stored in `t` will be lost.

**46.331.2.6** `int table3d::extract_y ( double y, table & t )`

##### Note

All of the information previously stored in `t` will be lost.

**46.331.2.7** `void table3d::clear_data ( )`

This leaves the column names intact and does not remove the constants.

**46.331.2.8** `int table3d::summary ( std::ostream * out, int ncol = 79 ) const`

Outputs the number of constants, the grid information, and a list of the slice names

46.331.2.9 `int table3d::hist_update ( double ix, double iy, std::string scol, double inc = 1.0 )`

Assuming that the histogram bins are given in column named `ix_col`, this updates the histogram found in column `scol` at index location `ix` by incrementing it by an amount given in `inc`.

46.331.2.10 `double table3d::hist_get ( double ix, double iy, std::string scol ) const`

Assuming that the histogram bins are given in column named `ix_col`, this returns the histogram entry found in column `scol` at index location `ix`.

46.331.2.11 `int table3d::hist_set ( double ix, double iy, std::string scol, double value )`

Assuming that the histogram bins are given in column named `ix_col`, this sets the histogram entry found in column `scol` at index location `ix` to the value given in `value`.

The documentation for this class was generated from the following file:

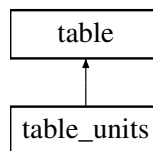
- `table3d.h`

## 46.332 table\_units Class Reference

Data table class with units.

```
#include <table_units.h>
```

Inheritance diagram for `table_units`:



### 46.332.1 Detailed Description

**Idea for Future** Make table methods virtual? (not necessary yet since `delete_column()` isn't referred to internally)

Definition at line 38 of file `table_units.h`.

### Public Member Functions

- `table_units` (int cmaxlines=0)  
*Create a new `table_units` with space for `nlines` ≤ `cmaxlines`.*
- `std::string get_unit` (std::string scol) const  
*Get the unit for column `scol`.*
- `int remove_unit` (std::string scol)  
*Remove the unit for column `scol`.*
- `int set_unit` (std::string scol, std::string unit)  
*Set the unit for column `scol` to `unit`.*
- `int convert_to_unit` (std::string scol, std::string unit, bool err\_on\_fail=true)  
*Convert the units of column `scol` to `unit`.*
- `double get_conv` (std::string old\_unit, std::string new\_unit)  
*Get the conversion factor from `old_unit` to `new_unit`.*
- `virtual int delete_column` (std::string scol)  
*Delete column named `scol`.*
- `virtual const char * type` ()



Return the type, "table\_units".

- virtual int **summary** (std::ostream \*out, int ncol=79) const  
Output a summary of the information stored.
- int **set\_convert** (convert\_units &c)  
Set the convert units object.
- int **show\_units** ()  
Show the unit cache as given by `convert_units::print_cache()`
- size\_t **get\_nunits** ()  
Return the number of columns with units.

#### Copy constructors

- **table\_units** (const table\_units &t)
- **table\_units** (const table &t)
- **table\_units & operator=** (const table\_units &t)
- **table\_units & operator=** (const table &t)  
Copy constructor.

#### Data Fields

- **convert\_units def\_cu**  
The default object for unit conversions.

#### Protected Types

##### Unit map iterator types

- typedef std::map< std::string, std::string, string\_comp > ::iterator **uiter**
- typedef std::map< std::string, std::string, string\_comp > ::const\_iterator **uciter**

#### Protected Attributes

- **convert\_units \* cup**  
The pointer to the convert units object.
- std::map< std::string, std::string, string\_comp > **utree**  
Unit map.

The documentation for this class was generated from the following file:

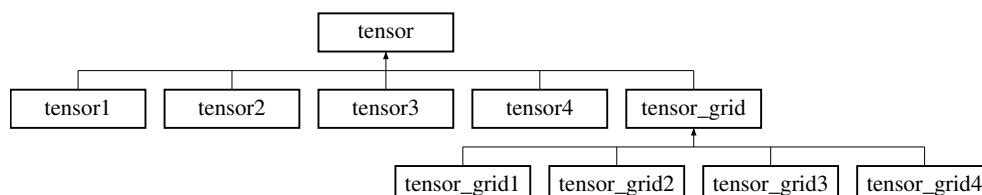
- table\_units.h

## 46.333 tensor Class Reference

Tensor class with arbitrary dimensions.

```
#include <tensor.h>
```

Inheritance diagram for tensor:



## 46.333.1 Detailed Description

The elements of a tensor are typically specified as a list of `size_t` numbers with length equal to the tensor rank. For a rank-4 tensor named `t`, the element `t[1][2][0][3]` can be obtained with something similar to

```
size_t ix[4]={1,2,0,3};
double x=t.get(ix);
```

Empty tensors have zero rank.

Slices of tensors are subsets obtained from fixing the index of several dimensions, while letting other dimensions vary. For a slice with one dimension not fixed, see [vector\\_slice\(\)](#). For a slice with two dimensions not fixed, see [matrix\\_slice\(\)](#).

For I/O with tensors, see [hdf\\_io.h](#).

**Idea for Future** Could implement arithmetic operators `+` and `-` and some different products.

**Idea for Future** Implement copies to and from vector and matrices

**Idea for Future** Implement tensor contractions, i.e. `tensor = tensor * tensor`

**Idea for Future** Consider making a template type to replace `double`, e.g. `value_t`.

**Idea for Future** Could be interesting to write an iterator for this class.

Definition at line 93 of file `tensor.h`.

## Public Member Functions

- [tensor](#) ()  
*Create an empty tensor with zero rank.*
- `template<class size_vec_t >`  
[tensor](#) (size\_t rank, const size\_vec\_t &dim)  
*Create a tensor of rank rank with sizes given in dim.*

## Set functions

- `template<class size_vec_t >`  
`void set` (const size\_vec\_t &index, double val)  
*Set the element indexed by index to value val.*
- `void set_all` (double x)  
*Set all elements in a tensor to some fixed value.*

## Get functions

- `template<class size_vec_t >`  
`double & get` (const size\_vec\_t &index)  
*Get the element indexed by index.*
- `template<class size_vec_t >`  
`double const & get` (const size\_vec\_t &index) const  
*Get a const reference to the element indexed by index.*

## Slice functions

- `template<class size_vec_t >`  
[ovector\\_array\\_stride vector\\_slice](#) (size\_t ix, const size\_vec\_t &index)  
*Fix all but one index to create a vector.*
- `template<class size_vec_t >`  
[omatrix\\_array matrix\\_slice](#) (size\_t ix, const size\_vec\_t &index)  
*Fix all but two indices to create a matrix.*

## Memory allocation

- `template<class size_vec_t>`  
`void allocate (size_t rank, const size_vec_t &dim)`  
*Allocate space for a tensor of rank `rank` with sizes given in `dim`.*
- `void free ()`  
*Free allocated space (also sets rank to zero)*

## Size functions

- `size_t get_rank () const`  
*Return the rank of the tensor.*
- `size_t get_size (size_t i) const`  
*Returns the size of the `i`th index.*
- `const uvector_size_t & get_size_arr () const`  
*Return the full array of sizes.*
- `const uvector & get_data () const`  
*Return the full array of sizes.*
- `size_t total_size () const`  
*Returns the size of the tensor (the product of the sizes over every index)*

## Index manipulation

- `template<class size_vec_t>`  
`size_t pack_indices (const size_vec_t &index)`  
*Pack the indices into a single array index.*
- `template<class size_vec_t>`  
`void unpack_indices (size_t ix, size_vec_t &index)`  
*Unpack the single array index into indices.*

## Protected Attributes

- `uvector data`  
*The data.*
- `uvector_size_t size`  
*A rank-sized array of the sizes of each dimension.*
- `size_t rk`  
*Rank.*

## 46.333.2 Constructor &amp; Destructor Documentation

46.333.2.1 `template<class size_vec_t> tensor::tensor ( size_t rank, const size_vec_t & dim ) [inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`. If the user requests any of the sizes to be zero, this constructor will call the error handler, create an empty tensor, and will allocate no memory.

Definition at line 125 of file `tensor.h`.

## 46.333.3 Member Function Documentation

46.333.3.1 `template<class size_vec_t> ovector_array_stride tensor::vector_slice ( size_t ix, const size_vec_t & index ) [inline]`

This fixes all of the indices to the values given in `index` except for the index number `ix`, and returns the corresponding vector, whose length is equal to the size of the tensor in that index. The value `index[ix]` is ignored.

For example, for a rank 3 tensor allocated with

```
tensor t;
size_t dim[3]={3,4,5};
t.allocate(3,dim);
```

the following code

```
size_t index[3]={1,0,3};
ovector_view v=t.vector_slice(1,index);
```

Gives a vector  $v$  of length 4 which refers to the values  $t(1,0,3)$ ,  $t(1,1,3)$ ,  $t(1,2,3)$ , and  $t(1,3,3)$ .

Definition at line 275 of file tensor.h.

**46.333.3.2** `template<class size_vec_t> omatrix_array tensor::matrix_slice ( size_t ix, const size_vec_t & index )` `[inline]`

This fixes all of the indices to the values given in `index` except for the index number `ix` and the last index, and returns the corresponding matrix, whose size is equal to the size of the tensor in the two indices which are not fixed.

Since the last index is always fixed, the parameter `ix` is limited to be  $\in [0, \text{rank} - 2]$ .

Definition at line 303 of file tensor.h.

**46.333.3.3** `template<class size_vec_t> void tensor::allocate ( size_t rank, const size_vec_t & dim )` `[inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`.

If memory was previously allocated, it will be freed before the new allocation.

If the user requests any of the sizes to be zero, this function will call the error handler and will allocate no memory. If memory was previously allocated, the tensor is left unmodified and no deallocation is performed.

Reimplemented in [tensor\\_grid](#).

Definition at line 348 of file tensor.h.

The documentation for this class was generated from the following file:

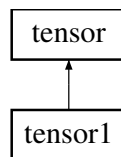
- [tensor.h](#)

## 46.334 tensor1 Class Reference

Rank 1 tensor.

```
#include <tensor.h>
```

Inheritance diagram for tensor1:



### 46.334.1 Detailed Description

Definition at line 924 of file tensor.h.

#### Public Member Functions

- [tensor1](#) ()  
*Create an empty tensor.*
- [tensor1](#) (size\_t sz)  
*Create a rank 1 tensor of size sz.*

- double & [get](#) (size\_t ix)  
*Get the element indexed by ix.*
- const double & [get](#) (size\_t ix) const  
*Get the element indexed by ix.*
- void [set](#) (size\_t index, double val)  
*Set the element indexed by index to value val.*
- void [set](#) (size\_t \*index, double val)  
*Set the element indexed by index to value val.*
- double & [operator\[\]](#) (size\_t ix)  
*Get an element using array-like indexing.*
- double & [operator\(\)](#) (size\_t ix)  
*Get an element using operator()*

#### 46.334.2 Member Function Documentation

##### 46.334.2.1 void [tensor1::set](#) ( size\_t \* index, double val ) [inline]

(We have to explicitly provide this version since the [set\(\)](#) function is overloaded in this child of [tensor](#).)

Definition at line 952 of file [tensor.h](#).

The documentation for this class was generated from the following file:

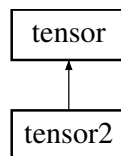
- [tensor.h](#)

## 46.335 tensor2 Class Reference

Rank 2 tensor.

```
#include <tensor.h>
```

Inheritance diagram for [tensor2](#):



#### 46.335.1 Detailed Description

Definition at line 1010 of file [tensor.h](#).

#### Public Member Functions

- [tensor2](#) ()  
*Create an empty tensor.*
- [tensor2](#) (size\_t sz, size\_t sz2)  
*Create a rank 2 tensor of size (sz,sz2)*
- double & [get](#) (size\_t ix1, size\_t ix2)  
*Get the element indexed by (ix1,ix2)*
- const double & [get](#) (size\_t ix1, size\_t ix2) const  
*Get the element indexed by (ix1,ix2)*
- void [set](#) (size\_t ix1, size\_t ix2, double val)  
*Set the element indexed by (ix1,ix2) to value val.*
- void [set](#) (size\_t \*index, double val)

*Set the element indexed by `index` to value `val`.*

- `double & operator() (size_t ix, size_t iy)`

*Get the element indexed by `(ix1,ix2)`*

#### 46.335.2 Member Function Documentation

46.335.2.1 `void tensor2::set ( size_t * index, double val ) [inline]`

(We have to explicitly provide this version since the `set()` function is overloaded in this child of `tensor`.)

Definition at line 1050 of file `tensor.h`.

The documentation for this class was generated from the following file:

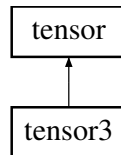
- `tensor.h`

## 46.336 tensor3 Class Reference

Rank 3 tensor.

```
#include <tensor.h>
```

Inheritance diagram for `tensor3`:



#### 46.336.1 Detailed Description

Definition at line 1111 of file `tensor.h`.

##### Public Member Functions

- `tensor3 ()`  
*Create an empty tensor.*
- `tensor3 (size_t sz, size_t sz2, size_t sz3)`  
*Create a rank 3 tensor of size `(sz,sz2,sz3)`*
- `double & get (size_t ix1, size_t ix2, size_t ix3)`  
*Get the element indexed by `(ix1,ix2,ix3)`*
- `const double & get (size_t ix1, size_t ix2, size_t ix3) const`  
*Get the element indexed by `(ix1,ix2,ix3)`*
- `void set (size_t ix1, size_t ix2, size_t ix3, double val)`  
*Set the element indexed by `(ix1,ix2,ix3)` to value `val`.*
- `void set (size_t *index, double val)`  
*Set the element indexed by `index` to value `val`.*

#### 46.336.2 Member Function Documentation

46.336.2.1 `void tensor3::set ( size_t * index, double val ) [inline]`

(We have to explicitly provide this version since the `set()` function is overloaded in this child of `tensor`.)

Definition at line 1152 of file tensor.h.

The documentation for this class was generated from the following file:

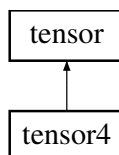
- [tensor.h](#)

## 46.337 tensor4 Class Reference

Rank 4 tensor.

```
#include <tensor.h>
```

Inheritance diagram for tensor4:



### 46.337.1 Detailed Description

Definition at line 1210 of file tensor.h.

#### Public Member Functions

- [tensor4](#) ()  
*Create an empty tensor.*
- [tensor4](#) (size\_t sz, size\_t sz2, size\_t sz3, size\_t sz4)  
*Create a rank 4 tensor of size (sz,sz2,sz3,sz4)*
- double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4)  
*Get the element indexed by (ix1,ix2,ix3,ix4)*
- const double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4) const  
*Get the element indexed by (ix1,ix2,ix3,ix4)*
- void [set](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4, double val)  
*Set the element indexed by (ix1,ix2,ix3,ix4) to value val.*
- void [set](#) (size\_t \*index, double val)  
*Set the element indexed by index to value val.*

### 46.337.2 Member Function Documentation

46.337.2.1 void [tensor4::set](#) ( size\_t \* *index*, double *val* ) [inline]

(We have to explicitly provide this version since the [set\(\)](#) function is overloaded in this child of [tensor](#).)

Definition at line 1256 of file tensor.h.

The documentation for this class was generated from the following file:

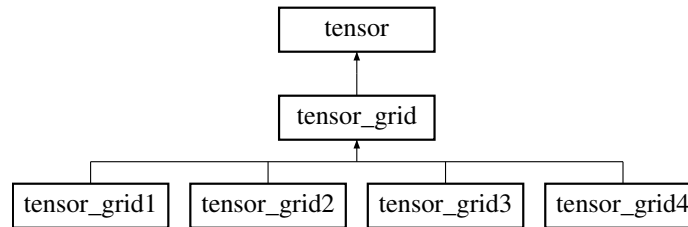
- [tensor.h](#)

## 46.338 tensor\_grid Class Reference

Tensor class with arbitrary dimensions with a grid.

```
#include <tensor.h>
```

Inheritance diagram for tensor\_grid:



#### 46.338.1 Detailed Description

This tensor class allows one to assign the indexes to numerical scales, so that n-dimensional interpolation can be performed. To set the grid, use [set\\_grid\(\)](#) and then interpolation can be done using [interpolate\(\)](#).

By convention, member functions ending in the `_val` suffix return the closest grid-point to some user-specified values.

**Idea for Future** Only allocate space for grid if it is set

**Idea for Future** Could implement arithmetic operators + and - and some different products.

**Idea for Future** Consider creating a [set\\_grid\(\)](#) function which takes grids from an object like `hist_grid`. Maybe make a constructor for a `tensor_grid` object which just takes as input a set of grids?

Definition at line 501 of file `tensor.h`.

#### Public Member Functions

- [tensor\\_grid\(\)](#)  
*Create an empty tensor with zero rank.*
- `template<class size_vec_t >`  
[tensor\\_grid](#) (size\_t rank, const size\_vec\_t &dim)  
*Create a tensor of rank rank with sizes given in dim.*

#### Set functions

- `template<class vec_t >`  
`int` [set\\_val](#) (const vec\_t &grdp, double val)  
*Set the element closest to grid point grdp to value val.*
- `template<class vec_t, class vec2_t >`  
`int` [set\\_val](#) (const vec\_t &grdp, double val, vec2\_t &closest)  
*Set the element closest to grid point grdp to value val.*

#### Get functions

- `template<class vec_t >`  
`double` [get\\_val](#) (const vec\_t &grdp)  
*Get the element closest to grid point grdp.*
- `template<class vec_t, class vec2_t >`  
`double` [get\\_val](#) (const vec\_t &grdp, const vec2\_t &closest)  
*Get the element closest to grid point grdp to value val.*



## Memory allocation

- `template<class size_vec_t>`  
`int allocate (size_t rank, const size_vec_t &dim)`  
*Allocate space for a tensor of rank `rank` with sizes given in `dim`.*
- `int free ()`  
*Free allocated space (also sets rank to zero)*

## Grid manipulation

- `bool is_grid_set () const`  
*Return true if the grid has been set.*
- `template<class vec_t>`  
`int set_grid (const vec_t &grid_vec)`  
*Set the grid.*
- `size_t lookup_grid (size_t i, double val)`  
*Lookup index for grid closest to `val`.*
- `double get_grid (size_t i, size_t j) const`  
*Lookup `j`th value on the `i`th grid.*
- `template<class vec_t, class size_vec_t>`  
`int lookup_grid_vec (const vec_t &vals, const size_vec_t &indices) const`  
*Lookup indices for grid closest point to `vals`.*
- `size_t lookup_grid_val (size_t i, double &val, double &val2)`  
*Lookup index for grid closest to `val`, returning the grid point.*

## Protected Attributes

- `uvector grid`  
*A rank-sized set of arrays for the grid points.*
- `bool grid_set`  
*If true, the grid has been set by the user.*
- `base_interp_mgr< uvector_base > * bim1`  
*The interpolation manager.*
- `base_interp_mgr< uvector_const_subvector > * bim2`  
*The subvector interpolation manager.*

## Interpolation

- `def_interp_mgr< uvector_base, linear_interp > dim1`
- `def_interp_mgr< uvector_const_subvector, linear_interp > dim2`
- `int set_interp (base_interp_mgr< uvector_base > &bi1, base_interp_mgr< uvector_const_subvector > &bi2)`  
*Set interpolation managers.*
- `double interpolate (double *vals)`  
*Interpolate values `vals` into the tensor, returning the result.*

## 46.338.2 Constructor &amp; Destructor Documentation

46.338.2.1 `template<class size_vec_t> tensor_grid::tensor_grid ( size_t rank, const size_vec_t & dim ) [inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`. If the user requests any of the sizes to be zero, this constructor will call the error handler, create an empty tensor, and will allocate no memory.

Definition at line 538 of file `tensor.h`.

## 46.338.3 Member Function Documentation

46.338.3.1 `template<class vec_t, class vec2_t> int tensor_grid::set_val ( const vec_t & grdp, double val, vec2_t & closest ) [inline]`

The parameters `closest` and `grdp` may be identical, allowing one to update a vector `grdp` with the closest grid point.

Definition at line 584 of file `tensor.h`.

46.338.3.2 `template<class size_vec_t> int tensor_grid::allocate ( size_t rank, const size_vec_t & dim ) [inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`.

If memory was previously allocated, it will be freed before the new allocation and previously specified grid data will be lost.

If the user requests any of the sizes to be zero, this function will call the error handler and will allocate no memory. If memory was previously allocated, the tensor is left unmodified and no deallocation is performed.

Reimplemented from [tensor](#).

Definition at line 667 of file `tensor.h`.

46.338.3.3 `template<class vec_t> int tensor_grid::set_grid ( const vec_t & grid_vec ) [inline]`

The grid must be specified for all of the dimensions at once. Denote  $(\text{size})_0$  as the size of the first dimension,  $(\text{size})_1$  as the size of the second dimension, and so on. Then the first  $(\text{size})_0$  entries in `grid` must be the grid for the first dimension, the next  $(\text{size})_1$  entries must be the grid for the second dimension, and so on. Thus `grid` must be a vector of size

$$\sum_{i=0}^{\text{rank}} (\text{size})_i$$

Note that the grid is copied so the function argument may be destroyed by the user after calling `set_grid()` without affecting the tensor grid.

**Idea for Future** Define a more generic interface for matrix types

Definition at line 725 of file `tensor.h`.

46.338.3.4 `template<class vec_t, class size_vec_t> int tensor_grid::lookup_grid_vec ( const vec_t & vals, const size_vec_t & indices ) const [inline]`

The values in `vals` are not modified by this function.

Definition at line 779 of file `tensor.h`.

46.338.3.5 `double tensor_grid::interpolate ( double * vals ) [inline]`

This is a quick and dirty implementation of n-dimensional interpolation by recursive application of the 1-dimensional routine from [smart\\_interp\\_vec](#), using the base interpolation object specified in the template parameter `base_interp_t`. This will be slow for sufficiently large data sets.

**Idea for Future** Maybe make this a template as well?

**Idea for Future** It should be straightforward to improve the scaling of this algorithm significantly by creating a "window" of local points around the point of interest. This could be done easily by constructing an initial subtensor. However, this should probably be superseded by a more generic alternative which avoids explicit use of the 1-d interpolation types.

Definition at line 839 of file `tensor.h`.

The documentation for this class was generated from the following file:

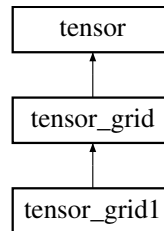
- [tensor.h](#)

## 46.339 `tensor_grid1` Class Reference

Rank 1 tensor with a grid.

```
#include <tensor.h>
```

Inheritance diagram for tensor\_grid1:



#### 46.339.1 Detailed Description

Definition at line 965 of file tensor.h.

##### Public Member Functions

- [tensor\\_grid1](#) ()  
*Create an empty tensor.*
- [tensor\\_grid1](#) (size\_t sz)  
*Create a rank 2 tensor of size (sz,sz,sz3)*
- double & [get](#) (size\_t ix1)  
*Get the element indexed by (ix1)*
- const double & [get](#) (size\_t ix1) const  
*Get the element indexed by (ix1)*
- void [set](#) (size\_t ix1, double val)  
*Set the element indexed by (ix1) to value val.*
- double [interp](#) (double x)  
*Interpolate x and return the results.*

The documentation for this class was generated from the following file:

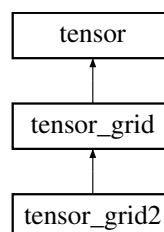
- [tensor.h](#)

## 46.340 tensor\_grid2 Class Reference

Rank 2 tensor with a grid.

```
#include <tensor.h>
```

Inheritance diagram for tensor\_grid2:



#### 46.340.1 Detailed Description

Definition at line 1062 of file tensor.h.

## Public Member Functions

- [tensor\\_grid2](#) ()  
*Create an empty tensor.*
- [tensor\\_grid2](#) (size\_t sz, size\_t sz2)  
*Create a rank 2 tensor of size (sz,sz2)*
- double & [get](#) (size\_t ix1, size\_t ix2)  
*Get the element indexed by (ix1,ix2)*
- const double & [get](#) (size\_t ix1, size\_t ix2) const  
*Get the element indexed by (ix1,ix2)*
- void [set](#) (size\_t ix1, size\_t ix2, double val)  
*Set the element indexed by (ix1,ix2) to value val.*
- double [interp](#) (double x, double y)  
*Interpolate (x,y) and return the results.*

The documentation for this class was generated from the following file:

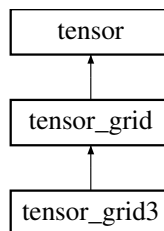
- [tensor.h](#)

## 46.341 tensor\_grid3 Class Reference

Rank 3 tensor with a grid.

```
#include <tensor.h>
```

Inheritance diagram for tensor\_grid3:



## 46.341.1 Detailed Description

Definition at line 1160 of file tensor.h.

## Public Member Functions

- [tensor\\_grid3](#) ()  
*Create an empty tensor.*
- [tensor\\_grid3](#) (size\_t sz, size\_t sz2, size\_t sz3)  
*Create a rank 3 tensor of size (sz,sz2,sz3)*
- double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3)  
*Get the element indexed by (ix1,ix2,ix3)*
- const double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3) const  
*Get the element indexed by (ix1,ix2,ix3)*
- void [set](#) (size\_t ix1, size\_t ix2, size\_t ix3, double val)  
*Set the element indexed by (ix1,ix2,ix3) to value val.*
- double [interp](#) (double x, double y, double z)  
*Interpolate (x,y,z) and return the results.*

The documentation for this class was generated from the following file:

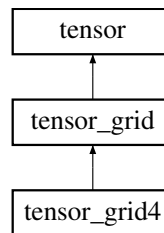
- [tensor.h](#)

46.342 `tensor_grid4` Class Reference

Rank 4 tensor with a grid.

```
#include <tensor.h>
```

Inheritance diagram for `tensor_grid4`:



## 46.342.1 Detailed Description

Definition at line 1264 of file `tensor.h`.

## Public Member Functions

- [`tensor\_grid4`](#) ()  
*Create an empty tensor.*
- [`tensor\_grid4`](#) (size\_t sz, size\_t sz2, size\_t sz3, size\_t sz4)  
*Create a rank 4 tensor of size (sz,sz2,sz3,sz4)*
- double & [`get`](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4)  
*Get the element indexed by (ix1,ix2,ix3,ix4)*
- const double & [`get`](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4) const  
*Get the element indexed by (ix1,ix2,ix3,ix4)*
- void [`set`](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4, double val)  
*Set the element indexed by (ix1,ix2,ix3,ix4) to value val.*
- double [`interp`](#) (double x, double y, double z, double a)  
*Interpolate (x,y,z,a) and return the results.*

The documentation for this class was generated from the following file:

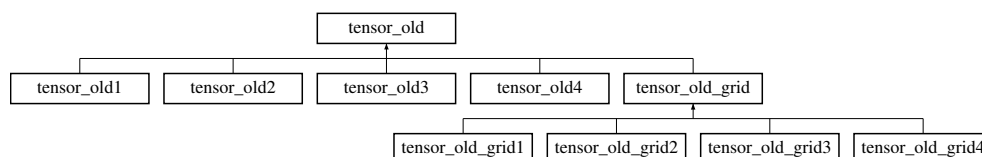
- [`tensor.h`](#)

46.343 `tensor_old` Class Reference

Tensor\_Old class with arbitrary dimensions.

```
#include <tensor_old.h>
```

Inheritance diagram for `tensor_old`:



## 46.343.1 Detailed Description

The elements of a `tensor_old` are typically specified as a list of `size_t` numbers with length equal to the `tensor_old` rank. For a rank-4 `tensor_old` named `t`, the element `t[1][2][0][3]` can be obtained with something similar to

```
size_t ix[4]={1,2,0,3};
double x=t.get(ix);
```

Empty `tensor_olds` have zero rank.

Slices of `tensor_olds` are subsets obtained from fixing the index of several dimensions, while letting other dimensions vary. For a slice with one dimension not fixed, see `vector_slice()`. For a slice with two dimensions not fixed, see `matrix_slice()`.

For I/O with `tensor_olds`, see `hdf_io.h`.

**Idea for Future** Could implement arithmetic operators `+` and `-` and some different products.

**Idea for Future** Implement copies to and from vector and matrices

**Idea for Future** Implement `tensor_old` contractions, i.e. `tensor_old = tensor_old * tensor_old`

**Idea for Future** Consider making a template type to replace `double`, e.g. `value_t`.

**Idea for Future** Could be interesting to write an iterator for this class.

Definition at line 93 of file `tensor_old.h`.

## Public Member Functions

- `tensor_old()`  
*Create an empty `tensor_old` with zero rank.*
- `template<class uint_vec_t>`  
`tensor_old` (`size_t` rank, `const uint_vec_t &dim`)  
*Create a `tensor_old` of rank `rank` with sizes given in `dim`.*

## Set functions

- `template<class uint_vec_t>`  
`void set` (`const uint_vec_t &index`, `double val`)  
*Set the element indexed by `index` to value `val`.*
- `void set_all` (`double x`)  
*Set all elements in a `tensor_old` to some fixed value.*

## Get functions

- `template<class uint_vec_t>`  
`double & get` (`const uint_vec_t &index`)  
*Get the element indexed by `index`.*
- `template<class uint_vec_t>`  
`double const & get` (`const uint_vec_t &index`) `const`  
*Get a const reference to the element indexed by `index`.*

## Slice functions

- `template<class uint_vec_t>`  
`ovector_array_stride vector_slice` (`size_t ix`, `const uint_vec_t &index`)  
*Fix all but one index to create a vector.*
- `template<class uint_vec_t>`  
`omatrix_array matrix_slice` (`size_t ix`, `const uint_vec_t &index`)  
*Fix all but two indices to create a matrix.*

**Memory allocation**

- `template<class uint_vec_t>`  
`void tensor\_old\_allocate (size_t rank, const uint_vec_t &dim)`  
*Allocate space for a [tensor\\_old](#) of rank `rank` with sizes given in `dim`.*
- `void tensor\_old\_free ()`  
*Free allocated space (also sets rank to zero)*

**Size functions**

- `size_t get\_rank () const`  
*Return the rank of the [tensor\\_old](#).*
- `size_t get\_size (size_t i) const`  
*Returns the size of the `i`th index.*
- `const size_t * get\_size\_arr () const`  
*Return the full array of sizes.*
- `const double * get\_data () const`  
*Return the full array of sizes.*
- `size_t total\_size () const`  
*Returns the size of the [tensor\\_old](#) (the product of the sizes over every index)*

**Index manipulation**

- `template<class uint_vec_t>`  
`size_t pack\_indices (const uint_vec_t &index)`  
*Pack the indices into a single array index.*
- `template<class uint_vec_t>`  
`void unpack\_indices (size_t ix, uint_vec_t &index)`  
*Unpack the single array index into indices.*

**Protected Attributes**

- `double * data`  
*The data.*
- `size_t * size`  
*A rank-sized array of the sizes of each dimension.*
- `size_t rk`  
*Rank.*

**46.343.2 Constructor & Destructor Documentation**

**46.343.2.1** `template<class uint_vec_t> tensor\_old::tensor\_old ( size_t rank, const uint_vec_t & dim ) [inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`. If the user requests any of the sizes to be zero, this constructor will call the error handler, create an empty [tensor\\_old](#), and will allocate no memory.

Definition at line 127 of file `tensor_old.h`.

**46.343.3 Member Function Documentation**

**46.343.3.1** `template<class uint_vec_t> ovector\_array\_stride tensor\_old::vector\_slice ( size_t ix, const uint_vec_t & index ) [inline]`

This fixes all of the indices to the values given in `index` except for the index number `ix`, and returns the corresponding vector, whose length is equal to the size of the [tensor\\_old](#) in that index. The value `index[ix]` is ignored.

For example, for a rank 3 [tensor\\_old](#) allocated with

```
tensor_old t;
size_t dim[3]={3,4,5};
t.tensor_old_allocate(3,dim);
```

the following code

```
size_t index[3]={1,0,3};
ovector_view v=t.vector_slice(1,index);
```

Gives a vector `v` of length 4 which refers to the values `t(1,0,3)`, `t(1,1,3)`, `t(1,2,3)`, and `t(1,3,3)`.

Definition at line 282 of file `tensor_old.h`.

**46.343.3.2** `template<class uint_vec_t> omatrix_array tensor_old::matrix_slice ( size_t ix, const uint_vec_t & index ) [inline]`

This fixes all of the indices to the values given in `index` except for the index number `ix` and the last index, and returns the corresponding matrix, whose size is equal to the size of the [tensor\\_old](#) in the two indices which are not fixed.

Since the last index is always fixed, the parameter `ix` is limited to be  $\in [0, \text{rank} - 2]$ .

Definition at line 310 of file `tensor_old.h`.

**46.343.3.3** `template<class uint_vec_t> void tensor_old::tensor_old_allocate ( size_t rank, const uint_vec_t & dim ) [inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`.

If memory was previously allocated, it will be freed before the new allocation.

If the user requests any of the sizes to be zero, this function will call the error handler and will allocate no memory. If memory was previously allocated, the [tensor\\_old](#) is left unmodified and no deallocation is performed.

Reimplemented in [tensor\\_old\\_grid](#).

Definition at line 355 of file `tensor_old.h`.

The documentation for this class was generated from the following file:

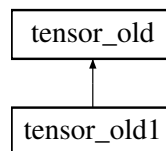
- [tensor\\_old.h](#)

## 46.344 `tensor_old1` Class Reference

Rank 1 [tensor\\_old](#).

```
#include <tensor_old.h>
```

Inheritance diagram for `tensor_old1`:



### 46.344.1 Detailed Description

Definition at line 970 of file `tensor_old.h`.

#### Public Member Functions

- [tensor\\_old1](#) ()  
*Create an empty [tensor\\_old](#).*
- [tensor\\_old1](#) (size\_t sz)  
*Create a rank 1 [tensor\\_old](#) of size *sz*.*



- double & [get](#) (size\_t ix)  
*Get the element indexed by ix.*
- const double & [get](#) (size\_t ix) const  
*Get the element indexed by ix.*
- void [set](#) (size\_t index, double val)  
*Set the element indexed by index to value val.*
- void [set](#) (size\_t \*index, double val)  
*Set the element indexed by index to value val.*
- double & [operator\[\]](#) (size\_t ix)  
*Get an element using array-like indexing.*
- double & [operator\(\)](#) (size\_t ix)  
*Get an element using operator()*

#### 46.344.2 Member Function Documentation

46.344.2.1 void `tensor_old1::set` ( size\_t \* *index*, double *val* ) [inline]

(We have to explicitly provide this version since the `set()` function is overloaded in this child of `tensor_old`.)

Definition at line 994 of file `tensor_old.h`.

The documentation for this class was generated from the following file:

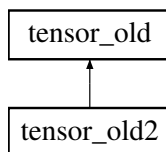
- [tensor\\_old.h](#)

### 46.345 `tensor_old2` Class Reference

Rank 2 [tensor\\_old](#).

```
#include <tensor_old.h>
```

Inheritance diagram for `tensor_old2`:



#### 46.345.1 Detailed Description

Definition at line 1064 of file `tensor_old.h`.

##### Public Member Functions

- [tensor\\_old2](#) ()  
*Create an empty [tensor\\_old](#).*
- [tensor\\_old2](#) (size\_t sz, size\_t sz2)  
*Create a rank 2 [tensor\\_old](#) of size (sz,sz2)*
- double & [get](#) (size\_t ix1, size\_t ix2)  
*Get the element indexed by (ix1,ix2)*
- const double & [get](#) (size\_t ix1, size\_t ix2) const  
*Get the element indexed by (ix1,ix2)*
- void [set](#) (size\_t ix1, size\_t ix2, double val)  
*Set the element indexed by (ix1,ix2) to value val.*
- void [set](#) (size\_t \*index, double val)

*Set the element indexed by `index` to value `val`.*

- `double &operator()` (`size_t ix`, `size_t iy`)  
*Get the element indexed by `(ix1,ix2)`*

#### 46.345.2 Member Function Documentation

46.345.2.1 `void tensor_old2::set ( size_t * index, double val )` [`inline`]

(We have to explicitly provide this version since the `set()` function is overloaded in this child of `tensor_old`.)

Definition at line 1104 of file `tensor_old.h`.

The documentation for this class was generated from the following file:

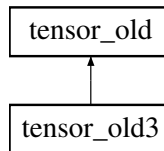
- [tensor\\_old.h](#)

### 46.346 `tensor_old3` Class Reference

Rank 3 `tensor_old`.

```
#include <tensor_old.h>
```

Inheritance diagram for `tensor_old3`:



#### 46.346.1 Detailed Description

Definition at line 1177 of file `tensor_old.h`.

##### Public Member Functions

- `tensor_old3 ()`  
*Create an empty `tensor_old`.*
- `tensor_old3 (size_t sz, size_t sz2, size_t sz3)`  
*Create a rank 3 `tensor_old` of size `(sz,sz2,sz3)`*
- `double &get (size_t ix1, size_t ix2, size_t ix3)`  
*Get the element indexed by `(ix1,ix2,ix3)`*
- `const double &get (size_t ix1, size_t ix2, size_t ix3) const`  
*Get the element indexed by `(ix1,ix2,ix3)`*
- `void set (size_t ix1, size_t ix2, size_t ix3, double val)`  
*Set the element indexed by `(ix1,ix2,ix3)` to value `val`.*
- `void set (size_t *index, double val)`  
*Set the element indexed by `index` to value `val`.*

#### 46.346.2 Member Function Documentation

46.346.2.1 `void tensor_old3::set ( size_t * index, double val )` [`inline`]

(We have to explicitly provide this version since the `set()` function is overloaded in this child of `tensor_old`.)

Definition at line 1218 of file `tensor_old.h`.

The documentation for this class was generated from the following file:

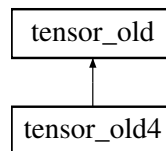
- [tensor\\_old.h](#)

## 46.347 `tensor_old4` Class Reference

Rank 4 [tensor\\_old](#).

```
#include <tensor_old.h>
```

Inheritance diagram for `tensor_old4`:



### 46.347.1 Detailed Description

Definition at line 1289 of file `tensor_old.h`.

#### Public Member Functions

- [tensor\\_old4](#) ()  
*Create an empty [tensor\\_old](#).*
- [tensor\\_old4](#) (size\_t sz, size\_t sz2, size\_t sz3, size\_t sz4)  
*Create a rank 4 [tensor\\_old](#) of size (sz,sz2,sz3,sz4)*
- double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4)  
*Get the element indexed by (ix1,ix2,ix3,ix4)*
- const double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4) const  
*Get the element indexed by (ix1,ix2,ix3,ix4)*
- void [set](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4, double val)  
*Set the element indexed by (ix1,ix2,ix3,ix4) to value val.*
- void [set](#) (size\_t \*index, double val)  
*Set the element indexed by index to value val.*

### 46.347.2 Member Function Documentation

46.347.2.1 void `tensor_old4::set` ( size\_t \* *index*, double *val* ) [inline]

(We have to explicitly provide this version since the `set()` function is overloaded in this child of [tensor\\_old](#).)

