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I. MODEL

This is the manual for the supernova equation of state (EOS) tables calculated with the statistical model with excluded volume and interactions, as presented in Ref. [1]. In this manual we focus on the different nuclear interactions and nuclear mass tables used for the calculation of the EOS tables and the tables themselves. We do not repeat the entire description of the EOS model, but only list the changes compared to the published description of the model.

List of changes

• Excited states: Excited states are now only considered up to the binding energy *BE* of the corresponding nucleus:

$$g_{A,Z}(T) = g_{A,Z}^0 + \frac{c_1}{A^{5/3}} \int_0^{E_{max}} dE^* e^{-E^*/T} \exp\left(\sqrt{2a(A)E^*}\right)$$
(1)

where we use $E_{max} = BE$, to represent that the excited states still have to be bound. The inclusion of excited states up to infinite energies has only a minor influence on the composition but leads to an unphysically large contribution of excited states to the energy density and entropy.

- Neutron-drip nuclei: We determine the neutron drip line and eliminate all nuclei of the mass tables behind it. This concerns the experimental nuclei from Ref. [2] and from the theoretical nuclear mass tables as well (the mass tables are described in Sec. IV). We did this because nuclear structure calculations for these nuclei are not very reliable. Furthermore, this gives a consistent criterion which nuclei are considered for the calculation of the EOS.
- Definition of electron and proton chemical potentials: In Ref. [1] the electron chemical potential contained a contribution from the Coulomb interactions, given by: $\frac{PCoul}{n_e}$. Now we include this Coulomb part of the chemical potential in the proton chemical potential, so that the stored electron chemical potential is just the normal chemical potential of the Fermi-Dirac distribution function. The same definition was used in the EOS tables of Refs. [3] and [4, 5]. Note that both definitions are physically meaningful. However, the present definition has the advantage, that the EOS is also thermodynamic consistent, if the electron contribution is not included in the table. This was not the case in the previous definition.
- Nucleon masses: We always use the experimental values of the nucleon masses, also within the relativistic mean-field (RMF) part of the calculation. This avoids any spurious jumps when going from the ideal gas regime to large densities where the RMF interactions become important. However, this represents a slight change of the actual RMF parameterization. We checked that the small change of the nucleon masses to their real values is negligible for the nuclear matter properties.

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Quantity	Symbol	Value	Unit
fine structure constant	α	$7.2973525376\!\times\!10^{-3}$	_
speed of light	c	29979245800	$\mathrm{cm/s}$
reduced Planck's constant times c	$\hbar c$	197.3269631	MeV fm
electron mass	m_e	0.51099891	MeV/c^2
neutron mass	m_n	939.565346	MeV/c^2
proton mass	m_p	938.272013	${ m MeV/c^2}$

TABLE I: Values of physical constants used in the calculation.

	$n_B^0 \ [\mathrm{fm}^{-3}]$	BE/A [MeV]	$K [{ m MeV}]$	$K' \; [\frac{{\rm MeV}}{{\rm fm}^3}]$	$J \; [{ m MeV}]$	$L \left[\frac{\text{MeV}}{\text{fm}^3}\right]$	m^{\ast}/m^{RMF}	$M_{max} [{ m M}_{\odot}]$
TM1	0.146	-16.31	282	-286	36.95	110.99	0.634	2.21
TMA	0.147	-16.03	318	-572	30.66	90.14	0.635	2.02
FSUgold	0.148	-16.27	230	-524	32.56	60.44	0.611	1.74
NL3	0.148	-16.24	271	203	37.39	118.50	0.595	2.79

TABLE II: Nuclear matter and neutron star properties of the relativistic mean field models TM1 [6], TMA [7], FSUgold [8, 10] and NL3 [9]. Listed are the saturation density n_B^0 , binding energy BE/A, incompressibility K, skewness coefficient K', symmetry energy J, symmetry energy slope coefficient L, the effective mass m^* divided by the RMF mass m^{RMF} at saturation density, and the maximum mass M_{max} of a cold neutron star.