Definition at line 1335 of file `tensor_old.h`.

The documentation for this class was generated from the following file:

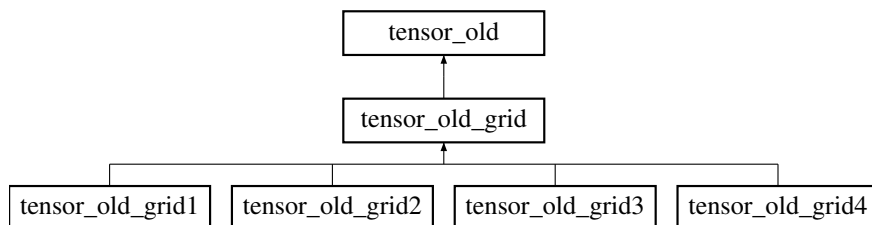
- [tensor\\_old.h](#)

## 46.348 `tensor_old_grid` Class Reference

Tensor\_Old class with arbitrary dimensions with a grid.

```
#include <tensor_old.h>
```

Inheritance diagram for `tensor_old_grid`:



#### 46.348.1 Detailed Description

This `tensor_old` class allows one to assign the indexes to numerical scales, so that n-dimensional interpolation can be performed. To set the grid, use `set_grid()` and then interpolation can be done using `interpolate()`.

By convention, member functions ending in the `_val` suffix return the closest grid-point to some user-specified values.

**Idea for Future** Only allocate space for grid if it is set

**Idea for Future** Could implement arithmetic operators `+` and `-` and some different products.

**Idea for Future** Consider creating a `set_grid()` function which takes grids from an object like `hist_grid`. Maybe make a constructor for a `tensor_old_grid` object which just takes as input a set of grids?

Definition at line 508 of file `tensor_old.h`.

#### Public Member Functions

- `tensor_old_grid()`  
Create an empty `tensor_old` with zero rank.
- `template<class uint_vec_t>`  
`tensor_old_grid` (size\_t rank, const uint\_vec\_t &dim)  
Create a `tensor_old` of rank `rank` with sizes given in `dim`.

#### Set functions

- `template<class vec_t>`  
`int set_val` (const vec\_t &grdp, double val)  
Set the element closest to grid point `grdp` to value `val`.
- `template<class vec_t, class vec2_t>`  
`int set_val` (const vec\_t &grdp, double val, vec2\_t &closest)  
Set the element closest to grid point `grdp` to value `val`.

#### Get functions

- `template<class vec_t>`  
`double get_val` (const vec\_t &grdp)  
Get the element closest to grid point `grdp`.
- `template<class vec_t, class vec2_t>`  
`double get_val` (const vec\_t &grdp, const vec2\_t &closest)  
Get the element closest to grid point `grdp` to value `val`.

## Memory allocation

- `template<class uint_vec_t>`  
`int tensor_old_allocate (size_t rank, const uint_vec_t &dim)`  
*Allocate space for a `tensor_old` of rank `rank` with sizes given in `dim`.*
- `int tensor_old_free ()`  
*Free allocated space (also sets rank to zero)*

## Grid manipulation

- `bool is_grid_set () const`  
*Return true if the grid has been set.*
- `template<class vec_t>`  
`int set_grid (const vec_t &grid)`  
*Set the grid.*
- `int set_grid_old (double **vals)`
- `size_t lookup_grid (size_t i, double val)`  
*Lookup index for grid closest to `val`.*
- `double get_grid (size_t i, size_t j) const`  
*Lookup index for grid closest to `val`.*
- `template<class vec_t, class uint_vec_t>`  
`int lookup_grid_vec (const vec_t &vals, const uint_vec_t &indices) const`  
*Lookup indices for grid closest point to `vals`.*
- `size_t lookup_grid_val (size_t i, double &val, double &val2)`  
*Lookup index for grid closest to `val`, returning the grid point.*

## Protected Attributes

- `double ** grd`  
*A rank-sized set of arrays for the grid points.*
- `bool grid_set`  
*If true, the grid has been set by the user.*
- `base_interp_mgr< double * > * bim1`  
*The interpolation manager.*
- `base_interp_mgr< array_const_subvector > * bim2`  
*The subvector interpolation manager.*

## Interpolation

- `def_interp_mgr< double *, linear_interp > dim1`
- `def_interp_mgr< array_const_subvector, linear_interp > dim2`
- `int set_interp (base_interp_mgr< double * > &bi1, base_interp_mgr< array_const_subvector > &bi2)`  
*Set interpolation managers.*
- `double interpolate (double *vals)`  
*Interpolate values `vals` into the `tensor_old`, returning the result.*

## 46.348.2 Constructor &amp; Destructor Documentation

46.348.2.1 `template<class uint_vec_t> tensor_old_grid::tensor_old_grid ( size_t rank, const uint_vec_t & dim ) [inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`. If the user requests any of the sizes to be zero, this constructor will call the error handler, create an empty `tensor_old`, and will allocate no memory.

Definition at line 546 of file `tensor_old.h`.

## 46.348.3 Member Function Documentation

46.348.3.1 `template<class vec_t, class vec2_t> int tensor_old_grid::set_val ( const vec_t & grdp, double val, vec2_t & closest )` `[inline]`

The parameters `closest` and `grdp` may be identical, allowing one to update a vector `grdp` with the closest grid point.

Definition at line 604 of file `tensor_old.h`.

46.348.3.2 `template<class uint_vec_t> int tensor_old_grid::tensor_old_allocate ( size_t rank, const uint_vec_t & dim )` `[inline]`

The parameter `dim` must be a pointer to an array of sizes with length `rank`.

If memory was previously allocated, it will be freed before the new allocation and previously specified grid data will be lost.

If the user requests any of the sizes to be zero, this function will call the error handler and will allocate no memory. If memory was previously allocated, the `tensor_old` is left unmodified and no deallocation is performed.

Reimplemented from `tensor_old`.

Definition at line 696 of file `tensor_old.h`.

46.348.3.3 `template<class vec_t> int tensor_old_grid::set_grid ( const vec_t & grid )` `[inline]`

The grid must be specified for all of the dimensions at once. Denote  $(\text{size})_0$  as the size of the first dimension,  $(\text{size})_1$  as the size of the second dimension, and so on. Then the first  $(\text{size})_0$  entries in `grid` must be the grid for the first dimension, the next  $(\text{size})_1$  entries must be the grid for the second dimension, and so on. Thus `grid` must be a vector of size

$$\sum_{i=0}^{\text{rank}} (\text{size})_i$$

Note that the grid is copied so the function argument may be destroyed by the user after calling `set_grid()` without affecting the `tensor_old` grid.

**Idea for Future** Define a more generic interface for matrix types

Definition at line 757 of file `tensor_old.h`.

46.348.3.4 `template<class vec_t, class uint_vec_t> int tensor_old_grid::lookup_grid_vec ( const vec_t & vals, const uint_vec_t & indices ) const` `[inline]`

The values in `vals` are not modified by this function.

Definition at line 821 of file `tensor_old.h`.

46.348.3.5 `double tensor_old_grid::interpolate ( double * vals )` `[inline]`

This is a quick and dirty implementation of n-dimensional interpolation by recursive application of the 1-dimensional routine from `smart_interp_vec`, using the base interpolation object specified in the template parameter `base_interp_t`. This will be slow for sufficiently large data sets.

**Idea for Future** Maybe make this a template as well?

**Idea for Future** It should be straightforward to improve the scaling of this algorithm significantly by creating a "window" of local points around the point of interest. This could be done easily by constructing an initial `subtensor_old`. However, this should probably be superseded by a more generic alternative which avoids explicit use of the 1-d interpolation types.

Definition at line 886 of file `tensor_old.h`.

The documentation for this class was generated from the following file:

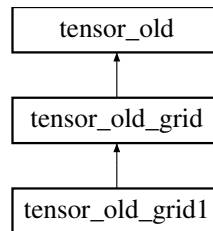
- [tensor\\_old.h](#)

## 46.349 tensor\_old\_grid1 Class Reference

Rank 2 [tensor\\_old](#) with a grid.

```
#include <tensor_old.h>
```

Inheritance diagram for tensor\_old\_grid1:



### 46.349.1 Detailed Description

Definition at line 1007 of file [tensor\\_old.h](#).

#### Public Member Functions

- [tensor\\_old\\_grid1](#) ()  
*Create an empty [tensor\\_old](#).*
- [tensor\\_old\\_grid1](#) (size\_t sz)  
*Create a rank 2 [tensor\\_old](#) of size (sz,sz2,sz3)*
- double & [get](#) (size\_t ix1)  
*Get the element indexed by (ix1)*
- const double & [get](#) (size\_t ix1) const  
*Get the element indexed by (ix1)*
- void [set](#) (size\_t ix1, double val)  
*Set the element indexed by (ix1) to value val.*
- double [interp](#) (double x)  
*Interpolate x and return the results.*

The documentation for this class was generated from the following file:

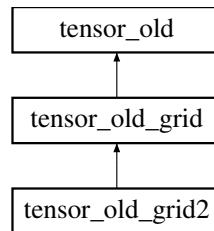
- [tensor\\_old.h](#)

## 46.350 tensor\_old\_grid2 Class Reference

Rank 2 [tensor\\_old](#) with a grid.

```
#include <tensor_old.h>
```

Inheritance diagram for tensor\_old\_grid2:



#### 46.350.1 Detailed Description

Definition at line 1116 of file tensor\_old.h.

##### Public Member Functions

- [tensor\\_old\\_grid2](#) ()  
Create an empty *tensor\_old*.
- [tensor\\_old\\_grid2](#) (size\_t sz, size\_t sz2)  
Create a rank 2 *tensor\_old* of size (sz,sz2)
- double & [get](#) (size\_t ix1, size\_t ix2)  
Get the element indexed by (ix1,ix2)
- const double & [get](#) (size\_t ix1, size\_t ix2) const  
Get the element indexed by (ix1,ix2)
- void [set](#) (size\_t ix1, size\_t ix2, double val)  
Set the element indexed by (ix1,ix2) to value *val*.
- double [interp](#) (double x, double y)  
Interpolate (x,y) and return the results.

The documentation for this class was generated from the following file:

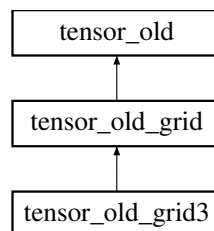
- [tensor\\_old.h](#)

#### 46.351 tensor\_old\_grid3 Class Reference

Rank 3 [tensor\\_old](#) with a grid.

```
#include <tensor_old.h>
```

Inheritance diagram for tensor\_old\_grid3:



#### 46.351.1 Detailed Description

Definition at line 1226 of file tensor\_old.h.



## Public Member Functions

- [tensor\\_old\\_grid3](#) ()  
Create an empty *tensor\_old*.
- [tensor\\_old\\_grid3](#) (size\_t sz, size\_t sz2, size\_t sz3)  
Create a rank 3 *tensor\_old* of size (sz,sz2,sz3)
- double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3)  
Get the element indexed by (ix1,ix2,ix3)
- const double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3) const  
Get the element indexed by (ix1,ix2,ix3)
- void [set](#) (size\_t ix1, size\_t ix2, size\_t ix3, double val)  
Set the element indexed by (ix1,ix2,ix3) to value val.
- double [interp](#) (double x, double y, double z)  
Interpolate (x,y,z) and return the results.

The documentation for this class was generated from the following file:

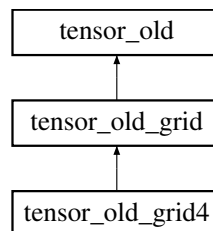
- [tensor\\_old.h](#)

## 46.352 tensor\_old\_grid4 Class Reference

Rank 4 *tensor\_old* with a grid.

```
#include <tensor_old.h>
```

Inheritance diagram for tensor\_old\_grid4:



## 46.352.1 Detailed Description

Definition at line 1343 of file tensor\_old.h.

## Public Member Functions

- [tensor\\_old\\_grid4](#) ()  
Create an empty *tensor\_old*.
- [tensor\\_old\\_grid4](#) (size\_t sz, size\_t sz2, size\_t sz3, size\_t sz4)  
Create a rank 4 *tensor\_old* of size (sz,sz2,sz3,sz4)
- double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4)  
Get the element indexed by (ix1,ix2,ix3,ix4)
- const double & [get](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4) const  
Get the element indexed by (ix1,ix2,ix3,ix4)
- void [set](#) (size\_t ix1, size\_t ix2, size\_t ix3, size\_t ix4, double val)  
Set the element indexed by (ix1,ix2,ix3,ix4) to value val.
- double [interp](#) (double x, double y, double z, double a)  
Interpolate (x,y,z,a) and return the results.

The documentation for this class was generated from the following file:

- [tensor\\_old.h](#)

## 46.353 test\_mgr Class Reference

A class to manage testing and record success and failure.

```
#include <test_mgr.h>
```

### 46.353.1 Detailed Description

**Idea for Future** `test_mgr::success` and `test_mgr::last_fail` should be protected, but that breaks the `operator+()` function. Can this be fixed?

Definition at line 37 of file `test_mgr.h`.

### Public Member Functions

- `bool report ()`  
*Provide a report of all tests so far.*
- `std::string get_last_fail ()`  
*Returns the description of the last test that failed.*
- `void set_output_level (int l)`  
*Set the output level.*
- `int get_ntests ()`  
*Return the number of tests performed so far.*

### The testing methods

- `bool test_rel (double result, double expected, double rel_error, std::string description)`  
*Test for  $|result - expected|/expected < rel\_error$ .*
- `bool test_abs (double result, double expected, double abs_error, std::string description)`  
*Test for  $|result - expected| < abs\_error$ .*
- `bool test_fact (double result, double expected, double factor, std::string description)`  
*Test for  $1/factor < result/expected < factor$ .*
- `bool test_str (std::string result, std::string expected, std::string description)`  
*Test for  $result = expected$ .*
- `bool test_gen (bool value, std::string description)`  
*Test for  $result = expected$ .*
- `template<class vec_t, class vec2_t >`  
`bool test_rel_arr (int nv, const vec_t &result, const vec2_t &expected, double rel_error, std::string description)`  
*Test for  $|result - expected|/expected < rel\_error$  over each element of an array.*
- `template<class mat_t, class mat2_t >`  
`bool test_rel_mat (int nr, int nc, const mat_t &result, const mat2_t &expected, double rel_error, std::string description)`  
*Test for  $|result - expected|/expected < rel\_error$  over each element of an array.*
- `template<class vec_t, class vec2_t >`  
`bool test_abs_arr (int nv, const vec_t &result, const vec2_t &expected, double rel_error, std::string description)`  
*Test for  $|result - expected| < abs\_error$  over each element of an array.*
- `template<class vec_t, class vec2_t >`  
`bool test_fact_arr (int nv, const vec_t &result, const vec2_t &expected, double factor, std::string description)`  
*Test for  $1/factor < result/expected < factor$  over each element of an array.*
- `template<class vec_t >`  
`bool test_gen_arr (int nv, const vec_t &result, const vec_t &expected, std::string description)`  
*Test for equality of a generic array.*

### Data Fields

- `bool success`  
*True if all tests have passed.*
- `std::string last_fail`  
*The description of the last failed test.*

### Protected Member Functions

- void `process_test` (bool ret, std::string d2, std::string description)  
*A helper function for processing tests.*

### Protected Attributes

- int `ntests`  
*The number of tests performed.*
- int `output_level`  
*The output level.*

### Friends

- const `test_mgr operator+` (const `test_mgr` &left, const `test_mgr` &right)  
*Add two `test_mgr` objects (if either failed, the sum fails)*

## 46.353.2 Member Function Documentation

### 46.353.2.1 bool test\_mgr::report ( )

Returns true if all tests have passed and false if at least one test failed.

### 46.353.2.2 void test\_mgr::set\_output\_level ( int / ) [inline]

Possible values:

- 0 = No output
- 1 = Output only tests that fail
- 2 = Output all tests

Definition at line 79 of file `test_mgr.h`.

The documentation for this class was generated from the following file:

- `test_mgr.h`

## 46.354 twod\_eqi\_intp Class Reference

Two-dimensional interpolation for equally-spaced intervals.

```
#include <twod_eqi_intp.h>
```

### 46.354.1 Detailed Description

**Note**

This class is unfinished.

This implements the relations from Abramowitz and Stegun:

$$f(x_0 + ph, y_0 + qk) =$$

3-point

$$(1 - p - q)f_{0,0} + pf_{1,0} + qf_{0,1}$$

4-point

$$(1 - p)(1 - q)f_{0,0} + p(1 - q)f_{1,0} + q(1 - p)f_{0,1} + pqf_{1,1}$$

6-point

$$\frac{q(q-1)}{2}f_{0,-1} + \frac{p(p-1)}{2}f_{-1,0} + (1 + pq - p^2 - q^2)f_{0,0} + \frac{p(p-2q+1)}{2}f_{1,0} + \frac{q(q-2p+1)}{2}f_{0,1} + pqf_{1,1}$$

Definition at line 56 of file twod\_eqi\_intp.h.

**Public Member Functions**

- double [interp](#) (double x, double y)  
*Perform the 2-d interpolation.*
- int [set\\_type](#) (int type)  
*Set the interpolation type.*

**Data Fields**

- double [xoff](#)  
*Offset in x-direction.*
- double [yoff](#)  
*Offset in y-direction.*

**46.354.2 Member Function Documentation****46.354.2.1 int twod\_eqi\_intp::set\_type ( int type ) [inline]**

- 3: 3-point
- 4: 4-point
- 6: 6-point (default)

Definition at line 79 of file twod\_eqi\_intp.h.

The documentation for this class was generated from the following file:

- twod\_eqi\_intp.h

**46.355 twod\_intp Class Reference**

Two-dimensional interpolation class.

```
#include <twod_intp.h>
```

## 46.355.1 Detailed Description

This class implements two-dimensional interpolation. Derivatives and integrals along both x- and y-directions can be computed. The storage of the matrix to be specified in the function `set_data()` and this function is designed to follow the format:

	$x_0$	$x_1$	$x_2$
$y_0$	$M_{00}$	$M_{01}$	$M_{02}$
$y_1$	$M_{10}$	$M_{11}$	$M_{12}$
$y_2$	$M_{20}$	$M_{21}$	$M_{22}$

thus the matrix should be  $M[i][j]$  where  $i$  is the y index and  $j$  is the x index. (See also the discussion in the User's guide in the section called [Rows and columns vs. x and y.](#))

The function `set_data()`, does not copy the data, it stores pointers to the data. If the data is modified, then the function `reset_interp()` must be called to reset the interpolation information with the original pointer information. The storage for the data, including the arrays `x_grid` and `y_grid` are all managed by the user.

By default, cubic spline interpolation with natural boundary conditions is used. This can be changed with the `set_interp()` function.

There is an example for the usage of this class given in `examples/ex_twod_intp.cpp`.

**Idea for Future** Could also include mixed second/first derivatives: `deriv_xxy` and `deriv_xyy`.

**Idea for Future** Implement an improved caching system in case, for example `xfirst` is true and the last interpolation used the same value of `x`.

Definition at line 99 of file `twod_intp.h`.

## Public Member Functions

- int `set_data` (size\_t n\_x, size\_t n\_y, `ovector` &x\_grid, `ovector` &y\_grid, `omatrix` &data, bool x\_first=true)  
*Initialize the data for the 2-dimensional interpolation.*
- int `reset_interp` ()  
*Reset the stored interpolation since the data has changed.*
- double `interp` (double x, double y)  
*Perform the 2-d interpolation.*
- double `deriv_x` (double x, double y)  
*Compute the partial derivative in the x-direction.*
- double `deriv2_x` (double x, double y)  
*Compute the partial second derivative in the x-direction.*
- double `integ_x` (double x0, double x1, double y)  
*Compute the integral in the x-direction between x=x0 and x=x1.*
- double `deriv_y` (double x, double y)  
*Compute the partial derivative in the y-direction.*
- double `deriv2_y` (double x, double y)  
*Compute the partial second derivative in the y-direction.*
- double `integ_y` (double x, double y0, double y1)  
*Compute the integral in the y-direction between y=y0 and y=y1.*
- double `deriv_xy` (double x, double y)  
*Compute the mixed partial derivative  $\frac{\partial^2 f}{\partial x \partial y}$ .*
- int `set_interp` (base\_interp\_mgr< `ovector_const_view` > &b1, base\_interp\_mgr< `ovector_const_subvector` > &b2)  
*Specify the base interpolation objects to use.*
- int `unset_data` ()  
*Inform the class the data has been modified or changed in a way that `set_data()` will need to be called again.*

## 46.355.2 Member Function Documentation

46.355.2.1 `int twod_intp::set_data ( size_t n_x, size_t n_y, ovector & x_grid, ovector & y_grid, omatrix & data, bool x_first = true )`

The interpolation type (passed directly to `int_type`) is specified in `int_type` and the data is specified in `data`. The data should be arranged so that the first array index is the y-value (the "row") and the second array index is the x-value (the "column"). The arrays `xfun` and `yfun` specify the two independent variables. `xfun` should be an array of length `nx`, and should be an array of length `ny`. The array `data` should be a two-dimensional array of size `[ny][nx]`.

If `x_first` is true, then `set_data()` creates interpolation objects for each of the rows. Calls to `interp()` then uses these to create a column at the specified value of `x`. An interpolation object is created at this column to find the value of the function at the specified value `y`. If `x_first` is false, the opposite strategy is employed. These two options may give slightly different results.

46.355.2.2 `int twod_intp::reset_interp ( )`

This will return an error if the `set_data()` has not been called

46.355.2.3 `int twod_intp::set_interp ( base_interp_mgr< ovector_const_view > & b1, base_interp_mgr< ovector_const_subvector > & b2 ) [inline]`

This allows the user to provide new interpolation objects for use in the two-dimensional interpolation. For example,

```
twod_intp ti;
ovector x(20), y(40);
omatrix d(40,20);

// Fill x, y, and d with the data, choose linear interpolation
// instead of the default cubic spline
def_interp_mgr<ovector_const_view,linear_interp> dim1;
def_interp_mgr<ovector_const_subvector,linear_interp> dim2;

ti.set_interp(dim1,dim2);
ti.set_data(20,40,x,y,d,true);
```

This function automatically calls `reset_interp()` and `reset_data()` if the data has already been set to reset the internal interpolation objects.

Definition at line 197 of file `twod_intp.h`.

The documentation for this class was generated from the following file:

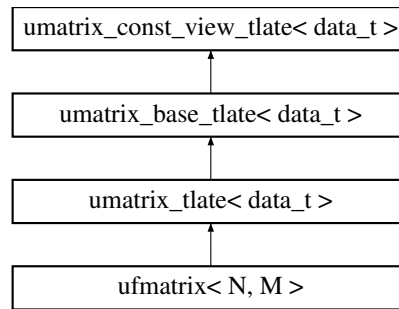
- `twod_intp.h`

46.356 `ufmatrix< N, M >` Class Template Reference

A matrix where the memory allocation is performed in the constructor.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for `ufmatrix< N, M >`:



#### 46.356.1 Detailed Description

```
template<size_t N, size_t M>class ufmatrix< N, M >
```

Definition at line 915 of file `umatrix_tlate.h`.

The documentation for this class was generated from the following file:

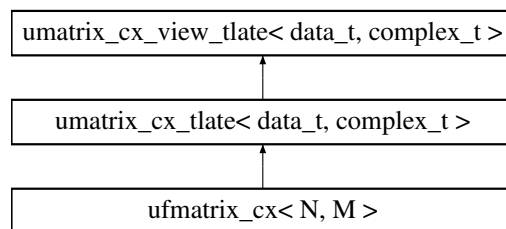
- [umatrix\\_tlate.h](#)

### 46.357 `ufmatrix_cx< N, M >` Class Template Reference

A matrix where the memory allocation is performed in the constructor.

```
#include <umatrix_cx_tlate.h>
```

Inheritance diagram for `ufmatrix_cx< N, M >`:



#### 46.357.1 Detailed Description

```
template<size_t N, size_t M>class ufmatrix_cx< N, M >
```

Definition at line 708 of file `umatrix_cx_tlate.h`.

The documentation for this class was generated from the following file:

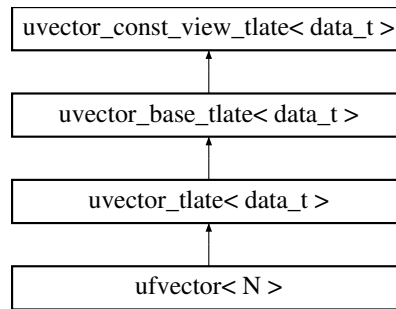
- [umatrix\\_cx\\_tlate.h](#)

### 46.358 `ufvector< N >` Class Template Reference

A vector with unit-stride where the memory allocation is performed in the constructor.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `ufvector< N >`:



#### 46.358.1 Detailed Description

template<size\_t N = 0>class uvector< N >

Definition at line 1054 of file uvector\_tlate.h.

The documentation for this class was generated from the following file:

- [uvector\\_tlate.h](#)

### 46.359 umatrix\_alloc Class Reference

A simple class to provide an [allocate\(\)](#) function for [umatrix](#).

```
#include <umatrix_tlate.h>
```

#### 46.359.1 Detailed Description

Definition at line 903 of file umatrix\_tlate.h.

##### Public Member Functions

- void [allocate](#) ([umatrix](#) &o, int i, int j)  
*Allocate v for i elements.*
- void [free](#) ([umatrix](#) &o)  
*Free memory.*

The documentation for this class was generated from the following file:

- [umatrix\\_tlate.h](#)

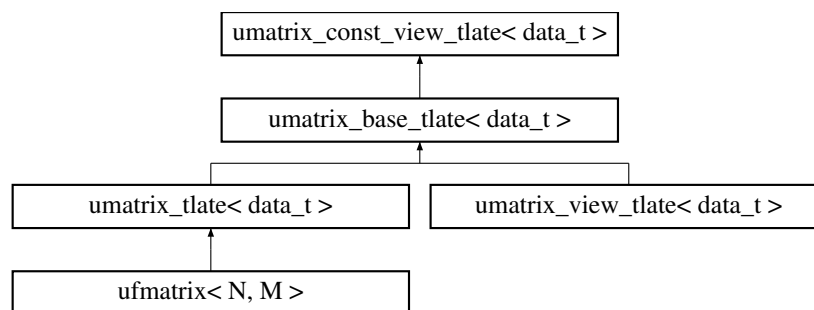
### 46.360 umatrix\_base\_tlate< data\_t > Class Template Reference

A matrix view of double-precision numbers.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for umatrix\_base\_tlate< data\_t >:





### 46.360.1 Detailed Description

`template<class data_t>class umatrix_base_tlate< data_t >`

Definition at line 200 of file `umatrix_tlate.h`.

#### Public Member Functions

##### Copy constructors

- `umatrix_base_tlate` (`umatrix_base_tlate` &`v`)  
*Shallow copy constructor - create a new view of the same matrix.*
- `umatrix_base_tlate` & `operator=` (`umatrix_base_tlate` &`v`)  
*Shallow copy constructor - create a new view of the same matrix.*

##### Get and set methods

- `data_t` \* `operator[]` (`size_t` `i`)  
*Array-like indexing.*
- `const data_t` \* `operator[]` (`size_t` `i`) `const`  
*Array-like indexing.*
- `data_t` & `operator()` (`size_t` `i`, `size_t` `j`)  
*Array-like indexing.*
- `const data_t` & `operator()` (`size_t` `i`, `size_t` `j`) `const`  
*Array-like indexing.*
- `data_t` \* `get_ptr` (`size_t` `i`, `size_t` `j`)  
*Get pointer (with optional range-checking)*
- `int` `set` (`size_t` `i`, `size_t` `j`, `data_t` `val`)  
*Set (with optional range-checking)*
- `int` `set_all` (`data_t` `val`)  
*Set all of the value to be the value `val`.*

##### Arithmetic

- `umatrix_base_tlate< data_t >` & `operator+=` (`const umatrix_base_tlate< data_t >` &`x`)  
*operator+=*
- `umatrix_base_tlate< data_t >` & `operator-=` (`const umatrix_base_tlate< data_t >` &`x`)  
*operator-=*
- `umatrix_base_tlate< data_t >` & `operator+=` (`const data_t` &`y`)  
*operator+=*
- `umatrix_base_tlate< data_t >` & `operator-=` (`const data_t` &`y`)  
*operator-=*
- `umatrix_base_tlate< data_t >` & `operator*=` (`const data_t` &`y`)  
*operator\*=*

## Protected Member Functions

- [umatrix\\_base\\_tlate\(\)](#)  
*Empty constructor.*

The documentation for this class was generated from the following file:

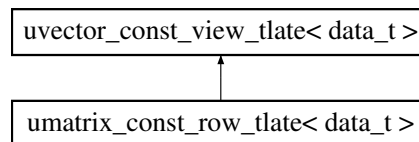
- [umatrix\\_tlate.h](#)

46.361 `umatrix_const_row_tlate< data_t >` Class Template Reference

Create a const vector from a row of a matrix.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for `umatrix_const_row_tlate< data_t >`:



## 46.361.1 Detailed Description

```
template<class data_t>class umatrix_const_row_tlate< data_t >
```

Definition at line 818 of file `umatrix_tlate.h`.

## Public Member Functions

- [umatrix\\_const\\_row\\_tlate](#) (const [umatrix\\_base\\_tlate< data\\_t >](#) &m, size\_t i)  
*Create a vector from row *i* of matrix *m*.*

The documentation for this class was generated from the following file:

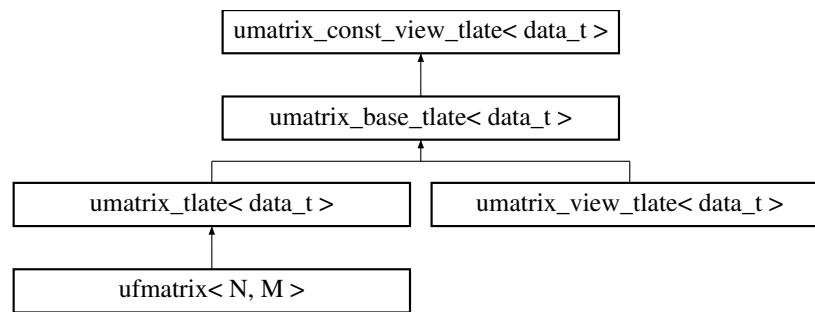
- [umatrix\\_tlate.h](#)

46.362 `umatrix_const_view_tlate< data_t >` Class Template Reference

A matrix view of double-precision numbers.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for `umatrix_const_view_tlate< data_t >`:



### 46.362.1 Detailed Description

`template<class data_t>class umatrix_const_view_tlate< data_t >`

Definition at line 48 of file `umatrix_tlate.h`.

#### Public Member Functions

##### Copy constructors

- `umatrix_const_view_tlate` (const `umatrix_const_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- `umatrix_const_view_tlate` & `operator=` (const `umatrix_const_view_tlate` &v)  
*Shallow copy constructor - create a new view of the same matrix.*

##### Get and set methods

- const `data_t` \* `operator[]` (size\_t i) const  
*Array-like indexing.*
- const `data_t` & `operator()` (size\_t i, size\_t j) const  
*Array-like indexing.*
- `data_t` `get` (size\_t i, size\_t j) const  
*Get (with optional range-checking)*
- const `data_t` \* `get_const_ptr` (size\_t i, size\_t j) const  
*Get pointer (with optional range-checking)*
- size\_t `rows` () const  
*Method to return number of rows.*
- size\_t `cols` () const  
*Method to return number of columns.*

##### Other methods

- bool `is_owner` () const  
*Return true if this object owns the data it refers to.*

#### Protected Member Functions

- `umatrix_const_view_tlate` ()  
*Empty constructor provided for use by `umatrix_tlate(const umatrix_tlate &v)`*

#### Protected Attributes

- `data_t` \* `data`  
*The data.*
- size\_t `size1`

*The number of rows.*

- `size_t` [size2](#)

*The number of columns.*

- `int` [owner](#)

*Zero if memory is owned elsewhere, 1 otherwise.*

#### 46.362.2 Member Function Documentation

**46.362.2.1** `template<class data_t> size_t umatrix_const_view_tlate< data_t >::rows ( ) const` `[inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 162 of file `umatrix_tlate.h`.

**46.362.2.2** `template<class data_t> size_t umatrix_const_view_tlate< data_t >::cols ( ) const` `[inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 171 of file `umatrix_tlate.h`.

The documentation for this class was generated from the following file:

- [umatrix\\_tlate.h](#)

### 46.363 `umatrix_cx_alloc` Class Reference

A simple class to provide an `allocate()` function for `umatrix_cx`.

```
#include <umatrix_cx_tlate.h>
```

#### 46.363.1 Detailed Description

Definition at line 696 of file `umatrix_cx_tlate.h`.

##### Public Member Functions

- `void` [allocate](#) (`umatrix_cx` &o, `int` i, `int` j)  
*Allocate v for i elements.*
- `void` [free](#) (`umatrix_cx` &o)  
*Free memory.*

The documentation for this class was generated from the following file:

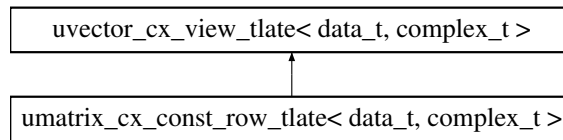
- [umatrix\\_cx\\_tlate.h](#)

### 46.364 `umatrix_cx_const_row_tlate< data_t, complex_t >` Class Template Reference

Create a const vector from a row of a matrix.

```
#include <umatrix_cx_tlate.h>
```

Inheritance diagram for `umatrix_cx_const_row_tlate< data_t, complex_t >`:



#### 46.364.1 Detailed Description

```
template<class data_t, class complex_t>class umatrix_cx_const_row_tlate< data_t, complex_t >
```

Definition at line 624 of file `umatrix_cx_tlate.h`.

#### Public Member Functions

- [umatrix\\_cx\\_const\\_row\\_tlate](#) (const [umatrix\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > &m, size\_t i)  
*Create a vector from row i of matrix m.*

The documentation for this class was generated from the following file:

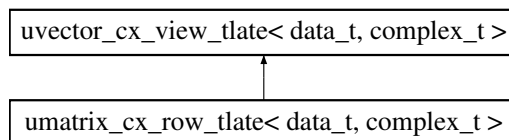
- [umatrix\\_cx\\_tlate.h](#)

### 46.365 `umatrix_cx_row_tlate< data_t, complex_t >` Class Template Reference

Create a vector from a row of a matrix.

```
#include <umatrix_cx_tlate.h>
```

Inheritance diagram for `umatrix_cx_row_tlate< data_t, complex_t >`:



#### 46.365.1 Detailed Description

```
template<class data_t, class complex_t>class umatrix_cx_row_tlate< data_t, complex_t >
```

Definition at line 608 of file `umatrix_cx_tlate.h`.

#### Public Member Functions

- [umatrix\\_cx\\_row\\_tlate](#) ([umatrix\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > &m, size\_t i)  
*Create a vector from row i of matrix m.*

The documentation for this class was generated from the following file:

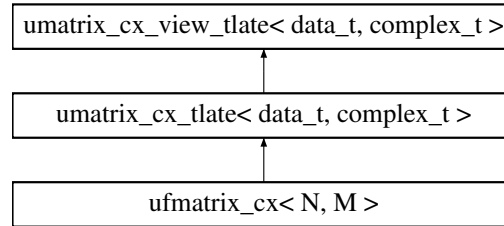
- [umatrix\\_cx\\_tlate.h](#)

**46.366 `umatrix_cx_tlate< data_t, complex_t >` Class Template Reference**

A matrix of double-precision numbers.

```
#include <umatrix_cx_tlate.h>
```

Inheritance diagram for `umatrix_cx_tlate< data_t, complex_t >`:

**46.366.1 Detailed Description**

```
template<class data_t, class complex_t>class umatrix_cx_tlate< data_t, complex_t >
```

Definition at line 366 of file `umatrix_cx_tlate.h`.

**Public Member Functions****Standard constructor**

- [umatrix\\_cx\\_tlate](#) (size\_t r=0, size\_t c=0)  
*Create an umatrix of size n with owner as 'true'.*

**Copy constructors**

- [umatrix\\_cx\\_tlate](#) (const [umatrix\\_cx\\_tlate](#) &v)  
*Deep copy constructor; allocate new space and make a copy.*
- [umatrix\\_cx\\_tlate](#) (const [umatrix\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > &v)  
*Deep copy constructor; allocate new space and make a copy.*
- [umatrix\\_cx\\_tlate](#) & operator= (const [umatrix\\_cx\\_tlate](#) &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- [umatrix\\_cx\\_tlate](#) & operator= (const [umatrix\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > &v)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- [umatrix\\_cx\\_tlate](#) (size\_t n, [uvector\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > uva[ ])  
*Deep copy from an array of uvectors.*
- [umatrix\\_cx\\_tlate](#) (size\_t n, size\_t n2, data\_t \*\*csa)  
*Deep copy from a C-style 2-d array.*

**Memory allocation**

- int [allocate](#) (size\_t nrows, size\_t ncols)  
*Allocate memory after freeing any memory presently in use.*
- int [free](#) ()  
*Free the memory.*

**Other methods**

- [umatrix\\_cx\\_tlate](#)< data\_t, complex\_t > [transpose](#) ()  
*Compute the transpose (even if matrix is not square)*

## 46.366.2 Member Function Documentation

46.366.2.1 `template<class data_t, class complex_t> int umatrix_cx_tlate< data_t, complex_t >::free ( ) [inline]`

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 578 of file `umatrix_cx_tlate.h`.

The documentation for this class was generated from the following file:

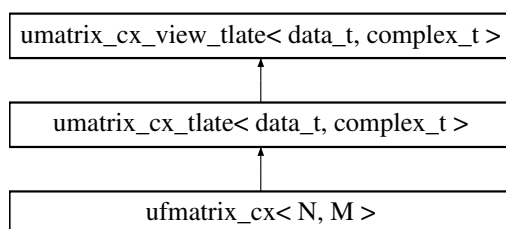
- [umatrix\\_cx\\_tlate.h](#)

46.367 `umatrix_cx_view_tlate< data_t, complex_t >` Class Template Reference

A matrix view of complex numbers.

```
#include <umatrix_cx_tlate.h>
```

Inheritance diagram for `umatrix_cx_view_tlate< data_t, complex_t >`:



## 46.367.1 Detailed Description

```
template<class data_t, class complex_t>class umatrix_cx_view_tlate< data_t, complex_t >
```

Definition at line 49 of file `umatrix_cx_tlate.h`.