II. PHYSICAL CONSTANTS

For all physical constants we use the 2006 CODATA values (www.codata.org), which are listed in Table I. In this document, we use natural units $\hbar = c = k_B = 1$.

III. NUCLEAR INTERACTIONS

For the relativistic mean-field (RMF) interactions of the nucleons we use the parameter sets TM1 [6], TMA [7], FSUgold [8] and NL3 [9]. For the parameter set NL3 [9] binding energies and charge radii of 10 nuclei and neutron radii were included in the fit procedure. In this parameterization only cubic and quartic scalar self interactions are considered in addition to the normal couplings to the nucleons.

TM1 was developed together with TM2, which were fitted to binding energies and charge radii of light (TM2) and heavy nuclei (TM1). TMA is based on an interpolation of these two parameter sets. The coupling parameters g_i of the set TMA are chosen to be mass-number dependent of the form $g_i = a_i + b_i/A^{0.4}$, with a_i and b_i being constants, to have a good description of nuclei over the entire range of mass number. For uniform nuclear matter the couplings become constants and are given by a_i . TMA was also used in Ref. [1], where our EOS model was described in detail. The Lagrangians of TM1 and TMA have the same form, only the coupling parameters and meson masses are different. Compared to the NL3, vector self interactions are included, which modify the high density behavior of the EOS.

In FSUgold in addition the coupling between the omega- and the rho-meson is included. This leads to a different behavior of the density dependence of the symmetry energy, see e.g. [10]. Table II lists some characteristic saturation properties of uniform nuclear matter, and the resulting maximum mass of a cold neutron star of the four different parameterizations. The nuclear matter properties in Table II are calculated for T = 0, and like the EOS tables with the real nucleon masses m_n and m_p . The maximum masses where calculated directly with the EOS tables, for the lowest available temperature of T = 0.1 MeV.

IV. MASS TABLES

All EOS tables take into account the experimental data on nuclear masses from Audi, Wapstra, and Thibault [2]. For the masses of the experimentally unknown nuclei we take different theoretical nuclear structure calculations in form of nuclear mass tables. The TMA interactions are combined with the mass table of Geng et al. [11] which is also calculated with the relativistic mean field model TMA. Thus all nuclear interactions are consistent. The mass

table lists 6969 even-even, even-odd and odd-odd nuclei, extending from ¹⁶O to ³³¹100 from slightly above the proton to slightly below the neutron drip line. The nuclear binding energies are calculated under consideration of axial deformations and the pairing is included with a BCS-type δ -force. For the parametrization TM1 we do not have a suitable mass table at hand, thus we cannot avoid the minor "inconsistency" to use the table of Geng et al. [11], which is based on the TMA parameterization. For FSUgold we take a mass table which was calculated by X. Roca-Maza, see e.g. [12]. This table contains 1512 even-even nuclei, from the proton to the neutron drip, with $14 \le A \le 348$ and $8 \le Z \le 100$. No deformations are included and the pairing is introduced through a BCS approach with constant matrix elements (GA). The constant matrix element for neutrons has been fitted to reproduce the experimental binding in the tin isotopic chain and the constant matrix element for protons to the experimental binding in the N = 82 isotonic chain. The mass table for NL3 from Lalazissis and Raman [13] lists 1315 even-even nuclei with $10 \le Z \le 98$ using the BCS pairing scheme with constant pairing gap and taking into account axial deformations.

MESH OF THE EOS TABLES V.

Note that two different formats of the EOS tables are provided, first in an extended format and second in the Shen 98 format, i.e. in a format similar to the EOS tables of Ref. [4]. The different formats are explained in detail below. The EOS tables cover the following range:

• temperature T: 0.1 MeV $\leq T \lesssim 158.5$ MeV; exponential mesh of $\log_{10}(\Delta T) = 0.04$, giving 81 T-values. The temperature can be calculated from the temperature index i = 1, ..., 81 by:

$$T = 0.1 \cdot 10^{0.04(i-1)} \text{ MeV} .$$
⁽²⁾

• electron fraction Y_e :

Extended format: $0 \le Y_e \le 0.6$; linear mesh of $\Delta Y_e = 0.01$, giving 61 Y_e -values.

Shen 98 format: $0.01 \le Y_e \le 0.6$; linear mesh of $\Delta Y_e = 0.01$, giving 60 Y_e -values ($Y_e = 0$ is not included in the table).

The nominal electron fraction can be calculated from the electron fraction index j = 0, ..., 60, respectively j = 1, ..., 60, by:

$$Y_e = j \cdot 0.01 . \tag{3}$$

It is equal to the total proton fraction Y_p , due to charge neutrality.

• baryon number density n_B : 10^{-12} fm⁻³ $\leq n_B \leq 10$ fm⁻³; exponential mesh of $\log_{10}(\Delta n_B) = 0.04$, giving 326 n_B -values.

The nominal baryon number density can be calculated from the baryon number density index k = 1, ..., 326 by:

$$n_B = 10^{-12} \cdot 10^{0.04(k-1)} \,\mathrm{fm}^{-3} \,. \tag{4}$$

The different T, n_B and Y_e values sum up to 1610766 EOS grid points for the extended format and 1584360 EOS grid points for the Shen 98 format.

DESCRIPTION OF THE TABLES - EXTENDED FORMAT VI.

Entries of the tables Α.

The tables in the extended format contain the contribution of photons, electrons and positrons. In the following, all thermodynamic variables which are not further specified correspond to the definitions as given in Ref. [1]. For each density grid point the following 18 different thermodynamic quantities are listed and denoted by the EOS entry index l = 1, ..., 18:

- 1. baryon number density: $n_B \text{ [fm}^{-3]}$ n_B is given by $n_B = n_n + n_p + \sum_{A,Z} An_{A,Z}$, whereas here and in the following always $A \ge 2$ in the sum, and $n_{A,Z}$ is the number density of nucleus (A, Z).

2. total proton fraction: Y_p The total proton fraction is defined by:

$$Y_p = \frac{n_p + \sum_{A,Z} Z n_{A,Z}}{n_n + n_p + \sum_{A,Z} A n_{A,Z}},$$
(5)

which is equal to the electron fraction Y_e due to electric charge neutrality.

3. total energy per baryon: E^{tot} [MeV]

 E^{tot} is the total energy per baryon including rest masses:

$$E^{tot} = \frac{\epsilon^{tot}}{n_B} \tag{6}$$

$$\epsilon^{tot} = \xi \epsilon_{nuc}^{0}(T, n'_{n}, n'_{p}) + \sum_{A,Z} \epsilon_{A,Z}^{0}(T, n_{A,Z}) + f_{Coul}(n_{e}, \{n_{A,Z}\}) + \epsilon_{e}^{0} + \epsilon_{\gamma} , \qquad (7)$$

whereas n'_n and n'_p are the local number densities of neutrons, respectively protons, which are related to the total neutron and proton number densities by the filling factor $\xi = 1 - \sum_{A,Z} A n_{A,Z}/n_B^0$:

$$n_n = \xi n'_n \tag{8}$$

$$n_p = \xi n'_p . \tag{9}$$

4. total pressure: p^{tot} [MeV/fm³] The total pressure is given by:

$$p^{tot} = p^{0}_{nuc}(T, n'_{n}, n'_{p}) + \frac{1}{\kappa} \sum_{A,Z} p^{0}_{A,Z}(T, n_{A,Z}) + p_{Coul}(n_{e}, \{n_{A,Z}\}) + p^{0}_{e} + p_{\gamma} , \qquad (10)$$

whereas $\kappa = 1 - n_B / n_B^0$ is the free volume fraction.