## Public Member Functions

## Copy constructors

- [umatrix\\_cx\\_view\\_tlate](#) (const [umatrix\\_cx\\_view\\_tlate](#) &v)  
*So2scllow copy constructor - create a new view of the same matrix.*
- [umatrix\\_cx\\_view\\_tlate](#) & [operator=](#) (const [umatrix\\_cx\\_view\\_tlate](#) &v)  
*So2scllow copy constructor - create a new view of the same matrix.*

## Get and set methods

- `complex_t * operator\[\] (size_t i)`  
*Array-like indexing.*
- `const complex_t * operator\[\] (size_t i) const`  
*Array-like indexing.*
- `complex_t & operator\(\) (size_t i, size_t j)`  
*Array-like indexing.*
- `const complex_t & operator\(\) (size_t i, size_t j) const`  
*Array-like indexing.*
- `complex_t get (size_t i, size_t j) const`  
*Get (with optional range-checking)*
- `complex_t * get\_ptr (size_t i, size_t j)`  
*Get pointer (with optional range-checking)*

- `const complex_t * get_const_ptr (size_t i, size_t j) const`  
*Get pointer (with optional range-checking)*
- `int set (size_t i, size_t j, complex_t val)`  
*Set (with optional range-checking)*
- `int set (size_t i, size_t j, data_t re, data_t im)`  
*Set (with optional range-checking)*
- `int set_all (complex_t val)`  
*Set all of the value to be the value val.*
- `size_t rows () const`  
*Method to return number of rows.*
- `size_t cols () const`  
*Method to return number of columns.*

#### Other methods

- `bool is_owner () const`  
*Return true if this object owns the data it refers to.*

#### Arithmetic

- `umatrix_cx_view_tlate< data_t, complex_t > & operator+= (const umatrix_cx_view_tlate< data_t, complex_t > &x)`  
*operator+=*
- `umatrix_cx_view_tlate< data_t, complex_t > & operator-= (const umatrix_cx_view_tlate< data_t, complex_t > &x)`  
*operator-=*
- `umatrix_cx_view_tlate< data_t, complex_t > & operator+= (const data_t &y)`  
*operator+=*
- `umatrix_cx_view_tlate< data_t, complex_t > & operator-= (const data_t &y)`  
*operator-=*
- `umatrix_cx_view_tlate< data_t, complex_t > & operator*= (const data_t &y)`  
*operator\*=*

#### Protected Member Functions

- `umatrix_cx_view_tlate ()`  
*Empty constructor provided for use by umatrix\_cx\_tlate(const umatrix\_cx\_tlate &v)*

#### Protected Attributes

- `data_t * data`  
*The data.*
- `size_t size1`  
*The number of rows.*
- `size_t size2`  
*The number of columns.*
- `int owner`  
*Zero if memory is owned elsewhere, 1 otherwise.*

### 46.367.2 Member Function Documentation

**46.367.2.1** `template<class data_t, class complex_t> size_t umatrix_cx_view_tlate< data_t, complex_t >::rows ( ) const` [inline]

If no memory has been allocated, this will quietly return zero.

Definition at line 259 of file `umatrix_cx_tlate.h`.

**46.367.2.2** `template<class data_t, class complex_t> size_t umatrix_cx_view_tlate< data_t, complex_t >::cols ( ) const` [inline]

If no memory has been allocated, this will quietly return zero.

Definition at line 268 of file `umatrix_cx_tlate.h`.

The documentation for this class was generated from the following file:



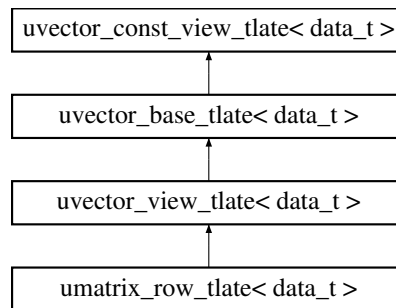
- [umatrix\\_cx\\_tlate.h](#)

## 46.368 `umatrix_row_tlate< data_t >` Class Template Reference

Create a vector from a row of a matrix.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for `umatrix_row_tlate< data_t >`:



### 46.368.1 Detailed Description

```
template<class data_t>class umatrix_row_tlate< data_t >
```

Definition at line 800 of file `umatrix_tlate.h`.

#### Public Member Functions

- [umatrix\\_row\\_tlate](#) ([umatrix\\_base\\_tlate< data\\_t >](#) &m, size\_t i)  
*Create a vector from row i of matrix m.*

The documentation for this class was generated from the following file:

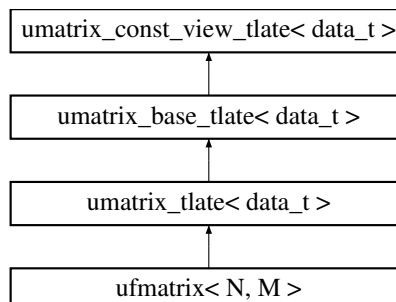
- [umatrix\\_tlate.h](#)

## 46.369 `umatrix_tlate< data_t >` Class Template Reference

A matrix of double-precision numbers.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for `umatrix_tlate< data_t >`:



## 46.369.1 Detailed Description

```
template<class data_t>class umatrix_tlate< data_t >
```

Definition at line 561 of file `umatrix_tlate.h`.

## Public Member Functions

## Standard constructor

- `umatrix_tlate` (`size_t r=0`, `size_t c=0`)  
*Create an umatrix of size `n` with owner as 'true'.*

## Copy constructors

- `umatrix_tlate` (`const umatrix_tlate &v`)  
*Deep copy constructor; allocate new space and make a copy.*
- `umatrix_tlate` (`const umatrix_view_tlate< data_t > &v`)  
*Deep copy constructor; allocate new space and make a copy.*
- `umatrix_tlate & operator=` (`const umatrix_tlate &v`)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `umatrix_tlate & operator=` (`const umatrix_view_tlate< data_t > &v`)  
*Deep copy constructor; if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `umatrix_tlate` (`size_t n`, `uvector_view_tlate< data_t > uva[]`)  
*Deep copy from an array of uvectors.*
- `umatrix_tlate` (`size_t n`, `size_t n2`, `data_t **csa`)  
*Deep copy from a C-style 2-d array.*

## Memory allocation

- `int allocate` (`size_t nrow`s, `size_t ncol`s)  
*Allocate memory after freeing any memory presently in use.*
- `int free` ()  
*Free the memory.*

## Other methods

- `umatrix_tlate< data_t > transpose` ()  
*Compute the transpose (even if matrix is not square)*

## 46.369.2 Member Function Documentation

```
46.369.2.1 template<class data_t> int umatrix_tlate< data_t >::free ( ) [inline]
```

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 770 of file `umatrix_tlate.h`.

The documentation for this class was generated from the following file:

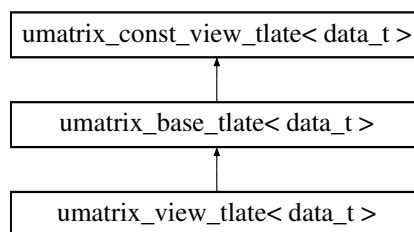
- [umatrix\\_tlate.h](#)

46.370 `umatrix_view_tlate< data_t >` Class Template Reference

A matrix view of double-precision numbers.

```
#include <umatrix_tlate.h>
```

Inheritance diagram for `umatrix_view_tlate< data_t >`:



#### 46.370.1 Detailed Description

`template<class data_t>class umatrix_view_tlate< data_t >`

Definition at line 422 of file `umatrix_tlate.h`.

#### Public Member Functions

##### Copy constructors

- [umatrix\\_view\\_tlate](#) (const [umatrix\\_view\\_tlate](#) &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- [umatrix\\_view\\_tlate](#) & [operator=](#) (const [umatrix\\_view\\_tlate](#) &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- [umatrix\\_view\\_tlate](#) ([umatrix\\_base\\_tlate](#)< data\_t > &v)  
*Shallow copy constructor - create a new view of the same matrix.*
- [umatrix\\_view\\_tlate](#) & [operator=](#) ([umatrix\\_base\\_tlate](#)< data\_t > &v)  
*Shallow copy constructor - create a new view of the same matrix.*

##### Get and set methods

- `data_t * operator\[\] (size_t i) const`  
*Array-like indexing.*
- `data_t & operator\(\) (size_t i, size_t j) const`  
*Array-like indexing.*
- `data_t * get\_ptr (size_t i, size_t j) const`  
*Get pointer (with optional range-checking)*
- `int set (size_t i, size_t j, data_t val) const`  
*Set (with optional range-checking)*
- `int set\_all (double val) const`  
*Set all of the value to be the value val.*

#### Protected Member Functions

- [umatrix\\_view\\_tlate](#) ()  
*Empty constructor.*

The documentation for this class was generated from the following file:

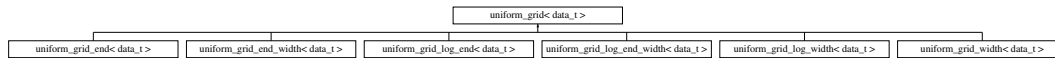
- [umatrix\\_tlate.h](#)

## 46.371 `uniform_grid< data_t >` Class Template Reference

A class representing a uniform linear or logarithmic grid.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid< data_t >`:



### 46.371.1 Detailed Description

`template<class data_t = double>class uniform_grid< data_t >`

#### Note

This class has no public constructors and is to be instantiated through its children.

Definition at line 37 of file `uniform_grid.h`.

#### Public Member Functions

- `size_t get_nbins ()`  
*Get the number of bins (regions in between grid points)*
- `size_t get_npoints ()`  
*Get the number of points in the grid (always `get_nbins()+1`)*
- `bool is_log ()`  
*Return true if the grid is logarithmic.*
- `template<class vec_t >`  
`void vector (vec_t &v)`  
*Fill a vector with the specified grid.*
- `const data_t operator[] (size_t i) const`  
*Get the grid point with index  $i$  ( $i \in [0, n_{bins}]$ )*

#### Protected Member Functions

- `uniform_grid (data_t start, data_t end, data_t width, size_t n_bins, bool log=false)`  
*Construct a grid with specified values.*

#### Protected Attributes

- `data_t g_start`  
*The low-side of the first bin.*
- `data_t g_end`  
*The high-side of the last bin.*
- `data_t g_width`  
*The width of each bin.*
- `size_t g_n_bins`  
*The number of bins.*
- `bool g_log`  
*If true, use a logarithmic scale.*

### 46.371.2 Constructor & Destructor Documentation

46.371.2.1 `template<class data_t = double> uniform_grid< data_t >::uniform_grid ( data_t start, data_t end, data_t width, size_t n_bins, bool log = false ) [inline, protected]`

## Note

This function is not public because it might create grids that are non-sensical. We require users to create grid objects using one of the children which don't allow non-sensical grids.

Definition at line 64 of file `uniform_grid.h`.

The documentation for this class was generated from the following file:

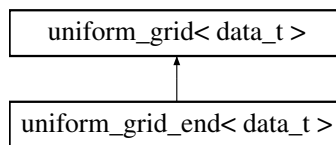
- `uniform_grid.h`

## 46.372 `uniform_grid_end< data_t >` Class Template Reference

Linear grid with fixed number of bins and fixed endpoint.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid_end< data_t >`:



### 46.372.1 Detailed Description

```
template<class data_t = double>class uniform_grid_end< data_t >
```

Definition at line 159 of file `uniform_grid.h`.

#### Public Member Functions

- **`uniform_grid_end`** (`data_t` start, `data_t` end, `size_t` n\_bins)

The documentation for this class was generated from the following file:

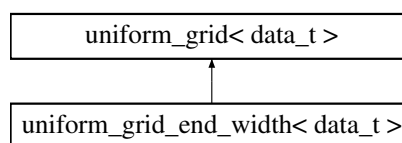
- `uniform_grid.h`

## 46.373 `uniform_grid_end_width< data_t >` Class Template Reference

Linear grid with fixed endpoint and fixed bin size.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid_end_width< data_t >`:



## 46.373.1 Detailed Description

```
template<class data_t = double>class uniform_grid_end_width< data_t >
```

Definition at line 180 of file `uniform_grid.h`.

## Public Member Functions

- **`uniform_grid_end_width`** (`data_t` start, `data_t` end, `data_t` width)

The documentation for this class was generated from the following file:

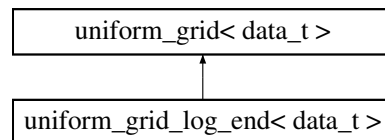
- `uniform_grid.h`

46.374 `uniform_grid_log_end< data_t >` Class Template Reference

Logarithmic grid with fixed number of bins and fixed endpoint.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid_log_end< data_t >`:



## 46.374.1 Detailed Description

```
template<class data_t = double>class uniform_grid_log_end< data_t >
```

Definition at line 191 of file `uniform_grid.h`.

## Public Member Functions

- **`uniform_grid_log_end`** (`data_t` start, `data_t` end, `size_t` n\_bins)

The documentation for this class was generated from the following file:

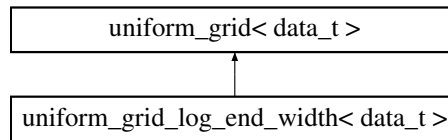
- `uniform_grid.h`

46.375 `uniform_grid_log_end_width< data_t >` Class Template Reference

Logarithmic grid with fixed endpoint and fixed bin size.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid_log_end_width< data_t >`:



#### 46.375.1 Detailed Description

```
template<class data_t = double>class uniform_grid_log_end_width< data_t >
```

Definition at line 213 of file `uniform_grid.h`.

#### Public Member Functions

- **`uniform_grid_log_end_width`** (`data_t` start, `data_t` end, `data_t` width)

The documentation for this class was generated from the following file:

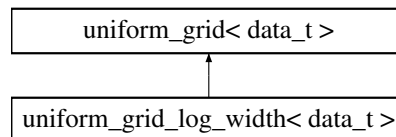
- `uniform_grid.h`

### 46.376 `uniform_grid_log_width< data_t >` Class Template Reference

Logarithmic grid with fixed number of bins and fixed bin size.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid_log_width< data_t >`:



#### 46.376.1 Detailed Description

```
template<class data_t = double>class uniform_grid_log_width< data_t >
```

Definition at line 202 of file `uniform_grid.h`.

#### Public Member Functions

- **`uniform_grid_log_width`** (`data_t` start, `data_t` width, `size_t` n\_bins)

The documentation for this class was generated from the following file:

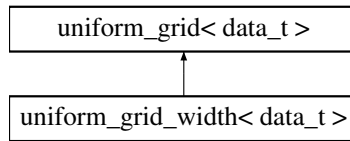
- `uniform_grid.h`

## 46.377 `uniform_grid_width< data_t >` Class Template Reference

Linear grid with fixed number of bins and fixed bin size.

```
#include <uniform_grid.h>
```

Inheritance diagram for `uniform_grid_width< data_t >`:



### 46.377.1 Detailed Description

```
template<class data_t = double>class uniform_grid_width< data_t >
```

Definition at line 170 of file `uniform_grid.h`.

#### Public Member Functions

- **`uniform_grid_width`** (`data_t` start, `data_t` width, `size_t` n\_bins)

The documentation for this class was generated from the following file:

- `uniform_grid.h`

## 46.378 `convert_units::unit_t` Struct Reference

The type for caching unit conversions.

```
#include <convert_units.h>
```

### 46.378.1 Detailed Description

Definition at line 85 of file `convert_units.h`.

#### Data Fields

- `std::string` **`f`**  
*The input unit.*
- `std::string` **`t`**  
*The output unit.*
- `double` **`c`**  
*The conversion factor.*

The documentation for this struct was generated from the following file:

- `convert_units.h`



## 46.379 o2scl\_linalg::uvector\_2\_mem Class Reference

Allocation object for 2 arrays of equal size.

```
#include <tridiag_base.h>
```

### 46.379.1 Detailed Description

This class is used in [solve\\_tridiag\\_nonsym\(\)](#).

Definition at line 131 of file tridiag\_base.h.

#### Public Member Functions

- void **allocate** (size\_t n)
- void **free** ()

#### Data Fields

- [o2scl::uvector](#) **v1**
- [o2scl::uvector](#) **v2**

The documentation for this class was generated from the following file:

- [tridiag\\_base.h](#)

## 46.380 o2scl\_linalg::uvector\_4\_mem Class Reference

Allocation object for 4 arrays of equal size.

```
#include <tridiag_base.h>
```

### 46.380.1 Detailed Description

This class is used in [solve\\_tridiag\\_sym\(\)](#) and [solve\\_cyc\\_tridiag\\_nonsym\(\)](#).

Definition at line 149 of file tridiag\_base.h.

#### Public Member Functions

- void **allocate** (size\_t n)
- void **free** ()

#### Data Fields

- [o2scl::uvector](#) **v1**
- [o2scl::uvector](#) **v2**
- [o2scl::uvector](#) **v3**
- [o2scl::uvector](#) **v4**

The documentation for this class was generated from the following file:

- [tridiag\\_base.h](#)
-

## 46.381 o2scl\_linalg::uvector\_5\_mem Class Reference

Allocation object for 5 arrays of equal size.

```
#include <tridiag_base.h>
```

### 46.381.1 Detailed Description

This class is used in [solve\\_cyc\\_tridiag\\_sym\(\)](#).

Definition at line 170 of file tridiag\_base.h.

#### Public Member Functions

- void **allocate** (size\_t n)
- void **free** ()

#### Data Fields

- [o2scl::uvector](#) **v1**
- [o2scl::uvector](#) **v2**
- [o2scl::uvector](#) **v3**
- [o2scl::uvector](#) **v4**
- [o2scl::uvector](#) **v5**

The documentation for this class was generated from the following file:

- [tridiag\\_base.h](#)

## 46.382 uvector\_alloc Class Reference

A simple class to provide an [allocate\(\)](#) function for [uvector](#).

```
#include <uvector_tlate.h>
```

### 46.382.1 Detailed Description

Definition at line 1020 of file uvector\_tlate.h.

#### Public Member Functions

- void [allocate](#) ([uvector](#) &o, size\_t i)  
*Allocate v for i elements.*
- void [free](#) ([uvector](#) &o)  
*Free memory.*

The documentation for this class was generated from the following file:

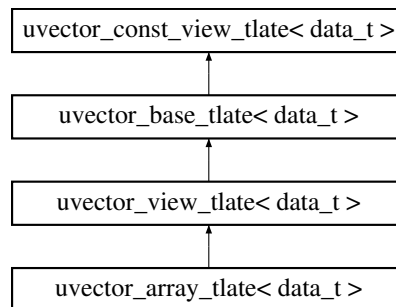
- [uvector\\_tlate.h](#)
-

**46.383 `uvector_array_tlate< data_t >` Class Template Reference**

Create a vector from an array.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_array_tlate< data_t >`:

**46.383.1 Detailed Description**

```
template<class data_t>class uvector_array_tlate< data_t >
```

Definition at line 872 of file `uvector_tlate.h`.

**Public Member Functions**

- [`uvector\_array\_tlate`](#) (`size_t n`, `data_t *dat`)  
*Create a vector from `dat` with size `n`.*

The documentation for this class was generated from the following file:

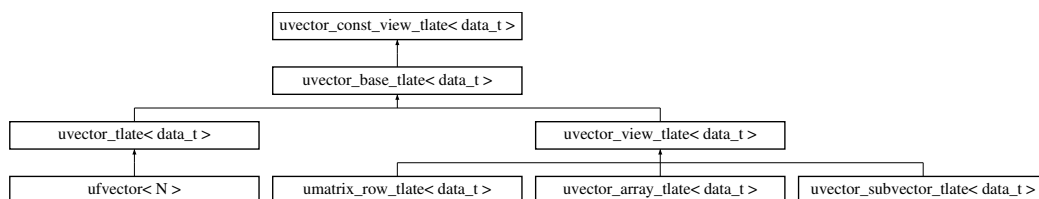
- [`uvector\_tlate.h`](#)

**46.384 `uvector_base_tlate< data_t >` Class Template Reference**

A base class for `uvector` and `uvector_view`.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_base_tlate< data_t >`:

**46.384.1 Detailed Description**

```
template<class data_t>class uvector_base_tlate< data_t >
```

This class provides a base class for `uvector` and `uvector_view`, mostly useful for creating function arguments which accept either `uvector` or `uvector_view`.

Definition at line 286 of file `uvector_tlate.h`.

## Public Member Functions

### Copy constructors

- `uvector_base_tlate` (`uvector_base_tlate` &`v`)  
*Copy constructor - create a new view of the same vector.*
- `uvector_base_tlate` & `operator=` (`uvector_base_tlate` &`v`)  
*Copy constructor - create a new view of the same vector.*

### Get and set methods

- `data_t` & `operator[]` (`size_t` `i`)  
*Array-like indexing.*
- `const data_t` & `operator[]` (`size_t` `i`) `const`  
*Array-like indexing.*
- `data_t` & `operator()` (`size_t` `i`)  
*Array-like indexing.*
- `const data_t` & `operator()` (`size_t` `i`) `const`  
*Array-like indexing.*
- `data_t` \* `get_ptr` (`size_t` `i`)  
*Get pointer (with optional range-checking)*
- `int` `set` (`size_t` `i`, `data_t` `val`)  
*Set (with optional range-checking)*
- `int` `set_all` (`data_t` `val`)  
*Set all of the value to be the value `val`.*

### Arithmetic

- `uvector_base_tlate< data_t >` & `operator+=` (`const uvector_base_tlate< data_t >` &`x`)  
*operator+=*
- `uvector_base_tlate< data_t >` & `operator-=` (`const uvector_base_tlate< data_t >` &`x`)  
*operator-=*
- `uvector_base_tlate< data_t >` & `operator+=` (`const data_t` &`y`)  
*operator+=*
- `uvector_base_tlate< data_t >` & `operator-=` (`const data_t` &`y`)  
*operator-=*
- `uvector_base_tlate< data_t >` & `operator*=` (`const data_t` &`y`)  
*operator\*=*

## Protected Member Functions

- `uvector_base_tlate` ()  
*Empty constructor for use by children.*

## 46.384.2 Constructor & Destructor Documentation

46.384.2.1 `template<class data_t> uvector_base_tlate< data_t >::uvector_base_tlate ( )` [`inline`, `protected`]

Definition at line 473 of file `uvector_tlate.h`.

The documentation for this class was generated from the following file:

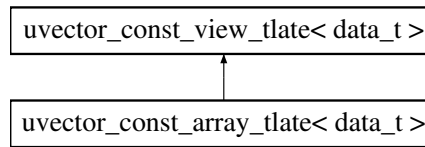
- `uvector_tlate.h`

**46.385 `uvector_const_array_tlate< data_t >` Class Template Reference**

Create a vector from an const array.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_const_array_tlate< data_t >`:

**46.385.1 Detailed Description**

```
template<class data_t>class uvector_const_array_tlate< data_t >
```

Definition at line 906 of file `uvector_tlate.h`.

**Public Member Functions**

- [`uvector\_const\_array\_tlate`](#) (`size_t n`, `const data_t *dat`)  
Create a vector from *dat* with size *n*.

The documentation for this class was generated from the following file:

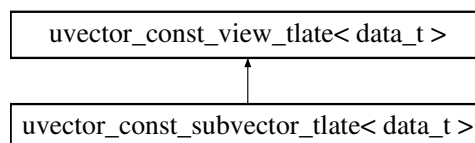
- [uvector\\_tlate.h](#)

**46.386 `uvector_const_subvector_tlate< data_t >` Class Template Reference**

Create a const vector from a subvector of another vector.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_const_subvector_tlate< data_t >`:

**46.386.1 Detailed Description**

```
template<class data_t>class uvector_const_subvector_tlate< data_t >
```

Definition at line 926 of file `uvector_tlate.h`.

**Public Member Functions**

- [`uvector\_const\_subvector\_tlate`](#) (`const uvector_base_tlate< data_t > &orig`, `size_t offset`, `size_t n`)

Create a vector from *orig*.

The documentation for this class was generated from the following file:

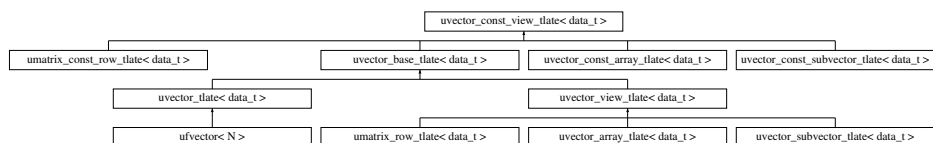
- [uvector\\_tlate.h](#)

## 46.387 `uvector_const_view_tlate< data_t >` Class Template Reference

A const vector view with unit stride.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_const_view_tlate< data_t >`:



### 46.387.1 Detailed Description

```
template<class data_t>class uvector_const_view_tlate< data_t >
```

**Idea for Future** Could allow user-defined specification of restrict keyword

Definition at line 64 of file `uvector_tlate.h`.

#### Public Member Functions

- `data_t norm () const`  
*Norm.*

#### Copy constructors

- `uvector_const_view_tlate (const uvector_const_view_tlate &v)`  
*Copy constructor - create a new view of the same vector.*
- `uvector_const_view_tlate & operator= (const uvector_const_view_tlate &v)`  
*Copy constructor - create a new view of the same vector.*

#### Get and set methods

- `const data_t & operator[] (size_t i) const`  
*Array-like indexing.*
- `const data_t & operator() (size_t i) const`  
*Array-like indexing.*
- `data_t get (size_t i) const`  
*Get (with optional range-checking)*
- `const data_t * get_const_ptr (size_t i) const`  
*Get pointer (with optional range-checking)*
- `size_t size () const`  
*Method to return vector size.*

## Other methods

- `bool is_owner () const`  
*Return true if this object owns the data it refers to.*
- `size_t lookup (const data_t x0) const`  
*Exhaustively look through the array for a particular value.*
- `data_t max () const`  
*Find the maximum element.*
- `data_t min () const`  
*Find the minimum element.*

## Protected Member Functions

- `uvector_const_view_tlate ()`  
*Empty constructor provided for use by `uvector_tlate(const uvector_tlate &v)`*

## Protected Attributes

- `data_t * data`  
*The data.*
- `size_t sz`  
*The vector sz.*
- `int owner`  
*Zero if memory is owned elsewhere, 1 otherwise.*

## Friends

- class `uvector_base_tlate< data_t >`
- class `uvector_view_tlate< data_t >`
- class `uvector_tlate< data_t >`
- class `uvector_subvector_tlate< data_t >`
- class `uvector_const_subvector_tlate< data_t >`

## 46.387.2 Member Function Documentation

46.387.2.1 `template<class data_t> size_t uvector_const_view_tlate< data_t >::size ( ) const [inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 176 of file `uvector_tlate.h`.

46.387.2.2 `template<class data_t> size_t uvector_const_view_tlate< data_t >::lookup ( const data_t x0 ) const [inline]`

This can only fail if *all* of the entries in the array are not finite, in which case it calls `O2SCL_ERR()` and returns 0.

If more than one entry is the same distance from `x0`, this function returns the entry with smallest index.

Definition at line 200 of file `uvector_tlate.h`.

46.387.2.3 `template<class data_t> data_t uvector_const_view_tlate< data_t >::norm ( ) const [inline]`

**Todo** Fix this so that `norm()` is computed as in `ovector` and so that integer norms are performed separately.

Definition at line 259 of file `uvector_tlate.h`.

The documentation for this class was generated from the following file:

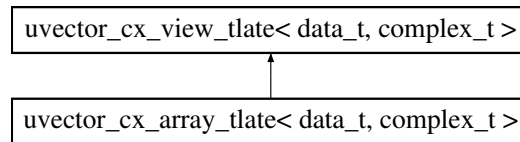
- `uvector_tlate.h`

**46.388 `uvector_cx_array_tlate< data_t, complex_t >` Class Template Reference**

Create a vector from an array.

```
#include <uvector_cx_tlate.h>
```

Inheritance diagram for `uvector_cx_array_tlate< data_t, complex_t >`:

**46.388.1 Detailed Description**

```
template<class data_t, class complex_t>class uvector_cx_array_tlate< data_t, complex_t >
```

Definition at line 488 of file `uvector_cx_tlate.h`.

**Public Member Functions**

- [`uvector\_cx\_array\_tlate`](#) (`size_t n`, `data_t *dat`)  
*Create a vector from `dat` with size `n`.*

The documentation for this class was generated from the following file:

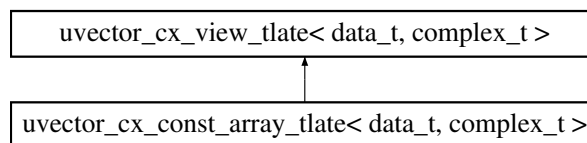
- [`uvector\_cx\_tlate.h`](#)

**46.389 `uvector_cx_const_array_tlate< data_t, complex_t >` Class Template Reference**

Create a vector from an array.

```
#include <uvector_cx_tlate.h>
```

Inheritance diagram for `uvector_cx_const_array_tlate< data_t, complex_t >`:

**46.389.1 Detailed Description**

```
template<class data_t, class complex_t>class uvector_cx_const_array_tlate< data_t, complex_t >
```

Definition at line 522 of file `uvector_cx_tlate.h`.

**Public Member Functions**

- [`uvector\_cx\_const\_array\_tlate`](#) (`size_t n`, `const data_t *dat`)  
*Create a vector from `dat` with size `n`.*



## Protected Member Functions

These are inaccessible to ensure the vector is `\c const`.

- `data_t & operator[]` (`size_t i`)  
*Array-like indexing.*
- `data_t & operator()` (`size_t i`)  
*Array-like indexing.*
- `data_t * get_ptr` (`size_t i`)  
*Get pointer (with optional range-checking)*
- `int set` (`size_t i`, `data_t val`)
- `int set_all` (`double val`)
- `uvector_cx_view_tlate< data_t, complex_t > & operator+=` (`const uvector_cx_view_tlate< data_t, complex_t > &x`)  
*operator+=*
- `uvector_cx_view_tlate< data_t, complex_t > & operator-=` (`const uvector_cx_view_tlate< data_t, complex_t > &x`)  
*operator-=*
- `uvector_cx_view_tlate< data_t, complex_t > & operator*=` (`const data_t &y`)  
*operator\*=*

The documentation for this class was generated from the following file:

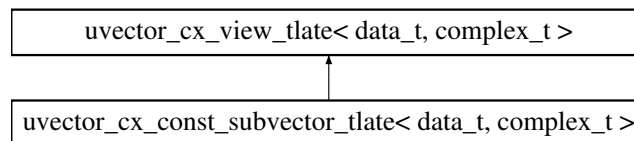
- [uvector\\_cx\\_tlate.h](#)

46.390 `uvector_cx_const_subvector_tlate< data_t, complex_t >` Class Template Reference

Create a vector from a subvector of another.

```
#include <uvector_cx_tlate.h>
```

Inheritance diagram for `uvector_cx_const_subvector_tlate< data_t, complex_t >`:



## 46.390.1 Detailed Description

```
template<class data_t, class complex_t>class uvector_cx_const_subvector_tlate< data_t, complex_t >
```

Definition at line 570 of file `uvector_cx_tlate.h`.

## Public Member Functions

- `uvector_cx_const_subvector_tlate` (`const uvector_cx_view_tlate< data_t, complex_t > &orig`, `size_t offset`, `size_t n`)  
*Create a vector from orig.*

The documentation for this class was generated from the following file:

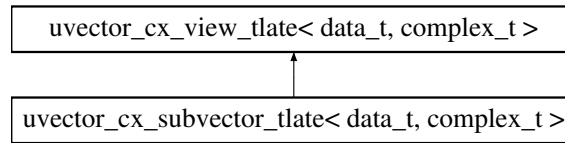
- [uvector\\_cx\\_tlate.h](#)

**46.391 `uvector_cx_subvector_tlate< data_t, complex_t >` Class Template Reference**

Create a vector from a subvector of another.

```
#include <uvector_cx_tlate.h>
```

Inheritance diagram for `uvector_cx_subvector_tlate< data_t, complex_t >`:

**46.391.1 Detailed Description**

```
template<class data_t, class complex_t>class uvector_cx_subvector_tlate< data_t, complex_t >
```

Definition at line 503 of file `uvector_cx_tlate.h`.

**Public Member Functions**

- [uvector\\_cx\\_subvector\\_tlate](#) ([uvector\\_cx\\_view\\_tlate< data\\_t, complex\\_t >](#) &orig, size\_t offset, size\_t n)  
*Create a vector from orig.*

The documentation for this class was generated from the following file:

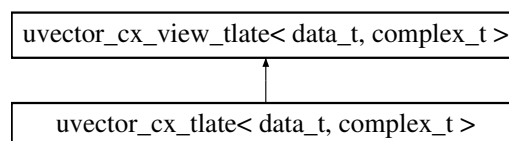
- [uvector\\_cx\\_tlate.h](#)

**46.392 `uvector_cx_tlate< data_t, complex_t >` Class Template Reference**

A vector of double-precision numbers with unit stride.

```
#include <uvector_cx_tlate.h>
```

Inheritance diagram for `uvector_cx_tlate< data_t, complex_t >`:

**46.392.1 Detailed Description**

```
template<class data_t, class complex_t>class uvector_cx_tlate< data_t, complex_t >
```

There is also an `<<` operator for this class documented "Functions" section of [uvector\\_tlate.h](#).

Definition at line 313 of file `uvector_cx_tlate.h`.

## Public Member Functions

## Standard constructor

- `uvector_cx_tlate` (size\_t n=0)  
Create an `uvector_cx` of size `n` with owner as 'true'.

## Copy constructors

- `uvector_cx_tlate` (const `uvector_cx_tlate` &v)  
Deep copy constructor - allocate new space and make a copy.
- `uvector_cx_tlate` (const `uvector_cx_view_tlate< data_t, complex_t >` &v)  
Deep copy constructor - allocate new space and make a copy.
- `uvector_cx_tlate & operator=` (const `uvector_cx_tlate` &v)  
Deep copy constructor - if owner is true, allocate space and make a new copy, otherwise, just copy into the view.
- `uvector_cx_tlate & operator=` (const `uvector_cx_view_tlate< data_t, complex_t >` &v)  
Deep copy constructor - if owner is true, allocate space and make a new copy, otherwise, just copy into the view.

## Memory allocation

- int `allocate` (size\_t nsize)  
Allocate memory for size `n` after freeing any memory presently in use.
- int `free` ()  
Free the memory.

## 46.392.2 Member Function Documentation

46.392.2.1 `template<class data_t, class complex_t> int uvector_cx_tlate< data_t, complex_t >::free ( ) [inline]`

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 473 of file `uvector_cx_tlate.h`.

The documentation for this class was generated from the following file:

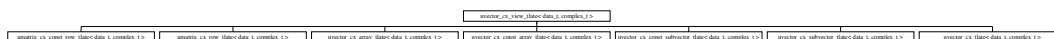
- [uvector\\_cx\\_tlate.h](#)

46.393 `uvector_cx_view_tlate< data_t, complex_t >` Class Template Reference

A vector view of complex numbers with unit stride.

```
#include <uvector_cx_tlate.h>
```

Inheritance diagram for `uvector_cx_view_tlate< data_t, complex_t >`:



## 46.393.1 Detailed Description

```
template<class data_t, class complex_t> class uvector_cx_view_tlate< data_t, complex_t >
```

**Idea for Future** Write `lookup()` method, and possibly an `erase()` method.

Definition at line 47 of file `uvector_cx_tlate.h`.

## Public Member Functions

## Copy constructors

- `uvector_cx_view_tlate` (const `uvector_cx_view_tlate` &*v*)  
*Copy constructor - create a new view of the same vector.*
- `uvector_cx_view_tlate` & `operator=` (const `uvector_cx_view_tlate` &*v*)  
*Copy constructor - create a new view of the same vector.*

## Get and set methods

- `complex_t` & `operator[]` (size\_t *i*)  
*Array-like indexing.*
- const `complex_t` & `operator[]` (size\_t *i*) const  
*Array-like indexing.*
- `complex_t` & `operator()` (size\_t *i*)  
*Array-like indexing.*
- const `complex_t` & `operator()` (size\_t *i*) const  
*Array-like indexing.*
- `complex_t` `get` (size\_t *i*) const  
*Get (with optional range-checking)*
- `complex_t` \* `get_ptr` (size\_t *i*)  
*Get pointer (with optional range-checking)*
- const `complex_t` \* `get_const_ptr` (size\_t *i*) const  
*Get pointer (with optional range-checking)*
- int `set` (size\_t *i*, const `complex_t` &*val*)  
*Set (with optional range-checking)*
- int `set_all` (const `complex_t` &*val*)  
*Set all of the value to be the value val.*
- size\_t `size` () const  
*Method to return vector size.*

## Other methods

- bool `is_owner` () const  
*Return true if this object owns the data it refers to.*

## Arithmetic

- `uvector_cx_view_tlate< data_t, complex_t >` & `operator+=` (const `uvector_cx_view_tlate< data_t, complex_t >` &*x*)  
*operator+=*
- `uvector_cx_view_tlate< data_t, complex_t >` & `operator-=` (const `uvector_cx_view_tlate< data_t, complex_t >` &*x*)  
*operator-=*
- `uvector_cx_view_tlate< data_t, complex_t >` & `operator+=` (const `data_t` &*y*)  
*operator+=*
- `uvector_cx_view_tlate< data_t, complex_t >` & `operator-=` (const `data_t` &*y*)  
*operator-=*
- `uvector_cx_view_tlate< data_t, complex_t >` & `operator*=` (const `data_t` &*y*)  
*operator\*=*
- `data_t` `norm` () const  
*Norm.*

## Protected Member Functions

- `uvector_cx_view_tlate` ()  
*Empty constructor provided for use by `uvector_cx_tlate(const uvector_cx_tlate &v)`*

## Protected Attributes

- `data_t` \* `data`  
*The data.*
- size\_t `sz`  
*The vector sz.*
- int `owner`  
*Zero if memory is owned elsewhere, 1 otherwise.*

## 46.393.2 Member Function Documentation

46.393.2.1 `template<class data_t, class complex_t> size_t uvector_cx_view_tlate< data_t, complex_t >::size ( ) const` `[inline]`

If no memory has been allocated, this will quietly return zero.

Definition at line 228 of file `uvector_cx_tlate.h`.

The documentation for this class was generated from the following file:

- [uvector\\_cx\\_tlate.h](#)

46.394 `uvector_int_alloc` Class Reference

A simple class to provide an `allocate()` function for `uvector_int`.

```
#include <uvector_tlate.h>
```

## 46.394.1 Detailed Description

Definition at line 1031 of file `uvector_tlate.h`.

## Public Member Functions

- void `allocate` (`uvector_int` &o, size\_t i)  
*Allocate v for i elements.*
- void `free` (`uvector_int` &o)  
*Free memory.*

The documentation for this class was generated from the following file:

- [uvector\\_tlate.h](#)

46.395 `uvector_size_t_alloc` Class Reference

A simple class to provide an `allocate()` function for `uvector_size_t`.

```
#include <uvector_tlate.h>
```

## 46.395.1 Detailed Description

Definition at line 1042 of file `uvector_tlate.h`.

## Public Member Functions

- void `allocate` (`uvector_size_t` &o, size\_t i)  
*Allocate v for i elements.*
- void `free` (`uvector_size_t` &o)  
*Free memory.*

The documentation for this class was generated from the following file:

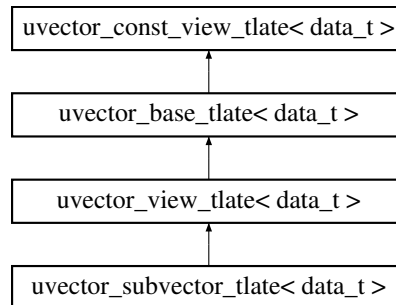
- [uvector\\_tlate.h](#)

**46.396 `uvector_subvector_tlate< data_t >` Class Template Reference**

Create a vector from a subvector of another.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_subvector_tlate< data_t >`:

**46.396.1 Detailed Description**

```
template<class data_t>class uvector_subvector_tlate< data_t >
```

Definition at line 887 of file `uvector_tlate.h`.

**Public Member Functions**

- [`uvector\_subvector\_tlate`](#) ([`uvector\_base\_tlate< data\_t >`](#) &orig, `size_t` offset, `size_t` n)  
*Create a vector from orig.*

The documentation for this class was generated from the following file:

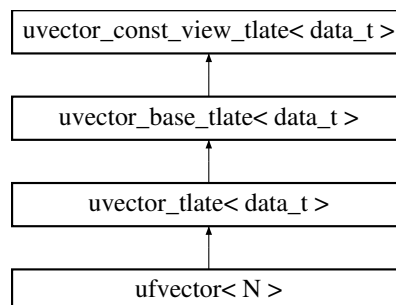
- [`uvector\_tlate.h`](#)

**46.397 `uvector_tlate< data_t >` Class Template Reference**

A vector with unit stride.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_tlate< data_t >`:



## 46.397.1 Detailed Description

```
template<class data_t>class uvector_tlate< data_t >
```

There are several useful methods which are defined in the parent class, [uvector\\_view\\_tlate](#) . There is also an `<<` operator for this class documented "Functions" section of [uvector\\_tlate.h](#).

Definition at line 621 of file `uvector_tlate.h`.

## Public Member Functions

- `int sort_unique ()`  
*Sort the vector and ensure all elements are unique by removing duplicates.*

## Standard constructor

- `uvector_tlate (size_t n=0)`  
*Create an uvector of size `n` with owner as 'true'.*

## Copy constructors

- `uvector_tlate (const uvector_tlate &v)`  
*Deep copy constructor - allocate new space and make a copy.*
- `uvector_tlate (const uvector_const_view_tlate< data_t > &v)`  
*Deep copy constructor - allocate new space and make a copy.*
- `uvector_tlate & operator= (const uvector_tlate &v)`  
*Deep copy constructor - if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*
- `uvector_tlate & operator= (const uvector_const_view_tlate< data_t > &v)`  
*Deep copy constructor - if owner is true, allocate space and make a new copy, otherwise, just copy into the view.*

## Memory allocation

- `int allocate (size_t nsize)`  
*Allocate memory for size `n` after freeing any memory presently in use.*
- `int free ()`  
*Free the memory.*

## Other methods

- `int erase (size_t ix)`  
*Erase an element from the array.*

## Friends

- `class uvector_view_tlate< data_t >`

## 46.397.2 Member Function Documentation

46.397.2.1 `template<class data_t> int uvector_tlate< data_t >::allocate ( size_t nsize ) [inline]`

If `nsize` is zero, this only frees the memory and allocates no additional memory.

Definition at line 784 of file `uvector_tlate.h`.

46.397.2.2 `template<class data_t> int uvector_tlate< data_t >::free ( ) [inline]`

This function will safely do nothing if used without first allocating memory or if called multiple times in succession.

Definition at line 805 of file `uvector_tlate.h`.

The documentation for this class was generated from the following file:

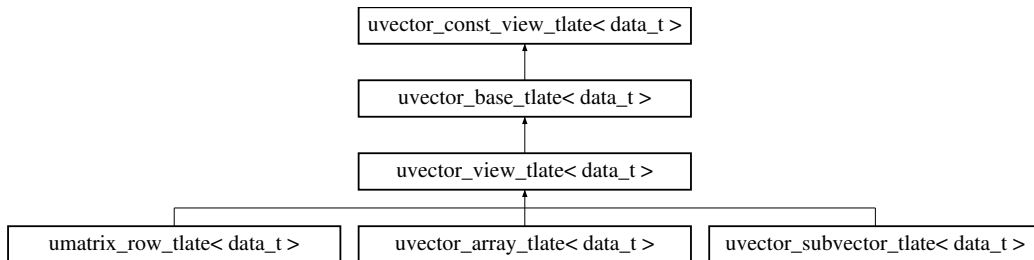
- [uvector\\_tlate.h](#)

46.398 `uvector_view_tlate< data_t >` Class Template Reference

A base class for uvectors.

```
#include <uvector_tlate.h>
```

Inheritance diagram for `uvector_view_tlate< data_t >`:



## 46.398.1 Detailed Description

```
template<class data_t>class uvector_view_tlate< data_t >
```

Definition at line 485 of file `uvector_tlate.h`.

## Public Member Functions

## Copy constructors

- `uvector_view_tlate` (const `uvector_view_tlate` &*v*)  
*Copy constructor - create a new view of the same vector.*
- `uvector_view_tlate` & `operator=` (const `uvector_view_tlate` &*v*)  
*Copy constructor - create a new view of the same vector.*
- `uvector_view_tlate` (`uvector_base_tlate`< *data\_t* > &*v*)  
*Copy constructor - create a new view of the same vector.*
- `uvector_view_tlate` & `operator=` (`uvector_base_tlate`< *data\_t* > &*v*)  
*Copy constructor - create a new view of the same vector.*

## Get and set methods

- *data\_t* & `operator[]` (size\_t *i*) const  
*Array-like indexing.*
- *data\_t* & `operator()` (size\_t *i*) const  
*Array-like indexing.*
- *data\_t* \* `get_ptr` (size\_t *i*) const  
*Get pointer (with optional range-checking)*
- int `set` (size\_t *i*, *data\_t* *val*) const  
*Set (with optional range-checking)*
- int `set_all` (*data\_t* *val*) const  
*Set all of the value to be the value val.*

## Protected Member Functions

- `uvector_view_tlate` ()  
*Empty constructor provided for use by `uvector_view_tlate(const uvector_view_tlate &v)`*

The documentation for this class was generated from the following file:

- `uvector_tlate.h`

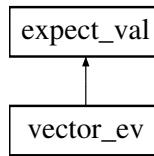


**46.399 vector\_ev Class Reference**

Vector expectation value.

```
#include <expect_val.h>
```

Inheritance diagram for `vector_ev`:

**46.399.1 Detailed Description**

See [expect\\_val](#) for some general notes on this and related classes.

This class is experimental.

This is similar to [scalar\\_ev](#), except that it allows updating and statistics for a set of scalars en masse. The data is stored internally in [uvector](#) and [umatrix](#) objects, but the public member functions operate with template types which are compatible with any vector class which provides `double &operator[]`.

Internally, data is stored in matrices designating the first (row) index as the user-specified vector index and designating the second (column) index as the block index.

Definition at line 325 of file `expect_val.h`.

**Public Member Functions**

- [vector\\_ev](#) (size\_t n)  
*Create for a vector of size n with no blocking.*
- [vector\\_ev](#) (size\_t n, size\_t n\_blocks, size\_t n\_per\_block)  
*Create for a vector of size n with n\_blocks blocks and n\_per\_block points block.*
- virtual void [set\\_blocks](#) (size\_t n, size\_t n\_blocks, size\_t n\_per\_block)  
*Set for a vector of size n with n\_blocks blocks and n\_per\_block points block.*
- [vector\\_ev](#) (const [vector\\_ev](#) &ev)  
*Copy constructor.*
- [vector\\_ev](#) & [operator=](#) (const [vector\\_ev](#) &ev)  
*Copy constructor.*
- virtual void [free](#) ()  
*Free allocated data.*
- virtual void [reset](#) ()  
*Clear all the data.*
- template<class vec\_t >  
void [add](#) (vec\_t &v)  
*Add measurement of value val.*

**Report statistics**

- template<class vec\_t, class vec2\_t, class vec3\_t >  
void [current\\_avg\\_stats](#) (vec\_t &avg, vec2\_t &std\_dev, vec3\_t &avg\_err, size\_t &m\_block, size\_t &m\_per\_block) const  
*Report current average, standard deviation, and the error in the average and include block information.*
- template<class vec\_t, class vec2\_t, class vec3\_t >  
void [current\\_avg](#) (vec\_t &avg, vec2\_t &std\_dev, vec3\_t &avg\_err) const  
*Report current average, standard deviation, and the error in the average.*
- template<class vec\_t, class vec2\_t, class vec3\_t >  
void [reblock\\_avg\\_stats](#) (size\_t new\_blocks, vec\_t &avg, vec2\_t &std\_dev, vec3\_t &avg\_err, size\_t &m\_per\_block) const

*Report average, standard deviation, and the error in the average assuming a new block size.*

- `template<class vec_t, class vec2_t, class vec3_t >`

`void reblock_avg (size_t new_blocks, vec_t &avg, vec2_t &std_dev, vec3_t &avg_err) const`

*Report average, standard deviation, and the error in the average assuming a new block size.*

#### Protected Attributes

- `umatrix last`  
*The most recent values for each block.*
- `umatrix vals`  
*The average for each block.*
- `uvector current`  
*The current rolling average.*
- `size_t nvec`  
*The size of the vector.*

The documentation for this class was generated from the following file:

- `expect_val.h`

## 46.400 xmatrix Class Reference

A version of `omatrix` with better error checking.

```
#include <omatrix_tlate.h>
```

Inherits `omatrix_tlate< double, gsl_matrix, gsl_vector_norm, gsl_block >`.

### 46.400.1 Detailed Description

This demonstrates how `operator[]` could return an `ovector_array` object and thus provide more bounds-checking. This would demand including a new parameter in `omatrix_view_tlate` which contains the vector type.

Definition at line 1352 of file `omatrix_tlate.h`.

#### Public Member Functions

- `xmatrix (size_t r=0, size_t c=0)`
- `ovector_array operator[] (size_t i)`  
*Array-like indexing.*
- `const ovector_const_array operator[] (size_t i) const`  
*Array-like indexing.*

The documentation for this class was generated from the following file:

- `omatrix_tlate.h`

## 47 File Documentation

### 47.1 array.h File Reference

Various array classes.

```
#include <iostream> #include <cmath> #include <string> #include <fstream> #include <sstream> ×
#include <vector> #include <map> #include <o2scl/err_hnd.h> #include <gsl/gsl_ieee_utils.-
h> #include <gsl/gsl_sort.h>
```

### 47.1.1 Detailed Description

For a more general discussion of vectors and matrices in O<sub>2</sub>scl , see the [Arrays, Vectors, Matrices and Tensors](#) of the User's Guide.

This file contains classes and functions for operating with C-style 1- or 2-dimensional arrays and pointers to double. For an example of the usage of the array allocation classes, see the [Multi-dimensional solver](#) . For more generic operations on generic vector objects (including in some cases C-style arrays), see also the file [vector.h](#) .

This file contains the allocation classes

- [array\\_alloc](#)
- [array\\_2d\\_alloc](#)
- [pointer\\_alloc](#)
- [pointer\\_2d\\_alloc](#)

the classes for the manipulation of arrays in [smart\\_interp](#)

- [array\\_reverse](#)
- [array\\_subvector](#)
- [array\\_subvector\\_reverse](#)
- [array\\_const\\_reverse](#)
- [array\\_const\\_subvector](#)
- [array\\_const\\_subvector\\_reverse](#)

the array equivalent of `omatrix_row` and `omatrix_col` (see usage in `src/ode/ode_it_solve_ts.cpp`)

- [array\\_2d\\_row](#)
- [array\\_2d\\_col](#)

#### Note

The classes

- [array\\_reverse](#)
- [array\\_subvector](#)
- [array\\_subvector\\_reverse](#)
- [array\\_const\\_reverse](#)
- [array\\_const\\_subvector](#)
- [array\\_const\\_subvector\\_reverse](#)

can be used with pointers or arrays, but [array\\_alloc](#) and [pointer\\_alloc](#) are *not* interchangeable.

**Idea for Future** Create a class which views a C-style array as a matrix and offers an operator `( , )`

Definition in file [array.h](#).

---

## Data Structures

- class [array\\_alloc< vec\\_t >](#)  
A simple class to provide an [allocate\(\)](#) function for arrays.
- class [array\\_2d\\_alloc< mat\\_t >](#)  
A simple class to provide an [allocate\(\)](#) function for 2-dimensional arrays.
- class [pointer\\_alloc< base\\_t >](#)  
A simple class to provide an [allocate\(\)](#) function for pointers.
- class [pointer\\_2d\\_alloc< base\\_t >](#)  
A simple class to provide an [allocate\(\)](#) function for pointers.
- struct [pointer\\_2d\\_alloc< base\\_t >::pointer\\_comp](#)
- class [array\\_reverse< sz >](#)  
A simple class which reverses the order of an array.
- class [array\\_const\\_reverse< sz >](#)  
A simple class which reverses the order of an array.
- class [array\\_subvector](#)  
A simple subvector class for an array (without error checking)
- class [array\\_2d\\_col< R, C, data\\_t >](#)  
Column of a 2d array.
- class [array\\_2d\\_row< array\\_2d\\_t, data\\_t >](#)  
Row of a 2d array.
- class [array\\_const\\_subvector](#)  
A simple subvector class for a const array (without error checking)
- class [array\\_subvector\\_reverse](#)  
Reverse a subvector of an array.
- class [array\\_const\\_subvector\\_reverse](#)  
Reverse a subvector of a const array.

## 47.2 cblas\_base.h File Reference

O2scl basic linear algebra function templates.

## 47.2.1 Detailed Description

See [o2scl\\_cblas](#) for more documentation on these functions.

**Idea for Future** Add float and complex versions.

**Idea for Future** There are some Level-1 BLAS functions which are already present in [vector.h](#). Should we move all of them to one place or the other? The ones in [vector.h](#) are generic in the sense that they can use doubles or floats, but the ones here can use either () or [].

Definition in file [cblas\\_base.h](#).

## Namespaces

- namespace [o2scl\\_cblas](#)  
Namespace for O2scl CBLAS function templates with operator[].

## Enumerations

- enum [o2scl\\_cblas::o2cblas\\_order](#) { [o2cblas\\_RowMajor](#) = 101, [o2cblas\\_ColMajor](#) = 102 }  
Matrix order, either column-major or row-major.
- enum [o2scl\\_cblas::o2cblas\\_transpose](#) { [o2cblas\\_NoTrans](#) = 111, [o2cblas\\_Trans](#) = 112, [o2cblas\\_ConjTrans](#) = 113 }  
Transpose operations.

- enum `o2scl_cblas::o2cblas_uplo` { `o2cblas_Upper` = 121, `o2cblas_Lower` = 122 }  
*Upper- or lower-triangular.*
- enum `o2scl_cblas::o2cblas_diag` { `o2cblas_NonUnit` = 131, `o2cblas_Unit` = 132 }  
*Unit or generic diagonal.*
- enum `o2scl_cblas::o2cblas_side` { `o2cblas_Left` = 141, `o2cblas_Right` = 142 }  
*Left or right sided operation.*

## Functions

### Level-1 BLAS functions

- template<class vec\_t >  
double `o2scl_cblas::dasum` (const size\_t N, const vec\_t &X)  
*Compute the absolute sum of vector elements.*
- template<class vec\_t, class vec2\_t >  
void `o2scl_cblas::daxpy` (const double alpha, const size\_t N, const vec\_t &X, vec2\_t &Y)  
*Compute  $y = \alpha x + y$ .*
- template<class vec\_t, class vec2\_t >  
double `o2scl_cblas::ddot` (const size\_t N, const vec\_t &X, const vec2\_t &Y)  
*Compute  $r = x \cdot y$ .*
- template<class vec\_t >  
double `o2scl_cblas::dnrm2` (const size\_t N, const vec\_t &X)  
*Compute the norm of the vector X.*
- template<class vec\_t >  
void `o2scl_cblas::dscal` (const double alpha, const size\_t N, vec\_t &X)  
*Compute  $x = \alpha x$ .*

### Level-2 BLAS functions

- template<class mat\_t, class vec\_t >  
void `o2scl_cblas::dgemv` (const enum o2cblas\_order order, const enum o2cblas\_transpose TransA, const size\_t M, const size\_t N, const double alpha, const mat\_t &A, const vec\_t &X, const double beta, vec\_t &Y)  
*Compute  $y = \alpha [\text{op}(A)]x + \beta y$ .*
- template<class mat\_t, class vec\_t >  
void `o2scl_cblas::dtrsv` (const enum o2cblas\_order order, const enum o2cblas\_uplo Uplo, const enum o2cblas\_transpose TransA, const enum o2cblas\_diag Diag, const size\_t M, const size\_t N, const mat\_t &A, vec\_t &X)  
*Compute  $x = \text{op}(A)^{-1}x$ .*
- template<class mat\_t, class vec\_t >  
void `o2scl_cblas::dtrmv` (const enum o2cblas\_order Order, const enum o2cblas\_uplo Uplo, const enum o2cblas\_transpose TransA, const enum o2cblas\_diag Diag, const size\_t N, const mat\_t &A, vec\_t &x)  
*Compute  $x = \text{op}(A)x$  for the triangular matrix A.*

### Level-3 BLAS functions

- template<class mat\_t >  
void `o2scl_cblas::dgemm` (const enum o2cblas\_order Order, const enum o2cblas\_transpose TransA, const enum o2cblas\_transpose TransB, const size\_t M, const size\_t N, const size\_t K, const double alpha, const mat\_t &A, const mat\_t &B, const double beta, mat\_t &C)  
*Compute  $y = \alpha \text{op}(A)\text{op}(B) + \beta C$ .*

### Helper BLAS functions - Subvectors

- template<class vec\_t, class vec2\_t >  
void `o2scl_cblas::daxpy_subvec` (const double alpha, const size\_t N, const vec\_t &X, vec2\_t &Y, const size\_t ie)  
*Compute  $y = \alpha x + y$  beginning with index  $ie$  and ending with index  $N-1$ .*
- template<class vec\_t, class vec2\_t >  
double `o2scl_cblas::ddot_subvec` (const size\_t N, const vec\_t &X, const vec2\_t &Y, const size\_t ie)  
*Compute  $r = x \cdot y$  beginning with index  $ie$  and ending with index  $N-1$ .*
- template<class vec\_t >  
double `o2scl_cblas::dnrm2_subvec` (const size\_t N, const vec\_t &X, const size\_t ie)

*Compute the norm of the vector  $x$  beginning with index  $ie$  and ending with index  $N-1$ .*

- `template<class vec_t >`  
`void o2scl_cblas::dscal_subvec` (const double alpha, const size\_t N, vec\_t &X, const size\_t ie)  
*Compute  $x = \alpha x$  beginning with index  $ie$  and ending with index  $N-1$ .*

#### Helper BLAS functions - Subcolumns of a matrix

- `template<class mat_t, class vec_t >`  
`void o2scl_cblas::daxpy_subcol` (const double alpha, const size\_t M, const mat\_t &X, const size\_t ir, const size\_t ic, vec\_t &y)  
*Compute  $y = \alpha x + y$  for a subcolumn of a matrix.*
- `template<class mat_t, class vec_t >`  
`double o2scl_cblas::ddot_subcol` (const size\_t M, const mat\_t &X, const size\_t ir, const size\_t ic, const vec\_t &y)  
*Compute  $r = x \cdot y$  for a subcolumn of a matrix.*
- `template<class mat_t >`  
`double o2scl_cblas::dnrm2_subcol` (const mat\_t &A, const size\_t ir, const size\_t ic, const size\_t M)  
*Compute the norm of a subcolumn of a matrix.*
- `template<class mat_t >`  
`void o2scl_cblas::dscal_subcol` (mat\_t &A, const size\_t ir, const size\_t ic, const size\_t M, const double alpha)  
*Compute  $x = \alpha x$  for a subcolumn of a matrix.*

#### Helper BLAS functions - Subrows of a matrix

- `template<class mat_t, class vec_t >`  
`void o2scl_cblas::daxpy_subrow` (const double alpha, const size\_t N, const mat\_t &X, const size\_t ir, const size\_t ic, vec\_t &Y)  
*Compute  $y = \alpha x + y$  for a subrow of a matrix.*
- `template<class mat_t, class vec_t >`  
`double o2scl_cblas::ddot_subrow` (const size\_t N, const mat\_t &X, const size\_t ir, const size\_t ic, const vec\_t &Y)  
*Compute  $r = x \cdot y$  for a subrow of a matrix.*
- `template<class mat_t >`  
`double o2scl_cblas::dnrm2_subrow` (const mat\_t &M, const size\_t ir, const size\_t ic, const size\_t N)  
*Compute the norm of a subrow of a matrix.*
- `template<class mat_t >`  
`void o2scl_cblas::dscal_subrow` (mat\_t &A, const size\_t ir, const size\_t ic, const size\_t N, const double alpha)  
*Compute  $x = \alpha x$  for a subrow of a matrix.*

## 47.3 columnify.h File Reference

Functions to create output in columns.

```
#include <iostream> #include <string> #include <vector> #include <o2scl/misc.h> #include
<o2scl/array.h>
```

### 47.3.1 Detailed Description

Definition in file [columnify.h](#).

#### Data Structures

- class [columnify](#)  
*Create nicely formatted columns from a table of strings.*

#### Functions

- `template<class mat_t >`  
`int matrix_out_paren` (std::ostream &os, mat\_t &A, size\_t nrow, size\_t ncol)  
*A operator for simple matrix output using `operator()`*

- `template<class mat_t >`  
`int matrix_cx_out_paren (std::ostream &os, mat_t &A, size_t nrows, size_t ncols)`  
*A operator for simple complex matrix output using `operator()`*
- `template<class mat_t >`  
`int matrix_out (std::ostream &os, mat_t &A, size_t nrows, size_t ncols)`  
*A operator for simple matrix output using `operator[]`.*

### 47.3.2 Function Documentation

#### 47.3.2.1 `template<class mat_t > int matrix_out_paren ( std::ostream & os, mat_t & A, size_t nrows, size_t ncols )`

The type `mat_t` can be any matrix type which allows individual element access using `operator()` (`size_t, size_t`).

This outputs all of the matrix elements using output settings specified by `os`. The alignment performed by `columnify` using `columnify::align_dp`, i.e. the numbers are aligned by their decimal points. If the numbers have no decimal points, then the decimal point is assumed to be to the right of the last character in the string representation of the number.

Definition at line 245 of file `columnify.h`.

#### 47.3.2.2 `template<class mat_t > int matrix_cx_out_paren ( std::ostream & os, mat_t & A, size_t nrows, size_t ncols )`

**Todo** Doesn't this only work for GSL matrices? Compare this to the corresponding vector functions

Definition at line 278 of file `columnify.h`.

#### 47.3.2.3 `template<class mat_t > int matrix_out ( std::ostream & os, mat_t & A, size_t nrows, size_t ncols )`

The type `mat_t` can be any 2d-array type which allows individual element access using `[size_t][size_t]`

This outputs all of the matrix elements using output settings specified by `os`. The alignment performed by `columnify` using `columnify::align_dp`, i.e. the numbers are aligned by their decimal points. If the numbers have no decimal points, then the decimal point is assumed to be to the right of the last character in the string representation of the number.

**Idea for Future** If all of the matrix elements are positive integers and scientific mode is not set, then we can avoid printing the extra spaces.

Definition at line 323 of file `columnify.h`.

## 47.4 cx\_arith.h File Reference

Complex arithmetic.

```
#include <iostream> #include <complex> #include <cmath> #include <gsl/gsl_math.h> #include
<gsl/gsl_complex.h> #include <gsl/gsl_complex_math.h>
```

### 47.4.1 Detailed Description

#### Note

One should be careful about including this header file, especially in other header files as it overloads some of the standard mathematical functions, i.e. `sqrt()`. If you need access to both these functions and the standard functions for double objects, the easiest way is probably to include this file in a source (not header file) and use `using namespace std`. This used to be in a separate namespace, called `o2scl_arith`, but this causes problems with Koenig lookup in template classes for `operator*()` when defined for vector addition (for example).

**Idea for Future** Define operators with assignment for complex + double?

Definition in file `cx_arith.h`.

## Functions

- `gsl_complex complex_to_gsl` (`std::complex< double > &d`)  
*Convert a complex number to GSL form.*
- `std::complex< double > gsl_to_complex` (`gsl_complex &g`)  
*Convert a complex number to STL form.*

## Binary operators for two complex numbers

- `gsl_complex operator+` (`gsl_complex x, gsl_complex y`)  
*Add two complex numbers.*
- `gsl_complex operator-` (`gsl_complex x, gsl_complex y`)  
*Subtract two complex numbers.*
- `gsl_complex operator*` (`gsl_complex x, gsl_complex y`)  
*Multiply two complex numbers.*
- `gsl_complex operator/` (`gsl_complex x, gsl_complex y`)  
*Divide two complex numbers.*

## Binary operators with assignment for two complex numbers

- `gsl_complex operator+=` (`gsl_complex &x, gsl_complex y`)  
*Add a complex number.*
- `gsl_complex operator-=` (`gsl_complex &x, gsl_complex y`)  
*Subtract a complex number.*
- `gsl_complex operator*=` (`gsl_complex &x, gsl_complex y`)  
*Multiply a complex number.*
- `gsl_complex operator/=` (`gsl_complex &x, gsl_complex y`)  
*Divide a complex number.*

## Binary operators with assignment for a complex and real

- `gsl_complex operator+` (`gsl_complex x, double y`)  
*Add a complex and real number.*
- `gsl_complex operator+` (`double y, gsl_complex x`)  
*Add a complex and real number.*
- `gsl_complex operator-` (`gsl_complex x, double y`)  
*Subtract a complex and real number.*
- `gsl_complex operator-` (`double y, gsl_complex x`)  
*Subtract a complex and real number.*
- `gsl_complex operator*` (`gsl_complex x, double y`)  
*Multiply a complex and real number.*
- `gsl_complex operator*` (`double y, gsl_complex x`)  
*Multiply a complex and real number.*
- `gsl_complex operator/` (`gsl_complex x, double y`)  
*Divide a complex and real number.*

## Miscellaneous functions

- `double arg` (`gsl_complex x`)
- `double abs` (`gsl_complex x`)
- `double abs2` (`gsl_complex z`)
- `gsl_complex conjugate` (`gsl_complex a`)

## Square root and exponent functions

- `gsl_complex sqrt` (`gsl_complex a`)
- `gsl_complex sqrt_real` (`double x`)
- `gsl_complex pow` (`gsl_complex a, gsl_complex b`)
- `gsl_complex pow_real` (`gsl_complex a, double b`)

## Logarithmic and exponential functions

- `double logabs` (`gsl_complex z`)
- `gsl_complex exp` (`gsl_complex a`)
- `gsl_complex log` (`gsl_complex a`)
- `gsl_complex log10` (`gsl_complex a`)
- `gsl_complex log_b` (`gsl_complex a, gsl_complex b`)



## Trigonometric functions

- `gsl_complex sin` (`gsl_complex a`)
- `gsl_complex cos` (`gsl_complex a`)
- `gsl_complex tan` (`gsl_complex a`)
- `gsl_complex sec` (`gsl_complex a`)
- `gsl_complex csc` (`gsl_complex a`)
- `gsl_complex cot` (`gsl_complex a`)
- `gsl_complex asin` (`gsl_complex a`)
- `gsl_complex asin_real` (`double a`)
- `gsl_complex acos` (`gsl_complex a`)
- `gsl_complex acos_real` (`double a`)
- `gsl_complex atan` (`gsl_complex a`)
- `gsl_complex asec` (`gsl_complex a`)
- `gsl_complex asec_real` (`double a`)
- `gsl_complex acsc` (`gsl_complex a`)
- `gsl_complex acsc_real` (`double a`)
- `gsl_complex acot` (`gsl_complex a`)

## Hyperbolic trigonometric functions

- `gsl_complex sinh` (`gsl_complex a`)
- `gsl_complex cosh` (`gsl_complex a`)
- `gsl_complex tanh` (`gsl_complex a`)
- `gsl_complex sech` (`gsl_complex a`)
- `gsl_complex csch` (`gsl_complex a`)
- `gsl_complex coth` (`gsl_complex a`)
- `gsl_complex asinh` (`gsl_complex a`)
- `gsl_complex acosh` (`gsl_complex a`)
- `gsl_complex acosh_real` (`double a`)
- `gsl_complex atanh` (`gsl_complex a`)
- `gsl_complex atanh_real` (`double a`)
- `gsl_complex asech` (`gsl_complex a`)
- `gsl_complex acsch` (`gsl_complex a`)
- `gsl_complex acoth` (`gsl_complex a`)

## 47.5 err\_hnd.h File Reference

File for definitions for `err_hnd_type` and `err_hnd_gsl`.

```
#include <iostream> #include <string> #include <gsl/gsl_errno.h>
```

## 47.5.1 Detailed Description

See also [exception.h](#) .

Definition in file [err\\_hnd.h](#).

## Data Structures

- class [err\\_hnd\\_type](#)  
*Class defining an error handler [abstract base].*
- class [err\\_hnd\\_gsl](#)  
*The error handler.*

## Defines

- #define `O2SCL_ERR`(`d`, `n`) `o2scl::set_err_fn(d, __FILE__, __LINE__, n);`  
*Set an error with message `d` and code `n`.*
- #define `O2SCL_CONV`(`d`, `n`, `b`) { if (`b`) `o2scl::set_err_fn(d, __FILE__, __LINE__, n); }`  
*Set a "convergence" error.*
- #define `O2SCL_ERR2`(`d`, `d2`, `n`)  
*Set an error, two-string version.*

- `#define O2SCL_CONV2(d, d2, n, b)`  
*Set a "convergence" error; two-string version.*
- `#define O2SCL_ERR_RET(d, n) do { o2scl::set_err_fn(d, __FILE__, __LINE__, n); return n; } while (0)`  
*Set an error and return the error value.*
- `#define O2SCL_CONV_RET(d, n, b)`  
*Set a "convergence" error and return the error value.*
- `#define O2SCL_ERR2_RET(d, d2, n)`  
*Set an error and return the error value, two-string version.*
- `#define O2SCL_CONV2_RET(d, d2, n, b)`  
*Set an error and return the error value, two-string version.*
- `#define O2SCL_ASSERT(ev)`  
*A version of `assert`, i.e. exit if the error value is non-zero and do nothing otherwise.*
- `#define O2SCL_BOOL_ASSERT(ev, str)`  
*A version of `assert` for bool types. Exit if the argument is false.*

## Enumerations

- `enum { gsl_success = 0, gsl_failure = -1, gsl_continue = -2, gsl_edom = 1, gsl_erange = 2, gsl_efault = 3, gsl_einval = 4, gsl_efailed = 5, gsl_efactor = 6, gsl_esanity = 7, gsl_enomem = 8, gsl_ebadfunc = 9, gsl_erunaway = 10, gsl_emaxiter = 11, gsl_ezerodiv = 12, gsl_ebadtol = 13, gsl_etol = 14, gsl_eundrflw = 15, gsl_eovrflw = 16, gsl_eloss = 17, gsl_eround = 18, gsl_ebadlen = 19, gsl_enotsqr = 20, gsl_esing = 21, gsl_ediverge = 22, gsl_eunsup = 23, gsl_eunimpl = 24, gsl_ecache = 25, gsl_etable = 26, gsl_enoprog = 27, gsl_enoproj = 28, gsl_etolf = 29, gsl_etolx = 30, gsl_etolg = 31, gsl_eof = 32, gsl_enotfound = 33, gsl_ememtype = 34, gsl_eilenotfound = 35, gsl_eindex = 36, gsl_outsidecons = 37 }`  
*The integer error definitions.*

## Functions

- `void set_err_fn (const char *desc, const char *file, int line, int errnum)`  
*Set an error.*
- `void error_update (int &ret, int err)`  
*Update an error value `err` with the value in `ret`.*

## Variables

- `err_hnd_type * err_hnd`  
*The global error handler pointer.*
- `err_hnd_gsl alt_err_hnd`  
*An alternate GSL-like error handler.*

### 47.5.2 Define Documentation

#### 47.5.2.1 `#define O2SCL_ERR2( d, d2, n )`

##### Value:

```
o2scl::set_err_fn( (std::string(d)+d2).c_str(), \
                  __FILE__, __LINE__, n );
```

Definition at line 306 of file `err_hnd.h`.

#### 47.5.2.2 `#define O2SCL_CONV2( d, d2, n, b )`

##### Value:

```
{ if (b)
    o2scl::set_err_fn( (std::string(d)+d2).c_str(), \
                      __FILE__, __LINE__, n ); }
```

Definition at line 311 of file err\_hnd.h.

#### 47.5.2.3 #define O2SCL\_CONV\_RET( d, n, b )

**Value:**

```
do { if (!b) { return 0; } else { \
    o2scl::set_err_fn(d, __FILE__, __LINE__, n); return n; } } while (0)
```

Definition at line 322 of file err\_hnd.h.

#### 47.5.2.4 #define O2SCL\_ERR2\_RET( d, d2, n )

**Value:**

```
do { o2scl::set_err_fn((std::string(d)+d2).c_str(), \
    __FILE__, __LINE__, n); return n; } while (0)
```

Definition at line 328 of file err\_hnd.h.

#### 47.5.2.5 #define O2SCL\_CONV2\_RET( d, d2, n, b )

**Value:**

```
do { if (!b) {return 0; } else { \
    o2scl::set_err_fn((std::string(d)+d2).c_str(), \
    __FILE__, __LINE__, n); return n; } } while (0)
```

Definition at line 334 of file err\_hnd.h.

#### 47.5.2.6 #define O2SCL\_ASSERT( ev )

**Value:**

```
do { if (ev!=0) { std::cout << "O2scl: Macro err_assert() causing exit" \
    << " from error " << ev << " at " \
    << __LINE__ << " in file:\n " \
    << __FILE__ << std::endl; \
    std::cout << "Error handler string:\n " << err_hnd->get_str() \
    << std::endl; exit(ev); } } while (0)
```

**Idea for Future** Make this consistent with assert() using NDEBUG?

Definition at line 359 of file err\_hnd.h.

#### 47.5.2.7 #define O2SCL\_BOOL\_ASSERT( ev, str )

**Value:**

```
do { if (ev==false) { \
    std::cout << "O2scl: Macro bool_assert() causing exit at line " \
    << __LINE__ << " in file:\n " \
    << __FILE__ << std::endl; \
    std::cout << "Given string: " << str \
    << std::endl; exit(-1); } } while (0)
```

Definition at line 370 of file err\_hnd.h.

### 47.5.3 Enumeration Type Documentation

#### 47.5.3.1 anonymous enum

The errors associated with the integers between -2 and 32 are from GSL, the rest are specific to O2scl .

Enumerator:

- gsl\_success***  
Success (GSL)
  - gsl\_failure***  
Failure (GSL)
  - gsl\_continue***  
iteration has not converged (GSL)
  - gsl\_edom***  
input domain error, e.g.  $\sqrt{-1}$  (GSL)
  - gsl\_erange***  
output range error, e.g.  $\exp(1e100)$  (GSL)
  - gsl\_efault***  
invalid pointer (GSL)
  - gsl\_einval***  
invalid argument supplied by user (GSL)
  - gsl\_efailed***  
generic failure (GSL)
  - gsl\_efactor***  
factorization failed (GSL)
  - gsl\_esanity***  
sanity check failed - shouldn't happen (GSL)
  - gsl\_enomem***  
malloc failed (GSL)
  - gsl\_ebadfunc***  
problem with user-supplied function (GSL)
  - gsl\_erunaway***  
iterative process is out of control (GSL)
  - gsl\_emaxiter***  
exceeded max number of iterations (GSL)
  - gsl\_ezerodiv***  
tried to divide by zero (GSL)
  - gsl\_ebadtol***  
user specified an invalid tolerance (GSL)
  - gsl\_etol***  
failed to reach the specified tolerance (GSL)
  - gsl\_eundrflw***  
underflow (GSL)
  - gsl\_eovrflw***  
overflow (GSL)
  - gsl\_eloss***  
loss of accuracy (GSL)
  - gsl\_eround***  
failed because of roundoff error (GSL)
  - gsl\_ebadlen***  
matrix, vector lengths are not conformant (GSL)
  - gsl\_enotsqr***  
matrix not square (GSL)
  - gsl\_esing***  
apparent singularity detected (GSL)
  - gsl\_ediverge***  
integral or series is divergent (GSL)
  - gsl\_eunsup***  
requested feature is not supported by the hardware (GSL)
-

<b><i>gsl_eunimpl</i></b>	requested feature not (yet) implemented (GSL)
<b><i>gsl_ecache</i></b>	cache limit exceeded (GSL)
<b><i>gsl_etable</i></b>	table limit exceeded (GSL)
<b><i>gsl_enoprog</i></b>	iteration is not making progress toward solution (GSL)
<b><i>gsl_enoproj</i></b>	jacobian evaluations are not improving the solution (GSL)
<b><i>gsl_etolf</i></b>	cannot reach the specified tolerance in f (GSL)
<b><i>gsl_etolx</i></b>	cannot reach the specified tolerance in x (GSL)
<b><i>gsl_etolg</i></b>	cannot reach the specified tolerance in gradient (GSL)
<b><i>gsl_eof</i></b>	end of file (GSL)
<b><i>gsl_enotfound</i></b>	Generic "not found" result.
<b><i>gsl_ememtype</i></b>	Incorrect type for memory object.
<b><i>gsl_efilenotfound</i></b>	File not found.
<b><i>gsl_eindex</i></b>	Invalid index for array or matrix.
<b><i>gsl_outsidecons</i></b>	Outside constraint region.