5. total entropy per baryon: S^{tot} [k_B]

The total entropy per baryon is related to the baryonic entropy density via

$$S^{tot} = \frac{s^{tot}}{n_B} \tag{11}$$

$$s^{tot} = \sum_{A,Z}^{N_B} s^0_{A,Z}(T, n_{A,Z}) + \xi s^0_{nuc}(T, n'_n, n'_p) + \sum_{A,Z} n_{A,Z} \ln(\kappa) + s^0_e + s_\gamma .$$
(12)

6. neutron chemical potential relative to the neutron mass: μ_n^{nonrel} [MeV]

The neutron chemical potential is given in its non-relativistic equivalent form, i.e. without the neutron mass m_n :

$$\mu_n^{nonrel} = \mu_n - m_n \tag{13}$$

$$= \mu_n^0(T, n'_n, n'_p) + \frac{1}{n_B^0 \kappa} \sum_{A,Z} p_{A,Z}^0(T, n_{A,Z}) - m_n .$$
(14)

7. proton chemical potential relative to the proton mass: μ_p^{nonrel} [MeV]

The proton chemical potential is given in its non-relativistic equivalent form, i.e. without the proton mass m_p :

$$\mu_p^{nonrel} = \mu_p - m_p \tag{15}$$

$$= \mu_p^0(T, n'_n, n'_p) + \frac{1}{n_B^0 \kappa} \sum_{A,Z} p_{A,Z}^0(T, n_{A,Z}) + \frac{p_{Coul}}{n_e} - m_p , \qquad (16)$$

Note that the above expression for μ_p differs from the original definition in Ref. [1]. The Coulomb part of the chemical potential is now included here in the proton chemical potential instead of in the electron chemical potential, see also Sec. I.

8. electron chemical potential relative to the electron mass: μ_e^{nonrel} [MeV]

The electron chemical potential is given in its non-relativistic equivalent form, i.e. without the electron mass m_e :

$$\mu_e^{nonrel} = \mu_e - m_e \tag{17}$$

$$= \mu_e^0 - m_e$$
. (18)

Compared to the original definition of the electron chemical potential in Ref. [1], the Coulomb part of the chemical potential is now included in the proton chemical potential, see also Sec. I. Thus μ_e^{nonrel} is now just the kinetic part of the chemical potential.

9. total free energy per baryon: F^{tot} [MeV] The total free energy per baryon including rest masses is given by:

$$F^{tot} = \frac{f^{tot}}{n_B}$$
(19)
$$f^{tot} = \sum_{A,Z} f^0_{A,Z}(T, n_{A,Z}) + f_{Coul}(n_e, \{n_{A,Z}\})$$
$$+ \xi f^0_{nuc}(T, n'_n, n'_p) - T \sum_{A,Z} n_{A,Z} \ln(\kappa) + f^0_e + f_{\gamma} .$$
(20)

10. mass fraction of unbound neutrons: X_n The mass fraction of unbound neutrons is given by:

$$X_n = n_n / n_B . (21)$$

11. mass fraction of unbound protons: X_p The mass fraction of unbound protons is given by:

$$X_p = n_p/n_B . (22)$$

12. mass fraction of deuterons: X_d The mass fraction of deuterons (A = 2, Z = 1) is given by:

$$X_d = 2n_{2,1}/n_B . (23)$$

13. mass fraction of tritons: X_t The mass fraction of tritons (A = 3, Z = 1) is given by:

$$X_t = 3n_{3,1}/n_B . (24)$$

14. mass fraction of helions: X_h The mass fraction of helions (A = 3, Z = 2) is given by:

$$X_h = 3n_{3,2}/n_B . (25)$$

15. mass fraction of alphas: X_{α} The mass fraction of alphas (A = 4, Z = 2) is given by:

$$X_{\alpha} = 4n_{4,2}/n_B . (26)$$

16. mass fraction of heavy nuclei: X_A The mass fraction of heavy nuclei is defined by:

 $X_{A} = \sum_{A,Z} {}^{\prime} A n_{A,Z} / n_{B} , \qquad (27)$

whereas the prime on the sum denotes all nuclei except neutrons, protons, deuterons, tritons, helions, alphas.