Definition at line 45 of file `err_hnd.h`.

#### 47.5.4 Function Documentation

**47.5.4.1** `void error_update ( int &ret, int err ) [inline]`

If `ret` is zero, this sets `ret` to the value `err`, and if `ret` is nonzero this function does nothing.

Definition at line 352 of file `err_hnd.h`.

## 47.6 exception.h File Reference

File for definitions for [err\\_hnd\\_cpp](#) and the exceptions.

```
#include <stdexcept> #include <iostream> #include <o2scl/err_hnd.h>
```

#### 47.6.1 Detailed Description

See also [err\\_hnd.h](#).

Definition in file [exception.h](#).

## Data Structures

- class [exc\\_exception](#)  
*Generic exception.*
- class [exc\\_logic\\_error](#)  
*Logic error exception.*
- class [exc\\_invalid\\_argument](#)  
*Invalid argument exception.*
- class [exc\\_runtime\\_error](#)  
*Generic runtime error exception.*
- class [exc\\_range\\_error](#)  
*Range error runtime exception.*
- class [exc\\_overflow\\_error](#)  
*Overflow error runtime exception.*
- class [exc\\_ios\\_failure](#)  
*I/O failure error exception.*
- class [err\\_hnd\\_cpp](#)  
*Error handler to throw C++ exceptions.*

## Variables

- [err\\_hnd\\_cpp def\\_err\\_hnd](#)  
*The default error handler.*

## 47.7 givens.h File Reference

File for Givens rotations.

```
#include <gsl/gsl_math.h> #include <o2scl/err_hnd.h> #include <o2scl/permutation.h> #include
<o2scl/cblas.h> #include <o2scl/vec_arith.h> #include <o2scl/givens_base.h>
```

## 47.7.1 Detailed Description

Definition in file [givens.h](#).

## Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*

## Defines

- `#define O2SCL_IX(V, i) V[i]`
- `#define O2SCL_IX2(M, i, j) M[i][j]`

## Functions

- void [o2scl\\_linalg::create\\_givens](#) (const double a, const double b, double &c, double &s)  
*Desc.*

## 47.8 givens\_base.h File Reference

File for Givens rotations.

## 47.8.1 Detailed Description

**Todo** Make sure `create_givens()` in `givens.h` is documented.

Definition in file `givens_base.h`.

## Namespaces

- namespace `o2scl_linalg`  
*The namespace for linear algebra classes and functions.*

## Functions

- template<class mat1\_t, class mat2\_t>  
void `o2scl_linalg::apply_givens_qr` (size\_t M, size\_t N, mat1\_t &Q, mat2\_t &R, size\_t i, size\_t j, double c, double s)  
*Apply a rotation to matrices from the QR decomposition.*
- template<class mat1\_t, class mat2\_t>  
void `o2scl_linalg::apply_givens_lq` (size\_t M, size\_t N, mat1\_t &Q, mat2\_t &L, size\_t i, size\_t j, double c, double s)  
*Apply a rotation to matrices from the LQ decomposition.*
- template<class vec\_t>  
void `o2scl_linalg::apply_givens_vec` (vec\_t &v, size\_t i, size\_t j, double c, double s)  
*Apply a rotation to a vector;  $v \rightarrow G^T v$ .*

## 47.9 graph.h File Reference

Experimental functions for use with Root.

```
#include <string> #include <Gtypes.h> #include <TApplication.h> #include <TArrow.h> #include
<TAxis.h> #include <TBox.h> #include <TCanvas.h> #include <TColor.h> #include <TF1.h> ×
#include <TGraph.h> #include <TGraphErrors.h> #include <TGaxis.h> #include <TH1.h> #include
<TH2.h> #include <TLatex.h> #include <TLegend.h> #include <TLine.h> #include <TList.h> ×
#include <TMarker.h> #include <TObjArray.h> #include <TROOT.h> #include <TStyle.h> #include
<TPolyLine.h> #include <o2scl/constants.h> #include <o2scl/table_units.h>
```

## 47.9.1 Detailed Description

All of the functions in `graph.h` are documented in the `o2scl_graph` namespace.

Definition in file `graph.h`.

## Namespaces

- namespace `o2scl_graph`  
*Namespace for experimental functions for use with Root.*

## Functions

- void `o2scl_graph::arrow` (double x1, double y1, double x2, double y2, TLine \*&line, TPolyLine \*&poly, double size=0.1, double size2=0.8, double alpha1=0.35)  
*Draw a pretty arrow from (x1,y1) to (x2,y2)*
- int `o2scl_graph::new_graph` (TCanvas \*&c1, TPad \*&p1, TH1 \*&th1, std::string CanvasName, std::string WindowName, std::string PadName, double lleft, double lbottom, double lright, double ltop, int left=0, int top=0, int right=700, int bottom=700, bool logx=false, bool logy=false)

*Make a canvas and pad.*

- int `o2scl_graph::new_graph_ticks` (TCanvas \*&c1, TPad \*&p1, TH1 \*&th1, std::string CanvasName, std::string WindowName, std::string PadName, double lleft, double lbottom, double lright, double ltop, TGaxis \*&a1, TGaxis \*&a2, int left=0, int top=0, int right=700, int bottom=700, bool logx=false, bool logy=false)

*Make a canvas and pad with more tick marks.*

- TGraph \* `o2scl_graph::table_graph` (o2scl::table\_units &at, std::string scolx, std::string scoly, int style=1, int color=1)

*Graph two columns from a data table.*

- TGraphErrors \* `o2scl_graph::table_graph_errors` (o2scl::table\_units &at, std::string scolx, std::string scoly, std::string xerr, std::string yerr, int style=1, int color=1)

*Plot colums from a data table with error bars.*

- int `o2scl_graph::two_up_graph` (TCanvas \*&c1, TPad \*&p1, TPad \*&p2, TH1 \*&th1, TH1 \*&th2, std::string CanvasName, std::string WindowName, std::string Pad1Name, std::string Pad2Name, double lowx1, double highx1, double lowx2, double highx2, double lowy, double highy, int left=0, int top=0, int right=1000, int bottom=700, bool logx1=false, bool logx2=false, bool logy=false, double alpha=1.3, double margin=0.1)

*Make a canvas with a two-up graph, side-by-side.*

- int `o2scl_graph::two_up_graphy` (TCanvas \*&c1, TPad \*&p1, TPad \*&p2, TH1 \*&th1, TH1 \*&th2, std::string CanvasName, std::string WindowName, std::string Pad1Name, std::string Pad2Name, double lowx, double highx, double lowy1, double highy1, double lowy2, double highy2, int left=0, int top=0, int right=1000, int bottom=700, bool logx=false, bool logy1=false, bool logy2=false, double alpha=1.3, double margin=0.1)

*Make a canvas with two plots, one on top of the other.*

## Variables

### Some useful colors

- const int `o2scl_graph::kGray20` = kGray
- const int `o2scl_graph::kGray40` = kGray+1
- const int `o2scl_graph::kGray60` = kGray+2
- const int `o2scl_graph::kGray80` = kGray+3

### Markers

- const int `o2scl_graph::m_small_dot` = 1
- const int `o2scl_graph::m_plus` = 2
- const int `o2scl_graph::m_asterisk` = 3
- const int `o2scl_graph::m_circle` = 4
- const int `o2scl_graph::m_times` = 5
- const int `o2scl_graph::m_med_dot` = 6
- const int `o2scl_graph::m_large_dot` = 7
- const int `o2scl_graph::m_fill_circle` = 8
- const int `o2scl_graph::m_fill_square` = 21
- const int `o2scl_graph::m_fill_up_triangle` = 22
- const int `o2scl_graph::m_fill_dn_triangle` = 23
- const int `o2scl_graph::m_open_circle` = 24
- const int `o2scl_graph::m_open_square` = 25
- const int `o2scl_graph::m_open_up_triangle` = 26
- const int `o2scl_graph::m_open_diamond` = 27
- const int `o2scl_graph::m_open_plus` = 28
- const int `o2scl_graph::m_fill_star` = 29
- const int `o2scl_graph::m_open_star` = 30
- const int `o2scl_graph::m_asterisk2` = 31
- const int `o2scl_graph::m_open_dn_triangle` = 32
- const int `o2scl_graph::m_fill_diamond` = 33
- const int `o2scl_graph::m_fill_plus` = 34

## 47.10 hdf\_io.h File Reference

File for HDF I/O for [table](#) and [table3d](#).

```
#include <hdf5.h> #include <o2scl/table.h> #include <o2scl/table_units.h> #include <o2scl/table3d.h> #include <o2scl/constants.h> #include <o2scl/hist.h> #include <o2scl/hist_2d.h> #include <o2scl/tensor.h> #include <o2scl/hdf_file.h>
```



## 47.10.1 Detailed Description

Definition in file [hdf\\_io.h](#).

## Data Structures

- struct [iterate\\_parms](#)  
A structure to pass information to and from [iterate\\_func\(\)](#)

## Functions

- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::table &t, std::string name)  
Output a *table* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::table &t, std::string name="")  
Input a *table* from a HDF file.
- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::table\_units &t, std::string name)  
Output a *table\_units* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::table\_units &t, std::string name="")  
Input a *table\_units* from a HDF file.
- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::table3d &t, std::string name)  
Output a *table3d* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::table3d &t, std::string name="")  
Input a *table3d* from a HDF file.
- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::hist &t, std::string name)  
Output a *hist* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::hist &t, std::string name="")  
Input a *hist* from a HDF file.
- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::hist\_2d &t, std::string name)  
Output a *hist\_2d* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::hist\_2d &t, std::string name="")  
Input a *hist\_2d* from a HDF file.
- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::tensor &t, std::string name)  
Output a *tensor* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::tensor &t, std::string name="")  
Input a *tensor* from a HDF file.
- int [hdf\\_output](#) ([hdf\\_file](#) &hf, const o2scl::tensor\_grid &t, std::string name)  
Output a *tensor* to a HDF file.
- int [hdf\\_input](#) ([hdf\\_file](#) &hf, o2scl::tensor\_grid &t, std::string name="")  
Input a *tensor* from a HDF file.

## Helper struct and functions

- int [iterate\\_func](#) (hid\_t loc, const char \*name, const H5L\_info\_t \*inf, void \*op\_data)  
Look at location *loc* in an HDF file for an *O2scl* object.
- int [find\\_group\\_by\\_type](#) ([hdf\\_file](#) &hf, std::string type, std::string &group\_name, int verbose=0)  
Look in [hdf\\_file](#) *hf* for an *O2scl* object of type *type* and if found, set *group\_name* to the associated object name.

## 47.10.2 Function Documentation

## 47.10.2.1 int hdf\_output ( hdf\_file &amp; hf, const o2scl::table\_units &amp; t, std::string name )

The unit conversion object, as specified in [table\\_units::set\\_convert\(\)](#) is not written to the HDF file. Thus when a [table\\_units](#) object is read from a file, it always uses the default unit conversion object.

## 47.10.2.2 int hdf\_input ( hdf\_file &amp; hf, o2scl::table\_units &amp; t, std::string name = " " )

The unit conversion object, as specified in [table\\_units::set\\_convert\(\)](#) is not written to the HDF file. Thus when a [table\\_units](#) object is read from a file, it always uses the default unit conversion object.

47.10.2.3 `int iterate_func ( hid_t loc, const char * name, const H5L_info_t * inf, void * op_data )`

This is used by `find_group_by_type()` where `op_data` is a pointer to an object of type `iterate_parms` to look for O<sub>2</sub>scl objects of a specified type without knowing the group name.

47.10.2.4 `int find_group_by_type ( hdf_file & hf, std::string type, std::string & group_name, int verbose = 0 )`

This function returns 1 if an object of type `type` is found and 0 if it fails.

## 47.11 hh\_base.h File Reference

File for householder solver.

```
#include <o2scl/err_hnd.h> #include <o2scl/cblas.h> #include <o2scl/permutation.h> #include
<o2scl/vec_arith.h>
```

### 47.11.1 Detailed Description

Definition in file [hh\\_base.h](#).

#### Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*

#### Functions

- `template<class mat_t, class vec_t, class vec2_t>`  
`int o2scl_linalg::HH_solve (size_t n, mat_t &A, const vec_t &b, vec2_t &x)`  
*Solve linear system after Householder decomposition.*
- `template<class mat_t, class vec_t>`  
`int o2scl_linalg::HH_svx (size_t N, size_t M, mat_t &A, vec_t &x)`  
*Solve a linear system after Householder decomposition in place.*

## 47.12 householder\_base.h File Reference

File for Householder transformations.

```
#include <gsl/gsl_machine.h> #include <o2scl/err_hnd.h> #include <o2scl/cblas.h> #include
<o2scl/permutation.h> #include <o2scl/vec_arith.h>
```

### 47.12.1 Detailed Description

**Todo** Better documentation for the Householder functions.

Definition in file [householder\\_base.h](#).

#### Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*

## Functions

- template<class vec\_t >  
double [o2scl\\_linalg::householder\\_transform](#) (const size\_t n, vec\_t &v)  
*Replace the vector  $v$  with a Householder vector and a coefficient tau that annihilates  $v[1]$  through  $v[n-1]$  (inclusive)*
- template<class mat\_t >  
double [o2scl\\_linalg::householder\\_transform\\_subcol](#) (mat\_t &A, const size\_t ir, const size\_t ic, const size\_t M)  
*Compute the Householder transform of a vector formed with  $n$  rows of a column of a matrix.*
- template<class mat\_t >  
double [o2scl\\_linalg::householder\\_transform\\_subrow](#) (mat\_t &A, const size\_t ir, const size\_t ic, const size\_t N)  
*Compute the Householder transform of a vector formed with the last  $n$  columns of a row of a matrix.*
- template<class vec\_t, class mat\_t >  
void [o2scl\\_linalg::householder\\_hm](#) (const size\_t M, const size\_t N, double tau, const vec\_t &v, mat\_t &A)  
*Apply a Householder transformation  $(v, \tau)$  to matrix  $A$  of size  $M$  by  $N$ .*
- template<class mat\_t >  
void [o2scl\\_linalg::householder\\_hm\\_sub](#) (mat\_t &M, const size\_t ir, const size\_t ic, const size\_t nr, const size\_t nc, const mat\_t &M2, const size\_t ir2, const size\_t ic2, double tau)  
*Apply a Householder transformation to submatrix of a larger matrix.*
- template<class mat1\_t, class mat2\_t >  
void [o2scl\\_linalg::householder\\_hm\\_sub2](#) (const size\_t M, const size\_t ic, double tau, const mat1\_t &mv, mat2\_t &A)  
*Special version of Householder transformation for [QR\\_unpack\(\)](#)*
- template<class vec\_t, class vec2\_t >  
void [o2scl\\_linalg::householder\\_hv](#) (const size\_t N, double tau, const vec\_t &v, vec2\_t &w)  
*Apply a Householder transformation  $v$  to vector  $w$ .*
- template<class mat\_t, class vec\_t >  
void [o2scl\\_linalg::householder\\_hv\\_subcol](#) (const mat\_t &A, vec\_t &w, double tau, const size\_t ie, const size\_t N)  
*Apply a Householder transformation  $v$  to vector  $w$  where  $v$  is stored as a column in a matrix  $A$ .*
- template<class mat\_t >  
void [o2scl\\_linalg::householder\\_hm1](#) (const size\_t M, const size\_t N, double tau, mat\_t &A)  
*Apply a Householder transformation  $(v, \tau)$  to a matrix being build up from the identity matrix, using the first column of  $A$  as a - Householder vector.*
- template<class vec\_t, class mat\_t >  
void [o2scl\\_linalg::householder\\_mh](#) (const size\_t M, const size\_t N, double tau, const vec\_t &v, mat\_t &A)  
*Apply the Householder transformation  $(v, \tau)$  to the right-hand side of the matrix  $A$ .*
- template<class mat\_t, class mat2\_t >  
void [o2scl\\_linalg::householder\\_mh\\_sub](#) (mat\_t &M, const size\_t ir, const size\_t ic, const size\_t nr, const size\_t nc, const mat2\_t &M2, const size\_t ir2, const size\_t ic2, double tau)  
*Apply the Householder transformation  $(v, \tau)$  to the right-hand side of the matrix  $A$ .*

## 47.13 lib\_settings.h File Reference

File for definitions for [lib\\_settings\\_class](#).

```
#include <iostream> #include <string>
```

## 47.13.1 Detailed Description

Definition in file [lib\\_settings.h](#).

## Data Structures

- class [lib\\_settings\\_class](#)  
*A class to manage global library settings.*

## Namespaces

- namespace [o2scl](#)  
*The main O<sub>2</sub>scl namespace.*
- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*
- namespace [o2scl\\_linalg\\_paren](#)  
*The namespace for linear algebra classes and functions with operator()*

## Variables

- [lib\\_settings\\_class lib\\_settings](#)  
*The global library settings object.*

## 47.13.2 Variable Documentation

## 47.13.2.1 lib\_settings\_class lib\_settings

This global object is used by [polylog](#) and some of the O<sub>2</sub>scl\_eos classes to find data files. It may also be used by the end-user to probe details of the O<sub>2</sub>scl installation.

## 47.14 lu.h File Reference

File for LU decomposition and associated solver.

```
#include <o2scl/err_hnd.h> #include <o2scl/permutation.h> #include <o2scl/cblas.h> #include
<o2scl/vec_arith.h> #include <o2scl/lu_base.h>
```

## 47.14.1 Detailed Description

Definition in file [lu.h](#).

## Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*
- namespace [o2scl\\_linalg\\_paren](#)  
*The namespace for linear algebra classes and functions with operator()*

## Defines

- `#define O2SCL_IX(V, i) V[i]`
- `#define O2SCL_IX2(M, i, j) M[i][j]`
- `#define O2SCL_IX(V, i) V(i)`
- `#define O2SCL_IX2(M, i, j) M(i,j)`

## Functions

- `template<size_t N>`  
`int o2scl\_linalg::LU\_decomp\_array\_2d (const size_t n, double A[][N], o2scl::permutation &p, int &signum)`  
*Specialized version of LU\_decomp for C-style 2D arrays.*

## 47.15 lu\_base.h File Reference

File for LU decomposition and associated solver.

### 47.15.1 Detailed Description

Definition in file [lu\\_base.h](#).

#### Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*

#### Functions

- `template<class mat_t >`  
`int o2scl\_linalg::diagonal\_has\_zero (const size_t N, mat_t &A)`  
*Return 1 if at least one of the elements in the diagonal is zero.*
- `template<class mat_t >`  
`int o2scl\_linalg::LU\_decomp (const size_t N, mat_t &A, o2scl::permutation &p, int &signum)`  
*Compute the LU decomposition of the matrix A.*
- `template<class mat_t, class mat_row_t >`  
`int o2scl\_linalg::LU\_decomp\_alt (const size_t N, mat_t &A, o2scl::permutation &p, int &signum)`
- `template<class mat_t, class vec_t, class vec2_t >`  
`int o2scl\_linalg::LU\_solve (const size_t N, const mat_t &LU, const o2scl::permutation &p, const vec_t &b, vec2_t &x)`  
*Solve a linear system after LU decomposition.*
- `template<class mat_t, class vec_t >`  
`int o2scl\_linalg::LU\_svx (const size_t N, const mat_t &LU, const o2scl::permutation &p, vec_t &x)`  
*Solve a linear system after LU decomposition in place.*
- `template<class mat_t, class mat2_t, class vec_t, class vec2_t, class vec3_t >`  
`int o2scl\_linalg::LU\_refine (const size_t N, const mat_t &A, const mat2_t &LU, const o2scl::permutation &p, const vec_t &b, vec2_t &x, vec3_t &residual)`  
*Refine the solution of a linear system.*
- `template<class mat_t, class mat2_t, class mat_col_t >`  
`int o2scl\_linalg::LU\_invert (const size_t N, const mat_t &LU, const o2scl::permutation &p, mat2_t &inverse)`  
*Compute the inverse of a matrix from its LU decomposition.*
- `template<class mat_t >`  
`double o2scl\_linalg::LU\_det (const size_t N, const mat_t &LU, int signum)`  
*Compute the determinant of a matrix from its LU decomposition.*
- `template<class mat_t >`  
`double o2scl\_linalg::LU\_lndet (const size_t N, const mat_t &LU)`  
*Compute the logarithm of the absolute value of the determinant of a matrix from its LU decomposition.*
- `template<class mat_t >`  
`int o2scl\_linalg::LU\_sgndet (const size_t N, const mat_t &LU, int signum)`  
*Compute the sign of the determinant of a matrix from its LU decomposition.*

## 47.16 minimize.h File Reference

One-dimensional minimization base class and associated functions.

```
#include <cmath> #include <o2scl/err_hnd.h> #include <o2scl/funct.h>
```

### 47.16.1 Detailed Description

Definition in file [minimize.h](#).

## Data Structures

- class `minimize< func_t, dfunc_t >`  
*One-dimensional minimization [abstract base].*
- class `minimize_bkt< func_t, dfunc_t >`  
*One-dimensional bracketing minimization [abstract base].*
- class `minimize_de< func_t, dfunc_t >`  
*One-dimensional minimization using derivatives [abstract base].*

## Functions

- double `constraint` (double `x`, double `center`, double `width`, double `height`)  
*Constrain  $x$  to be within `width` of the value given by `center`.*
- double `cont_constraint` (double `x`, double `center`, double `width`, double `height`, double `tightness`=40.0, double `exp_arg_limit`=50.0)  
*Constrain  $x$  to be within `width` of the value given by `center`.*
- double `lower_bound` (double `x`, double `center`, double `width`, double `height`)  
*Constrain  $x$  to be greater than the value given by `center`.*
- double `cont_lower_bound` (double `x`, double `center`, double `width`, double `height`, double `tightness`=40.0, double `exp_arg_limit`=50.0)  
*Constrain  $x$  to be greater than the value given by `center`.*

## 47.16.2 Function Documentation

47.16.2.1 `double constraint ( double x, double center, double width, double height ) [inline]`

Defining  $c = \text{center}$ ,  $w = \text{width}$ ,  $h = \text{height}$ , this returns the value  $h(1 + |x - c - w|/w)$  if  $x > c + w$  and  $h(1 + |x - c + w|/w)$  if  $x < c - w$ . The value near  $x = c - w$  or  $x = c + w$  is  $h$  (the value of the function exactly at these points is zero) and the value at  $x = c - 2w$  or  $x = c + 2w$  is  $2h$ .

It is important to note that, for large distances of  $x$  from `center`, this only scales linearly. If you are trying to constrain a function which decreases more than linearly by making  $x$  far from `center`, then a minimizer may ignore this constraint.

Definition at line 370 of file `minimize.h`.

47.16.2.2 `double cont_constraint ( double x, double center, double width, double height, double tightness = 40.0, double exp_arg_limit = 50.0 ) [inline]`

Defining  $c = \text{center}$ ,  $w = \text{width}$ ,  $h = \text{height}$ ,  $t = \text{tightness}$ , and  $\ell = \text{exp\_arg\_limit}$ , this returns the value

$$h \left( \frac{x - c}{w} \right)^2 \left[ 1 + e^{t(x - c + w)(c + w - x)/w^2} \right]^{-1}$$

This function is continuous and differentiable. Note that if  $x = c$ , then the function returns zero.

The exponential is handled gracefully by assuming that anything smaller than  $\exp(-\ell)$  is zero. This creates a small discontinuity which can be removed with the sufficiently large value of  $\ell$ .

It is important to note that, for large distances of  $x$  from `center`, this scales quadratically. If you are trying to constrain a function which decreases faster than quadratically by making  $x$  far from `center`, then a minimizer may ignore this constraint.

In the limit  $t \rightarrow \infty$ , this function converges towards the squared value of `constraint()`, except exactly at the points  $x = c - w$  and  $x = c + w$ .

Definition at line 411 of file `minimize.h`.

47.16.2.3 `double lower_bound ( double x, double center, double width, double height ) [inline]`

Defining  $c = \text{center}$ ,  $w = \text{width}$ ,  $h = \text{height}$ , this returns  $h(1 + |x - c|/w)$  if  $x < c$  and zero otherwise. The value at  $x = c$  is  $h$ , while the value at  $x = c - w$  is  $2h$ .

It is important to note that, for large distances of  $x$  from `center`, this only scales linearly. If you are trying to constrain a function which decreases more than linearly by making  $x$  far from `center`, then a minimizer may ignore this constraint.

Definition at line 438 of file `minimize.h`.

```
47.16.2.4 double cont_lower_bound ( double x, double center, double width, double height, double tightness = 40.0, double exp_arg_limit =
50.0 ) [inline]
```

Defining  $c = \text{center}$ ,  $w = \text{width}$ ,  $h = \text{height}$ ,  $t = \text{tightness}$ , and  $\ell = \text{exp\_arg\_limit}$ , this returns  $h(c - x + w)/(w + w \exp(t(x - c)/w))$  and has the advantage of being a continuous and differentiable function. The value of the function exactly at  $x = c$  is  $h/2$ , but for  $x$  just below  $c$  the function is  $h$  and just above  $c$  the function is quite small.

The exponential is handled gracefully by assuming that anything smaller than  $\exp(-\ell)$  is zero. This creates a small discontinuity which can be removed with the sufficiently large value of  $\ell$ .

It is important to note that, for large distances of  $x$  from `center`, this only scales linearly. If you are trying to constrain a function which decreases more than linearly by making  $x$  far from `center`, then a minimizer may ignore this constraint.

In the limit  $t \rightarrow \infty$ , this function converges towards `lower_bound()`, except exactly at the point  $x = c$ .

Definition at line 472 of file `minimize.h`.

## 47.17 misc.h File Reference

Miscellaneous functions.

```
#include <cstdlib> #include <iostream> #include <cmath> #include <string> #include <fstream> ×
#include <sstream> #include <vector> #include <gsl/gsl_vector.h> #include <gsl/gsl_ieee-
_utils.h> #include <o2scl/err_hnd.h> #include <o2scl/lib_settings.h>
```

### 47.17.1 Detailed Description

Definition in file `misc.h`.

#### Data Structures

- struct `string_comp`  
*Simple string comparison.*
- class `gen_test_number< tot >`  
*Generate number sequence for testing.*

#### Functions

- double `fermi_function` (double  $E$ , double  $\mu$ , double  $T$ , double  $\text{limit}=40.0$ )  
*Calculate a Fermi-Dirac distribution function safely.*
- template<class string\_arr\_t>  
int `screenify` (size\_t  $n_{\text{in}}$ , const string\_arr\_t & $\text{in\_cols}$ , std::vector< std::string > & $\text{out\_cols}$ , size\_t  $\text{max\_size}=80$ )  
*Reformat the columns for output of width size.*
- int `count_words` (std::string  $\text{str}$ )  
*Count the number of words in the string str.*
- int `remove_whitespace` (std::string & $s$ )  
*Remove all whitespace from the string s.*
- std::string `binary_to_hex` (std::string  $s$ )  
*Take a string of binary quads and compress them to hexadecimal digits.*
- template<class type\_t>  
int `gsl_alloc_arrays` (size\_t  $n_v$ , size\_t  $m_{\text{size}}$ , const char \* $\text{names}[]$ , type\_t \* $\text{ptrs}[]$ , std::string  $\text{func\_name}$ )  
*A convenient function to allocate several arrays of the same size.*

- `template<class type_t>`  
`int gsl_alloc_arrays (size_t nv, size_t msize, const char *names[], type_t *ptrs[], std::string func_name, type_t val)`  
*A convenient function to allocate and initialize several arrays of the same size.*
- `int gsl_alloc_gvecs (size_t nv, size_t msize, const char *names[], gsl_vector ***ptrs, std::string func_name)`  
*A convenient function to allocate and initialize several arrays of the same size.*
- `double quadratic_extremum_x (double x1, double x2, double x3, double y1, double y2, double y3)`  
*Return the x value of the extremum of a quadratic defined by three (x,y) pairs.*
- `double quadratic_extremum_y (double x1, double x2, double x3, double y1, double y2, double y3)`  
*Return the y value of the extremum of a quadratic defined by three (x,y) pairs.*

## 47.17.2 Function Documentation

### 47.17.2.1 `double fermi_function ( double E, double mu, double T, double limit = 40.0 )`

$$[1 + \exp(E/T - \mu/T)]^{-1}$$

This calculates a Fermi-Dirac distribution function guaranteeing that numbers larger than  $\exp(\text{limit})$  and smaller than  $\exp(-\text{limit})$  will be avoided. The default value of `limit=40` ensures accuracy to within 1 part in  $10^{17}$  compared to the maximum of the distribution (which is unity).

Note that this function may return Inf or NAN if `limit` is too large, depending on the machine precision.

### 47.17.2.2 `template<class string_arr_t> int screenify ( size_t nin, const string_arr_t & in_cols, std::vector< std::string > & out_cols, size_t max_size = 80 )`

Given a string array `in_cols` of size `nin`, `screenify()` reformats the array into columns creating a new string array `out_cols`.

For example, for an array of 10 strings

```
test1
test_of_string2
test_of_string3
test_of_string4
test5
test_of_string6
test_of_string7
test_of_string8
test_of_string9
test_of_string10
```

`screenify()` will create an array of 3 new strings:

```
test1          test_of_string4  test_of_string7  test_of_string10
test_of_string2 test5          test_of_string8
test_of_string3 test_of_string6  test_of_string9
```

If the value of `max_size` is less than the length of the longest input string (plus one for a space character), then the output strings may have a larger length than `max_size`.

Definition at line 94 of file `misc.h`.

### 47.17.2.3 `int count_words ( std::string str )`

Words are defined as groups of characters separated by whitespace, where whitespace is any combination of adjacent spaces, tabs, carriage returns, etc. On most systems, whitespace is usually defined as any character corresponding to the integers 9 (horizontal tab), 10 (line feed), 11 (vertical tab), 12 (form feed), 13 (carriage return), and 32 (space bar). The test program `misc_ts` enumerates the characters between 0 and 255 (inclusive) that count as whitespace for this purpose.

Note that this function is used in `text_in_file::string_in` to perform string input.



47.17.2.4 `int remove_whitespace ( std::string & s )`

This function removes all characters in `s` which correspond to the integer values 9, 10, 11, 12, 13, or 32.

47.17.2.5 `std::string binary_to_hex ( std::string s )`

This function proceeds from left to right, ignoring parts of the string that do not consist of sequences of four '1's or '0's.

47.17.2.6 `template<class type_t> int gsl_alloc_arrays ( size_t nv, size_t msize, const char * names[], type_t * ptrs[], std::string func_name )`

Allocate memory for `nv` vectors of size `msize` with names specified in `names` and function name `func_name` to produce pointers in `ptrs`. This function is used internally to allocate several vectors in succession, taking care to free memory and call the error handler when an allocation fails.

The caller must make sure that previously allocated memory will be freed and an error is thrown if this function returns a non-zero value.

This function is used, for example, in [gsl\\_miser](#).

Definition at line 290 of file `misc.h`.

47.17.2.7 `template<class type_t> int gsl_calloc_arrays ( size_t nv, size_t msize, const char * names[], type_t * ptrs[], std::string func_name, type_t val )`

The caller must make sure that previously allocated memory will be freed and an error is thrown if this function returns a non-zero value.

Definition at line 320 of file `misc.h`.

47.17.2.8 `int gsl_calloc_gvecs ( size_t nv, size_t msize, const char * names[], gsl_vector *** ptrs, std::string func_name )`

The caller must make sure that previously allocated memory will be freed and an error is thrown if this function returns a non-zero value.

47.17.2.9 `double quadratic_extremum_x ( double x1, double x2, double x3, double y1, double y2, double y3 )`

**Idea for Future** Make a function `quadratic_points(double x1, double x2, double x3, double y1, double y2, double y3, double &a, double &b, double &c)?`

**Idea for Future** Make a `quadratic_extremum_xy()`?

47.18 `omatrix_cx_tlate.h` File Reference

File for definitions of complex matrices.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <o2scl/err_hnd.h> #include <gsl/gsl_matrix.h> #include <gsl/gsl_complex.h> #include
<o2scl/ovector_tlate.h> #include <o2scl/ovector_cx_tlate.h>
```

## 47.18.1 Detailed Description

Definition in file [omatrix\\_cx\\_tlate.h](#).

## Data Structures

- class `omatrix_cx_view_tlate< data_t, parent_t, block_t, complex_t >`  
A matrix view of double-precision numbers.
- class `omatrix_cx_tlate< data_t, parent_t, block_t, complex_t >`

*A matrix of double-precision numbers.*

- class `omatrix_cx_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`  
*Create a vector from a row of a matrix.*
- class `omatrix_cx_const_row_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`  
*Create a vector from a row of a matrix.*
- class `omatrix_cx_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`  
*Create a vector from a column of a matrix.*
- class `omatrix_cx_const_col_tlate< data_t, mparent_t, vparent_t, block_t, complex_t >`  
*Create a vector from a column of a matrix.*

## Typedefs

- typedef `omatrix_cx_tlate` < double, gsl\_matrix\_complex, gsl\_block\_complex, gsl\_complex > `omatrix_cx`  
*omatrix\_cx typedef*
- typedef `omatrix_cx_view_tlate` < double, gsl\_matrix\_complex, gsl\_block\_complex, gsl\_complex > `omatrix_cx_view`  
*omatrix\_cx\_view typedef*
- typedef `omatrix_cx_row_tlate` < double, gsl\_matrix\_complex, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > `omatrix_cx_row`  
*omatrix\_cx\_row typedef*
- typedef `omatrix_cx_col_tlate` < double, gsl\_matrix\_complex, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > `omatrix_cx_col`  
*omatrix\_cx\_col typedef*
- typedef `omatrix_cx_const_row_tlate` < double, gsl\_matrix\_complex, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > `omatrix_cx_const_row`  
*omatrix\_cx\_const\_row typedef*
- typedef `omatrix_cx_const_col_tlate` < double, gsl\_matrix\_complex, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > `omatrix_cx_const_col`  
*omatrix\_cx\_const\_col typedef*

## 47.19 `omatrix_tlate.h` File Reference

File for definitions of matrices.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <gsl/gsl_matrix.h> #include <gsl/gsl_ieee_utils.h> #include <o2scl/err_hnd.h> ×
#include <o2scl/ovector_tlate.h> #include <o2scl/array.h>
```

### 47.19.1 Detailed Description

**Idea for Future** The `xmatrix` class demonstrates how `operator[]` could return an `ovector_array` object and thus provide more bounds-checking. This would demand including a new parameter in `omatrix_view_tlate` which contains the vector type.

Definition in file `omatrix_tlate.h`.

## Data Structures

- class `omatrix_const_view_tlate< data_t, mparent_t, block_t >`  
*A const matrix view of omatrix objects.*
- class `omatrix_base_tlate< data_t, mparent_t, block_t >`  
*A base class for omatrix and omatrix\_view.*
- class `omatrix_view_tlate< data_t, mparent_t, block_t >`  
*A matrix view of double-precision numbers.*
- class `omatrix_tlate< data_t, mparent_t, vparent_t, block_t >`  
*A matrix of double-precision numbers.*
- class `omatrix_array_tlate< data_t, mparent_t, block_t >`

- Create a matrix from an array.
- class [omatrix\\_row\\_tlate](#)< data\_t, mparent\_t, vparent\_t, block\_t >  
Create a vector from a row of a matrix.
- class [omatrix\\_const\\_row\\_tlate](#)< data\_t, mparent\_t, vparent\_t, block\_t >  
Create a const vector from a row of a matrix.
- class [omatrix\\_col\\_tlate](#)< data\_t, mparent\_t, vparent\_t, block\_t >  
Create a vector from a column of a matrix.
- class [omatrix\\_const\\_col\\_tlate](#)< data\_t, mparent\_t, vparent\_t, block\_t >  
Create a const vector from a column of a matrix.
- class [omatrix\\_diag\\_tlate](#)< data\_t, mparent\_t, vparent\_t, block\_t >  
Create a vector from the main diagonal.
- class [omatrix\\_const\\_diag\\_tlate](#)< data\_t, mparent\_t, vparent\_t, block\_t >  
Create a vector from the main diagonal.
- class [omatrix\\_alloc](#)  
A simple class to provide an [allocate\(\)](#) function for [omatrix](#).
- class [ofmatrix](#)< N, M >
- class [xmatrix](#)  
A version of [omatrix](#) with better error checking.

## Typedefs

- typedef [omatrix\\_tlate](#)< double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix](#)  
*omatrix typedef*
- typedef [omatrix\\_view\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_block](#) > [omatrix\\_view](#)  
*omatrix\_view typedef*
- typedef [omatrix\\_const\\_view\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_block](#) > [omatrix\\_const\\_view](#)  
*omatrix\_const\_view typedef*
- typedef [omatrix\\_base\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_block](#) > [omatrix\\_base](#)  
*omatrix\_base typedef*
- typedef [omatrix\\_row\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix\\_row](#)  
*omatrix\_row typedef*
- typedef [omatrix\\_col\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix\\_col](#)  
*omatrix\_col typedef*
- typedef [omatrix\\_const\\_row\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix\\_const\\_row](#)  
*omatrix\_const\_row typedef*
- typedef [omatrix\\_const\\_col\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix\\_const\\_col](#)  
*omatrix\_const\_col typedef*
- typedef [omatrix\\_diag\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix\\_diag](#)  
*omatrix\_diag typedef*
- typedef [omatrix\\_const\\_diag\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [omatrix\\_const\\_diag](#)  
*omatrix\_const\_diag typedef*
- typedef [omatrix\\_array\\_tlate](#) < double, [gsl\\_matrix](#), [gsl\\_block](#) > [omatrix\\_array](#)  
*omatrix\_array typedef*
- typedef [omatrix\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int](#)  
*omatrix\_int typedef*
- typedef [omatrix\\_view\\_tlate](#) < int, [gsl\\_matrix\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_view](#)  
*omatrix\_int\_view typedef*
- typedef [omatrix\\_base\\_tlate](#) < int, [gsl\\_matrix\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_base](#)  
*omatrix\_int\_base typedef*
- typedef [omatrix\\_const\\_view\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_const\\_view](#)  
*omatrix\_int\_const\_view typedef*
- typedef [omatrix\\_row\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_row](#)  
*omatrix\_int\_row typedef*
- typedef [omatrix\\_col\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_col](#)  
*omatrix\_int\_col typedef*
- typedef [omatrix\\_const\\_row\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_const\\_row](#)  
*omatrix\_int\_const\_row typedef*
- typedef [omatrix\\_const\\_col\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_const\\_col](#)  
*omatrix\_int\_const\_col typedef*
- typedef [omatrix\\_diag\\_tlate](#) < int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_diag](#)

- omatrix\_int\_diag typedef*
- typedef [omatrix\\_const\\_diag\\_tlate](#)< int, [gsl\\_matrix\\_int](#), [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_const\\_diag](#)  
*omatrix\_int\_const\_diag typedef*
- typedef [omatrix\\_array\\_tlate](#) < int, [gsl\\_matrix\\_int](#), [gsl\\_block\\_int](#) > [omatrix\\_int\\_array](#)  
*omatrix\_int\_array typedef*

## Functions

- template<class data\_t, class parent\_t, class block\_t >  
std::ostream & [operator<<](#) (std::ostream &os, const [omatrix\\_const\\_view\\_tlate](#)< data\_t, parent\_t, block\_t > &v)  
*A operator for output of omatrix objects.*

## 47.19.2 Function Documentation

47.19.2.1 `template<class data_t, class parent_t, class block_t > std::ostream& operator<< ( std::ostream & os, const omatrix\_const\_view\_tlate< data_t, parent_t, block_t > & v )`

This outputs all of the matrix elements. Each row is output with an newline character at the end of each row. Positive values are preceded by an extra space. A 2x2 example:

```
-3.751935e-05 -6.785864e-04
-6.785864e-04 1.631984e-02
```

The function `gsl_ieee_double_to_rep()` is used to determine the sign of a number, so that "-0.0" as distinct from "+0.0" is handled correctly.