17. averaged mass number of heavy nuclei: < A >

The mass number of the averaged heavy nucleus is defined by:

$$=\frac{\sum_{A,Z} 'An_{A,Z}}{\sum_{A,Z} 'n_{A,Z}}.$$
 (28)

18. averaged charge number of heavy nuclei: $\langle Z \rangle$

The charge number of the averaged heavy nucleus is defined in the analog way:

$$\langle Z \rangle = \frac{\sum_{A,Z} 'Z n_{A,Z}}{\sum_{A,Z} 'n_{A,Z}}$$
 (29)

B. Storage of the data

The EOS tables in the extended format are stored as binary files, which were created with the Intel fortran comiler ifort on a 64 bit machine. We plan to provide binary tables in the HDF5 standard in the future. The data is written as a single line from the array eos(1:t_entries,0:y_entries,1:nb_entries,1:entries) with t_entries = 81, y_entries = 60, nb_entries = 326, and entries = 18. A fortran module for the EOS is provided which contains a simple Fortran routine which reads in the table. Note that in this routine also the temperature is calculated from Eq. (2) and then stored as a separate array. We also provide a small example program which illustrates the usage of the module and the EOS table.

VII. DESCRIPTION OF THE TABLES - SHEN 98 FORMAT

A. Entries of the tables

The information is stored in a format which is very similar to the table of Shen et al. [4, 5] so that it can easily be implemented in running codes. In these tables only the baryonic contribution is given, i.e. photons, electrons, positrons and neutrinos have to be added separately. In the following, all thermodynamic variables which are not further specified are defined analogous to Subsec. VIA, but without the electron/positron and photon contribution. For each density grid point the following 19 different thermodynamic quantities are listed:

1. logarithm of baryon mass density: $\log_{10}(\rho_B)$ [g/cm³] The baryon mass density is defined as the baryon number density times the value of the atomic mass unit $m_u = 931.49432$ MeV used in Ref. [4, 5]:

$$\rho_B = n_B m_u . aga{30}$$

- 2. baryon number density: n_B [fm⁻³]
- 3. logarithm of total proton fraction: $\log_{10}(Y_p)$
- 4. total proton fraction: Y_p
- 5. baryonic part of the free energy per baryon relative to 938 MeV: ΔF_B [MeV] Like in the table of Shen et al. 938 MeV are subtracted from the baryonic part of the relativistic free energy per baryon:

$$\Delta F_B = \frac{f_B}{n_B} - 938 \text{ MeV} . \tag{31}$$

6. baryonic part of the energy per baryon relative to m_u : ΔE_B [MeV] ΔE_B is the baryonic part of the relativistic energy per baryon relative to the atomic mass unit m_u :

$$\Delta E_B = \frac{\epsilon_B}{n_B} - m_u . \tag{32}$$

7. baryonic part of the entropy per baryon S_B : $[k_B]$ The baryonic part of the entropy per baryon is related to the baryonic entropy density via

$$S_B = \frac{s_B}{n_B} \,. \tag{33}$$

8. average mass number of heavy nuclei: $\langle A \rangle_{Z6}$ The average mass number of heavy nuclei is defined by

$$_{Z6} = \frac{\sum_{A,Z\geq 6} An_{A,Z}}{\sum_{A,Z\geq 6} n_{A,Z}},$$
(34)

where we introduced the distinction between light and heavy nuclei for the Shen 98 format by the proton number 6, i.e. carbon.