**Idea for Future** This assumes that scientific mode is on and showpos is off. It'd be nice to fix this.

Definition at line 1284 of file `omatrix_tlate.h`.

## 47.20 ovector\_cx\_tlate.h File Reference

File for definitions of complex vectors.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream>
#include <vector> #include <complex> #include <o2scl/err_hnd.h> #include <o2scl/ovector-
_tlate.h> #include <gsl/gsl_vector.h> #include <gsl/gsl_complex.h>
```

## 47.20.1 Detailed Description

Definition in file `ovector_cx_tlate.h`.

## Data Structures

- class [ovector\\_cx\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*A vector view of double-precision numbers.*
- class [ovector\\_cx\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*A vector of double-precision numbers.*
- class [ovector\\_cx\\_array\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*Create a vector from an array.*
- class [ovector\\_cx\\_array\\_stride\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*Create a vector from an array with a stride.*
- class [ovector\\_cx\\_subvector\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >

*Create a vector from a subvector of another.*

- class [ovector\\_cx\\_const\\_array\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*Create a vector from an array.*
- class [ovector\\_cx\\_const\\_array\\_stride\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*Create a vector from an array\_stride.*
- class [ovector\\_cx\\_const\\_subvector\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t >  
*Create a vector from a subvector of another.*
- class [ovector\\_cx\\_real\\_tlate](#)< data\_t, vparent\_t, block\_t, cvparent\_t, cblock\_t, complex\_t >  
*Create a real vector from the real parts of a complex vector.*
- class [ovector\\_cx\\_imag\\_tlate](#)< data\_t, vparent\_t, block\_t, cvparent\_t, cblock\_t, complex\_t >  
*Create a imaginary vector from the imaginary parts of a complex vector.*
- class [ofvector\\_cx](#)< N >  
*A complex vector where the memory allocation is performed in the constructor.*

## Typedefs

- typedef [ovector\\_cx\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx](#)  
*ovector\_cx typedef*
- typedef [ovector\\_cx\\_view\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_view](#)  
*ovector\_cx\_view typedef*
- typedef [ovector\\_cx\\_array\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_array](#)  
*ovector\_cx\_array typedef*
- typedef [ovector\\_cx\\_array\\_stride\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_array\\_stride](#)  
*ovector\_cx\_array\_stride typedef*
- typedef [ovector\\_cx\\_subvector\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_subvector](#)  
*ovector\_cx\_subvector typedef*
- typedef [ovector\\_cx\\_const\\_array\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_const\\_array](#)  
*ovector\_cx\_const\_array typedef*
- typedef [ovector\\_cx\\_const\\_array\\_stride\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_const\\_array\\_stride](#)  
*ovector\_cx\_const\_array\_stride typedef*
- typedef [ovector\\_cx\\_const\\_subvector\\_tlate](#) < double, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_const\\_subvector](#)  
*ovector\_cx\_const\_subvector typedef*
- typedef [ovector\\_cx\\_real\\_tlate](#) < double, gsl\_vector, gsl\_block, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_real](#)  
*ovector\_cx\_real typedef*
- typedef [ovector\\_cx\\_imag\\_tlate](#) < double, gsl\_vector, gsl\_block, gsl\_vector\_complex, gsl\_block\_complex, gsl\_complex > [ovector\\_cx\\_imag](#)  
*ovector\_cx\_imag typedef*

## Functions

- template<class data\_t, class vparent\_t, class block\_t, class complex\_t >  
[ovector\\_cx\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t > [conjugate](#) ([ovector\\_cx\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t > &v)  
*Conjugate a vector.*
- template<class data\_t, class vparent\_t, class block\_t, class complex\_t >  
std::ostream & [operator<<](#) (std::ostream &os, const [ovector\\_cx\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t, complex\_t > &v)  
*A operator for naive vector output.*

## 47.20.2 Function Documentation

47.20.2.1 `template<class data_t, class vparent_t, class block_t, class complex_t> std::ostream& operator<< ( std::ostream & os, const ovector_cx_view_tlate< data_t, vparent_t, block_t, complex_t > & v )`

This outputs all of the vector elements in the form (r,i). All of these are separated by one space character, though no trailing space or endl is sent to the output.

Definition at line 1066 of file ovector\_cx\_tlate.h.

## 47.21 ovector\_rev\_tlate.h File Reference

File for definitions of reversed vectors.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <vector> #include <gsl/gsl_vector.h> #include <o2scl/err_hnd.h> #include <o2scl/string-
_conv.h> #include <o2scl/ovector_tlate.h> #include <o2scl/array.h> #include <o2scl/vector.-
h>
```

## 47.21.1 Detailed Description

Definition in file [ovector\\_rev\\_tlate.h](#).

## Data Structures

- class [ovector\\_reverse\\_tlate< data\\_t, vparent\\_t, block\\_t >](#)  
*Reversed view of a vector.*
- class [ovector\\_const\\_reverse\\_tlate< data\\_t, vparent\\_t, block\\_t >](#)  
*Reversed view of a vector.*
- class [ovector\\_subvector\\_reverse\\_tlate< data\\_t, vparent\\_t, block\\_t >](#)  
*Reversed view of a subvector.*
- class [ovector\\_const\\_subvector\\_reverse\\_tlate< data\\_t, vparent\\_t, block\\_t >](#)  
*Reversed view of a const subvector.*

## Typedefs

- typedef [ovector\\_reverse\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_reverse](#)  
*ovector\_reverse typedef*
- typedef [ovector\\_const\\_reverse\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_const\\_reverse](#)  
*ovector\_const\_reverse typedef*
- typedef [ovector\\_subvector\\_reverse\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_subvector\\_reverse](#)  
*ovector\_subvector\_reverse typedef*
- typedef [ovector\\_const\\_subvector\\_reverse\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_const\\_subvector\\_reverse](#)  
*ovector\_const\_subvector\_reverse typedef*
- typedef [ovector\\_reverse\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_reverse](#)  
*ovector\_int\_reverse typedef*
- typedef [ovector\\_const\\_reverse\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_const\\_reverse](#)  
*ovector\_int\_const\_reverse typedef*
- typedef [ovector\\_subvector\\_reverse\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_subvector\\_reverse](#)  
*ovector\_int\_subvector\_reverse typedef*
- typedef [ovector\\_const\\_subvector\\_reverse\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_const\\_subvector\\_reverse](#)  
*ovector\_int\_const\_subvector\_reverse typedef*

## 47.22 ovector\_tlate.h File Reference

File for definitions of vectors.

```
#include <iostream> #include <cstdlib> #include <cmath> #include <string> #include <fstream> ×
#include <sstream> #include <vector> #include <gsl/gsl_vector.h> #include <gsl/gsl_sys.-
h> #include <o2scl/err_hnd.h> #include <o2scl/string_conv.h> #include <o2scl/uvector_tlate.-
h> #include <o2scl/array.h> #include <o2scl/vector.h>
```

### 47.22.1 Detailed Description

**Idea for Future** Clean up maybe by moving, for example, ovector reverse classes to a different header file

**Idea for Future** Define ovector\_uint classes?

Definition in file [ovector\\_tlate.h](#).

### Data Structures

- class [gsl\\_vector\\_norm](#)  
*Norm object for gsl vectors.*
- class [ovector\\_const\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*A const vector view with finite stride.*
- class [ovector\\_const\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t >::const\_iterator  
*A const iterator for ovector.*
- class [ovector\\_const\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t >::iterator  
*An iterator for ovector.*
- class [ovector\\_base\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*A base class for ovector and ovector\_view.*
- class [ovector\\_view\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*A vector view with finite stride.*
- class [ovector\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*A vector with finite stride.*
- class [ovector\\_array\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*Create a vector from an array.*
- class [ovector\\_array\\_stride\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*Create a vector from an array with a stride.*
- class [ovector\\_subvector\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*Create a vector from a subvector of another.*
- class [ovector\\_const\\_array\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*Create a const vector from an array.*
- class [ovector\\_const\\_array\\_stride\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*Create a const vector from an array with a stride.*
- class [ovector\\_const\\_subvector\\_tlate](#)< data\_t, vparent\_t, block\_t >  
*Create a const vector from a subvector of another vector.*
- class [ovector\\_alloc](#)  
*A simple class to provide an `allocate()` function for ovector.*
- class [ovector\\_int\\_alloc](#)  
*A simple class to provide an `allocate()` function for ovector\_int.*
- class [ofvector](#)< N >  
*A vector where the memory allocation is performed in the constructor.*

### Typedefs

- typedef [ovector\\_tlate](#)< double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector](#)  
*ovector typedef*
- typedef [ovector\\_base\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_base](#)

- ovector\_base* typedef
- typedef [ovector\\_view\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_view](#)  
*ovector\_view* typedef
- typedef [ovector\\_const\\_view\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_const\\_view](#)  
*ovector\_const\_view* typedef
- typedef [ovector\\_array\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_array](#)  
*ovector\_array* typedef
- typedef [ovector\\_array\\_stride\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_array\\_stride](#)  
*ovector\_array\_stride* typedef
- typedef [ovector\\_subvector\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_subvector](#)  
*ovector\_subvector* typedef
- typedef [ovector\\_const\\_array\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_const\\_array](#)  
*ovector\_const\_array* typedef
- typedef [ovector\\_const\\_array\\_stride\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_const\\_array\\_stride](#)  
*ovector\_const\_array\_stride* typedef
- typedef [ovector\\_const\\_subvector\\_tlate](#) < double, [gsl\\_vector\\_norm](#), [gsl\\_block](#) > [ovector\\_const\\_subvector](#)  
*ovector\_const\_subvector* typedef
- typedef [ovector\\_tlate](#)< int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int](#)  
*ovector\_int* typedef
- typedef [ovector\\_base\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_base](#)  
*ovector\_int\_base* typedef
- typedef [ovector\\_view\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_view](#)  
*ovector\_int\_view* typedef
- typedef [ovector\\_const\\_view\\_tlate](#)< int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_const\\_view](#)  
*ovector\_int\_const\_base* typedef
- typedef [ovector\\_array\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_array](#)  
*ovector\_int\_array* typedef
- typedef [ovector\\_array\\_stride\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_array\\_stride](#)  
*ovector\_int\_array\_stride* typedef
- typedef [ovector\\_subvector\\_tlate](#)< int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_subvector](#)  
*ovector\_int\_subvector* typedef
- typedef [ovector\\_const\\_array\\_tlate](#)< int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_const\\_array](#)  
*ovector\_int\_const\_array* typedef
- typedef [ovector\\_const\\_array\\_stride\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_const\\_array\\_stride](#)  
*ovector\_int\_const\_array\_stride* typedef
- typedef [ovector\\_const\\_subvector\\_tlate](#) < int, [gsl\\_vector\\_int](#), [gsl\\_block\\_int](#) > [ovector\\_int\\_const\\_subvector](#)  
*ovector\_int\_const\_subvector* typedef

## Functions

- `template<class data_t, class vparent_t, class block_t >`  
`std::ostream & operator<< (std::ostream &os, const ovector\_const\_view\_tlate< data_t, vparent_t, block_t > &v)`  
*A operator for naive vector output.*

## 47.22.2 Function Documentation

- 47.22.2.1 `template<class data_t, class vparent_t, class block_t > std::ostream& operator<< ( std::ostream & os, const ovector\_const\_view\_tlate< data_t, vparent_t, block_t > & v )`

This outputs all of the vector elements. All of these are separated by one space character, though no trailing space or `endl` is sent to the output. If the vector is empty, nothing is done.

Definition at line 1845 of file `ovector_tlate.h`.



## 47.23 permutation.h File Reference

File containing permutation class and associated functions.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <vector> #include <gsl/gsl_vector.h> #include <gsl/gsl_permutation.h> #include
<o2scl/err_hnd.h> #include <o2scl/string_conv.h> #include <o2scl/uvector_tlate.h> #include
<o2scl/array.h> #include <o2scl/vector.h>
```

### 47.23.1 Detailed Description

Definition in file [permutation.h](#).

#### Data Structures

- class [permutation](#)  
*A class for representing permutations.*

#### Functions

- `std::ostream & operator<< (std::ostream &os, const permutation &p)`  
*Output operator for permutations.*

### 47.23.2 Function Documentation

#### 47.23.2.1 `std::ostream& operator<< ( std::ostream & os, const permutation & p )`

A space is output between the permutation elements but no space or newline character is output after the last element.

If the size is zero, this function outputs nothing and does not call the error handler.

## 47.24 poly.h File Reference

Classes for solving polynomials.

```
#include <iostream> #include <complex> #include <gsl/gsl_math.h> #include <gsl/gsl_complex-
_math.h> #include <gsl/gsl_complex.h> #include <gsl/gsl_poly.h> #include <o2scl/constants.-
h> #include <o2scl/err_hnd.h>
```

### 47.24.1 Detailed Description

#### Warning

One must be careful about using `pow()` in functions using `complex<double>` since `pow(((complex<double>)0.0),3.0)` returns `(nan,nan)`. Instead, we should use `pow(((complex<double>)0.0),3)` which takes an integer for the second argument. The `sqrt()` function, always succeeds i.e. `sqrt(((complex<double>)0.0))=0.0`

**Idea for Future** The quartics are tested only for `a4=1`, which should probably be generalized.

Definition in file [poly.h](#).

## Data Structures

- class [quadratic\\_real](#)  
Solve a quadratic polynomial with real coefficients and real roots [abstract base].
- class [quadratic\\_real\\_coeff](#)  
Solve a quadratic polynomial with real coefficients and complex roots [abstract base].
- class [quadratic\\_complex](#)  
Solve a quadratic polynomial with complex coefficients and complex roots [abstract base].
- class [cubic\\_real](#)  
Solve a cubic polynomial with real coefficients and real roots [abstract base].
- class [cubic\\_real\\_coeff](#)  
Solve a cubic polynomial with real coefficients and complex roots [abstract base].
- class [cubic\\_complex](#)  
Solve a cubic polynomial with complex coefficients and complex roots [abstract base].
- class [quartic\\_real](#)  
Solve a quartic polynomial with real coefficients and real roots [abstract base].
- class [quartic\\_real\\_coeff](#)  
Solve a quartic polynomial with real coefficients and complex roots [abstract base].
- class [quartic\\_complex](#)  
Solve a quartic polynomial with complex coefficients and complex roots [abstract base].
- class [poly\\_real\\_coeff](#)  
Solve a general polynomial with real coefficients and complex roots [abstract base].
- class [poly\\_complex](#)  
Solve a general polynomial with complex coefficients [abstract base].
- class [cern\\_cubic\\_real\\_coeff](#)  
Solve a cubic with real coefficients and complex roots (CERNLIB)
- class [cern\\_quartic\\_real\\_coeff](#)  
Solve a quartic with real coefficients and complex roots (CERNLIB)
- class [gsl\\_quadratic\\_real\\_coeff](#)  
Solve a quadratic with real coefficients and complex roots (GSL)
- class [gsl\\_cubic\\_real\\_coeff](#)  
Solve a cubic with real coefficients and complex roots (GSL)
- class [gsl\\_quartic\\_real](#)  
Solve a quartic with real coefficients and real roots (GSL)
- class [gsl\\_quartic\\_real2](#)  
Solve a quartic with real coefficients and real roots (GSL)
- class [gsl\\_poly\\_real\\_coeff](#)  
Solve a general polynomial with real coefficients (GSL)
- class [quadratic\\_std\\_complex](#)  
Solve a quadratic with complex coefficients and complex roots.
- class [cubic\\_std\\_complex](#)  
Solve a cubic with complex coefficients and complex roots.
- class [simple\\_quartic\\_real](#)  
Solve a quartic with real coefficients and real roots.
- class [simple\\_quartic\\_complex](#)  
Solve a quartic with complex coefficients and complex roots.

## 47.25 qr\_base.h File Reference

File for QR decomposition and associated solver.

```
#include <o2scl/householder.h> #include <o2scl/givens.h>
```

## 47.25.1 Detailed Description

Definition in file [qr\\_base.h](#).

## Namespaces

- namespace `o2scl_linalg`  
*The namespace for linear algebra classes and functions.*

## Functions

- template<class mat\_t, class vec\_t >  
void `o2scl_linalg::QR_decomp` (size\_t M, size\_t N, mat\_t &A, vec\_t &tau)  
*Compute the QR decomposition of matrix A.*
- template<class mat\_t, class vec\_t, class vec2\_t, class vec3\_t >  
void `o2scl_linalg::QR_solve` (size\_t N, const mat\_t &QR, const vec\_t &tau, const vec2\_t &b, vec3\_t &x)  
*Solve the system  $Ax = b$  using the QR factorization.*
- template<class mat\_t, class vec\_t, class vec2\_t >  
void `o2scl_linalg::QR_svx` (size\_t M, size\_t N, const mat\_t &QR, const vec\_t &tau, vec2\_t &x)  
*Solve the system  $Ax = b$  in place using the QR factorization.*
- template<class mat\_t, class vec\_t, class vec2\_t >  
void `o2scl_linalg::QR_QTvec` (const size\_t M, const size\_t N, const mat\_t &QR, const vec\_t &tau, vec2\_t &v)  
*Form the product  $Q^T v$  from a QR factorized matrix.*
- template<class mat1\_t, class mat2\_t, class mat3\_t, class vec\_t >  
void `o2scl_linalg::QR_unpack` (const size\_t M, const size\_t N, const mat1\_t &QR, const vec\_t &tau, mat2\_t &Q, mat3\_t &R)  
  
*Unpack the QR matrix to the individual Q and R components.*
- template<class mat1\_t, class mat2\_t, class vec1\_t, class vec2\_t >  
void `o2scl_linalg::QR_update` (size\_t M, size\_t N, mat1\_t &Q, mat2\_t &R, vec1\_t &w, vec2\_t &v)  
*Update a QR factorisation for  $A = QR$ ,  $A' = A + u v^T$ .*

## 47.26 smart\_interp.h File Reference

File for "smart" interpolation routines.

```
#include <o2scl/interp.h> #include <o2scl/vector.h>
```

## 47.26.1 Detailed Description

In addition to the smart interpolation routines, this file contains the template functions `vector_find_level()`, `vector_integ_linear()` and `vector_invert_enclosed_sum()`.

Definition in file `smart_interp.h`.

## Data Structures

- class `smart_interp< vec_t, svec_t >`  
*Smart interpolation class.*
- class `smart_interp_vec< vec_t, svec_t, alloc_vec_t, alloc_t >`  
*Smart interpolation class with pre-specified vectors.*
- class `sma_interp< n >`  
*A specialization of smart\_interp for C-style double arrays.*
- class `sma_interp_vec< arr_t >`  
*A specialization of smart\_interp\_vec for C-style double arrays.*

## Typedefs

- typedef `smart_interp< ovector_const_view, ovector_const_subvector > sm_interp`
- typedef `smart_interp_vec< ovector_const_view, ovector_const_subvector, ovector, ovector_alloc > sm_interp_vec`

## Functions

- `template<class vec_t, class vec2_t >`  
`int vector_find_level (double level, size_t n, vec_t &x, vec2_t &y, ovector &locs)`  
*Perform inverse linear interpolation.*
- `template<class vec_t >`  
`double vector_integ_linear (size_t n, vec_t &x, vec_t &y)`  
*Compute the integral over  $y(x)$  using linear interpolation.*
- `template<class vec_t >`  
`int vector_invert_enclosed_sum (double sum, size_t n, vec_t &x, vec_t &y, double &lev)`  
*Compute the endpoints which enclose the regions whose integral is equal to  $sum$ .*

## 47.26.2 Function Documentation

47.26.2.1 `template<class vec_t, class vec2_t > int vector_find_level ( double level, size_t n, vec_t &x, vec2_t &y, ovector &locs )`

This function performs inverse linear interpolation of the data defined by `x` and `y`, finding all points in `x` which have the property  $level = y(x)$ . All points for which this relation holds are put into the vector `locs`. The previous information contained in vector `locs` before the function call is destroyed.

This is the 1-dimensional analog of finding contour levels as the `contour` class does for 2 dimensions.

Definition at line 867 of file `smart_interp.h`.

47.26.2.2 `template<class vec_t > int vector_invert_enclosed_sum ( double sum, size_t n, vec_t &x, vec_t &y, double &lev )`

Defining a new function,  $g(y_0)$  which takes as input any  $y$ -value,  $y_0$  from the function  $y(x)$  (specified with the parameters `x` and `y`) and outputs the integral of the function  $y(x)$  over all regions where  $y(x) > y_0$ . This function inverts  $g(y)$ , taking the value of an integral as input, and returns the corresponding  $y$ -value in the variable `lev`.

In order to make sure that the interpretation of the integral is unambiguous, this function requires that the first and last values of `y` are equal, i.e. `y[0]==y[n-1]`.

This function is particularly useful, for example, in computing the region which defines 68% around a peak of data, thus providing approximate  $1\sigma$  limits.

Linear interpolation is used to describe the function  $g$ , and the precision of this function is limited by this assumption. This function may also sometimes fail if `sum` is very close to the minimum or maximum value of the function  $g$ .

Definition at line 938 of file `smart_interp.h`.

## 47.27 string\_conv.h File Reference

Various string conversion functions.

```
#include <iostream> #include <cmath> #include <string> #include <fstream> #include <sstream> ×
#include <o2scl/lib_settings.h> #include <gsl/gsl_ieee_utils.h>
```

## 47.27.1 Detailed Description

Definition in file `string_conv.h`.

## Functions

- `std::string ptos (void *p)`  
*Convert a pointer to a string.*
- `std::string itos (int x)`  
*Convert an integer to a string.*

- `std::string uitos (size_t x)`  
*Convert a size\_t to a string.*
- `std::string btos (bool b)`  
*Convert a boolean value to a string.*
- `std::string dtos (double x, int prec=6, bool auto_prec=false)`  
*Convert a double to a string.*
- `size_t size_of_exponent (double x)`  
*Returns the number of characters required to display the exponent of x in scientific mode.*
- `std::string dtos (double x, std::ostream &format)`  
*Convert a double to a string using a specified format.*
- `int stoi (std::string s, bool err_on_fail=true)`  
*Convert a string to an integer.*
- `size_t stoui (std::string s, bool err_on_fail=true)`  
*Convert a string to a size\_t.*
- `bool stob (std::string s, bool err_on_fail=true)`  
*Convert a string to a boolean value.*
- `double stod (std::string s, bool err_on_fail=true)`  
*Convert a string to a double.*
- `std::string double_to_ieee_string (const double *x)`  
*Convert a double to a string containing IEEE representation.*
- `bool has_minus_sign (double *x)`  
*Find out if the number pointed to by x has a minus sign.*
- `bool is_number (std::string s)`  
*Return true if the string s is likely a integral or floating point number.*

## 47.27.2 Function Documentation

### 47.27.2.1 std::string ptos ( void \* p )

This uses an `ostringstream` to convert a pointer to a string and is architecture-dependent.

### 47.27.2.2 std::string btos ( bool b )

This returns "1" for true and "0" for false.

### 47.27.2.3 std::string dtos ( double x, int prec = 6, bool auto\_prec = false )

If `auto_prec` is false, then the number is converted to a string in the `ios::scientific` mode, otherwise, neither the scientific or fixed mode flags are set and the number is converted to a string in "automatic" mode.

### 47.27.2.4 size\_t size\_of\_exponent ( double x )

This returns 2 or 3, depending on whether or not the absolute magnitude of the exponent is greater than or equal to 100. It uses `stringstream` to convert the number to a string and counts the number of characters directly.

### 47.27.2.5 int stoi ( std::string s, bool err\_on\_fail = true )

If `err_on_fail` is true and the conversion fails, this function calls the error handler, otherwise this function just returns zero.

### 47.27.2.6 size\_t stoui ( std::string s, bool err\_on\_fail = true )

If `err_on_fail` is true and the conversion fails, this function calls the error handler, otherwise this function just returns zero.

### 47.27.2.7 bool stob ( std::string s, bool err\_on\_fail = true )

This returns true if only if the string has at least one character and the first non-whitespace character is either `t`, `T`, or one of the numbers 1 through 9.

If `err_on_fail` is true and the conversion fails, this function calls the error handler, otherwise this function just returns false.

47.27.2.8 `double stod ( std::string s, bool err_on_fail = true )`

If `err_on_fail` is true and the conversion fails, this function calls the error handler, otherwise this function just returns 0.0.

47.27.2.9 `std::string double_to_ieee_string ( const double * x )`

Modeled after the GSL function `gsl_ieee_fprintf_double()`, but converts to a string instead of a FILE \*.

47.27.2.10 `bool has_minus_sign ( double * x )`

This function returns true if the number pointed to by `x` has a minus sign using the GSL IEEE functions. It is useful, for example, in distinguishing "-0.0" from "+0.0".

47.27.2.11 `bool is_number ( std::string s )`

#### Note

The test employed is not exhaustive and this function may return `true` for some numbers and may return `false` for some non-numbers.

## 47.28 svdstep\_base.h File Reference

File for SVD decomposition.

### 47.28.1 Detailed Description

Definition in file [svdstep\\_base.h](#).

#### Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*

#### Functions

- `template<class vec_t, class vec2_t >`  
`int o2scl_linalg::chop_small_elements (size_t N, vec_t &d, vec2_t &f)`  
*Desc.*
- `template<class vec_t, class vec2_t >`  
`double o2scl_linalg::trailing_eigenvalue (size_t n, const vec_t &d, const vec_t &f)`  
*Desc.*
- `int o2scl_linalg::create_schur (double d0, double f0, double d1, double &c, double &s)`  
*Desc.*
- `template<class vec_t, class vec2_t, class mat_t, class mat2_t >`  
`int o2scl_linalg::svd2 (size_t M, size_t N, vec_t &d, vec2_t &f, mat_t &U, mat2_t &V)`  
*Desc.*
- `template<class vec_t, class vec2_t, class mat_t >`  
`int o2scl_linalg::chase_out_intermediate_zero (size_t M, size_t n, vec_t &d, vec2_t &f, mat_t &U, size_t k0)`  
*Desc.*
- `template<class vec_t, class vec2_t, class mat_t >`  
`int o2scl_linalg::chase_out_trailing_zero (size_t N, size_t n, vec_t &d, vec2_t &f, mat_t &V)`  
*Desc.*
- `template<class vec_t, class vec2_t, class mat_t, class mat2_t >`  
`int o2scl_linalg::qrstep (size_t M, size_t N, size_t n, vec_t &d, vec2_t &f, mat_t &U, mat2_t &V)`  
*Desc.*

## 47.29 **tensor.h** File Reference

File for definitions of tensors.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <gsl/gsl_matrix.h> #include <gsl/gsl_ieee_utils.h> #include <o2scl/err_hnd.h> ×
#include <o2scl/uvectortlate.h> #include <o2scl/umatrictlate.h> #include <o2scl/smart-
_interp.h>
```

### 47.29.1 Detailed Description

Definition in file [tensor.h](#).

#### Data Structures

- class [tensor](#)  
*Tensor class with arbitrary dimensions.*
- class [tensor\\_grid](#)  
*Tensor class with arbitrary dimensions with a grid.*
- class [tensor1](#)  
*Rank 1 tensor.*
- class [tensor\\_grid1](#)  
*Rank 1 tensor with a grid.*
- class [tensor2](#)  
*Rank 2 tensor.*
- class [tensor\\_grid2](#)  
*Rank 2 tensor with a grid.*
- class [tensor3](#)  
*Rank 3 tensor.*
- class [tensor\\_grid3](#)  
*Rank 3 tensor with a grid.*
- class [tensor4](#)  
*Rank 4 tensor.*
- class [tensor\\_grid4](#)  
*Rank 4 tensor with a grid.*

## 47.30 **tensor\_old.h** File Reference

File for definitions of tensor\_olds.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <gsl/gsl_matrix.h> #include <gsl/gsl_ieee_utils.h> #include <o2scl/err_hnd.h> ×
#include <o2scl/uvectortlate.h> #include <o2scl/umatrictlate.h> #include <o2scl/smart-
_interp.h>
```

### 47.30.1 Detailed Description

Definition in file [tensor\\_old.h](#).

#### Data Structures

- class [tensor\\_old](#)  
*Tensor\_Old class with arbitrary dimensions.*
- class [tensor\\_old\\_grid](#)  
*Tensor\_Old class with arbitrary dimensions with a grid.*

- class [tensor\\_old1](#)  
*Rank 1 [tensor\\_old](#).*
- class [tensor\\_old\\_grid1](#)  
*Rank 2 [tensor\\_old](#) with a grid.*
- class [tensor\\_old2](#)  
*Rank 2 [tensor\\_old](#).*
- class [tensor\\_old\\_grid2](#)  
*Rank 2 [tensor\\_old](#) with a grid.*
- class [tensor\\_old3](#)  
*Rank 3 [tensor\\_old](#).*
- class [tensor\\_old\\_grid3](#)  
*Rank 3 [tensor\\_old](#) with a grid.*
- class [tensor\\_old4](#)  
*Rank 4 [tensor\\_old](#).*
- class [tensor\\_old\\_grid4](#)  
*Rank 4 [tensor\\_old](#) with a grid.*

## 47.31 tridiag\_base.h File Reference

File for solving tridiagonal systems.

```
#include <o2scl/array.h> #include <o2scl/uvector_tlate.h>
```

### 47.31.1 Detailed Description

Definition in file [tridiag\\_base.h](#).

#### Data Structures

- class [o2scl\\_linalg::pointer\\_2\\_mem](#)  
*Allocation object for 2 C-style arrays of equal size.*
- class [o2scl\\_linalg::pointer\\_4\\_mem](#)  
*Allocation object for 4 C-style arrays of equal size.*
- class [o2scl\\_linalg::pointer\\_5\\_mem](#)  
*Allocation object for 5 C-style arrays of equal size.*
- class [o2scl\\_linalg::uvector\\_2\\_mem](#)  
*Allocation object for 2 arrays of equal size.*
- class [o2scl\\_linalg::uvector\\_4\\_mem](#)  
*Allocation object for 4 arrays of equal size.*
- class [o2scl\\_linalg::uvector\\_5\\_mem](#)  
*Allocation object for 5 arrays of equal size.*

#### Namespaces

- namespace [o2scl\\_linalg](#)  
*The namespace for linear algebra classes and functions.*

#### Functions

- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class mem\_t, class mem\_vec\_t >  
void [o2scl\\_linalg::solve\\_tridiag\\_sym](#) (const vec\_t &diag, const vec2\_t &offdiag, const vec3\_t &b, vec4\_t &x, size\_t N, mem\_t &m)  
*Solve a symmetric tridiagonal linear system with user-specified memory.*
- template<class vec\_t, class vec2\_t, class vec3\_t, class vec4\_t, class vec5\_t, class mem\_t, class mem\_vec\_t >  
void [o2scl\\_linalg::solve\\_tridiag\\_nonsym](#) (const vec\_t &diag, const vec2\_t &abovediag, const vec3\_t &belowdiag, const vec4\_t &rhs, vec5\_t &x, size\_t N, mem\_t &m)



*Solve an asymmetric tridiagonal linear system with user-specified memory.*

- `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class mem_t, class mem_vec_t >`  
`void o2scl_linalg::solve_cyc_tridiag_sym (const vec_t &diag, const vec2_t &offdiag, const vec3_t &b, vec4_t &x, size_t N, mem_t &m)`

*Solve a symmetric cyclic tridiagonal linear system with user specified memory.*

- `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class vec5_t, class mem_t, class mem_vec_t >`  
`void o2scl_linalg::solve_cyc_tridiag_nonsym (const vec_t &diag, const vec2_t &abovediag, const vec3_t &belowdiag, const vec4_t &rhs, vec5_t &x, size_t N, mem_t &m)`

*Solve an asymmetric cyclic tridiagonal linear system with user-specified memory.*

- `template<class vec_t, class vec2_t, class vec3_t, class vec4_t >`  
`void o2scl_linalg::solve_tridiag_sym (const vec_t &diag, const vec2_t &offdiag, const vec3_t &b, vec4_t &x, size_t N)`

*Solve a symmetric tridiagonal linear system.*

- `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class vec5_t >`  
`void o2scl_linalg::solve_tridiag_nonsym (const vec_t &diag, const vec2_t &abovediag, const vec3_t &belowdiag, const vec4_t &rhs, vec5_t &x, size_t N)`

*Solve an asymmetric tridiagonal linear system.*

- `template<class vec_t, class vec2_t, class vec3_t, class vec4_t >`  
`void o2scl_linalg::solve_cyc_tridiag_sym (const vec_t &diag, const vec2_t &offdiag, const vec3_t &b, vec4_t &x, size_t N)`

*Solve a symmetric cyclic tridiagonal linear system.*

- `template<class vec_t, class vec2_t, class vec3_t, class vec4_t, class vec5_t >`  
`void o2scl_linalg::solve_cyc_tridiag_nonsym (const vec_t &diag, const vec2_t &abovediag, const vec3_t &belowdiag, const vec4_t &rhs, vec5_t &x, size_t N)`

*Solve an asymmetric cyclic tridiagonal linear system.*

## 47.32 umatrix\_cx\_tlate.h File Reference

File for definitions of matrices.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <gsl/gsl_matrix.h> #include <gsl/gsl_ieee_utils.h> #include <o2scl/err_hnd.h> ×
#include <o2scl/uvector_tlate.h> #include <o2scl/uvector_cx_tlate.h>
```

### 47.32.1 Detailed Description

Definition in file [umatrix\\_cx\\_tlate.h](#).

#### Data Structures

- class [umatrix\\_cx\\_view\\_tlate< data\\_t, complex\\_t >](#)  
*A matrix view of complex numbers.*
- class [umatrix\\_cx\\_tlate< data\\_t, complex\\_t >](#)  
*A matrix of double-precision numbers.*
- class [umatrix\\_cx\\_row\\_tlate< data\\_t, complex\\_t >](#)  
*Create a vector from a row of a matrix.*
- class [umatrix\\_cx\\_const\\_row\\_tlate< data\\_t, complex\\_t >](#)  
*Create a const vector from a row of a matrix.*
- class [umatrix\\_cx\\_alloc](#)  
*A simple class to provide an [allocate\(\)](#) function for [umatrix\\_cx](#).*
- class [ufmatrix\\_cx< N, M >](#)  
*A matrix where the memory allocation is performed in the constructor.*

#### Typedefs

- `typedef umatrix\_cx\_tlate < double, gsl_complex > umatrix\_cx`  
*umatrix\_cx typedef*

- typedef [umatrix\\_cx\\_view\\_tlate](#) < double, gsl\_complex > [umatrix\\_cx\\_view](#)  
*umatrix\_cx\_view typedef*
- typedef [umatrix\\_cx\\_row\\_tlate](#) < double, gsl\_complex > [umatrix\\_cx\\_row](#)  
*umatrix\_cx\_row typedef*
- typedef [umatrix\\_cx\\_const\\_row\\_tlate](#) < double, gsl\_complex > [umatrix\\_cx\\_const\\_row](#)  
*umatrix\_cx\_const\_row typedef*

## Functions

- template<class data\_t, class complex\_t >  
std::ostream & [operator<<](#) (std::ostream &os, const [umatrix\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > &v)  
*A operator for naive matrix output.*

## 47.32.2 Function Documentation

**47.32.2.1** template<class data\_t, class complex\_t > std::ostream& [operator<<](#) ( std::ostream & os, const [umatrix\\_cx\\_view\\_tlate](#)< data\_t, complex\_t > & v )

This outputs all of the matrix elements. Each row is output with an newline character at the end of each row. Positive values are preceded by an extra space. A 2x2 example:

```
-3.751935e-05 -6.785864e-04
-6.785864e-04  1.631984e-02
```

The function `gsl_ieee_double_to_rep()` is used to determine the sign of a number, so that "-0.0" as distinct from "+0.0" is handled correctly.

## Note

At the moment, this function assumes that scientific mode is on and `showpos` is off.

**Idea for Future** Make this function work even when scientific mode is not on, either by converting to scientific mode and converting back, or by leaving scientific mode off and padding with spaces

Definition at line 671 of file `umatrix_cx_tlate.h`.