9. average charge number of heavy nuclei: $\langle Z \rangle_{Z6}$ The average charge number of heavy nuclei is defined in the analog way

$$< Z >_{Z6} = \frac{\sum_{A,Z \ge 6} Z n_{A,Z}}{\sum_{A,Z \ge 6} n_{A,Z}}.$$
 (35)

10. effective mass: m^* [MeV]

In the RMF calculation the real nucleon masses m_n and m_p are used, see Sec. I. As they are not equal, also the nucleon effective masses $m_n^* = m_n + g_\sigma \sigma$ and $m_p^* = m_p + g_\sigma \sigma$ are not equal. Instead of storing these two values, we store the following effective mass m^* :

$$m^* = m_{RMF} + g_\sigma \sigma , \qquad (36)$$

with the nucleon mass of the RMF parameterization m_{RMF} . We want to emphasize again that m_{RMF} is not used in the calculation of the EOS, but it is only taken here as a reference value.

- 11. mass fraction of unbound neutrons: X_n
- 12. mass fraction of unbound protons: X_p
- 13. mass fraction of light nuclei: $X_{a_{Z6}}$ The mass fraction of light nuclei is defined by

$$X_{a_{Z6}} = \sum_{A,Z \le 5} An_{A,Z}/n_B .$$
(37)

14. mass fraction of heavy nuclei: $X_{A_{Z6}}$ The mass fraction of heavy nuclei is defined by

$$X_{A_{Z6}} = \sum_{A,Z \ge 6} An_{A,Z}/n_B .$$
(38)

- 15. baryonic part of the pressure: $p_B \, [\text{MeV/fm}^3]$
- 16. neutron chemical potential relative to the neutron mass: μ_n^{nonrel} [MeV]
- 17. proton chemical potential relative to the proton mass: μ_p^{nonrel} [MeV] Note the comments and further definitions from Subsec. VIA.
- 18. average mass number of light nuclei: $\langle a \rangle_{Z6}$ The average mass number of light nuclei is defined by

$$\langle a \rangle_{Z6} = \frac{\sum_{A,Z \le 5} An_{A,Z}}{\sum_{A,Z \le 5} n_{A,Z}}$$
 (39)

19. average charge number of light nuclei: $\langle z \rangle_{Z6}$ The average charge number of light nuclei is defined in the analog way

$$\langle z \rangle_{Z6} = \frac{\sum_{A,Z \le 5} Z n_{A,Z}}{\sum_{A,Z \le 5} n_{A,Z}}$$
 (40)

B. Storage of the data

The EOS tables in the Shen 98 format are stored as ASCII files. We store the three-dimensional tables in the following way: first we fix T which is noted at the top of the block, second we fix Y_p and third n_B . The blocks with different T are divided by the line 'ccc...ccc'. A fortran module for the EOS is provided which contains a simple Fortran routine which reads in the table in the EOS array eos(1:t_entries,1:y_entries,1:nb_entries,1:entries) with t_entries = 81, y_entries = 60, nb_entries = 326, and entries = 19. Note that in this routine by default the temperature is read in from the table (and not calculated from Eq. (2) like in the extended format) and then stored as a separate array. We also provide a small example program which illustrates the usage of the module and the EOS table.

VIII. NUCLEAR COMPOSITION

In addition to the information about the nuclear composition in the EOS tables as specified in Subsecs. VIA and VIIA we provide a Fortran module which allows to calculate the number densities and mass fractions of all available nuclei. This module reads in a separate binary file which contains all the required data for the calculation. The binary file was created with the Intel fortran comiler ifort on a 64 bit machine. We plan to provide binary tables in the HDF5 standard in the future. Because most of the input data is not meaningful by itself, we do not list the entries of the data table here. The composition module contains a lot of comments and in addition an example program is provided which should explain the usage of the module and the implemented routines.