## 47.33 umatrix\_tlate.h File Reference

File for definitions of matrices.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <gsl/gsl_matrix.h> #include <gsl/gsl_ieee_utils.h> #include <o2scl/err_hnd.h> ×
#include <o2scl/uvectors_tlate.h>
```

## 47.33.1 Detailed Description

Definition in file [umatrix\\_tlate.h](#).

## Data Structures

- class [umatrix\\_const\\_view\\_tlate](#)< data\_t >  
*A matrix view of double-precision numbers.*
- class [umatrix\\_base\\_tlate](#)< data\_t >

- *A matrix view of double-precision numbers.*  
class [umatrix\\_view\\_tlate< data\\_t >](#)
- *A matrix view of double-precision numbers.*  
class [umatrix\\_tlate< data\\_t >](#)
- *A matrix of double-precision numbers.*  
class [umatrix\\_row\\_tlate< data\\_t >](#)
- *Create a vector from a row of a matrix.*  
class [umatrix\\_const\\_row\\_tlate< data\\_t >](#)
- *Create a const vector from a row of a matrix.*  
class [umatrix\\_alloc](#)
- *A simple class to provide an `allocate()` function for `umatrix`.*  
class [ufmatrix< N, M >](#)
- *A matrix where the memory allocation is performed in the constructor.*

## Typedefs

- typedef [umatrix\\_tlate< double >](#) [umatrix](#)  
*umatrix typedef*
- typedef [umatrix\\_view\\_tlate< double >](#) [umatrix\\_view](#)  
*umatrix\_view typedef*
- typedef [umatrix\\_base\\_tlate< double >](#) [umatrix\\_base](#)  
*umatrix\_base typedef*
- typedef [umatrix\\_const\\_view\\_tlate< double >](#) [umatrix\\_const\\_view](#)  
*umatrix\_const\_view typedef*
- typedef [umatrix\\_row\\_tlate< double >](#) [umatrix\\_row](#)  
*umatrix\_row typedef*
- typedef [umatrix\\_const\\_row\\_tlate< double >](#) [umatrix\\_const\\_row](#)  
*umatrix\_const\_row typedef*
- typedef [umatrix\\_tlate< int >](#) [umatrix\\_int](#)  
*umatrix\_int typedef*
- typedef [umatrix\\_view\\_tlate< int >](#) [umatrix\\_int\\_view](#)  
*umatrix\_int\_view typedef*
- typedef [umatrix\\_const\\_view\\_tlate< int >](#) [umatrix\\_int\\_const\\_view](#)  
*umatrix\_int\_const\_view typedef*
- typedef [umatrix\\_base\\_tlate< int >](#) [umatrix\\_int\\_base](#)  
*umatrix\_int\_base typedef*
- typedef [umatrix\\_row\\_tlate< int >](#) [umatrix\\_int\\_row](#)  
*umatrix\_int\_row typedef*
- typedef [umatrix\\_const\\_row\\_tlate< int >](#) [umatrix\\_int\\_const\\_row](#)  
*umatrix\_int\_const\_row typedef*

## Functions

- `template<class data_t >`  
`std::ostream & operator<< (std::ostream &os, const umatrix\_const\_view\_tlate< data\_t > &v)`  
*A operator for simple matrix output.*

### 47.33.2 Function Documentation

#### 47.33.2.1 `template<class data_t > std::ostream& operator<< ( std::ostream & os, const umatrix\_const\_view\_tlate< data\_t > & v )`

This outputs all of the matrix elements. Each row is output with an newline character at the end of each row. Positive values are preceded by an extra space. A 2x2 example:

```
-3.751935e-05 -6.785864e-04
-6.785864e-04  1.631984e-02
```

The function `gsl_ieee_double_to_rep()` is used to determine the sign of a number, so that "-0.0" as distinct from "+0.0" is handled correctly.

**Idea for Future** This assumes that scientific mode is on and `showpos` is off. It'd be nice to fix this.

Definition at line 878 of file `umatrix_tlate.h`.

## 47.34 `uvector_cx_tlate.h` File Reference

File for definitions of complex unit-stride vectors.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <vector> #include <o2scl/err_hnd.h> #include <gsl/gsl_vector.h>
```

### 47.34.1 Detailed Description

Definition in file `uvector_cx_tlate.h`.

#### Data Structures

- class `uvector_cx_view_tlate< data_t, complex_t >`  
*A vector view of complex numbers with unit stride.*
- class `uvector_cx_tlate< data_t, complex_t >`  
*A vector of double-precision numbers with unit stride.*
- class `uvector_cx_array_tlate< data_t, complex_t >`  
*Create a vector from an array.*
- class `uvector_cx_subvector_tlate< data_t, complex_t >`  
*Create a vector from a subvector of another.*
- class `uvector_cx_const_array_tlate< data_t, complex_t >`  
*Create a vector from an array.*
- class `uvector_cx_const_subvector_tlate< data_t, complex_t >`  
*Create a vector from a subvector of another.*

#### Typedefs

- typedef `uvector_cx_tlate < double, gsl_complex > uvector_cx`  
*uvector\_cx typedef*
- typedef `uvector_cx_view_tlate < double, gsl_complex > uvector_cx_view`  
*uvector\_cx\_view typedef*
- typedef `uvector_cx_array_tlate < double, gsl_complex > uvector_cx_array`  
*uvector\_cx\_array typedef*
- typedef `uvector_cx_subvector_tlate < double, gsl_complex > uvector_cx_subvector`  
*uvector\_cx\_subvector typedef*
- typedef `uvector_cx_const_array_tlate < double, gsl_complex > uvector_cx_const_array`  
*uvector\_cx\_const\_array typedef*
- typedef `uvector_cx_const_subvector_tlate < double, gsl_complex > uvector_cx_const_subvector`  
*uvector\_cx\_const\_subvector typedef*

#### Functions

- template<class `data_t`, class `complex_t` >  
`std::ostream & operator<< (std::ostream &os, const uvector_cx_view_tlate< data_t, complex_t > &v)`  
*A operator for naive vector output.*

## 47.34.2 Function Documentation

47.34.2.1 `template<class data_t, class complex_t> std::ostream& operator<< ( std::ostream & os, const uvector_cx_view_tlate< data_t, complex_t> & v )`

This outputs all of the vector elements. All of these are separated by one space character, though no trailing space or `endl` is sent to the output.

Definition at line 640 of file `uvector_cx_tlate.h`.

47.35 `uvector_tlate.h` File Reference

File for definitions of unit-stride vectors.

```
#include <iostream> #include <cstdlib> #include <string> #include <fstream> #include <sstream> ×
#include <vector> #include <gsl/gsl_vector.h> #include <o2scl/err_hnd.h> #include <o2scl/string-
_conv.h> #include <o2scl/array.h> #include <o2scl/vector.h>
```

## 47.35.1 Detailed Description

Definition in file `uvector_tlate.h`.

## Data Structures

- class `uvector_const_view_tlate< data_t >`  
*A const vector view with unit stride.*
- class `uvector_base_tlate< data_t >`  
*A base class for uvector and uvector\_view.*
- class `uvector_view_tlate< data_t >`  
*A base class for uvectors.*
- class `uvector_tlate< data_t >`  
*A vector with unit stride.*
- class `uvector_array_tlate< data_t >`  
*Create a vector from an array.*
- class `uvector_subvector_tlate< data_t >`  
*Create a vector from a subvector of another.*
- class `uvector_const_array_tlate< data_t >`  
*Create a vector from an const array.*
- class `uvector_const_subvector_tlate< data_t >`  
*Create a const vector from a subvector of another vector.*
- class `uvector_alloc`  
*A simple class to provide an `allocate()` function for uvector.*
- class `uvector_int_alloc`  
*A simple class to provide an `allocate()` function for uvector\_int.*
- class `uvector_size_t_alloc`  
*A simple class to provide an `allocate()` function for uvector\_size\_t.*
- class `ufvector< N >`  
*A vector with unit-stride where the memory allocation is performed in the constructor.*

## Typedefs

- typedef `uvector_tlate< double > uvector`  
*uvector typedef*
- typedef `uvector_view_tlate< double > uvector_view`  
*uvector\_view typedef*
- typedef `uvector_base_tlate< double > uvector_base`

- uvector\_base* typedef
- typedef `uvector_const_view_tlate` < double > `uvector_const_view`  
*uvector\_const\_view* typedef
- typedef `uvector_array_tlate` < double > `uvector_array`  
*uvector\_array* typedef
- typedef `uvector_subvector_tlate` < double > `uvector_subvector`  
*uvector\_subvector* typedef
- typedef `uvector_const_array_tlate` < double > `uvector_const_array`  
*uvector\_const\_array* typedef
- typedef `uvector_const_subvector_tlate` < double > `uvector_const_subvector`  
*uvector\_const\_subvector* typedef
- typedef `uvector_tlate`< int > `uvector_int`  
*uvector\_int* typedef
- typedef `uvector_view_tlate`< int > `uvector_int_view`  
*uvector\_int\_view* typedef
- typedef `uvector_base_tlate`< int > `uvector_int_base`  
*uvector\_int\_base* typedef
- typedef `uvector_const_view_tlate`< int > `uvector_int_const_view`  
*uvector\_int\_const\_view* typedef
- typedef `uvector_array_tlate`< int > `uvector_int_array`  
*uvector\_int\_array* typedef
- typedef `uvector_subvector_tlate`< int > `uvector_int_subvector`  
*uvector\_int\_subvector* typedef
- typedef `uvector_const_array_tlate`< int > `uvector_int_const_array`  
*uvector\_int\_const\_array* typedef
- typedef `uvector_const_subvector_tlate` < int > `uvector_int_const_subvector`  
*uvector\_int\_const\_subvector* typedef
- typedef `uvector_tlate`< size\_t > `uvector_size_t`  
*uvector\_size\_t* typedef
- typedef `uvector_view_tlate` < size\_t > `uvector_size_t_view`  
*uvector\_size\_t\_view* typedef
- typedef `uvector_base_tlate` < size\_t > `uvector_size_t_base`  
*uvector\_size\_t\_base* typedef
- typedef `uvector_const_view_tlate` < size\_t > `uvector_size_t_const_view`  
*uvector\_size\_t\_const\_view* typedef
- typedef `uvector_array_tlate` < size\_t > `uvector_size_t_array`  
*uvector\_size\_t\_array* typedef
- typedef `uvector_subvector_tlate` < size\_t > `uvector_size_t_subvector`  
*uvector\_size\_t\_subvector* typedef
- typedef `uvector_const_array_tlate` < size\_t > `uvector_size_t_const_array`  
*uvector\_size\_t\_const\_array* typedef
- typedef `uvector_const_subvector_tlate` < size\_t > `uvector_size_t_const_subvector`  
*uvector\_size\_t\_const\_subvector* typedef

## Functions

- template<class data\_t >  
std::ostream & `operator<<` (std::ostream &os, const `uvector_const_view_tlate`< data\_t > &v)  
*A operator for simple vector output.*

## 47.35.2 Function Documentation

47.35.2.1 `template<class data_t> std::ostream& operator<< ( std::ostream & os, const uvector_const_view_tlate< data_t > & v )`

This outputs all of the vector elements. All of these are separated by one space character, though no trailing space or `endl` is sent to the output. If the vector is empty, nothing is done.

Definition at line 1006 of file `uvector_tlate.h`.

## 47.36 vec\_arith.h File Reference

Vector and matrix arithmetic.

```
#include <iostream> #include <complex> #include <o2scl/ovector_tlate.h> #include <o2scl/omatrix-
_tlate.h> #include <o2scl/uvector_tlate.h> #include <o2scl/umatrix_tlate.h> #include <o2scl/ovect
_cx_tlate.h> #include <o2scl/omatrix_cx_tlate.h> #include <o2scl/uvector_cx_tlate.h> #include
<o2scl/umatrix_cx_tlate.h>
```

### 47.36.1 Detailed Description

By default, the following operators are defined:

```
ovector operator+(ovector_const_view &x, ovector_const_view &y);
ovector operator+(ovector_const_view &x, uvector_const_view &y);
ovector operator+(uvector_const_view &x, ovector_const_view &y);
uvector operator+(uvector_const_view &x, uvector_const_view &y);

ovector_cx operator+(ovector_cx_view &x, ovector_cx_view &y);
ovector_cx operator+(ovector_cx_view &x, uvector_cx_view &y);
ovector_cx operator+(uvector_cx_view &x, ovector_cx_view &y);
uvector_cx operator+(uvector_cx_view &x, uvector_cx_view &y);

ovector operator-(ovector_const_view &x, ovector_const_view &y);
ovector operator-(ovector_const_view &x, uvector_const_view &y);
ovector operator-(uvector_const_view &x, ovector_const_view &y);
uvector operator-(uvector_const_view &x, uvector_const_view &y);

ovector_cx operator-(ovector_cx_view &x, ovector_cx_view &y);
ovector_cx operator-(ovector_cx_view &x, uvector_cx_view &y);
ovector_cx operator-(uvector_cx_view &x, ovector_cx_view &y);
uvector_cx operator-(uvector_cx_view &x, uvector_cx_view &y);

ovector operator*(omatrix_const_view &x, ovector_const_view &y);
ovector operator*(omatrix_const_view &x, uvector_const_view &y);
ovector operator*(umatrix_const_view &x, ovector_const_view &y);
uvector operator*(umatrix_const_view &x, uvector_const_view &y);

ovector_cx operator*(omatrix_cx_view &x, ovector_cx_view &y);
ovector_cx operator*(omatrix_cx_view &x, uvector_cx_view &y);
ovector_cx operator*(umatrix_cx_view &x, ovector_cx_view &y);
uvector_cx operator*(umatrix_cx_view &x, uvector_cx_view &y);

ovector operator*(ovector_const_view &x, omatrix_const_view &y);
ovector operator*(ovector_const_view &x, umatrix_const_view &y);
ovector operator*(uvector_const_view &x, omatrix_const_view &y);
uvector operator*(ovector_const_view &x, umatrix_const_view &y);

ovector trans_mult(ovector_const_view &x, omatrix_const_view &y);
ovector trans_mult(ovector_const_view &x, umatrix_const_view &y);
ovector trans_mult(uvector_const_view &x, omatrix_const_view &y);
uvector trans_mult(ovector_const_view &x, umatrix_const_view &y);

double dot(ovector_const_view &x, ovector_const_view &y);
double dot(ovector_const_view &x, uvector_const_view &y);
double dot(uvector_const_view &x, ovector_const_view &y);
double dot(uvector_const_view &x, uvector_const_view &y);

double dot(ovector_cx_view &x, ovector_cx_view &y);
double dot(ovector_cx_view &x, uvector_cx_view &y);
double dot(uvector_cx_view &x, ovector_cx_view &y);
double dot(uvector_cx_view &x, uvector_cx_view &y);

ovector operator*(double x, ovector_const_view &y);
uvector operator*(double x, uvector_const_view &y);
ovector operator*(ovector_const_view &x, double y);
uvector operator*(uvector_const_view &x, double y);
```

```

ovector pair_prod(ovector_const_view &x, ovector_const_view &y);
ovector pair_prod(ovector_const_view &x, uvector_const_view &y);
ovector pair_prod(uvector_const_view &x, ovector_const_view &y);
uvector pair_prod(uvector_const_view &x, uvector_const_view &y);

ovector_cx pair_prod(ovector_cx_view &x, ovector_const_view &y);
ovector_cx pair_prod(ovector_cx_view &x, uvector_const_view &y);
ovector_cx pair_prod(uvector_cx_view &x, ovector_const_view &y);
uvector_cx pair_prod(uvector_cx_view &x, uvector_const_view &y);
ovector_cx pair_prod(ovector_const_view &x, ovector_cx_view &y);
ovector_cx pair_prod(ovector_const_view &x, uvector_cx_view &y);
ovector_cx pair_prod(uvector_const_view &x, ovector_cx_view &y);
uvector_cx pair_prod(uvector_const_view &x, uvector_cx_view &y);
ovector_cx pair_prod(ovector_cx_view &x, ovector_cx_view &y);
ovector_cx pair_prod(ovector_cx_view &x, uvector_cx_view &y);
ovector_cx pair_prod(uvector_cx_view &x, ovector_cx_view &y);
uvector_cx pair_prod(uvector_cx_view &x, uvector_cx_view &y);

bool operator==(ovector_const_view &x, ovector_const_view &y);
bool operator==(ovector_const_view &x, uvector_const_view &y);
bool operator==(uvector_const_view &x, ovector_const_view &y);
bool operator==(uvector_const_view &x, uvector_const_view &y);

bool operator!=(ovector_const_view &x, ovector_const_view &y);
bool operator!=(ovector_const_view &x, uvector_const_view &y);
bool operator!=(uvector_const_view &x, ovector_const_view &y);
bool operator!=(uvector_const_view &x, uvector_const_view &y);

```

#### Note

This used to be in a separate namespace, called `o2scl_arith`, but this causes problems with Koenig lookup in template classes for `operator*()` when defined for vector addition (for example).

**Idea for Future** Define operators for complex vector \* real matrix

**Idea for Future** Define == and != for complex vectors

**Idea for Future** These should be replaced by the BLAS routines where possible?

Definition in file `vec_arith.h`.

#### Defines

- `#define O2SCL_OP_VEC_VEC_ADD(vec1, vec2, vec3)`  
The header macro for vector-vector addition.
- `#define O2SCL_OP_VEC_VEC_SUB(vec1, vec2, vec3)`  
The header macro for vector-vector subtraction.
- `#define O2SCL_OP_MAT_VEC_MULT(vec1, vec2, mat)`  
The header macro for matrix-vector (right) multiplication.
- `#define O2SCL_OP_CMAT_CVEC_MULT(vec1, vec2, mat)`  
The header macro for complex matrix-vector (right) multiplication.
- `#define O2SCL_OP_VEC_MAT_MULT(vec1, vec2, mat)`  
The header macro for vector-matrix (left) multiplication.
- `#define O2SCL_OP_TRANS_MULT(vec1, vec2, mat)`  
The header macro for the `trans_mult` form of vector \* matrix.
- `#define O2SCL_OP_DOT_PROD(dtype, vec1, vec2)`  
The header macro for vector scalar (dot) product.
- `#define O2SCL_OP_CX_DOT_PROD(dtype, vec1, vec2)`  
The header macro for complex vector scalar (dot) product.
- `#define O2SCL_OP_SCA_VEC_MULT(dtype, vecv, vec)`



- *The header macro for scalar-vector multiplication.*
- #define [O2SCL\\_OP\\_VEC\\_SCA\\_MULT](#)(dtype, vecv, vec)
- *The header macro for vector-scalar multiplication.*
- #define [O2SCL\\_OP\\_VEC\\_VEC\\_PRO](#)(vec1, vec2, vec3)
- *The header macro for pairwise vector \* vector (where either vector can be real or complex)*
- #define [O2SCL\\_OPSRC\\_VEC\\_VEC\\_ADD](#)(vec1, vec2, vec3)
- *The source code macro for vector-vector addition.*
- #define [O2SCL\\_OPSRC\\_VEC\\_VEC\\_SUB](#)(vec1, vec2, vec3)
- *The source code macro for vector-vector subtraction.*
- #define [O2SCL\\_OPSRC\\_MAT\\_VEC\\_MULT](#)(vec1, vec2, mat)
- *The source code macro for matrix \* vector.*
- #define [O2SCL\\_OPSRC\\_CMAT\\_CVEC\\_MULT](#)(vec1, vec2, mat)
- *The source code macro for complex matrix \* complex vector.*
- #define [O2SCL\\_OPSRC\\_VEC\\_MAT\\_MULT](#)(vec1, vec2, mat)
- *The source code macro for the operator form of vector \* matrix.*
- #define [O2SCL\\_OPSRC\\_TRANS\\_MULT](#)(vec1, vec2, mat)
- *The source code macro for the `trans_mult` form of vector \* matrix.*
- #define [O2SCL\\_OPSRC\\_DOT\\_PROD](#)(dtype, vec1, vec2)
- *The source code macro for a vector dot product.*
- #define [O2SCL\\_OPSRC\\_CX\\_DOT\\_PROD](#)(dtype, vec1, vec2)
- *The source code macro for a complex vector dot product.*
- #define [O2SCL\\_OPSRC\\_SCA\\_VEC\\_MULT](#)(dtype, vecv, vec)
- *The source code macro for vector=scalar\*vector.*
- #define [O2SCL\\_OPSRC\\_VEC\\_SCA\\_MULT](#)(dtype, vecv, vec)
- *The source code macro for vector=vector\*scalar.*
- #define [O2SCL\\_OPSRC\\_VEC\\_VEC\\_PRO](#)(vec1, vec2, vec3)
- *The source code macro for pairwise vector \* vector (where either vector can be real or complex)*
- #define [O2SCL\\_OP\\_VEC\\_VEC\\_EQUAL](#)(vec1, vec2)
- *The header macro for vector==vector.*
- #define [O2SCL\\_OPSRC\\_VEC\\_VEC\\_EQUAL](#)(vec1, vec2)
- *The source code macro vector==vector.*
- #define [O2SCL\\_OP\\_VEC\\_VEC\\_NEQUAL](#)(vec1, vec2)
- *The header macro for vector!=vector.*
- #define [O2SCL\\_OPSRC\\_VEC\\_VEC\\_NEQUAL](#)(vec1, vec2)
- *The source code macro vector!=vector.*

## 47.36.2 Define Documentation

### 47.36.2.1 #define O2SCL\_OP\_VEC\_VEC\_ADD( vec1, vec2, vec3 )

#### Value:

```
vec1 operator+ \
(const vec2 &x, const vec3 &y);
```

Given types `vec1`, `vec2`, and `vec3`, this macro provides the function declaration for adding two vectors using the form

```
vec1 operator+(const vec2 &x, const vec3 &y);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_VEC\\_VEC\\_ADD](#).

#### Note

This used to be in a separate namespace, called `o2scl_arith`, but this causes problems with Koenig lookup in template classes for `operator*()` when defined for vector addition (for example).

Definition at line 158 of file `vec_arith.h`.

47.36.2.2 `#define O2SCL_OP_VEC_VEC_SUB( vec1, vec2, vec3 )`**Value:**

```
vec1 operator- \
    (const vec2 &x, const vec3 &y);
```

Given types `vec1`, `vec2`, and `vec3`, this macro provides the function declaration for adding two vectors using the form

```
vec1 operator-(const vec2 &x, const vec3 &y);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_VEC\\_VEC\\_SUB](#).

Definition at line 199 of file `vec_arith.h`.

47.36.2.3 `#define O2SCL_OP_MAT_VEC_MULT( vec1, vec2, mat )`**Value:**

```
vec1 operator* \
    (const mat &m, const vec2 &x);
```

Given types `vec1`, `vec2`, and `mat`, this macro provides the function declaration for adding two vectors using the form

```
vec1 operator*(const mat &m, const vec3 &x);
```

See also the blas version of this function [dgemv\(\)](#).

The corresponding definition is given in [O2SCL\\_OPSRC\\_MAT\\_VEC\\_MULT](#).

Definition at line 243 of file `vec_arith.h`.

47.36.2.4 `#define O2SCL_OP_CMAT_CVEC_MULT( vec1, vec2, mat )`**Value:**

```
vec1 operator* \
    (const mat &m, const vec2 &x);
```

Given types `vec1`, `vec2`, and `mat`, this macro provides the function declaration for adding two vectors using the form

```
vec1 operator*(const mat &m, const vec3 &x);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_CMAT\\_CVEC\\_MULT](#).

Definition at line 278 of file `vec_arith.h`.

47.36.2.5 `#define O2SCL_OP_VEC_MAT_MULT( vec1, vec2, mat )`**Value:**

```
vec1 operator* \
    (const vec2 &x, const mat &m);
```

Given types `vec1`, `vec2`, and `mat`, this macro provides the function declaration for adding two vectors using the form

```
vec1 operator*(const vec3 &x, const mat &m);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_VEC\\_MAT\\_MULT](#).

Definition at line 312 of file `vec_arith.h`.

---

**47.36.2.6 #define O2SCL\_OP\_TRANS\_MULT( vec1, vec2, mat )****Value:**

```
vec1 trans_mult \
    (const vec2 &x, const mat &m);
```

Definition at line 334 of file vec\_arith.h.

**47.36.2.7 #define O2SCL\_OP\_DOT\_PROD( dtype, vec1, vec2 )****Value:**

```
dtype dot \
    (const vec1 &x, const vec2 &y);
```

Given types vec1, vec2, and dtype, this macro provides the function declaration for adding two vectors using the form

```
dtype operator*(const vec1 &x, const vec2 &y);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_DOT\\_PROD](#).

Definition at line 367 of file vec\_arith.h.

**47.36.2.8 #define O2SCL\_OP\_CX\_DOT\_PROD( dtype, vec1, vec2 )****Value:**

```
dtype dot \
    (const vec1 &x, const vec2 &y);
```

Given types vec1, vec2, and dtype, this macro provides the function declaration for adding two vectors using the form

```
dtype operator*(const vec1 &x, const vec2 &y);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_CX\\_DOT\\_PROD](#).

Definition at line 401 of file vec\_arith.h.

**47.36.2.9 #define O2SCL\_OP\_SCA\_VEC\_MULT( dtype, vecv, vec )****Value:**

```
vec operator* \
    (const dtype &x, const vecv &y);
```

Given types vecv, vec, and dtype, this macro provides the function declaration for adding two vectors using the form

```
vec operator*(const dtype &x, const vecv &y);
```

The corresponding definition is given in [O2SCL\\_OPSRC\\_SCA\\_VEC\\_MULT](#).

Definition at line 434 of file vec\_arith.h.

**47.36.2.10 #define O2SCL\_OP\_VEC\_SCA\_MULT( dtype, vecv, vec )****Value:**

```
vec operator* \
    (const vecv &x, const dtype &y);
```

Given types vecv, vec, and dtype, this macro provides the function declaration for adding two vectors using the form

```
vec operator*(const vecv &x, const dtype &y);
```

The corresponding definition is given in [O2SCL\\_OP\\_SRC\\_VEC\\_SCA\\_MULT](#).

Definition at line 461 of file vec\_arith.h.

**47.36.2.11** `#define O2SCL_OP_VEC_VEC_PRO( vec1, vec2, vec3 )`

**Value:**

```
vec1 pair_prod \
(const vec2 &x, const vec3 &y);
```

Given types `vec1`, `vec2`, and `vec3`, this macro provides the function declaration for adding two vectors using the form

```
vec1 pair_prod(const vec2 &x, const vec3 &y);
```

The corresponding definition is given in [O2SCL\\_OP\\_SRC\\_VEC\\_VEC\\_PRO](#).

Definition at line 489 of file vec\_arith.h.

**47.36.2.12** `#define O2SCL_OP_SRC_VEC_VEC_ADD( vec1, vec2, vec3 )`

**Value:**

```
vec1 o2scl::operator+ \
(const vec2 &x, const vec3 &y) { \
    size_t m=x.size(); \
    if (y.size()<m) m=y.size(); \
    vec1 r(m); \
    for(size_t i=0;i<m;i++) { \
        r[i]=x[i]+y[i]; \
    } \
    return r; \
}
```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_VEC\\_ADD](#)

Definition at line 534 of file vec\_arith.h.

**47.36.2.13** `#define O2SCL_OP_SRC_VEC_VEC_SUB( vec1, vec2, vec3 )`

**Value:**

```
vec1 o2scl::operator- \
(const vec2 &x, const vec3 &y) { \
    size_t m=x.size(); \
    if (y.size()<m) m=y.size(); \
    vec1 r(m); \
    for(size_t i=0;i<m;i++) { \
        r[i]=x[i]-y[i]; \
    } \
    return r; \
}
```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_VEC\\_SUB](#)

Definition at line 550 of file vec\_arith.h.

**47.36.2.14** `#define O2SCL_OP_SRC_MAT_VEC_MULT( vec1, vec2, mat )`

**Value:**

```
vec1 o2scl::operator* \
```

```

(const mat &m, const vec2 &x) {
size_t nr=m.rows();
size_t nc=m.cols();
vec1 res(nr);
for(size_t i=0;i<nr;i++) {
double r=0.0;
for(size_t j=0;j<nc;j++) {
r+=m[i][j]*x[j];
}
res[i]=r;
}
return res;
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_MAT\\_VEC\\_MULT](#)

Definition at line 566 of file vec\_arith.h.

#### 47.36.2.15 #define O2SCL\_OPSRC\_CMAT\_CVEC\_MULT( vec1, vec2, mat )

**Value:**

```

vec1 o2scl::operator* \
(const mat &m, const vec2 &x) {
size_t nr=m.rows();
size_t nc=m.cols();
vec1 res(nr);
for(size_t i=0;i<nr;i++) {
double re=0.0;
double im=0.0;
for(size_t j=0;j<nc;j++) {
gsl_complex g=m[i][j]*x[j];
re+=g.dat[0];
im+=g.dat[1];
}
res[i].dat[0]=re;
res[i].dat[1]=im;
}
return res;
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_CMAT\\_CVEC\\_MULT](#)

Definition at line 586 of file vec\_arith.h.

#### 47.36.2.16 #define O2SCL\_OPSRC\_VEC\_MAT\_MULT( vec1, vec2, mat )

**Value:**

```

vec1 o2scl::operator* \
(const vec2 &x, const mat &m) {
size_t nr=m.rows();
size_t nc=m.cols();
vec1 res(nr);
for(size_t j=0;j<nc;j++) {
double r=0.0;
for(size_t i=0;i<nr;i++) {
r+=x[i]*m[i][j];
}
res[j]=r;
}
return res;
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_MAT\\_MULT](#)

Definition at line 610 of file vec\_arith.h.

47.36.2.17 #define O2SCL\_OP\_SRC\_TRANS\_MULT( *vec1*, *vec2*, *mat* )**Value:**

```

vec1 o2scl::trans_mult \
    (const vec2 &x, const mat &m) { \
    size_t nr=m.rows(); \
    size_t nc=m.cols(); \
    vec1 res(nr); \
    for(size_t j=0;j<nc;j++) { \
        double r=0.0; \
        for(size_t i=0;i<nr;i++) { \
            r+=x[i]*m[i][j]; \
        } \
        res[j]=r; \
    } \
    return res; \
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_TRANS\\_MULT](#)

Definition at line 631 of file vec\_arith.h.

47.36.2.18 #define O2SCL\_OP\_SRC\_DOT\_PROD( *dtype*, *vec1*, *vec2* )**Value:**

```

dtype o2scl::dot \
    (const vec1 &x, const vec2 &y) { \
    size_t m=x.size(); \
    if (y.size()<m) m=y.size(); \
    dtype r=0; \
    for(size_t i=0;i<m;i++) { \
        r+=x[i]*y[i]; \
    } \
    return r; \
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_DOT\\_PROD](#)

Definition at line 651 of file vec\_arith.h.

47.36.2.19 #define O2SCL\_OP\_SRC\_CX\_DOT\_PROD( *dtype*, *vec1*, *vec2* )**Value:**

```

dtype o2scl::dot \
    (const vec1 &x, const vec2 &y) { \
    size_t m=x.size(); \
    if (y.size()<m) m=y.size(); \
    dtype r={{0.0,0.0}}; \
    for(size_t i=0;i<m;i++) { \
        r+=x[i]*y[i]; \
    } \
    return r; \
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_CX\\_DOT\\_PROD](#)

Definition at line 667 of file vec\_arith.h.

47.36.2.20 #define O2SCL\_OP\_SRC\_SCA\_VEC\_MULT( *dtype*, *vecv*, *vec* )**Value:**

```

vec o2scl::operator* \

```

```

    (const dtype &x, const vecv &y) {
        size_t m=y.size();
        vec r(m);
        for(size_t i=0;i<m;i++) {
            r[i]=x*y[i];
        }
        return r;
    }

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_SCA\\_VEC\\_MULT](#)

Definition at line 683 of file vec\_arith.h.

#### 47.36.2.21 #define O2SCL\_OP\_SRC\_VEC\_SCA\_MULT( dtype, vecv, vec )

**Value:**

```

vec o2scl::operator* \
    (const vecv &x, const dtype &y) {
    size_t m=x.size();
    vec r(m);
    for(size_t i=0;i<m;i++) {
        r[i]=x[i]*y;
    }
    return r;
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_SCA\\_MULT](#)

Definition at line 698 of file vec\_arith.h.

#### 47.36.2.22 #define O2SCL\_OP\_SRC\_VEC\_VEC\_PRO( vec1, vec2, vec3 )

**Value:**

```

vec1 o2scl::pair_prod \
    (const vec2 &x, const vec3 &y) {
    size_t m=x.size();
    if (y.size()<m) m=y.size();
    vec1 r(m);
    for(size_t i=0;i<m;i++) {
        r[i]=x[i]*y[i];
    }
    return r;
}

```

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_VEC\\_PRO](#)

Definition at line 714 of file vec\_arith.h.

#### 47.36.2.23 #define O2SCL\_OP\_VEC\_VEC\_EQUAL( vec1, vec2 )

**Value:**

```

bool operator== \
    (const vec1 &x, const vec2 &y);

```

Given types `vec1` and `vec2`, this macro provides the function declaration for vector equality comparisons using

```
bool operator==(const vec1 &x, const vec2 &y);
```

**Note**

Two vectors with different sizes are defined to be not equal, no matter what their contents.

The corresponding definition is given in [O2SCL\\_OP\\_SRC\\_VEC\\_VEC\\_EQUAL](#).

Definition at line 739 of file vec\_arith.h.

**47.36.2.24** `#define O2SCL_OP_SRC_VEC_VEC_EQUAL( vec1, vec2 )`

**Value:**

```
bool o2scl::operator== \
    (const vec1 &x, const vec2 &y) {
    size_t m=x.size();
    size_t n=y.size();
    if (m!=n) return false;
    for(size_t i=0;i<m;i++) {
        if (x[i]!=y[i]) return false;
    }
    return true;
}
```

**Note**

Two vectors with different sizes are defined to be not equal, no matter what their contents.

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_VEC\\_EQUAL](#)

Definition at line 794 of file vec\_arith.h.

**47.36.2.25** `#define O2SCL_OP_VEC_VEC_NEQUAL( vec1, vec2 )`

**Value:**

```
bool operator!= \
    (const vec1 &x, const vec2 &y);
```

Given types `vec1` and `vec2`, this macro provides the function declaration for vector inequality comparisons using

```
bool operator==(const vec1 &x, const vec2 &y);
```

**Note**

Two vectors with different sizes are defined to be not equal, no matter what their contents.

The corresponding definition is given in [O2SCL\\_OP\\_SRC\\_VEC\\_VEC\\_NEQUAL](#).

Definition at line 819 of file vec\_arith.h.

**47.36.2.26** `#define O2SCL_OP_SRC_VEC_VEC_NEQUAL( vec1, vec2 )`

**Value:**

```
bool o2scl::operator!= \
    (const vec1 &x, const vec2 &y) {
    size_t m=x.size();
    size_t n=y.size();
    if (m!=n) return true;
    for(size_t i=0;i<m;i++) {
        if (x[i]!=y[i]) return true;
    }
    return false;
}
```



## Note

Two vectors with different sizes are defined to be not equal, no matter what their contents.

This define macro generates the function definition. See the function declaration [O2SCL\\_OP\\_VEC\\_VEC\\_NEQUAL](#)

Definition at line 874 of file `vec_arith.h`.

47.37 `vec_stats.h` File Reference

File containing statistics template functions.

```
#include <o2scl/err_hnd.h> #include <gsl/gsl_sort.h>
```

## 47.37.1 Detailed Description

This file contains several function templates for computing statistics of vectors of double-precision data. It includes mean, median, variance, standard deviation, covariance, correlation, and other functions.

No additional range checking is done on the vectors.

**Idea for Future** Consider generalizing to other data types.

Definition in file [vec\\_stats.h](#).

## Functions

## Vector functions

- `template<class vec_t >`  
`double vector_mean (size_t n, const vec_t &data)`  
*Compute the mean of the first n elements of a vector.*
- `template<class vec_t >`  
`double vector_variance_fmean (size_t n, const vec_t &data, double mean)`  
*Compute variance with specified mean known in advance.*
- `template<class vec_t >`  
`double vector_variance (size_t n, const vec_t &data, double mean)`  
*Compute the variance with specified mean.*
- `template<class vec_t >`  
`double vector_variance (size_t n, const vec_t &data)`  
*Compute the variance.*
- `template<class vec_t >`  
`double vector_stddev_fmean (size_t n, const vec_t &data, double mean)`  
*Standard deviation with specified mean known in advance.*
- `template<class vec_t >`  
`double vector_stddev (size_t n, const vec_t &data)`  
*Standard deviation with specified mean.*
- `template<class vec_t >`  
`double vector_stddev (size_t n, const vec_t &data, double mean)`  
*Standard deviation with specified mean.*
- `template<class vec_t >`  
`double vector_absdev (size_t n, const vec_t &data, double mean)`  
*Absolute deviation from the specified mean.*
- `template<class vec_t >`  
`double vector_absdev (size_t n, const vec_t &data)`  
*Absolute deviation from the computed mean.*
- `template<class vec_t >`  
`double vector_skew (size_t n, const vec_t &data, double mean, double stddev)`

- Skewness with specified mean and standard deviation.*
- template<class vec\_t >  
double **vector\_skew** (size\_t n, const vec\_t &data)  
*Skewness with computed mean and standard deviation.*
- template<class vec\_t >  
double **vector\_kurtosis** (size\_t n, const vec\_t &data, double mean, double stddev)  
*Kurtosis with specified mean and standard deviation.*
- template<class vec\_t >  
double **vector\_kurtosis** (size\_t n, const vec\_t &data)  
*Kurtosis with computed mean and standard deviation.*
- template<class vec\_t >  
double **vector\_lag1\_autocorr** (size\_t n, const vec\_t &data, double mean)  
*Lag-1 autocorrelation.*
- template<class vec\_t >  
double **vector\_lag1\_autocorr** (size\_t n, const vec\_t &data)  
*Lag-1 autocorrelation.*
- template<class vec\_t >  
double **vector\_covariance** (size\_t n, const vec\_t &data1, const vec\_t &data2, double mean1, double mean2)  
*Compute the covariance of two vectors.*
- template<class vec\_t >  
double **vector\_covariance** (size\_t n, const vec\_t &data1, const vec\_t &data2)  
*Compute the covariance of two vectors.*
- template<class vec\_t >  
double **vector\_correlation** (size\_t n, const vec\_t &data1, const vec\_t &data2)  
*Pearson's correlation.*
- template<class vec\_t, class vec2\_t >  
double **vector\_pvariance** (size\_t n1, const vec\_t &data1, size\_t n2, const vec2\_t &data2)  
*Pooled variance.*
- template<class vec\_t >  
double **vector\_quantile\_sorted** (size\_t n, const vec\_t &data, const double f)  
*Quantile from sorted data (ascending only)*
- template<class vec\_t >  
double **vector\_median\_sorted** (size\_t n, const vec\_t &data)  
*Return the median of sorted (ascending or descending) data.*
- template<class vec\_t, class vec2\_t, class vec3\_t >  
double **vector\_chi\_squared** (size\_t n, const vec\_t &obs, const vec2\_t &exp, const vec3\_t &err)  
*Compute the chi-squared statistic.*

#### Weighted vector functions

- template<class vec\_t >  
double **wvector\_mean** (size\_t n, const vec\_t &data, const vec\_t &weights)  
*Compute the mean of weighted data.*
- template<class vec\_t >  
double **wvector\_factor** (size\_t n, const vec\_t &weights)  
*Compute a normalization factor for weighted data.*
- template<class vec\_t, class vec2\_t >  
double **wvector\_variance\_fmean** (size\_t n, const vec\_t &data, const vec2\_t &weights, double wmean)  
*Compute the variance of a weighted vector with a mean known in advance.*
- template<class vec\_t, class vec2\_t >  
double **wvector\_variance** (size\_t n, const vec\_t &data, const vec2\_t &weights, double wmean)  
*Compute the variance of a weighted vector with specified mean.*
- template<class vec\_t, class vec2\_t >  
double **wvector\_variance** (size\_t n, const vec\_t &data, const vec2\_t &weights)  
*Compute the variance of a weighted vector where mean is computed automatically.*
- template<class vec\_t, class vec2\_t >  
double **wvector\_stddev\_fmean** (size\_t n, const vec\_t &data, const vec2\_t &weights, double wmean)  
*Compute the standard deviation of a weighted vector with a mean known in advance.*
- template<class vec\_t, class vec2\_t >  
double **wvector\_stddev** (size\_t n, const vec\_t &data, const vec2\_t &weights)  
*Compute the standard deviation of a weighted vector where mean is computed automatically.*
- template<class vec\_t, class vec2\_t >  
double **wvector\_stddev** (size\_t n, const vec\_t &data, const vec2\_t &weights, double wmean)

*Compute the standard deviation of a weighted vector with specified mean.*

- `template<class vec_t, class vec2_t>`  
`double wvector_sumsq (size_t n, const vec_t &data, const vec2_t &weights, double wmean)`

*Compute the weighted sum of squares of data about the specified weighted mean.*

- `template<class vec_t, class vec2_t>`  
`double wvector_sumsq (size_t n, const vec_t &data, const vec2_t &weights)`

*Compute the weighted sum of squares of data about the weighted mean.*

- `template<class vec_t, class vec2_t>`  
`double wvector_absdev (size_t n, const vec_t &data, const vec2_t &weights, double wmean)`

*Compute the absolute deviation of data about a specified mean.*

- `template<class vec_t, class vec2_t>`  
`double wvector_absdev (size_t n, const vec_t &data, const vec2_t &weights)`

*Compute the absolute deviation of data about a specified mean.*

- `template<class vec_t, class vec2_t>`  
`double wvector_skew (size_t n, const vec_t &data, const vec2_t &weights, double wmean, double wsd)`

*Compute the skewness of data with specified mean and standard deviation.*

- `template<class vec_t, class vec2_t>`  
`double wvector_skew (size_t n, const vec_t &data, const vec2_t &weights)`

*Compute the skewness of data with specified mean and standard deviation.*

- `template<class vec_t, class vec2_t>`  
`double wvector_kurtosis (size_t n, const vec_t &data, const vec2_t &weights, double wmean, double wsd)`

*Compute the kurtosis of data with specified mean and standard deviation.*

- `template<class vec_t, class vec2_t>`  
`double wvector_kurtosis (size_t n, const vec_t &data, const vec2_t &weights)`

*Compute the kurtosis of data with specified mean and standard deviation.*

## 47.37.2 Function Documentation

### 47.37.2.1 `template<class vec_t> double vector_mean ( size_t n, const vec_t & data )`

This function produces the same results as `gsl_stats_mean()`.

If `n` is zero, this will return zero.

Definition at line 55 of file `vec_stats.h`.

### 47.37.2.2 `template<class vec_t> double vector_variance_fmean ( size_t n, const vec_t & data, double mean )`

This function computes

$$\frac{1}{N} \sum_i (x_i - \mu)^2$$

where the value of  $\mu$  is given in `mean`.

This function produces the same results as `gsl_stats_variance_with_fixed_mean()`.

Definition at line 76 of file `vec_stats.h`.

### 47.37.2.3 `template<class vec_t> double vector_variance ( size_t n, const vec_t & data, double mean )`

This function computes

$$\frac{1}{N-1} \sum_i (x_i - \mu)^2$$

where the value of  $\mu$  is given in `mean`.

This function produces the same results as `gsl_stats_variance_m`.

If `n` is 0 or 1, this function will call the error handler.

Definition at line 100 of file `vec_stats.h`.

47.37.2.4 `template<class vec_t > double vector_variance ( size_t n, const vec_t & data )`

This function computes

$$\frac{1}{N-1} \sum_i (x_i - \mu)^2$$

where  $\mu$  is the mean computed with `vector_mean()`.

This function produces the same results as `gsl_stats_variance`.

If `n` is 0 or 1, this function will call the error handler.

Definition at line 124 of file `vec_stats.h`.

47.37.2.5 `template<class vec_t > double vector_stddev_fmean ( size_t n, const vec_t & data, double mean )`

This function computes

$$\sqrt{\frac{1}{N} \sum_i (x_i - \mu)^2}$$

where the value of  $\mu$  is given in `mean`.

This function produces the same results as `gsl_stats_sd_with_fixed_mean()`.

If `n` is zero, this function will return zero without calling the error handler.

Definition at line 151 of file `vec_stats.h`.

47.37.2.6 `template<class vec_t > double vector_stddev ( size_t n, const vec_t & data )`

This function computes

$$\sqrt{\frac{1}{N-1} \sum_i (x_i - \mu)^2}$$

where  $\mu$  is the mean computed with `vector_mean()`.

This function produces the same results as `gsl_stats_sd()`.

If `n` is 0 or 1, this function will call the error handler.

Definition at line 170 of file `vec_stats.h`.

47.37.2.7 `template<class vec_t > double vector_stddev ( size_t n, const vec_t & data, double mean )`

This function computes

$$\sqrt{\frac{1}{N-1} \sum_i (x_i - \mu)^2}$$

where the value of  $\mu$  is given in `mean`.

This function produces the same results as `gsl_stats_sd_m()`.

If `n` is 0 or 1, this function will call the error handler.

Definition at line 196 of file `vec_stats.h`.

47.37.2.8 `template<class vec_t > double vector_absdev ( size_t n, const vec_t & data, double mean )`

This function computes

$$\sum_i |x_i - \mu|$$

where the value of  $\mu$  is given in `mean`.

This function produces the same results as `gsl_stats_absdev_m()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 222 of file vec\_stats.h.

**47.37.2.9** `template<class vec_t> double vector_absdev ( size_t n, const vec_t & data )`

This function computes

$$\sum_i |x_i - \mu|$$

where the value of  $\mu$  is mean as computed from [vector\\_mean\(\)](#).

This function produces the same results as `gsl_stats_absdev()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 250 of file vec\_stats.h.

**47.37.2.10** `template<class vec_t> double vector_skew ( size_t n, const vec_t & data, double mean, double stddev )`

This function computes

$$\frac{1}{N} \sum_i \left[ \frac{(x_i - \mu)}{\sigma} \right]^3$$

where the values of  $\mu$  and  $\sigma$  are given in `mean` and `stddev`.

This function produces the same results as `gsl_stats_skew_m_sd()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 271 of file vec\_stats.h.

**47.37.2.11** `template<class vec_t> double vector_skew ( size_t n, const vec_t & data )`

This function computes

$$\frac{1}{N} \sum_i \left[ \frac{(x_i - \mu)}{\sigma} \right]^3$$

where the values of  $\mu$  and  $\sigma$  are computed using [vector\\_mean\(\)](#) and [vector\\_stddev\(\)](#).

This function produces the same results as `gsl_stats_skew()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 297 of file vec\_stats.h.

**47.37.2.12** `template<class vec_t> double vector_kurtosis ( size_t n, const vec_t & data, double mean, double stddev )`

This function computes

$$-3 + \frac{1}{N} \sum_i \left[ \frac{(x_i - \mu)}{\sigma} \right]^4$$

where the values of  $\mu$  and  $\sigma$  are given in `mean` and `stddev`.

This function produces the same results as `gsl_stats_kurtosis_m_sd()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 320 of file vec\_stats.h.

**47.37.2.13** `template<class vec_t> double vector_kurtosis ( size_t n, const vec_t & data )`

This function computes

$$-3 + \frac{1}{N} \sum_i \left[ \frac{(x_i - \mu)}{\sigma} \right]^4$$

where the values of  $\mu$  and  $\sigma$  are computed using [vector\\_mean\(\)](#) and [vector\\_stddev\(\)](#).

This function produces the same results as `gsl_stats_kurtosis()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 346 of file `vec_stats.h`.

**47.37.2.14** `template<class vec_t> double vector_lag1_autocorr ( size_t n, const vec_t & data, double mean )`

This function computes

$$\left[ \sum_i (x_i - \mu)(x_{i-1} - \mu) \right] \left[ \sum_i (x_i - \mu)^2 \right]^{-1}$$

This function produces the same results as `gsl_stats_lag1_autocorrelation_m()`.

If  $n$  is zero, this function will call the error handler.

Definition at line 369 of file `vec_stats.h`.

**47.37.2.15** `template<class vec_t> double vector_lag1_autocorr ( size_t n, const vec_t & data )`

This function computes

$$\left[ \sum_i (x_i - \mu)(x_{i-1} - \mu) \right] \left[ \sum_i (x_i - \mu)^2 \right]^{-1}$$

This function produces the same results as `gsl_stats_lag1_autocorrelation()`.

If  $n$  is zero, this function will call the error handler.

Definition at line 404 of file `vec_stats.h`.

**47.37.2.16** `template<class vec_t> double vector_covariance ( size_t n, const vec_t & data1, const vec_t & data2, double mean1, double mean2 )`

This function computes

$$\frac{1}{n-1} \sum_i (x_i - \bar{x})(y_i - \bar{y})$$

where  $\bar{x}$  and  $\bar{y}$  are specified in `mean1` and `mean2`, respectively.

This function produces the same results as `gsl_stats_covariance_m()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 426 of file `vec_stats.h`.

**47.37.2.17** `template<class vec_t> double vector_covariance ( size_t n, const vec_t & data1, const vec_t & data2 )`

This function computes

$$\frac{1}{n-1} \sum_i (x_i - \bar{x})(y_i - \bar{y})$$

where  $\bar{x}$  and  $\bar{y}$  are the averages of `data1` and `data2` and are computed automatically using [vector\\_mean\(\)](#).

This function produces the same results as `gsl_stats_covariance()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 455 of file `vec_stats.h`.

**47.37.2.18** `template<class vec_t> double vector_correlation ( size_t n, const vec_t & data1, const vec_t & data2 )`

This function computes the Pearson correlation coefficient between `data1` and `data2`.

This function produces the same results as `gsl_stats_correlation()`.

If  $n$  is zero, this function will call the error handler.

Definition at line 488 of file vec\_stats.h.

**47.37.2.19** `template<class vec_t, class vec2_t> double vector_pvariance ( size_t n1, const vec_t & data1, size_t n2, const vec2_t & data2 )`

**Todo** Document this

This function produces the same results as `gsl_stats_pvariance()`.

If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 543 of file vec\_stats.h.

**47.37.2.20** `template<class vec_t> double vector_quantile_sorted ( size_t n, const vec_t & data, const double f )`

This function returns the quantile  $f$  of data which has already been sorted in ascending order. The quantile,  $q$ , is found by interpolation using

$$q = (1 - \delta)x_i + \delta x_{i+1}$$

where  $i = \text{floor}[(n-1)f]$  and  $\delta = (n-1)f - i$ .

This function produces the same results as `gsl_stats_quantile_from_sorted_data()`.

No checks are made to ensure the data is sorted, or to ensure that  $0 \leq f \leq 1$ . If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 570 of file vec\_stats.h.

**47.37.2.21** `template<class vec_t> double vector_median_sorted ( size_t n, const vec_t & data )`

This function returns the median of sorted data (either ascending or descending), assuming the data has already been sorted. When the data set has an odd number of elements, the median is the value of the element at index  $(n-1)/2$ , otherwise, the median is taken to be the average of the elements at indices  $(n-1)/2$  and  $n/2$ .

This function produces the same results as `gsl_stats_median_from_sorted_data()`.

No checks are made to ensure the data is sorted. If  $n$  is zero, this function will return zero without calling the error handler.

Definition at line 598 of file vec\_stats.h.

**47.37.2.22** `template<class vec_t, class vec2_t, class vec3_t> double vector_chi_squared ( size_t n, const vec_t & obs, const vec2_t & exp, const vec3_t & err )`

This function computes

$$\sum_i \left( \frac{\text{obs}_i - \text{exp}_i}{\text{err}_i} \right)^2$$

where `obs` are the observed values, `exp` are the expected values, and `err` are the errors.

Definition at line 622 of file vec\_stats.h.

**47.37.2.23** `template<class vec_t> double wvector_mean ( size_t n, const vec_t & data, const vec_t & weights )`

This function computes

$$\left( \sum_i w_i x_i \right) \left( \sum_i w_i \right)^{-1}$$

This function produces the same results as `gsl_stats_wmean()`.

Definition at line 650 of file vec\_stats.h.

47.37.2.24 `template<class vec_t> double wvector_factor ( size_t n, const vec_t & weights )`

This function is used internally in `wvector_variance(size_t n, vec_t &data, const vec2_t &weights, double wmean)` and `wvector_stddev(size_t n, vec_t &data, const vec2_t &weights, double wmean)`.

Definition at line 672 of file `vec_stats.h`.

47.37.2.25 `template<class vec_t, class vec2_t> double wvector_variance_fmean ( size_t n, const vec_t & data, const vec2_t & weights, double wmean )`

This function computes

$$\left[ \sum_i w_i (x_i - \mu)^2 \right] \left[ \sum_i w_i \right]^{-1}$$

This function produces the same results as `gsl_stats_wvariance_with_fixed_mean()`.

Definition at line 702 of file `vec_stats.h`.

47.37.2.26 `template<class vec_t, class vec2_t> double wvector_variance ( size_t n, const vec_t & data, const vec2_t & weights, double wmean )`

This function produces the same results as `gsl_stats_wvariance_m()`.

Definition at line 725 of file `vec_stats.h`.

47.37.2.27 `template<class vec_t, class vec2_t> double wvector_variance ( size_t n, const vec_t & data, const vec2_t & weights )`

This function produces the same results as `gsl_stats_wvariance()`.

Definition at line 742 of file `vec_stats.h`.

47.37.2.28 `template<class vec_t, class vec2_t> double wvector_stddev_fmean ( size_t n, const vec_t & data, const vec2_t & weights, double wmean )`

This function produces the same results as `gsl_stats_wsd_with_fixed_mean()`.

Definition at line 756 of file `vec_stats.h`.

47.37.2.29 `template<class vec_t, class vec2_t> double wvector_stddev ( size_t n, const vec_t & data, const vec2_t & weights )`

This function produces the same results as `gsl_stats_wsd()`.

Definition at line 768 of file `vec_stats.h`.

47.37.2.30 `template<class vec_t, class vec2_t> double wvector_stddev ( size_t n, const vec_t & data, const vec2_t & weights, double wmean )`

This function produces the same results as `gsl_stats_wsd_m()`.

Definition at line 781 of file `vec_stats.h`.

47.37.2.31 `template<class vec_t, class vec2_t> double wvector_sumsq ( size_t n, const vec_t & data, const vec2_t & weights, double wmean )`

This function produces the same results as `gsl_stats_wtss_m()`.

Definition at line 797 of file `vec_stats.h`.

47.37.2.32 `template<class vec_t, class vec2_t> double wvector_sumsq ( size_t n, const vec_t & data, const vec2_t & weights )`

This function produces the same results as `gsl_stats_wtss()`.

Definition at line 818 of file `vec_stats.h`.



**47.37.2.33** `template<class vec_t, class vec2_t> double wvector_absdev ( size_t n, const vec_t & data, const vec2_t & weights, double wmean )`

This function produces the same results as `gsl_stats_wabsdev_m()`.

Definition at line 831 of file `vec_stats.h`.

**47.37.2.34** `template<class vec_t, class vec2_t> double wvector_absdev ( size_t n, const vec_t & data, const vec2_t & weights )`

This function produces the same results as `gsl_stats_wabsdev()`.

Definition at line 852 of file `vec_stats.h`.

**47.37.2.35** `template<class vec_t, class vec2_t> double wvector_skew ( size_t n, const vec_t & data, const vec2_t & weights, double wmean, double wsd )`

This function produces the same results as `gsl_stats_wskew_m_sd()`.

Definition at line 866 of file `vec_stats.h`.

**47.37.2.36** `template<class vec_t, class vec2_t> double wvector_skew ( size_t n, const vec_t & data, const vec2_t & weights )`

This function produces the same results as `gsl_stats_wskew()`.

Definition at line 888 of file `vec_stats.h`.

**47.37.2.37** `template<class vec_t, class vec2_t> double wvector_kurtosis ( size_t n, const vec_t & data, const vec2_t & weights, double wmean, double wsd )`

This function produces the same results as `gsl_stats_wkurtosis_m_sd()`.

Definition at line 901 of file `vec_stats.h`.

**47.37.2.38** `template<class vec_t, class vec2_t> double wvector_kurtosis ( size_t n, const vec_t & data, const vec2_t & weights )`

This function produces the same results as `gsl_stats_wkurtosis()`.

Definition at line 923 of file `vec_stats.h`.

## 47.38 vector.h File Reference

File for generic vector functions.

```
#include <iostream> #include <cmath> #include <string> #include <fstream> #include <sstream> ×
#include <o2scl/err_hnd.h> #include <o2scl/uniform_grid.h> #include <gsl/gsl_ieee_utils.-
h> #include <gsl/gsl_sort.h>
```

### 47.38.1 Detailed Description

This file contains a set of template functions which can be applied to almost any vector or matrix type which allow element access through `operator[]`. Detailed requirements on the template parameters are given in the functions below.

For a general discussion of vectors and matrices in `O2scl`, see the [Arrays, Vectors, Matrices and Tensors](#) of the User's Guide.

For overloaded arithmetic operators involving vectors and matrices, see [vec\\_arith.h](#). For statistics operations not included here, see [vec\\_stats.h](#) in the directory `src/other`. For assorted functions and classes which are specific to C-style arrays, see [array.h](#). Also related are the matrix output functions, [matrix\\_out\(\)](#), [matrix\\_cx\\_out\\_paren\(\)](#), and [matrix\\_out\\_paren\(\)](#) which are defined in [columnify.h](#) because they utilize the class [columnify](#) to format the output.

For functions which search for a value in an ordered (either increasing or decreasing) vector, see the class [search\\_vec](#).

**Idea for Future** Create a matrix transpose copy function?

**Idea for Future** Create matrix swap row and column functions

Definition in file [vector.h](#).

## Data Structures

- class [matrix\\_row](#)< [mat\\_t](#) >  
*Create a vector-like class from a row of a matrix.*

## Functions

- template<class [vec\\_t](#), class [data\\_t](#) >  
void [vector\\_grid](#) ([uniform\\_grid](#)< [data\\_t](#) > g, [vec\\_t](#) &v)  
*Fill a vector with a specified grid.*

### Copying functions

- template<class [vec\\_t](#), class [vec2\\_t](#) >  
void [vector\\_copy](#) (size\_t N, [vec\\_t](#) &src, [vec2\\_t](#) &dest)  
*Simple vector copy.*
- template<class [vec\\_t](#), class [vec2\\_t](#), class [base\\_t](#) >  
void [vector\\_swap](#) (size\_t N, [vec\\_t](#) &v1, [vec2\\_t](#) &v2)  
*Generic vector swap.*
- template<class [mat\\_t](#), class [mat2\\_t](#) >  
void [matrix\\_copy](#) (size\_t M, size\_t N, [mat\\_t](#) &src, [mat2\\_t](#) &dest)  
*Simple matrix copy.*
- template<class [vec\\_t](#), class [vec2\\_t](#) >  
void [vector\\_cx\\_copy\\_gsl](#) (size\_t N, [vec\\_t](#) &src, [vec2\\_t](#) &dest)  
*GSL complex vector copy.*
- template<class [mat\\_t](#), class [mat2\\_t](#) >  
void [matrix\\_cx\\_copy\\_gsl](#) (size\_t M, size\_t N, [mat\\_t](#) &src, [mat2\\_t](#) &dest)  
*GSL complex matrix copy.*

### Sorting functions

- template<class [vec\\_t](#), class [data\\_t](#) >  
void [sort\\_downheap](#) ([vec\\_t](#) &data, size\_t n, size\_t k)  
*Provide a downheap() function for [vector\\_sort\(\)](#)*
- template<class [vec\\_t](#), class [data\\_t](#) >  
int [vector\\_sort](#) (size\_t n, [vec\\_t](#) &data)  
*Sort a vector (in increasing order)*
- template<class [vec\\_t](#), class [vec\\_size\\_t](#) >  
int [sort\\_index\\_downheap](#) (size\_t N, const [vec\\_t](#) &data, [vec\\_size\\_t](#) &order, size\_t k)  
*Provide a downheap() function for [vector\\_sort\\_index\(\)](#)*
- template<class [vec\\_t](#), class [vec\\_size\\_t](#) >  
int [vector\\_sort\\_index](#) (size\_t n, const [vec\\_t](#) &data, [vec\\_size\\_t](#) &order)  
*Create a permutation which sorts a vector (in increasing order)*
- template<class [vec\\_t](#) >  
int [vector\\_sort\\_double](#) (size\_t n, [vec\\_t](#) &data)  
*Sort a vector of doubles (in increasing order)*

### Smallest and largest functions

- template<class [vec\\_t](#), class [data\\_t](#) >  
int [vector\\_smallest](#) (size\_t n, [vec\\_t](#) &data, size\_t k, [vec\\_t](#) &smallest)  
*Find the k smallest entries of a vector.*
- template<class [vec\\_t](#), class [data\\_t](#) >  
int [vector\\_largest](#) (size\_t n, [vec\\_t](#) &data, size\_t k, [vec\\_t](#) &largest)  
*Find the k largest entries of a vector.*

## Vector minimum and maximum functions

- `template<class vec_t, class data_t >`  
`data_t vector_max_value (size_t n, const vec_t &data)`  
*Compute the maximum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`size_t vector_max_index (size_t n, const vec_t &data)`  
*Compute the index which holds the maximum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`void vector_max (size_t n, const vec_t &data, size_t &index, data_t &val)`  
*Compute the maximum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`data_t vector_min_value (size_t n, const vec_t &data)`  
*Compute the minimum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`size_t vector_min_index (size_t n, const vec_t &data)`  
*Compute the index which holds the minimum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`void vector_min (size_t n, const vec_t &data, size_t &index, data_t &val)`  
*Compute the minimum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`void vector_minmax_value (size_t n, const vec_t &data, data_t &min, data_t &max)`  
*Compute the minimum and maximum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`void vector_minmax_index (size_t n, const vec_t &data, size_t &ix_min, size_t &ix_max)`  
*Compute the minimum and maximum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`void vector_minmax (size_t n, const vec_t &data, size_t &ix_min, data_t &min, size_t &ix_max, data_t &max)`  
*Compute the minimum and maximum of the first n elements of a vector.*

## Matrix minimum and maximum functions

- `template<class mat_t, class data_t >`  
`data_t matrix_max (size_t n, const size_t m, const mat_t &data)`  
*Compute the maximum of a matrix.*
- `template<class mat_t, class data_t >`  
`data_t matrix_min (size_t n, const size_t m, const mat_t &data)`  
*Compute the minimum of a matrix.*
- `template<class mat_t, class data_t >`  
`int matrix_minmax (size_t n, const size_t m, const mat_t &data, data_t &min, data_t &max)`  
*Compute the minimum and maximum of a matrix.*

## Searching functions

- `template<class vec_t >`  
`size_t vector_lookup (size_t n, const vec_t &x, double x0)`  
*Lookup element x0 in vector x of length n.*
- `template<class vec_t, class data_t >`  
`size_t vector_bsearch_inc (const data_t x0, const vec_t &x, size_t lo, size_t hi)`  
*Binary search a part of an increasing vector for x0.*
- `template<class vec_t, class data_t >`  
`size_t vector_bsearch_dec (const data_t x0, const vec_t &x, size_t lo, size_t hi)`  
*Binary search a part of a decreasing vector for x0.*
- `template<class vec_t, class data_t >`  
`size_t vector_bsearch (const data_t x0, const vec_t &x, size_t lo, size_t hi)`  
*Binary search a part of a monotonic vector for x0.*

## Miscellaneous mathematical functions

- `template<class vec_t, class data_t >`  
`data_t vector_sum (size_t n, const vec_t &data)`  
*Compute the sum of the first n elements of a vector.*
- `template<class vec_t, class data_t >`  
`data_t vector_norm (size_t n, const vec_t &x)`  
*Compute the norm of a vector of floating-point (single or double precision) numbers.*

## Other functions

- `template<class vec_t, class data_t >`  
`int vector_rotate (size_t n, vec_t &data, size_t k)`  
*"Rotate" a vector so that the kth element is now the beginning*
- `template<class vec_t, class data_t >`  
`int vector_reverse (size_t n, vec_t &data)`  
*Reverse a vector.*
- `template<class vec_t >`  
`int vector_out (std::ostream &os, size_t n, const vec_t &v, bool endlne=false)`  
*Output a vector to a stream.*

## 47.38.2 Function Documentation

47.38.2.1 `template<class vec_t, class vec2_t > void vector_copy ( size_t N, vec_t & src, vec2_t & dest )`

## Note

This ordering is reversed from the GSL function `gsl_vector_memcpy()`. This is to be used with

```
vector_copy(N, source, destination);
```

instead of

```
gsl_vector_memcpy(destination, source);
```

It is assumed that the memory allocation for `dest` has already been performed.

This function will work for any class `vec2_t` which has an operator[] which returns a reference to the corresponding element and class `vec_t` with an operator[] which returns either a reference or the value of the corresponding element.

Definition at line 90 of file `vector.h`.

47.38.2.2 `template<class vec_t, class vec2_t, class base_t > void vector_swap ( size_t N, vec_t & v1, vec2_t & v2 )`

This function swaps the elements of `v1` and `v2`, one element at a time.

Definition at line 110 of file `vector.h`.

47.38.2.3 `template<class mat_t, class mat2_t > void matrix_copy ( size_t M, size_t N, mat_t & src, mat2_t & dest )`

## Note

This ordering is reversed from the GSL function `gsl_matrix_memcpy()`. This is to be used with

```
matrix_copy(N, source, destination);
```

instead of

```
gsl_matrix_memcpy(destination, source);
```

It is assumed that the memory allocation for `dest` has already been performed.

This function will work for any class `vec2_t` which has an operator[][] which returns a reference to the corresponding element and class `vec_t` with an operator[][] which returns either a reference or the value of the corresponding element.

Definition at line 157 of file `vector.h`.

47.38.2.4 `template<class vec_t, class vec2_t > void vector.cx_copy_gsl ( size_t N, vec_t & src, vec2_t & dest )`

**Idea for Future** At present this works only with complex types based directly on the GSL complex format. This could be improved.

Definition at line 171 of file `vector.h`.

47.38.2.5 `template<class mat_t, class mat2_t> void matrix_cx_copy_gsl ( size_t M, size_t N, mat_t & src, mat2_t & dest )`

**Idea for Future** At present this works only with complex types based directly on the GSL complex format. This could be improved.

Definition at line 184 of file vector.h.

47.38.2.6 `template<class vec_t, class data_t> int vector_sort ( size_t n, vec_t & data )`

This is a generic sorting template function using a heapsort algorithm. It will work for any types `data_t` and `vec_t` for which

- `data_t` has a non-const version of `operator=`
- `data_t` has a less than operator to compare elements
- `vec_t::operator[]` returns a non-const reference to an object of type `data_t`

In particular, it will work with [ovector](#), [uvector](#), [ovector\\_int](#), [uvector\\_int](#) (and other related O<sub>2</sub>scl vector classes), the STL template class `std::vector`, and arrays and pointers of numeric, character, and string objects.

For example,

```
std::string list[3]={"dog","cat","fox"};
vector_sort<std::string[3],std::string>(3,list);
```

#### Note

With this function template alone, the user cannot avoid explicitly specifying the template types for this function because there is no parameter of type `data_t`, and function templates cannot handle default template types. For this reason, the function template [vector\\_sort\\_double\(\)](#) was also created which provides the convenience of not requiring the user to specify the vector template type.

This sorting routine is not stable, i.e. equal elements have arbitrary final ordering

This works similarly to the GSL function `gsl_sort_vector()`.

Definition at line 251 of file vector.h.

47.38.2.7 `template<class vec_t, class vec_size_t> int vector_sort_index ( size_t n, const vec_t & data, vec_size_t & order )`

This function takes a vector `data` and arranges a list of indices in `order`, which give a sorted version of the vector. The value `order[i]` gives the index of entry in `data` which corresponds to the *i*th value in the sorted vector. The vector `data` is unchanged by this function, and the initial values in `order` are ignored. Before calling this function, `order` must already be allocated as a vector of size `n`.

For example, after calling this function, a sorted version the vector can be output with

```
size_t n=5;
double data[5]={3.1,4.1,5.9,2.6,3.5};
permutation order(n);
vector_sort_index(n,data,order);
for(size_t i=0;i<n;i++) {
    cout << data[order[i]] << endl;
}
```

To create a permutation which stores as its *i*th element, the index of `data[i]` in the sorted vector, you can invert the permutation created by this function.

This is a generic sorting template function. It will work for any types `vec_t` and `vec_size_t` for which

- `vec_t` has an `operator[]`, and
- `vec_size_t` has an `operator[]` which returns a `size_t`. One possible type for `vec_size_t` is [permutation](#).

This works similarly to the GSL function `gsl_sort_index()`.

Definition at line 344 of file vector.h.

47.38.2.8 `template<class vec_t > int vector_sort_double ( size_t n, vec_t & data )`

This function is just a wrapper for

```
vector_sort<vec_t, double>(n, data);
```

See the documentation of [vector\\_sort\(\)](#) for more details.

Definition at line 396 of file vector.h.

47.38.2.9 `template<class vec_t, class data_t > int vector_smallest ( size_t n, vec_t & data, size_t k, vec_t & smallest )`

Given a vector `data` of size `n` this sets the first `k` entries of the vector `smallest` to the `k` smallest entries from vector `data` in ascending order. The vector `smallest` must be allocated beforehand to hold at least `k` elements.

This works similarly to the GSL function `gsl_sort_smallest()`.

#### Note

This  $\mathcal{O}(kN)$  algorithm is useful only when  $k \ll N$ .

If `k` is zero, then this function does nothing and returns [gsl\\_success](#).

Definition at line 419 of file vector.h.

47.38.2.10 `template<class vec_t, class data_t > int vector_largest ( size_t n, vec_t & data, size_t k, vec_t & largest )`

Given a vector `data` of size `n` this sets the first `k` entries of the vector `largest` to the `k` largest entries from vector `data` in descending order. The vector `largest` must be allocated beforehand to hold at least `k` elements.

This works similarly to the GSL function `gsl_sort_largest()`.

#### Note

This  $\mathcal{O}(kN)$  algorithm is useful only when  $k \ll N$ .

If `k` is zero, then this function does nothing and returns [gsl\\_success](#).

Definition at line 466 of file vector.h.

47.38.2.11 `template<class mat_t, class data_t > data_t matrix_max ( size_t n, const size_t m, const mat_t & data )`

**Idea for Future** Write `matrix_max_index()` and related functions similar to the way [vector\\_max\\_index\(\)](#) works.

Definition at line 701 of file vector.h.

47.38.2.12 `template<class vec_t > size_t vector_lookup ( size_t n, const vec_t & x, double x0 )`

This function finds the element in vector `x` which is closest to `x0`. It ignores all elements in `x` which are not finite. If the vector is empty (i.e. `n` is zero), or if all of the elements in `x` are not finite, then the error handler will be called.

This function works for all classes `vec_t` where an operator[] is defined which returns a double (either as a value or a reference).

**Idea for Future** Write `matrix_lookup()`.

Definition at line 820 of file vector.h.

47.38.2.13 `template<class vec_t, class data_t > size_t vector_bsearch_inc ( const data_t x0, const vec_t & x, size_t lo, size_t hi )`

This function performs a binary search of between `x[lo]` and `x[hi]`. It returns

- `lo` if `x0 < x[lo]`
- `i` if `x[i] <= x0 < x[i+2]` for `lo <= i < hi`
- `hi-1` if `x0 >= x[hi-1]`

The element at `x[hi]` is never referenced by this function. The parameter `hi` can be either the index of the last element (e.g. `n-1` for a vector of size `n` with starting index `0`), or the index of one element (e.g. `n` for a vector of size `n` and a starting index `0`) for a depending on whether or not the user wants to allow the function to return the index of the last element.

This function operates in the same way as `gsl_interp_bsearch()`.

The operation of this function is undefined if the data is not strictly monotonic, i.e. if some of the data elements are equal.

This function will call the error handler if `lo` is greater than `hi`.

Definition at line 874 of file `vector.h`.

**47.38.2.14** `template<class vec_t, class data_t> size_t vector_bsearch_dec ( const data_t x0, const vec_t & x, size_t lo, size_t hi )`

This function performs a binary search of between `x[lo]` and `x[hi]` (inclusive). It returns

- `lo` if `x0 > x[lo]`
- `i` if `x[i] >= x0 > x[i+1]` for `lo <= i < hi`
- `hi-1` if `x0 <= x[hi-1]`

The element at `x[hi]` is never referenced by this function. The parameter `hi` can be either the index of the last element (e.g. `n-1` for a vector of size `n` with starting index `0`), or the index of one element (e.g. `n` for a vector of size `n` and a starting index `0`) for a depending on whether or not the user wants to allow the function to return the index of the last element.

The operation of this function is undefined if the data is not strictly monotonic, i.e. if some of the data elements are equal.

This function will call the error handler if `lo` is greater than `hi`.

Definition at line 919 of file `vector.h`.

**47.38.2.15** `template<class vec_t, class data_t> size_t vector_bsearch ( const data_t x0, const vec_t & x, size_t lo, size_t hi )`

This wrapper just calls `vector_bsearch_inc()` or `vector_bsearch_dec()` depending on the ordering of `x`.

Definition at line 945 of file `vector.h`.

**47.38.2.16** `template<class vec_t, class data_t> data_t vector_sum ( size_t n, vec_t & data )`

If `n` is zero, this will set `sum` to zero and return `gsl_success`.

Definition at line 962 of file `vector.h`.

**47.38.2.17** `template<class vec_t, class data_t> data_t vector_norm ( size_t n, const vec_t & x )`

This function is a more generic version of `o2scl_cblas::dnrm2`.

Definition at line 978 of file `vector.h`.

**47.38.2.18** `template<class vec_t, class data_t> int vector_rotate ( size_t n, vec_t & data, size_t k )`

This is a generic template function which will work for any types `data_t` and `vec_t` for which

- `data_t` has an `operator=`
- `vec_t::operator[]` returns a reference to an object of type `data_t`

This function is used, for example, in `pinside`.

## Note

This function is not the same as a Givens rotation, which is typically referred to in BLAS routines as `drot()`.

Definition at line 1025 of file `vector.h`.

**47.38.2.19** `template<class vec_t, class data_t> int vector_reverse ( size_t n, vec_t & data )`

If `n` is zero, this function will silently do nothing.

Definition at line 1044 of file `vector.h`.

**47.38.2.20** `template<class vec_t> int vector_out ( std::ostream & os, size_t n, const vec_t & v, bool endline = false )`

No trailing space is output after the last element, and an `endline` is output only if `endline` is set to `true`. If the parameter `n` is zero, this function silently does nothing.

Note that the `O2scl` vector classes also have their own `operator<<()` defined for them.

This works with any class `vec_t` which has an `operator[]` which returns either the value of or a reference to the `i`th element and the element type has its own output operator which has been defined.

Definition at line 1070 of file `vector.h`.

## 47.39 vector\_derint.h File Reference

Derivatives of integrals of functions stored in vectors with implicit fixed-size grid.

```
#include <o2scl/ovector_tlate.h> #include <o2scl/interp.h>
```

### 47.39.1 Detailed Description

Integrate a function over a fixed-size grid specified in a vector. The integrals are always specified without the factor defining the grid size (i.e.  $\Delta x$ ), so the user must always multiply the result by the grid size afterwards to get the true integral.

These integration rules often expect a minimum number of points, so for smaller vectors they fall back onto rules which use fewer points. For empty vectors they return zero, for vectors of length 1, they always return the sole element of the vector, and for vectors of length 2, they always return the average of the two elements.

More points does not always mean higher accuracy.

Definition in file `vector_derint.h`.

### Functions

- `template<class vec_t, class vec2_t>`  
`void vector_deriv_threept (size_t n, vec_t &v, vec2_t &v2)`  
*Derivative of a vector with a three-point formula.*
- `template<class vec_t, class vec2_t>`  
`void vector_deriv_threept_tap (size_t n, vec_t &v, vec2_t &v2)`  
*Derivative of a vector with a three-point formula using two-point at the edges.*
- `template<class vec_t, class vec2_t>`  
`void vector_deriv_fivept (size_t n, vec_t &v, vec2_t &v2)`  
*Derivative of a vector with a five-point formula.*
- `template<class vec_t, class vec2_t>`  
`void vector_deriv_fivept_tap (size_t n, vec_t &v, vec2_t &v2)`  
*Derivative of a vector with a five-point formula with four- and three-point formulas used at the edges.*
- `template<class ovec_t>`  
`void vector_deriv_interp (size_t n, ovec_t &v, ovec_t &v2, o2scl::base_interp_mgr< ovec_t > &bim)`  
*Derivative from interpolation object.*



- `template<class vec_t >`  
`double vector_integ_trap (size_t n, vec_t &v)`  
*Integrate with an extended trapezoidal rule.*
- `template<class vec_t >`  
`double vector_integ_thrept (size_t n, vec_t &v)`  
*Integrate with an extended 3-point rule (extended Simpson's rule)*
- `template<class vec_t >`  
`double vector_integ_extended4 (size_t n, vec_t &v)`  
*Integrate with an extended rule for 4 or more points.*
- `template<class vec_t >`  
`double vector_integ_durand (size_t n, vec_t &v)`  
*Integrate with Durand's rule for 4 or more points.*
- `template<class vec_t >`  
`double vector_integ_extended8 (size_t n, vec_t &v)`  
*Integrate with an extended rule for 8 or more points.*
- `template<class ovec_t >`  
`double vector_integ_interp (size_t n, ovec_t &v, base_interp_mgr< ovec_t > &bim)`  
*Integral from interpolation object.*

## 47.39.2 Function Documentation

47.39.2.1 `template<class vec_t > double vector_integ_thrept ( size_t n, vec_t & v )`

### Note

This uses an untested hack I wrote for even n.

Definition at line 181 of file `vector_derint.h`.

47.39.2.2 `template<class vec_t > double vector_integ_extended4 ( size_t n, vec_t & v )`

This function falls back to the equivalent of `vector_integ_thrept()` for 3 points.

Definition at line 213 of file `vector_derint.h`.

47.39.2.3 `template<class vec_t > double vector_integ_durand ( size_t n, vec_t & v )`

This function falls back to the equivalent of `vector_integ_thrept()` for 3 points.

Definition at line 236 of file `vector_derint.h`.

47.39.2.4 `template<class vec_t > double vector_integ_extended8 ( size_t n, vec_t & v )`

This function falls back to `vector_integ_extended4()` for less than 8 points.

Definition at line 259 of file `vector_derint.h`.