The main subroutine of the module is $\mathtt{sub_dist}$, which calculates the nuclear distributions, the nuclear and nucleon densities and their mass fractions for given temperature index *i*, electron fraction index *j*, and baryon number density index *k* (see Sec. V). The mesh and its grid-points of the module correspond to the extended format of the EOS tables, i.e. the electron fraction $Y_p = 0$, respectively the electron fraction index j = 0, is included. The output of the module is:

- number density of unbound neutrons: n_n [fm⁻³]
- number density of unbound protons: n_p [fm⁻³]
- array with the number densities of all nuclei: $\{n_{A,Z}\}$ [fm⁻³]
- mass fraction of unbound neutrons: X_n
- mass fraction of unbound protons: X_p
- array with the mass fractions of all nuclei: $\{X_{A,Z}\}$ The mass fraction of nucleus (A, Z) is defined as

$$X_{A,Z} = \frac{An_{A,Z}}{n_B} \,. \tag{41}$$

IX. ACCURACY AND CONSISTENCY OF THE EOS TABLES

As the temperature is an input for the calculation of the tables, the values of T are exactly given by Eq. (2). Contrary, n_B and Y_p are determined by root-findings. The calculated and stored values for n_B and the total proton density $n_B Y_p$ (entries 1. and 2. of the EOS tables in the extended format) are allowed to have a maximum relative deviation from the precise grid-points given by Eqs. (3) and (4) of 10^{-8} . In some applications, e.g. for interpolation, it is better to have a strictly regularized grid. Therefore in the EOS modules the nominal baryon number density and the nominal electron fraction are calculated from Eq. (4), respectively Eq. (3), and then stored as separate arrays.

The modulus of the relative thermodynamic inconsistency

$$\Delta = \frac{Ts^{tot} - p^{tot} + Y_p n_B(\mu_e + \mu_p) + (1 - Y_p) n_B \mu_n}{\epsilon^{tot}} - 1$$
(42)

is everywhere below 10^{-10} for the binary tables in the extended format. For the ASCII tables in the Shen 98 format the inconsistency can be much larger because of round-off errors.

It is also checked that the mass fractions of the different particle species sum up to unity:

$$\Delta X = 1 - X_n + X_p + X_d + X_t + X_h + X_\alpha + X_A .$$
(43)

In the binary table $|\Delta X|$ is always below 10^{-11} . For the Shen 98 format,

$$\Delta X = 1 - X_n + X_p + X_{a_{Z6}} + X_{A_{Z6}} , \qquad (44)$$

the inconsistency can again be larger, due to round-off errors.

The composition module also allows to calculate directly the baryon number density (entry 1. of the EOS tables in the extended format). The relative deviation between the baryon number density calculated with the composition module and the stored value in the EOS table is everywhere below 10^{-10} .

X. ADDITIONAL COMMENTS

- Please note that we assume that nuclear matter is uniform above temperatures larger or equal to 20 MeV, i.e. consists only of neutrons and protons.
- For the chemical potentials we choose the true nucleon masses as the reference values, i.e., we are storing the non-relativistic equivalent form of the chemical potentials. If one uses the relativistic chemical potentials defined as e.g. $\mu_n = \mu_n^{nonrel} + m_n$ the difference $\mu_n \mu_p$ obviously includes the neutron to proton rest mass difference $Q = m_n m_p$. However, if the non-relativistic chemical potentials are used in reactions, Q has to be added by hand, like in every non-relativistic formulation.
- Please remember that the EOS model contains a Maxwell transition from NSE to uniform nucleon matter. As we do not think that it is important information, we do not describe the details of the calculation of the EOS entries in the Maxwell transition region. However, we want to remark that the electron contribution to the EOS in the transition region is not given by a single ideal Fermi-Dirac gas. Thus the subtraction of the electrons from the EOS is not straightforward. In the Shen 98 format this has been done already, but I do not recommend to try to do the same for the extended format without the knowledge about the details of the calculation. Please contact me if you need different formats of the tables.
- We wish you a lot of fun with the tables and highly appreciate any comments or feedback.
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